# STATISTICS Course Description 

## The College Board: Connecting Students to College Success

The College Board is a not-for-profit membership association whose mission is to connect students to college success and opportunity. Founded in 1900, the association is composed of more than 5,400 schools, colleges, universities, and other educational organizations. Each year, the College Board serves seven million students and their parents, 23,000 high schools, and 3,500 colleges through major programs and services in college admissions, guidance, assessment, financial aid, enrollment, and teaching and learning. Among its best-known programs are the $\mathrm{SAT}^{\circledR}$, the PSAT/NMSOT ${ }^{\circledR}$, and the Advanced Placement Program ${ }^{\circledR}$ ( AP $^{\circledR}$ ). The College Board is committed to the principles of excellence and equity, and that commitment is embodied in all of its programs, services, activities, and concerns.
For further information visit www.collegeboard.com.
The College Board and the Advanced Placement Program encourage teachers, AP Coordinators, and school administrators to make equitable access a guiding principle for their AP programs. The College Board is committed to the principle that all students deserve an opportunity to participate in rigorous and academically challenging courses and programs. All students who are willing to accept the challenge of a rigorous academic curriculum should be considered for admission to AP courses. The Board encourages the elimination of barriers that restrict access to AP courses for students from ethnic, racial, and socioeconomic groups that have been traditionally underrepresented in the AP Program. Schools should make every effort to ensure that their AP classes reflect the diversity of their student population.

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## Dear Colleague:

We know that $\mathrm{AP}^{\circledR}$ is a unique collaboration among motivated students, dedicated teachers, and committed high schools, colleges, and universities. Without your contributions, the rigorous instruction that takes place in classrooms around the world would not be possible.

In 2007, approximately 1.4 million students took more than 2.5 million AP Exams. Guiding these students were talented, hardworking teachers, who are the heart and soul of the AP Program. The College Board is grateful for the dedication of AP teachers and the administrators who support them.

One example of the collaboration that makes AP possible is the AP Course Audit, the process through which college faculty review AP teachers' syllabi to ensure that both teachers and administrators are aware of the expectations colleges and universities have for AP courses. This yearlong intensive assessment involved the review and analysis of more than 134,000 syllabi to determine which courses fulfill or exceed standards for college-level curricula. In total, 14,383 secondary schools worldwide succeeded in developing one or more courses that have received authorization from the College Board.

Through the AP Audit, teachers received a number of benefits. For example, you or your colleagues told us that the AP Audit helped you to obtain more current college textbooks for your students. A significant number of teachers said they were able to prevent the reduction of lab or instructional time that was scheduled to affect their courses. Because of the audit, 22,000 teachers said they were able to incorporate advances in their discipline that had not yet been added to their curricula. The searchable AP Course Ledger is online at collegeboard.com.

The College Board remains committed to supporting the work of AP teachers. AP workshops and Summer Institutes held around the world provide stimulating professional development for more than 60,000 teachers each year. Workshops provide teachers not only with valuable course-specific information but the opportunity to interact and network with their colleagues in the AP community.

This community is extended online at AP Central ${ }^{\circledR}$ where teachers can access a wide range of resources, information, and tools to support their work in the AP classroom. In response to requests from educators to make our Web site easier to use, the College Board implemented extensive improvements to collegeboard.com. A new "K-12 Teacher" homepage makes it easier to find an array of content and services. AP Central serves as an integral part of this enhanced collegeboard.com Web site.

We appreciate all of your efforts in the AP classroom and in the courses that prepare students for the rigor and challenge of AP. It is through the dedication and hard work of educators like you that a wider range of students than ever before is being given the opportunity to succeed in AP.


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## Welcome to the AP ${ }^{\oplus}$ Program

The Advanced Placement Program ${ }^{\circledR}$ (AP) is a collaborative effort among motivated students; dedicated teachers; and committed high schools, colleges, and universities. Since its inception in 1955, the Program has enabled millions of students to take college-level courses and exams, and to earn college credit or placement, while still in high school.

Most colleges and universities in the United States, as well as colleges and universities in more than 40 other countries, have an AP policy granting incoming students credit, placement, or both on the basis of their AP Exam grades. Many of these institutions grant up to a full year of college credit (sophomore standing) to students who earn a sufficient number of qualifying AP grades.

Each year, an increasing number of parents, students, teachers, high schools, and colleges and universities turn to the AP Program as a model of educational excellence.

More information about the AP Program is available at the back of this Course Description and at AP Central, the College Board's online home for AP professionals (apcentral.collegeboard.com). Students can find more information at the AP student site (www.collegeboard.com/apstudents).

## AP Courses

Thirty-seven AP courses in a wide variety of subject areas are available now. A committee of college faculty and master AP teachers designs each AP course to cover the information, skills, and assignments found in the corresponding college course. See page 2 for a complete list of AP courses and exams.

## AP Exams

Each AP course has a corresponding exam that participating schools worldwide administer in May (except for AP Studio Art, which is a portfolio assessment). AP Exams contain multiple-choice questions and a free-response section (essay, problem solving, or oral response).

AP Exams are a culminating assessment in all AP courses and are thus an integral part of the Program. As a result, many schools foster the expectation that students who enroll in an AP course will take the corresponding AP Exam. Because the College Board is committed to providing access to AP Exams for homeschooled students and students whose schools do not offer AP courses, it does not require students to take an AP course prior to taking an AP Exam.

## AP Course Audit

The AP Course Audit was created at the request of secondary school and college and university members of the College Board who sought a means to provide teachers and administrators with clear guidelines on the curricular and resource requirements that must be in place for AP courses. The AP Course Audit also helps colleges and universities better interpret secondary school courses marked "AP" on students' transcripts. To receive authorization from the College Board to label a course "AP,"
schools must demonstrate how their courses meet or exceed these requirements, which colleges and universities expect to see within a college-level curriculum.

The AP Program unequivocally supports the principle that each individual school must develop its own curriculum for courses labeled "AP." Rather than mandating any one curriculum for AP courses, the AP Course Audit instead provides each AP teacher with a set of expectations that college and secondary school faculty nationwide have established for college-level courses. AP teachers are encouraged to develop or maintain their own curriculum that either includes or exceeds each of these expectations; such courses will be authorized to use the "AP" designation. Credit for the success of AP courses belongs to the individual schools and teachers that create powerful, locally designed AP curricula.

Complete information about the AP Course Audit is available at AP Central.

## AP Courses and Exams

## Art

Art History
Studio Art: 2-D Design
Studio Art: 3-D Design
Studio Art: Drawing
Biology
Calculus
Calculus AB
Calculus BC
Chemistry
Chinese Language and Culture
Computer Science
Computer Science A
Computer Science AB*
Economics
Macroeconomics
Microeconomics
English
English Language and Composition
English Literature and Composition
Environmental Science
French
French Language
French Literature*

German Language
Government and Politics
Comparative Government and Politics
United States Government and Politics
History
European History
United States History
World History
Human Geography
Italian Language and Culture*
Japanese Language and Culture
Latin
Latin Literature ${ }^{*}$
Latin: Vergil
Music Theory
Physics
Physics B
Physics C: Electricity and Magnetism
Physics C: Mechanics
Psychology
Spanish
Spanish Language
Spanish Literature
Statistics
*AP Computer Science AB, AP French Literature, and AP Latin Literature will be discontinued after the May 2009 exam administration. AP Italian may also be discontinued if external funding is not secured by May 2009. Visit AP Central for details.

## AP Reading

AP Exams—with the exception of AP Studio Art, which is a portfolio assessment— consist of dozens of multiple-choice questions scored by machine, and free-response questions scored at the annual AP Reading by thousands of college faculty and expert AP teachers. AP Readers use scoring standards developed by college and university faculty who teach the corresponding college course. The AP Reading offers educators both significant professional development and the opportunity to network with colleagues. For more information about the AP Reading, or to apply to serve as a Reader, visit apcentral.collegeboard.com/readers.

## AP Exam Grades

The Readers' scores on the free-response questions are combined with the results of the computer-scored multiple-choice questions; the weighted raw scores are summed to give a composite score. The composite score is then converted to a grade on AP's 5-point scale:

| AP GRADE | QUALIFICATION |
| :---: | :--- |
| 5 | Extremely well qualified |
| 4 | Well qualified |
| 3 | Qualified |
| 2 | Possibly qualified |
| 1 | No recommendation |

AP Exam grades of 5 are equivalent to A grades in the corresponding college course. AP Exam grades of 4 are equivalent to grades of $\mathrm{A}-, \mathrm{B}+$, and B in college. AP Exam grades of 3 are equivalent to grades of $\mathrm{B}-, \mathrm{C}+$, and C in college.

## Credit and Placement for AP Grades

Thousands of four-year colleges grant credit, placement, or both for qualifying AP Exam grades, because these grades represent a level of achievement equivalent to that of students who take the corresponding college course. That college-level equivalency is ensured through several AP Program processes:

1. The involvement of college faculty in course and exam development and other AP activities. Currently, college faculty:

- Serve as chairs and members of the committees that develop the Course Descriptions and exams in each AP course.
- Are responsible for standard setting and are involved in the evaluation of student responses at the AP Reading. The Chief Reader for each AP subject is a college faculty member.
- Teach professional development institutes for experienced and new AP teachers.
- Serve as the senior reviewers in the annual AP Course Audit, ensuring AP teachers' syllabi meet the curriculum guidelines of college-level courses.

2. AP courses and exams are reviewed and updated regularly based on the results of curriculum surveys at up to 200 colleges and universities, collaborations among the College Board and key educational and disciplinary organizations, and the interactions of committee members with professional organizations in their discipline.
3. Periodic college comparability studies are undertaken in which the performance of college students on AP Exams is compared with that of AP students to confirm that the AP grade scale of 1 to 5 is properly aligned with current college standards.

For more information about the role of colleges and universities in the AP Program, visit the Higher Ed Services section of collegeboard.com at professionals .collegeboard.com/higher-ed.

## Setting Credit and Placement Policies for AP Grades

The College Board Web site for education professionals has a section geared toward colleges and universities that provides guidance in setting AP credit and placement policies and additional resources, including links to AP research studies, released exam questions, and sample student responses at varying levels of achievement for each AP Exam. Visit professionals.collegeboard.com/higher-ed/placement/ap.

The AP Credit Policy Info online search tool provides links to credit and placement policies at more than 1,000 colleges and universities. The tool helps students find the credit hours and advanced placement they can receive for qualifying exam scores within each AP subject. AP Credit Policy Info is available at www.collegeboard.com/ap/creditpolicy.

## AP Statistics

## INTRODUCTION

The Advanced Placement Program offers a course description and exam in statistics to secondary school students who wish to complete studies equivalent to a onesemester, introductory, non-calculus-based, college course in statistics.

Statistics and mathematics educators who serve as members of the AP Statistics Development Committee have prepared the Course Description and exam to reflect the content of a typical introductory college course in statistics. The exam is representative of such a course and therefore is considered appropriate for the measurement of skills and knowledge in the field of introductory statistics.

In colleges and universities, the number of students who take a statistics course is almost as large as the number of students who take a calculus course. A July 2002 article in the Chronicle of Higher Education reports that the enrollment in statistics courses from 1990 to 2000 increased by 45 percent-one testament to the growth of statistics in those institutions. An introductory statistics course, similar to the AP Statistics course, is typically required for majors such as social sciences, health sciences, and business. Every semester about 236,000 college and university students enroll in an introductory statistics course offered by a mathematics or statistics department. In addition, a large number of students enroll in an introductory statistics course offered by other departments. Science, engineering, and mathematics majors usually take an upper-level calculus-based course in statistics, for which the AP Statistics course is effective preparation.

## THECOURSE

The purpose of the AP course in statistics is to introduce students to the major concepts and tools for collecting, analyzing, and drawing conclusions from data. Students are exposed to four broad conceptual themes:

1. Exploring Data: Describing patterns and departures from patterns
2. Sampling and Experimentation: Planning and conducting a study
3. Anticipating Patterns: Exploring random phenomena using probability and simulation
4. Statistical Inference: Estimating population parameters and testing hypotheses

Students who successfully complete the course and exam may receive credit, advanced placement, or both for a one-semester introductory college statistics course. This does not necessarily imply that the high school course should be one semester long. Each high school needs to determine the length of its AP Statistics course to best serve the needs of its students. Statistics, like some other AP courses, could be effectively studied in a one-semester, a two-trimester, or a one-year course. Most schools, however, offer it as a one-year course.

## Student Selection

The College Board and the Advanced Placement Program encourage teachers, AP Coordinators, and school administrators to make equitable access a guiding principle for their AP programs. The College Board is committed to the principle that all students deserve an opportunity to participate in rigorous and academically challenging courses and programs. All students who are willing to accept the challenge of a rigorous academic curriculum should be considered for admission to AP courses. The Board encourages the elimination of barriers that restrict access to AP courses for students from ethnic, racial, and socioeconomic groups that have been traditionally underrepresented in the AP Program. Schools should make every effort to ensure that their AP classes reflect the diversity of their student population.

The AP Statistics course is an excellent option for any secondary school student who has successfully completed a second-year course in algebra and who possesses sufficient mathematical maturity and quantitative reasoning ability.

Because second-year algebra is the prerequisite course, AP Statistics usually will be taken in either the junior or senior year. The decisions about whether to take AP Statistics and when to take it depend on a student's plans:

- Students planning to take a science course in their senior year will benefit greatly from taking AP Statistics in their junior year.
- For students who would otherwise take no mathematics in their senior year, AP Statistics allows them to continue to develop their quantitative skills.
- Students who wish to leave open the option of taking calculus in college should include precalculus in their high school program and perhaps take AP Statistics concurrently with precalculus.

Students with the appropriate mathematical background are encouraged to take both AP Statistics and AP Calculus in high school.

Students who take the AP Statistics course are strongly encouraged to take the exam.

## Teaching the Course

The AP Statistics course lends itself naturally to a mode of teaching that engages students in constructing their own knowledge. For example, students working individually or in small groups can plan and perform data collection and analyses where the teacher serves in the role of a consultant, rather than a director. This approach gives students ample opportunity to think through problems, make decisions, and share questions and conclusions with other students as well as with the teacher.

Important components of the course should include the use of technology, projects and laboratories, cooperative group problem-solving, and writing, as a part of concept-oriented instruction and assessment. This approach to teaching AP Statistics will allow students to build interdisciplinary connections with other subjects and with their world outside school.

The AP Statistics course depends heavily on the availability of technology suitable for the interactive, investigative aspects of data analysis. Therefore, schools should make every effort to provide students and teachers easy access to computers to facilitate the teaching and learning of statistics.

Providing instructional information and educational opportunities for teachers is an important component of the AP Program. The College Board offers workshops, summer courses, and institutes for teachers in all AP courses. Further information about these and other training opportunities may be obtained at AP Central (apcentral.collegeboard.com) and from your College Board regional office (contact information is on the inside back cover). The Teachers' Resources section of AP Central offers reviews of textbooks, articles, Web sites, and other teaching resources. The electronic discussion groups (EDGs) accessible through AP Central also provide a moderated forum for exchanging ideas, insights, and practices among members of the AP professional community.

Additionally, the following publications provide some insight into the philosophy of the AP Statistics course.

Cobb, George, "Teaching Statistics: More Data, Less Lecturing." In Steen, Lynn Arthur, ed. 1992. Heeding the Call for Change: Suggestions for Curricular Action. Washington, D.C.: Mathematical Association of America. To order MAA publications call 800 331-1622 or go to www.maa.org.

Gordon, Florence and Sheldon, eds. 1992. Statistics for the Twenty-First Century, MAA Notes No. 26. Washington, D.C.: Mathematical Association of America.

Moore, Thomas, ed. 2000. Teaching Statistics: Resources for Undergraduate Instructors, MAA Notes Vol. 52. Washington, D.C.: Mathematical Association of America.

National Council of Teachers of Mathematics. 2003. Principles and Standards for School Mathematics, $3^{\text {rd }}$ ed. Reston, Va.: National Council of Teachers of Mathematics. www.nctm.org.

## Course Content Overview

The topics for AP Statistics are divided into four major themes: exploratory analysis ( $20-30$ percent of the exam), planning and conducting a study ( $10-15$ percent of the exam), probability ( $20-30$ percent of the exam), and statistical inference (30-40 percent of the exam).
I. Exploratory analysis of data makes use of graphical and numerical techniques to study patterns and departures from patterns. In examining distributions of data, students should be able to detect important characteristics, such as shape, location, variability, and unusual values. From careful observations of patterns in data, students can generate conjectures about relationships among variables. The notion of how one variable may be associated with another permeates almost all of statistics, from simple comparisons of proportions through linear regression. The difference between association and causation must accompany this conceptual development throughout.

## II. Data must be collected according to a well-developed plan if valid information

 is to be obtained. If data are to be collected to provide an answer to a question of interest, a careful plan must be developed. Both the type of analysis that is appropriate and the nature of conclusions that can be drawn from that analysis depend in a critical way on how the data was collected. Collecting data in a reasonable way, through either sampling or experimentation, is an essential step in the data analysis process.III. Probability is the tool used for anticipating what the distribution of data should look like under a given model. Random phenomena are not haphazard: they display an order that emerges only in the long run and is described by a distribution. The mathematical description of variation is central to statistics. The probability required for statistical inference is not primarily axiomatic or combinatorial but is oriented toward using probability distributions to describe data.
IV. Statistical inference guides the selection of appropriate models. Models and data interact in statistical work: models are used to draw conclusions from data, while the data are allowed to criticize and even falsify the model through inferential and diagnostic methods. Inference from data can be thought of as the process of selecting a reasonable model, including a statement in probability language, of how confident one can be about the selection.

## TOPIC OUTLINE

Following is an outline of the major topics covered by the AP Statistics Exam. The ordering here is intended to define the scope of the course but not necessarily the sequence. The percentages in parentheses for each content area indicate the coverage for that content area in the exam.
I. Exploring Data: Describing patterns and departures from patterns ( $20 \%-30 \%$ )

Exploratory analysis of data makes use of graphical and numerical techniques to study patterns and departures from patterns. Emphasis should be placed on interpreting information from graphical and numerical displays and summaries.
A. Constructing and interpreting graphical displays of distributions of univariate data (dotplot, stemplot, histogram, cumulative frequency plot)

1. Center and spread
2. Clusters and gaps
3. Outliers and other unusual features
4. Shape
B. Summarizing distributions of univariate data
5. Measuring center: median, mean
6. Measuring spread: range, interquartile range, standard deviation
7. Measuring position: quartiles, percentiles, standardized scores ( $z$-scores)
8. Using boxplots
9. The effect of changing units on summary measures
C. Comparing distributions of univariate data (dotplots, back-to-back stemplots, parallel boxplots)
10. Comparing center and spread: within group, between group variation
11. Comparing clusters and gaps
12. Comparing outliers and other unusual features
13. Comparing shapes
D. Exploring bivariate data
14. Analyzing patterns in scatterplots
15. Correlation and linearity
16. Least-squares regression line
17. Residual plots, outliers, and influential points
18. Transformations to achieve linearity: logarithmic and power transformations
E. Exploring categorical data
19. Frequency tables and bar charts
20. Marginal and joint frequencies for two-way tables
21. Conditional relative frequencies and association
22. Comparing distributions using bar charts
II. Sampling and Experimentation: Planning and conducting a study ( $10 \%-15 \%$ )

Data must be collected according to a well-developed plan if valid information on a conjecture is to be obtained. This plan includes clarifying the question and deciding upon a method of data collection and analysis.
A. Overview of methods of data collection

1. Census
2. Sample survey
3. Experiment
4. Observational study
B. Planning and conducting surveys
5. Characteristics of a well-designed and well-conducted survey
6. Populations, samples, and random selection
7. Sources of bias in sampling and surveys
8. Sampling methods, including simple random sampling, stratified random sampling, and cluster sampling
C. Planning and conducting experiments
9. Characteristics of a well-designed and well-conducted experiment
10. Treatments, control groups, experimental units, random assignments, and replication
11. Sources of bias and confounding, including placebo effect and blinding
12. Completely randomized design
13. Randomized block design, including matched pairs design
D. Generalizability of results and types of conclusions that can be drawn from observational studies, experiments, and surveys
III. Anticipating Patterns: Exploring random phenomena using probability and simulation (20\%-30\%)
Probability is the tool used for anticipating what the distribution of data should look like under a given model.
A. Probability
14. Interpreting probability, including long-run relative frequency interpretation
15. "Law of Large Numbers" concept
16. Addition rule, multiplication rule, conditional probability, and independence
17. Discrete random variables and their probability distributions, including binomial and geometric
18. Simulation of random behavior and probability distributions
19. Mean (expected value) and standard deviation of a random variable, and linear transformation of a random variable
B. Combining independent random variables
20. Notion of independence versus dependence
21. Mean and standard deviation for sums and differences of independent random variables
C. The normal distribution
22. Properties of the normal distribution
23. Using tables of the normal distribution
24. The normal distribution as a model for measurements
D. Sampling distributions
25. Sampling distribution of a sample proportion
26. Sampling distribution of a sample mean
27. Central Limit Theorem
28. Sampling distribution of a difference between two independent sample proportions
29. Sampling distribution of a difference between two independent sample means
30. Simulation of sampling distributions
31. t -distribution
32. Chi-square distribution
IV. Statistical Inference: Estimating population parameters and testing hypotheses ( $30 \%-40 \%$ )

## Statistical inference guides the selection of appropriate models.

A. Estimation (point estimators and confidence intervals)

1. Estimating population parameters and margins of error
2. Properties of point estimators, including unbiasedness and variability
3. Logic of confidence intervals, meaning of confidence level and confidence intervals, and properties of confidence intervals
4. Large sample confidence interval for a proportion
5. Large sample confidence interval for a difference between two proportions
6. Confidence interval for a mean
7. Confidence interval for a difference between two means (unpaired and paired)
8. Confidence interval for the slope of a least-squares regression line
B. Tests of significance
9. Logic of significance testing, null and alternative hypotheses; $p$-values; one- and two-sided tests; concepts of Type I and Type II errors; concept of power
10. Large sample test for a proportion
11. Large sample test for a difference between two proportions
12. Test for a mean
13. Test for a difference between two means (unpaired and paired)
14. Chi-square test for goodness of fit, homogeneity of proportions, and independence (one- and two-way tables)
15. Test for the slope of a least-squares regression line

## The Use of Technology

The AP Statistics course adheres to the philosophy and methods of modern data analysis. Although the distinction between graphing calculators and computers is becoming blurred as technology advances, at present the fundamental tool of data analysis is the computer. The computer does more than eliminate the drudgery of hand computation and graphing-it is an essential tool for structured inquiry.

Data analysis is a journey of discovery. It is an iterative process that involves a dialogue between the data and a mathematical model. As more is learned about the data, the model is refined and new questions are formed. The computer aids in this journey in some essential ways. First, it produces graphs that are specifically designed for data analysis. These graphical displays make it easier to observe patterns in data, to identify important subgroups of the data, and to locate any unusual data points. Second, the computer allows the student to fit complex mathematical models to the data and to assess how well the model fits the data by examining the residuals. Finally, the computer is helpful in identifying an observation that has an undue influence on the analysis and in isolating its effects.

In addition to its use in data analysis, the computer facilitates the simulation approach to probability that is emphasized in the AP Statistics course. Probabilities of random events, probability distributions of random variables, and sampling distributions of statistics can be studied conceptually, using simulation. This frees the student and teacher from a narrow approach that depends on a few simple probabilistic models.

Because the computer is central to what statisticians do, it is considered essential for teaching the AP Statistics course. However, it is not yet possible for students to have access to a computer during the AP Statistics Exam. Without a computer and under the conditions of a timed exam, students cannot be asked to perform the amount of computation that is needed for many statistical investigations. Consequently, standard computer output will be provided as necessary and students will be expected to interpret it. (See two examples of computer output in the Multiple-Choice Questions section on pages 22 and 24.)

A graphing calculator is a useful computational aid, particularly in analyzing small data sets, but should not be considered equivalent to a computer in the teaching of statistics. If a graphing calculator is used in the course, its computational capabilities should include standard statistical univariate and bivariate summaries through linear regression. Its graphical capabilities should include common univariate and bivariate displays such as histograms, boxplots, and scatterplots. Students find calculators where data are entered into a spreadsheet format particularly easy to use. Ideally, students should have access to both computers and calculators for work in and outside the classroom.

Currently, the graphing calculator is the only computational aid that is available to students for use as a tool for data analysis on the AP Exam. Students who utilize graphing calculators on the exam should be aware of the following policy.

It is not only inappropriate, but unethical, for students who are taking the AP Statistics Exam to have access to any information in their graphing calculators or elsewhere that is not directly related to upgrading the statistical functionality of older graphing calculators to make them comparable to statistical features found on newer models.
During the exam, students are not permitted to have access to any information in their graphing calculators or elsewhere that is not directly related to upgrading the statistical functionality of older graphing calculators to make them comparable to statistical features found on newer models.
Acceptable upgrades include improving the calculator's computational functionalities and/or graphical functionalities for data that students key into the calculator while taking the exam.
Unacceptable enhancements include, but are not limited to, keying or scanning text or response templates into the calculator. Students attempting to augment the capabilities of their graphing calculators in any way other than for the purpose of upgrading features, as described above, will be considered to be cheating on the exam.

## Formulas and Tables

Students enrolled in the AP Statistics course should concentrate their time and effort on developing a thorough understanding of the fundamental concepts of statistics. They do not need to memorize formulas.

The following list of formulas and tables will be furnished to students taking the AP Statistics Exam. Teachers are encouraged to familiarize their students with the form and notation of these formulas by making them accessible at the appropriate times during the course.

## I. Descriptive Statistics

$$
\begin{aligned}
& \bar{x}=\frac{\sum x_{i}}{n} \\
& s_{x}=\sqrt{\frac{1}{n-1} \sum\left(x_{i}-\bar{x}\right)^{2}} \\
& s_{p}=\sqrt{\frac{\left(n_{1}-1\right) s_{1}^{2}+\left(n_{2}-1\right) s_{2}^{2}}{\left(n_{1}-1\right)+\left(n_{2}-1\right)}} \\
& \hat{y}=b_{0}+b_{1} x \\
& b_{1}=\frac{\sum\left(x_{i}-\bar{x}\right)\left(y_{i}-\bar{y}\right)}{\sum\left(x_{i}-\bar{x}\right)^{2}} \\
& b_{0}=\bar{y}-b_{1} \bar{x} \\
& r=\frac{1}{n-1} \sum\left(\frac{x_{i}-\bar{x}}{s_{x}}\right)\left(\frac{y_{i}-\bar{y}}{s_{y}}\right) \\
& b_{1}=r \frac{s_{y}}{s_{x}} \\
& s_{b_{1}}=\frac{\sqrt{\frac{\sum\left(y_{i}-\hat{y}_{i}\right)^{2}}{n-2}}}{\sqrt{\sum\left(x_{i}-\bar{x}\right)^{2}}}
\end{aligned}
$$

## II. Probability

$$
\begin{aligned}
& P(A \cup B)=P(A)+P(B)-P(A \cap B) \\
& P(A \mid B)=\frac{P(A \cap B)}{P(B)} \\
& E(X)=\mu_{x}=\sum x_{i} p_{i} \\
& \operatorname{Var}(X)=\sigma_{x}^{2}=\sum\left(x_{i}-\mu_{x}\right)^{2} p_{i}
\end{aligned}
$$

If $X$ has a binomial distribution with parameters $n$ and $p$, then:
$P(X=k)=\binom{n}{k} p^{k}(1-p)^{n-k}$
$\mu_{x}=n p$
$\sigma_{x}=\sqrt{n p(1-p)}$
$\mu_{\hat{p}}=p$
$\sigma_{\hat{p}}=\sqrt{\frac{p(1-p)}{n}}$

If $\bar{x}$ is the mean of a random sample of size $n$ from an infinite population with mean $\mu$ and standard deviation $\sigma$, then:
$\mu_{\bar{x}}=\mu$
$\sigma_{\bar{x}}=\frac{\sigma}{\sqrt{n}}$

## III. Inferential Statistics

Standardized test statistic: $\frac{\text { statistic - parameter }}{\text { standard deviation of statistic }}$
Confidence interval: statistic $\pm$ (critical value) • (standard deviation of statistic)

Single-Sample

| Statistic | Standard Deviation <br> of Statistic |
| :---: | :---: |
| Sample Mean | $\frac{\sigma}{\sqrt{n}}$ |
| Sample Proportion | $\sqrt{\frac{p(1-p)}{n}}$ |

## Two-Sample

| Statistic | Standard Deviation <br> of Statistic |
| :---: | :---: |
| Difference of <br> sample means | $\sqrt{\frac{\sigma_{1}^{2}}{n_{1}}+\frac{\sigma_{2}^{2}}{n_{2}}}$ |
| Special case when <br> $\sigma_{1}=\sigma_{2}$ |  |
| Difference of <br> sample proportions | $\sqrt{\frac{\sigma \sqrt{\frac{1}{n_{1}}+\frac{1}{n_{2}}}}{\frac{p}{1}^{\left(1-p_{1}\right)}}+\frac{p_{2}\left(1-p_{2}\right)}{n_{2}}}$ |
| Special case when <br> $p_{1}$$p_{2}$ |  |
|  | $\sqrt{p(1-p)} \sqrt{\frac{1}{n_{1}}+\frac{1}{n_{2}}}$ |

Chi-square test statistic $=\sum \frac{(\text { observed }- \text { expected })^{2}}{\text { expected }}$

Table entry for $z$ is the probability lying below $z$.


Table A
Standard normal probabilities

| $z$ | . 00 | . 01 | . 02 | . 03 | . 04 | . 05 | . 06 | . 07 | . 08 | . 09 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -3.4 | . 0003 | . 0003 | . 0003 | . 0003 | . 0003 | . 0003 | . 0003 | . 0003 | . 0003 | . 0002 |
| -3.3 | . 0005 | . 0005 | . 0005 | . 0004 | . 0004 | . 0004 | . 0004 | . 0004 | . 0004 | . 0003 |
| -3.2 | . 0007 | . 0007 | . 0006 | . 0006 | . 0006 | . 0006 | . 0006 | . 0005 | . 0005 | . 0005 |
| -3.1 | . 0010 | . 0009 | . 0009 | . 0009 | . 0008 | . 0008 | . 0008 | . 0008 | . 0007 | . 0007 |
| -3.0 | . 0013 | . 0013 | . 0013 | . 0012 | . 0012 | . 0011 | . 0011 | . 0011 | . 0010 | . 0010 |
| -2.9 | . 0019 | . 0018 | . 0018 | . 0017 | . 0016 | . 0016 | . 0015 | . 0015 | . 0014 | . 0014 |
| -2.8 | . 0026 | . 0025 | . 0024 | . 0023 | . 0023 | . 0022 | . 0021 | . 0021 | . 0020 | . 0019 |
| -2.7 | . 0035 | . 0034 | . 0033 | . 0032 | . 0031 | . 0030 | . 0029 | . 0028 | . 0027 | . 0026 |
| -2.6 | . 0047 | . 0045 | . 0044 | . 0043 | . 0041 | . 0040 | . 0039 | . 0038 | . 0037 | . 0036 |
| -2.5 | . 0062 | . 0060 | . 0059 | . 0057 | . 0055 | . 0054 | . 0052 | . 0051 | . 0049 | . 0048 |
| -2.4 | . 0082 | . 0080 | . 0078 | . 0075 | . 0073 | . 0071 | . 0069 | . 0068 | . 0066 | . 0064 |
| -2.3 | . 0107 | . 0104 | . 0102 | . 0099 | . 0096 | . 0094 | . 0091 | . 0089 | . 0087 | . 0084 |
| -2.2 | . 0139 | . 0136 | . 0132 | . 0129 | . 0125 | . 0122 | . 0119 | . 0116 | . 0113 | . 0110 |
| -2.1 | . 0179 | . 0174 | . 0170 | . 0166 | . 0162 | . 0158 | . 0154 | . 0150 | . 0146 | . 0143 |
| -2.0 | . 0228 | . 0222 | . 0217 | . 0212 | . 0207 | . 0202 | . 0197 | . 0192 | . 0188 | . 0183 |
| -1.9 | . 0287 | . 0281 | . 0274 | . 0268 | . 0262 | . 0256 | . 0250 | . 0244 | . 0239 | . 0233 |
| -1.8 | . 0359 | . 0351 | . 0344 | . 0336 | . 0329 | . 0322 | . 0314 | . 0307 | . 0301 | . 0294 |
| -1.7 | . 0446 | . 0436 | . 0427 | . 0418 | . 0409 | . 0401 | . 0392 | . 0384 | . 0375 | . 0367 |
| -1.6 | . 0548 | . 0537 | . 0526 | . 0516 | . 0505 | . 0495 | . 0485 | . 0475 | . 0465 | . 0455 |
| -1.5 | . 0668 | . 0655 | . 0643 | . 0630 | . 0618 | . 0606 | . 0594 | . 0582 | . 0571 | . 0559 |
| -1.4 | . 0808 | . 0793 | . 0778 | . 0764 | . 0749 | . 0735 | . 0721 | . 0708 | . 0694 | . 0681 |
| -1.3 | . 0968 | . 0951 | . 0934 | . 0918 | . 0901 | . 0885 | . 0869 | . 0853 | . 0838 | . 0823 |
| -1.2 | . 1151 | . 1131 | . 1112 | . 1093 | . 1075 | . 1056 | . 1038 | . 1020 | . 1003 | . 0985 |
| -1.1 | . 1357 | . 1335 | . 1314 | . 1292 | . 1271 | . 1251 | . 1230 | . 1210 | . 1190 | . 1170 |
| -1.0 | . 1587 | . 1562 | . 1539 | . 1515 | . 1492 | . 1469 | . 1446 | . 1423 | . 1401 | . 1379 |
| -0.9 | . 1841 | . 1814 | . 1788 | . 1762 | . 1736 | . 1711 | . 1685 | . 1660 | . 1635 | . 1611 |
| -0.8 | . 2119 | . 2090 | . 2061 | . 2033 | . 2005 | . 1977 | . 1949 | . 1922 | . 1894 | . 1867 |
| -0.7 | . 2420 | . 2389 | . 2358 | . 2327 | . 2296 | . 2266 | . 2236 | . 2206 | . 2177 | . 2148 |
| -0.6 | . 2743 | . 2709 | . 2676 | . 2643 | . 2611 | . 2578 | . 2546 | . 2514 | . 2483 | . 2451 |
| -0.5 | . 3085 | . 3050 | . 3015 | . 2981 | . 2946 | . 2912 | . 2877 | . 2843 | . 2810 | . 2776 |
| -0.4 | . 3446 | . 3409 | . 3372 | . 3336 | . 3300 | . 3264 | . 3228 | . 3192 | . 3156 | . 3121 |
| -0.3 | . 3821 | . 3783 | . 3745 | . 3707 | . 3669 | . 3632 | . 3594 | . 3557 | . 3520 | . 3483 |
| -0.2 | . 4207 | . 4168 | . 4129 | . 4090 | . 4052 | . 4013 | . 3974 | . 3936 | . 3897 | . 3859 |
| -0.1 | . 4602 | . 4562 | . 4522 | . 4483 | . 4443 | . 4404 | . 4364 | . 4325 | . 4286 | . 4247 |
| -0.0 | . 5000 | . 4960 | . 4920 | . 4880 | . 4840 | . 4801 | . 4761 | . 4721 | . 4681 | . 4641 |

Table entry for $z$ is the probability lying below $z$.


Table A (Continued) Standard normal probabilities

| $z$ | . 00 | . 01 | . 02 | . 03 | . 04 | . 05 | . 06 | . 07 | . 08 | . 09 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0 | . 5000 | . 5040 | . 5080 | . 5120 | . 5160 | . 5199 | . 5239 | . 5279 | . 5319 | . 5359 |
| 0.1 | . 5398 | . 5438 | . 5478 | . 5517 | . 5557 | . 5596 | . 5636 | . 5675 | . 5714 | . 5753 |
| 0.2 | . 5793 | . 5832 | . 5871 | . 5910 | . 5948 | . 5987 | . 6026 | . 6064 | . 6103 | . 6141 |
| 0.3 | . 6179 | . 6217 | . 6255 | . 6293 | . 6331 | . 6368 | . 6406 | . 6443 | . 6480 | . 6517 |
| 0.4 | . 6554 | . 6591 | . 6628 | . 6664 | . 6700 | . 6736 | . 6772 | . 6808 | . 6844 | . 6879 |
| 0.5 | . 6915 | . 6950 | . 6985 | . 7019 | . 7054 | . 7088 | . 7123 | . 7157 | . 7190 | . 7224 |
| 0.6 | . 7257 | . 7291 | . 7324 | . 7357 | . 7389 | . 7422 | . 7454 | . 7486 | . 7517 | . 7549 |
| 0.7 | . 7580 | . 7611 | . 7642 | . 7673 | . 7704 | . 7734 | . 7764 | . 7794 | . 7823 | . 7852 |
| 0.8 | . 7881 | . 7910 | . 7939 | . 7967 | . 7995 | . 8023 | . 8051 | . 8078 | . 8106 | . 8133 |
| 0.9 | . 8159 | . 8186 | . 8212 | . 8238 | . 8264 | . 8289 | . 8315 | . 8340 | . 8365 | . 8389 |
| 1.0 | . 8413 | . 8438 | . 8461 | . 8485 | . 8508 | . 8531 | . 8554 | . 8577 | . 8599 | . 8621 |
| 1.1 | . 8643 | . 8665 | . 8686 | . 8708 | . 8729 | . 8749 | . 8770 | . 8790 | . 8810 | . 8830 |
| 1.2 | . 8849 | . 8869 | . 8888 | . 8907 | . 8925 | . 8944 | . 8962 | . 8980 | . 8997 | . 9015 |
| 1.3 | . 9032 | . 9049 | . 9066 | . 9082 | . 9099 | . 9115 | . 9131 | . 9147 | . 9162 | . 9177 |
| 1.4 | . 9192 | . 9207 | . 9222 | . 9236 | . 9251 | . 9265 | . 9279 | . 9292 | . 9306 | . 9319 |
| 1.5 | . 9332 | . 9345 | . 9357 | . 9370 | . 9382 | . 9394 | . 9406 | . 9418 | . 9429 | . 9441 |
| 1.6 | . 9452 | . 9463 | . 9474 | . 9484 | . 9495 | . 9505 | . 9515 | . 9525 | . 9535 | . 9545 |
| 1.7 | . 9554 | . 9564 | . 9573 | . 9582 | . 9591 | . 9599 | . 9608 | . 9616 | . 9625 | . 9633 |
| 1.8 | . 9641 | . 9649 | . 9656 | . 9664 | . 9671 | . 9678 | . 9686 | . 9693 | . 9699 | . 9706 |
| 1.9 | . 9713 | . 9719 | . 9726 | . 9732 | . 9738 | . 9744 | . 9750 | . 9756 | . 9761 | . 9767 |
| 2.0 | . 9772 | . 9778 | . 9783 | . 9788 | . 9793 | . 9798 | . 9803 | . 9808 | . 9812 | . 9817 |
| 2.1 | . 9821 | . 9826 | . 9830 | . 9834 | . 9838 | . 9842 | . 9846 | . 9850 | . 9854 | . 9857 |
| 2.2 | . 9861 | . 9864 | . 9868 | . 9871 | . 9875 | . 9878 | . 9881 | . 9884 | . 9887 | . 9890 |
| 2.3 | . 9893 | . 9896 | . 9898 | . 9901 | . 9904 | . 9906 | . 9909 | . 9911 | . 9913 | . 9916 |
| 2.4 | . 9918 | . 9920 | . 9922 | . 9925 | . 9927 | . 9929 | . 9931 | . 9932 | . 9934 | . 9936 |
| 2.5 | . 9938 | . 9940 | . 9941 | . 9943 | . 9945 | . 9946 | . 9948 | . 9949 | . 9951 | . 9952 |
| 2.6 | . 9953 | . 9955 | . 9956 | . 9957 | . 9959 | . 9960 | . 9961 | . 9962 | . 9963 | . 9964 |
| 2.7 | . 9965 | . 9966 | . 9967 | . 9968 | . 9969 | . 9970 | . 9971 | . 9972 | . 9973 | . 9974 |
| 2.8 | . 9974 | . 9975 | . 9976 | . 9977 | . 9977 | . 9978 | . 9979 | . 9979 | . 9980 | . 9981 |
| 2.9 | . 9981 | . 9982 | . 9982 | . 9983 | . 9984 | . 9984 | . 9985 | . 9985 | . 9986 | . 9986 |
| 3.0 | . 9987 | . 9987 | . 9987 | . 9988 | . 9988 | . 9989 | . 9989 | . 9989 | . 9990 | . 9990 |
| 3.1 | . 9990 | . 9991 | . 9991 | . 9991 | . 9992 | . 9992 | . 9992 | . 9992 | . 9993 | . 9993 |
| 3.2 | . 9993 | . 9993 | . 9994 | . 9994 | . 9994 | . 9994 | . 9994 | . 9995 | . 9995 | . 9995 |
| 3.3 | . 9995 | . 9995 | . 9995 | . 9996 | . 9996 | . 9996 | . 9996 | . 9996 | . 9996 | . 9997 |
| 3.4 | . 9997 | . 9997 | . 9997 | . 9997 | . 9997 | . 9997 | . 9997 | . 9997 | . 9997 | . 9998 |

Table entry for $p$ and $C$ is the point $t^{*}$ with probability $p$ lying above it and probability $C$ lying between $-t^{*}$ and $t^{*}$.


Table B
$t$ distribution critical values

|  | Tail probability $p$ |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| df | . 25 | . 20 | . 15 | . 10 | . 05 | . 025 | . 02 | . 01 | . 005 | . 0025 | . 001 | . 0005 |
| 1 | 1.000 | 1.376 | 1.963 | 3.078 | 6.314 | 12.71 | 15.89 | 31.82 | 63.66 | 127.3 | 318.3 | 636.6 |
| 2 | . 816 | 1.061 | 1.386 | 1.886 | 2.920 | 4.303 | 4.849 | 6.965 | 9.925 | 14.09 | 22.33 | 31.60 |
| 3 | . 765 | . 978 | 1.250 | 1.638 | 2.353 | 3.182 | 3.482 | 4.541 | 5.841 | 7.453 | 10.21 | 12.92 |
| 4 | . 741 | . 941 | 1.190 | 1.533 | 2.132 | 2.776 | 2.999 | 3.747 | 4.604 | 5.598 | 7.173 | 8.610 |
| 5 | . 727 | . 920 | 1.156 | 1.476 | 2.015 | 2.571 | 2.757 | 3.365 | 4.032 | 4.773 | 5.893 | 6.869 |
| 6 | . 718 | . 906 | 1.134 | 1.440 | 1.943 | 2.447 | 2.612 | 3.143 | 3.707 | 4.317 | 5.208 | 5.959 |
| 7 | . 711 | . 896 | 1.119 | 1.415 | 1.895 | 2.365 | 2.517 | 2.998 | 3.499 | 4.029 | 4.785 | 5.408 |
| 8 | . 706 | . 889 | 1.108 | 1.397 | 1.860 | 2.306 | 2.449 | 2.896 | 3.355 | 3.833 | 4.501 | 5.041 |
| 9 | . 703 | . 883 | 1.100 | 1.383 | 1.833 | 2.262 | 2.398 | 2.821 | 3.250 | 3.690 | 4.297 | 4.781 |
| 10 | . 700 | . 879 | 1.093 | 1.372 | 1.812 | 2.228 | 2.359 | 2.764 | 3.169 | 3.581 | 4.144 | 4.587 |
| 11 | . 697 | . 876 | 1.088 | 1.363 | 1.796 | 2.201 | 2.328 | 2.718 | 3.106 | 3.497 | 4.025 | 4.437 |
| 12 | . 695 | . 873 | 1.083 | 1.356 | 1.782 | 2.179 | 2.303 | 2.681 | 3.055 | 3.428 | 3.930 | 4.318 |
| 13 | . 694 | . 870 | 1.079 | 1.350 | 1.771 | 2.160 | 2.282 | 2.650 | 3.012 | 3.372 | 3.852 | 4.221 |
| 14 | . 692 | . 868 | 1.076 | 1.345 | 1.761 | 2.145 | 2.264 | 2.624 | 2.977 | 3.326 | 3.787 | 4.140 |
| 15 | . 691 | . 866 | 1.074 | 1.341 | 1.753 | 2.131 | 2.249 | 2.602 | 2.947 | 3.286 | 3.733 | 4.073 |
| 16 | . 690 | . 865 | 1.071 | 1.337 | 1.746 | 2.120 | 2.235 | 2.583 | 2.921 | 3.252 | 3.686 | 4.015 |
| 17 | . 689 | . 863 | 1.069 | 1.333 | 1.740 | 2.110 | 2.224 | 2.567 | 2.898 | 3.222 | 3.646 | 3.965 |
| 18 | . 688 | . 862 | 1.067 | 1.330 | 1.734 | 2.101 | 2.214 | 2.552 | 2.878 | 3.197 | 3.611 | 3.922 |
| 19 | . 688 | . 861 | 1.066 | 1.328 | 1.729 | 2.093 | 2.205 | 2.539 | 2.861 | 3.174 | 3.579 | 3.883 |
| 20 | . 687 | . 860 | 1.064 | 1.325 | 1.725 | 2.086 | 2.197 | 2.528 | 2.845 | 3.153 | 3.552 | 3.850 |
| 21 | . 686 | . 859 | 1.063 | 1.323 | 1.721 | 2.080 | 2.189 | 2.518 | 2.831 | 3.135 | 3.527 | 3.819 |
| 22 | . 686 | . 858 | 1.061 | 1.321 | 1.717 | 2.074 | 2.183 | 2.508 | 2.819 | 3.119 | 3.505 | 3.792 |
| 23 | . 685 | . 858 | 1.060 | 1.319 | 1.714 | 2.069 | 2.177 | 2.500 | 2.807 | 3.104 | 3.485 | 3.768 |
| 24 | . 685 | . 857 | 1.059 | 1.318 | 1.711 | 2.064 | 2.172 | 2.492 | 2.797 | 3.091 | 3.467 | 3.745 |
| 25 | . 684 | . 856 | 1.058 | 1.316 | 1.708 | 2.060 | 2.167 | 2.485 | 2.787 | 3.078 | 3.450 | 3.725 |
| 26 | . 684 | . 856 | 1.058 | 1.315 | 1.706 | 2.056 | 2.162 | 2.479 | 2.779 | 3.067 | 3.435 | 3.707 |
| 27 | . 684 | . 855 | 1.057 | 1.314 | 1.703 | 2.052 | 2.158 | 2.473 | 2.771 | 3.057 | 3.421 | 3.690 |
| 28 | . 683 | . 855 | 1.056 | 1.313 | 1.701 | 2.048 | 2.154 | 2.467 | 2.763 | 3.047 | 3.408 | 3.674 |
| 29 | . 683 | . 854 | 1.055 | 1.311 | 1.699 | 2.045 | 2.150 | 2.462 | 2.756 | 3.038 | 3.396 | 3.659 |
| 30 | . 683 | . 854 | 1.055 | 1.310 | 1.697 | 2.042 | 2.147 | 2.457 | 2.750 | 3.030 | 3.385 | 3.646 |
| 40 | . 681 | . 851 | 1.050 | 1.303 | 1.684 | 2.021 | 2.123 | 2.423 | 2.704 | 2.971 | 3.307 | 3.551 |
| 50 | . 679 | . 849 | 1.047 | 1.299 | 1.676 | 2.009 | 2.109 | 2.403 | 2.678 | 2.937 | 3.261 | 3.496 |
| 60 | . 679 | . 848 | 1.045 | 1.296 | 1.671 | 2.000 | 2.099 | 2.390 | 2.660 | 2.915 | 3.232 | 3.460 |
| 80 | . 678 | . 846 | 1.043 | 1.292 | 1.664 | 1.990 | 2.088 | 2.374 | 2.639 | 2.887 | 3.195 | 3.416 |
| 100 | . 677 | . 845 | 1.042 | 1.290 | 1.660 | 1.984 | 2.081 | 2.364 | 2.626 | 2.871 | 3.174 | 3.390 |
| 1000 | . 675 | . 842 | 1.037 | 1.282 | 1.646 | 1.962 | 2.056 | 2.330 | 2.581 | 2.813 | 3.098 | 3.300 |
| $\infty$ | . 674 | . 841 | 1.036 | 1.282 | 1.645 | 1.960 | 2.054 | 2.326 | 2.576 | 2.807 | 3.091 | 3.291 |
|  | 50\% | 60\% | 70\% | 80\% | 90\% | 95\% | 96\% | 98\% | 99\% | 99.5\% | 99.8\% | 99.9\% |
|  |  |  |  |  |  | fid | lev |  |  |  |  |  |

Table entry for $p$ is the point $\left(\chi^{2}\right)$ with probability $p$
lying above it.


Table C $\quad \chi^{2}$ critical values

|  | Tail probability $p$ |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| df | . 25 | . 20 | . 15 | . 10 | . 05 | . 025 | . 02 | . 01 | . 005 | . 0025 | . 001 |
| 1 | 1.32 | 1.64 | 2.07 | 2.71 | 3.84 | 5.02 | 5.41 | 6.63 | 7.88 | 9.14 | 10.83 |
| 2 | 2.77 | 3.22 | 3.79 | 4.61 | 5.99 | 7.38 | 7.82 | 9.21 | 10.60 | 11.98 | 13.82 |
| 3 | 4.11 | 4.64 | 5.32 | 6.25 | 7.81 | 9.35 | 9.84 | 11.34 | 12.84 | 14.32 | 16.27 |
| 4 | 5.39 | 5.99 | 6.74 | 7.78 | 9.49 | 11.14 | 11.67 | 13.28 | 14.86 | 16.42 | 18.47 |
| 5 | 6.63 | 7.29 | 8.12 | 9.24 | 11.07 | 12.83 | 13.39 | 15.09 | 16.75 | 18.39 | 20.51 |
| 6 | 7.84 | 8.56 | 9.45 | 10.64 | 12.59 | 14.45 | 15.03 | 16.81 | 18.55 | 20.25 | 22.46 |
| 7 | 9.04 | 9.80 | 10.75 | 12.02 | 14.07 | 16.01 | 16.62 | 18.48 | 20.28 | 22.04 | 24.32 |
| 8 | 10.22 | 11.03 | 12.03 | 13.36 | 15.51 | 17.53 | 18.17 | 20.09 | 21.95 | 23.77 | 26.12 |
| 9 | 11.39 | 12.24 | 13.29 | 14.68 | 16.92 | 19.02 | 19.68 | 21.67 | 23.59 | 25.46 | 27.88 |
| 10 | 12.55 | 13.44 | 14.53 | 15.99 | 18.31 | 20.48 | 21.16 | 23.21 | 25.19 | 27.11 | 29.59 |
| 11 | 13.70 | 14.63 | 15.77 | 17.28 | 19.68 | 21.92 | 22.62 | 24.72 | 26.76 | 28.73 | 31.26 |
| 12 | 14.85 | 15.81 | 16.99 | 18.55 | 21.03 | 23.34 | 24.05 | 26.22 | 28.30 | 30.32 | 32.91 |
| 13 | 15.98 | 16.98 | 18.20 | 19.81 | 22.36 | 24.74 | 25.47 | 27.69 | 29.82 | 31.88 | 34.53 |
| 14 | 17.12 | 18.15 | 19.41 | 21.06 | 23.68 | 26.12 | 26.87 | 29.14 | 31.32 | 33.43 | 36.12 |
| 15 | 18.25 | 19.31 | 20.60 | 22.31 | 25.00 | 27.49 | 28.26 | 30.58 | 32.80 | 34.95 | 37.70 |
| 16 | 19.37 | 20.47 | 21.79 | 23.54 | 26.30 | 28.85 | 29.63 | 32.00 | 34.27 | 36.46 | 39.25 |
| 17 | 20.49 | 21.61 | 22.98 | 24.77 | 27.59 | 30.19 | 31.00 | 33.41 | 35.72 | 37.95 | 40.79 |
| 18 | 21.60 | 22.76 | 24.16 | 25.99 | 28.87 | 31.53 | 32.35 | 34.81 | 37.16 | 39.42 | 42.31 |
| 19 | 22.72 | 23.90 | 25.33 | 27.20 | 30.14 | 32.85 | 33.69 | 36.19 | 38.58 | 40.88 | 43.82 |
| 20 | 23.83 | 25.04 | 26.50 | 28.41 | 31.41 | 34.17 | 35.02 | 37.57 | 40.00 | 42.34 | 45.31 |
| 21 | 24.93 | 26.17 | 27.66 | 29.62 | 32.67 | 35.48 | 36.34 | 38.93 | 41.40 | 43.78 | 46.80 |
| 22 | 26.04 | 27.30 | 28.82 | 30.81 | 33.92 | 36.78 | 37.66 | 40.29 | 42.80 | 45.20 | 48.27 |
| 23 | 27.14 | 28.43 | 29.98 | 32.01 | 35.17 | 38.08 | 38.97 | 41.64 | 44.18 | 46.62 | 49.73 |
| 24 | 28.24 | 29.55 | 31.13 | 33.20 | 36.42 | 39.36 | 40.27 | 42.98 | 45.56 | 48.03 | 51.18 |
| 25 | 29.34 | 30.68 | 32.28 | 34.38 | 37.65 | 40.65 | 41.57 | 44.31 | 46.93 | 49.44 | 52.62 |
| 26 | 30.43 | 31.79 | 33.43 | 35.56 | 38.89 | 41.92 | 42.86 | 45.64 | 48.29 | 50.83 | 54.05 |
| 27 | 31.53 | 32.91 | 34.57 | 36.74 | 40.11 | 43.19 | 44.14 | 46.96 | 49.64 | 52.22 | 55.48 |
| 28 | 32.62 | 34.03 | 35.71 | 37.92 | 41.34 | 44.46 | 45.42 | 48.28 | 50.99 | 53.59 | 56.89 |
| 29 | 33.71 | 35.14 | 36.85 | 39.09 | 42.56 | 45.72 | 46.69 | 49.59 | 52.34 | 54.97 | 58.30 |
| 30 | 34.80 | 36.25 | 37.99 | 40.26 | 43.77 | 46.98 | 47.96 | 50.89 | 53.67 | 56.33 | 59.70 |
| 40 | 45.62 | 47.27 | 49.24 | 51.81 | 55.76 | 59.34 | 60.44 | 63.69 | 66.77 | 69.70 | 73.40 |
| 50 | 56.33 | 58.16 | 60.35 | 63.17 | 67.50 | 71.42 | 72.61 | 76.15 | 79.49 | 82.66 | 86.66 |
| 60 | 66.98 | 68.97 | 71.34 | 74.40 | 79.08 | 83.30 | 84.58 | 88.38 | 91.95 | 95.34 | 99.61 |
| 80 | 88.13 | 90.41 | 93.11 | 96.58 | 101.9 | 106.6 | 108.1 | 112.3 | 116.3 | 120.1 | 124.8 |
| 100 | 109.1 | 111.7 | 114.7 | 118.5 | 124.3 | 129.6 | 131.1 | 135.8 | 140.2 | 144.3 | 149.4 |

## THEEXAM

The AP Statistics Exam is three hours long and seeks to determine how well a student has mastered the concepts and techniques of the subject matter of the course. This paper-and-pencil exam consists of (1) a 90 -minute multiple-choice section testing proficiency in a wide variety of topics, and (2) a 90 -minute free-response section requiring the student to answer open-ended questions and to complete an investigative task involving more extended reasoning. In the determination of the grade for the exam, the two sections will be given equal weight.

Each student will be expected to bring a graphing calculator with statistical capabilities to the exam. The expected computational and graphic features for these calculators are described in an earlier section. Minicomputers, pocket organizers, electronic writing pads (e.g., Newton), and calculators with QWERTY (i.e., typewriter) keyboards will not be allowed. Calculator memories will not be cleared. However, calculator memories may be used only for storing programs, not for storing notes. During the exam, students are not permitted to have access to any information in their graphing calculators or elsewhere that is not directly related to upgrading the statistical functionality of older graphing calculators to make them comparable to statistical features found on newer models. Acceptable upgrades include improving the calculator's computational functionalities and/or graphical functionalities for data that students key into the calculator while taking the exam. Unacceptable enhancements include, but are not limited to, keying or scanning text or response templates into the calculator. Students attempting to augment the capabilities of their graphing calculators in any way other than for the purpose of upgrading features as described above will be considered to be cheating on the exam. A student may bring up to two calculators to the exam.

## Multiple-Choice Questions

The following are examples of the kinds of multiple-choice questions found on the AP Statistics Exam; the answers to these questions follow question 18. The distribution of topics and the levels of difficulty are illustrative of the composition of the exam; however, this group of questions does not constitute a complete exam, nor does it show the complete range of questions that appear in an exam.

Students often ask whether they should guess on the multiple-choice section. Haphazard or random guessing is unlikely to improve scores, because one-fourth of the number of questions answered incorrectly will be subtracted from the number of questions answered correctly. However, students who have some knowledge of a question and can eliminate one or more answer choices will usually find it advantageous to guess from among the remaining choices.


1. In the scatterplot of $y$ versus $x$ shown above, the least squares regression line is superimposed on the plot. Which of the following points has the largest residual?
(A) $A$
(в) $B$
(c) $C$
(D) $D$
(e) $E$
2. Under which of the following conditions is it preferable to use stratified random sampling rather than simple random sampling?
(A) The population can be divided into a large number of strata so that each stratum contains only a few individuals.
(B) The population can be divided into a small number of strata so that each stratum contains a large number of individuals.
(c) The population can be divided into strata so that the individuals in each stratum are as much alike as possible.
(D) The population can be divided into strata so that the individuals in each stratum are as different as possible.
(E) The population can be divided into strata of equal sizes so that each individual in the population still has the same chance of being selected.
3. All bags entering a research facility are screened. Ninety-seven percent of the bags that contain forbidden material trigger an alarm. Fifteen percent of the bags that do not contain forbidden material also trigger the alarm. If 1 out of every 1,000 bags entering the building contains forbidden material, what is the probability that a bag that triggers the alarm will actually contain forbidden material?
(A) 0.00097
(B) 0.00640
(c) 0.03000
(D) 0.14550
(Е) 0.97000
4. A candy company claims that 10 percent of its candies are blue. A random sample of 200 of these candies is taken, and 16 are found to be blue. Which of the following tests would be most appropriate for establishing whether the candy company needs to change its claim?
(A) Matched pairs $t$-test
(B) One-sample proportion $z$-test
(C) Two-sample $t$-test
(D) Two-sample proportion $z$-test
(E) Chi-square test of association

DESCRIPTIVE STATISTICS

| Variable | N | Mean | Median | TrMean | StDev | SE Mean |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| score | 50 | 1045.7 | 1024.7 | 1041.9 | 221.9 | 31.4 |
| Variable | Minimum | Maximum | Q1 | Q3 |  |  |
| score | 628.9 | 1577.1 | 877.7 | 1219.5 |  |  |

5. Some descriptive statistics for a set of test scores are shown above. For this test, a certain student has a standardized score of $z=-1.2$. What score did this student receive on the test?
(A) 266.28
(в) 779.42
(c) 1008.02
(D) 1083.38
(E) 1311.98
6. In a test of $H_{0}: \mu=8$ versus $H_{a}: \mu \neq 8$, a sample of size 220 leads to a $p$-value of 0.034 . Which of the following must be true?
(A) A 95\% confidence interval for $\mu$ calculated from these data will not include $\mu=8$.
(в) At the $5 \%$ level if $\mathrm{H}_{0}$ is rejected, the probability of a Type II error is 0.034 .
(c) The $95 \%$ confidence interval for $\mu$ calculated from these data will be centered at $\mu=8$.
(D) The null hypothesis should not be rejected at the $5 \%$ level.
(E) The sample size is insufficient to draw a conclusion with $95 \%$ confidence.
7. A summer resort rents rowboats to customers but does not allow more than four people to a boat. Each boat is designed to hold no more than 800 pounds. Suppose the distribution of adult males who rent boats, including their clothes and gear, is normal with a mean of 190 pounds and standard deviation of 10 pounds. If the weights of individual passengers are independent, what is the probability that a group of four adult male passengers will exceed the acceptable weight limit of 800 pounds?
(A) 0.023
(в) 0.046
(c) 0.159
(D) 0.317
(Е) 0.977
8. Consider a data set of positive values, at least two of which are not equal. Which of the following sample statistics will be changed when each value in this data set is multiplied by a constant whose absolute value is greater than 1 ?
I. The mean
II. The median
III. The standard deviation
(A) I only
(B) II only
(c) III only
(D) I and II only
(E) I, II, and III
9. Each person in a simple random sample of 2,000 received a survey, and 317 people returned their survey. How could nonresponse cause the results of the survey to be biased?
(A) Those who did not respond reduced the sample size, and small samples have more bias than large samples.
(в) Those who did not respond caused a violation of the assumption of independence.
(c) Those who did not respond were indistinguishable from those who did not receive the survey.
(D) Those who did not respond represent a stratum, changing the simple random sample into a stratified random sample.
(E) Those who did respond may differ in some important way from those who did not respond.
10. In a certain game, a fair die is rolled and a player gains 20 points if the die shows a " 6 ." If the die does not show a " 6 ," the player loses 3 points. If the die were to be rolled 100 times, what would be the expected total gain or loss for the player?
(A) A gain of about 1,700 points
(в) A gain of about 583 points
(c) A gain of about 83 points
(D) A loss of about 250 points
(E) A loss of about 300 points
11. The Attila Barbell Company makes bars for weight lifting. The weights of the bars are independent and are normally distributed with a mean of 720 ounces ( 45 pounds) and a standard deviation of 4 ounces. The bars are shipped 10 in a box to the retailers. The weights of the empty boxes are normally distributed with a mean of 320 ounces and a standard deviation of 8 ounces. The weights of the boxes filled with 10 bars are expected to be normally distributed with a mean of 7,520 ounces and a standard deviation of
(A) $\sqrt{12}$ ounces
(B) $\sqrt{80}$ ounces
(c) $\sqrt{224}$ ounces
(D) 48 ounces
(E) $\sqrt{1,664}$ ounces
12. Exercise physiologists are investigating the relationship between lean body mass (in kilograms) and the resting metabolic rate (in calories per day) in sedentary males.

| Predictor | Coef | StDev | T | P |
| :--- | :---: | :---: | :---: | :---: |
| Constant | 264.0 | 276.9 | 0.95 | 0.363 |
| Mass | 22.563 | 6.360 | 3.55 | 0.005 |
|  |  |  |  |  |
| S $=144.9$ | R-Sq $=55.7 \%$ | $\mathrm{R}-\mathrm{Sq}(\mathrm{adj})=51.3 \%$ |  |  |

Based on the computer output above, which of the following is the best interpretation of the value of the slope of the regression line?
(A) For each additional kilogram of lean body mass, the resting metabolic rate increases on average by 22.563 calories per day.
(в) For each additional kilogram of lean body mass, the resting metabolic rate increases on average by 264.0 calories per day.
(c) For each additional kilogram of lean body mass, the resting metabolic rate increases on average by 144.9 calories per day.
(D) For each additional calorie per day for the resting metabolic rate, the lean body mass increases on average by 22.563 kilograms.
(e) For each additional calorie per day for the resting metabolic rate, the lean body mass increases on average by 264.0 kilograms.
13. An investigator was studying a territorial species of Central American termites, Nasutitermes corniger. Forty-nine termite pairs were randomly selected; both members of each of these pairs were from the same colony. Fifty-five additional termite pairs were randomly selected; the two members in each of these pairs were from different colonies. The pairs were placed in petri dishes and observed to see whether they exhibited aggressive behavior. The results are shown in the table below.

|  | Aggressive | Nonaggressive | Total |
| :---: | :---: | :---: | ---: |
| Same colony | $40(33.5)$ | $9(15.5)$ | 49 |
| Different colonies | $31(37.5)$ | $24(17.5)$ | 55 |
| Total | 71 | 33 | 104 |

A Chi-square test for homogeneity was conducted, resulting in $\chi^{2}=7.638$. The expected counts are shown in parentheses in the table. Which of the following sets of statements follows from these results?
(A) $\chi^{2}$ is not significant at the 0.05 level.
(B) $\chi^{2}$ is significant, $0.01<p<0.05$; the counts in the table suggest that termite pairs from the same colony are less likely to be aggressive than termite pairs from different colonies.
(c) $\chi^{2}$ is significant, $0.01<p<0.05$; the counts in the table suggest that termite pairs from different colonies are less likely to be aggressive than termite pairs from the same colony.
(D) $\chi^{2}$ is significant, $p<0.01$; the counts in the table suggest that termite pairs from the same colony are less likely to be aggressive than termite pairs from different colonies.
(E) $\chi^{2}$ is significant, $p<0.01$; the counts in the table suggest that termite pairs from different colonies are less likely to be aggressive than termite pairs from the same colony.
14. Consider $n$ pairs of numbers $\left(x_{1}, y_{1}\right),\left(x_{2}, y_{2}\right), \ldots$, and $\left(x_{n}, y_{n}\right)$. The mean and standard deviation of the $x$-values are $\bar{x}=5$ and $s_{x}=4$, respectively. The mean and standard deviation of the $y$-values are $\bar{y}=10$ and $s_{y}=10$, respectively. Of the following, which could be the least squares regression line?
(A) $\hat{y}=-5.0+3.0 x$
(B) $\hat{y}=3.0 x$
(C) $\hat{y}=5.0+2.5 x$
(D) $\hat{y}=8.5+0.3 x$
(E) $\hat{y}=10.0+0.4 x$
15. The mayor of a large city will run for governor if he believes that more than 30 percent of the voters in the state already support him. He will have a survey firm ask a random sample of $n$ voters whether or not they support him. He will use a large sample test for proportions to test the null hypothesis that the proportion of all voters who support him is 30 percent or less against the alternative that the percentage is higher than 30 percent. Suppose that 35 percent of all voters in the state actually support him. In which of the following situations would the power for this test be highest?
(A) The mayor uses a significance level of 0.01 and $n=250$ voters.
(в) The mayor uses a significance level of 0.01 and $n=500$ voters.
(c) The mayor uses a significance level of 0.01 and $n=1,000$ voters.
(D) The mayor uses a significance level of 0.05 and $n=500$ voters.
(E) The mayor uses a significance level of 0.05 and $n=1,000$ voters.
16. George and Michelle each claimed to have the better recipe for chocolate chip cookies. They decided to conduct a study to determine whose cookies were really better. They each baked a batch of cookies using their own recipe. George asked a random sample of his friends to taste his cookies and to complete a questionnaire on their quality. Michelle asked a random sample of her friends to complete the same questionnaire for her cookies. They then compared the results. Which of the following statements about this study is false?
(A) Because George and Michelle have a different population of friends, their sampling procedure makes it difficult to compare the recipes.
(в) Because George and Michelle each used only their own respective recipes, their cooking ability is confounded with the recipe quality.
(c) Because George and Michelle each used only the ovens in their houses, the recipe quality is confounded with the characteristics of the oven.
(D) Because George and Michelle used the same questionnaire, their results will generalize to the combined population of their friends.
(e) Because George and Michelle each baked one batch, there is no replication of the cookie recipes.
17. A large company is considering opening a franchise in St. Louis and wants to estimate the mean household income for the area using a simple random sample of households. Based on information from a pilot study, the company assumes that the standard deviation of household incomes is $\sigma=\$ 7,200$. Of the following, which is the least number of households that should be surveyed to obtain an estimate that is within $\$ 200$ of the true mean household income with 95 percent confidence?
(A) 75
(в) 1,300
(c) 5,200
(D) 5,500
(Е) 7,700
18. Courtney has constructed a cricket out of paper and rubber bands. According to the instructions for making the cricket, when it jumps it will land on its feet half of the time and on its back the other half of the time. In the first 50 jumps, Courtney's cricket landed on its feet 35 times. In the next 10 jumps, it landed on its feet only twice. Based on this experience, Courtney can conclude that
(A) the cricket was due to land on its feet less than half the time during the final 10 jumps, since it had landed too often on its feet during the first 50 jumps
(в) a confidence interval for estimating the cricket's true probability of landing on its feet is wider after the final 10 jumps than it was before the final 10 jumps
(c) a confidence interval for estimating the cricket's true probability of landing on its feet after the final 10 jumps is exactly the same as it was before the final 10 jumps
(D) a confidence interval for estimating the cricket's true probability of landing on its feet is more narrow after the final 10 jumps than it was before the final 10 jumps
(E) a confidence interval for estimating the cricket's true probability of landing on its feet based on the initial 50 jumps does not include 0.2 , so there must be a defect in the cricket's construction to account for the poor showing in the final 10 jumps

## Answers to Multiple-Choice Questions

| $1-\mathrm{A}$ | $4-\mathrm{B}$ | $7-\mathrm{A}$ | $10-\mathrm{C}$ | $13-\mathrm{E}$ | $16-\mathrm{D}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $2-\mathrm{C}$ | $5-\mathrm{B}$ | $8-\mathrm{E}$ | $11-\mathrm{C}$ | $14-\mathrm{D}$ | $17-\mathrm{C}$ |
| $3-\mathrm{B}$ | $6-\mathrm{A}$ | $9-\mathrm{E}$ | $12-\mathrm{A}$ | $15-\mathrm{E}$ | $18-\mathrm{D}$ |

## Free-Response Questions

In the free-response section of the AP Statistics Exam, students are asked to answer five questions and complete an investigative task. Each question is designed to be answered in approximately 12 minutes. The longer investigative task is designed to be answered in approximately 30 minutes.

Statistics is a discipline in which clear and complete communication is an essential skill. The free-response questions on the AP Statistics Exam require students to use their analytical, organizational, and communication skills to formulate cogent answers and provide students with an opportunity to:

- Relate two or more different content areas (i.e., exploratory data analysis, experimental design and sampling, probability, and statistical inference) as they formulate a complete response or solution to a statistics or probability problem.
- Demonstrate their mastery of statistics in a response format that permits the students to determine how they will organize and present each response.

The purpose of the investigative task is not only to evaluate the student's understanding in several content areas but also to assess his or her ability to integrate statistical ideas and apply them in a new context or in a nonroutine way.

## Scoring of Free-Response Questions

The evaluation of student responses on the free-response section of the AP Statistics Exam reflects the dual importance of statistical knowledge and good communication. The free-response questions and the investigative task are scored "holistically"; that is, each question's response is evaluated as "a complete package." With holistic scoring, after reading through the details of a student's response, the scorer makes a judgment about the overall quality of the response. This is different from "analytic" scoring, where the individual components to be evaluated in a student's response are specified in advance, and each component is given a value counting toward the overall score.

Holistic scoring is well suited for questions where the student is required to synthesize information and respond at least partially in written paragraphs, and for questions that could potentially generate multiple and diverse, but equally correct, responses. For example, an open-ended question may present data from a real-life study and ask the student not only to analyze the data but also to comment on how the study's protocol might be improved. Comments on improving the protocol might focus on improving the sampling method, controlling confounding variables, or seeking more power by increasing the sample size. In this context, holistic scoring represents a recognition not only of the existence of multiple reasonable approaches to a statistical analysis, but a realization of the existence of a statistical synergyi.e., that a quality student response is more than just the sum of its parts.

The AP Statistics scoring guideline (rubric) for each free-response question has five categories, numerically scored on a 0 to 4 scale. Each of these categories represents a level of quality in the student response. These levels of quality are defined on two dimensions: statistical knowledge and communication. The specific rubrics for each question are tied to a general template, which represents the descriptions of the quality levels as envisioned by the Development Committee. This general template is given in the following table, "A Guide to Scoring Free-Response Statistics Questions."

## A GUIDE TO SCORING FREE-RESPONSE STATISTICS QUESTIONS: THE CATEGORY DESCRIPTORS

| Score Descriptors | Statistical Knowledge | Communication |
| :---: | :---: | :---: |
|  | Identification of the important components of the problem Demonstration of the statistical concepts and techniques that result in a correct solution of the problem | Explanation of what was done and why, along with a statement of conclusions drawn in context |
| 4 Complete | - shows complete understanding of the problem's statistical components <br> - synthesizes a correct relationship among these components, perhaps with novelty and creativity <br> - uses appropriate and correctly executed statistical techniques <br> - May have minor arithmetic errors, but answers are still reasonable | - provides a clear, organized, and complete explanation, using correct terminology, of what was done and why <br> - states appropriate assumptions and caveats <br> - uses diagrams or plots when appropriate to aid in describing the solution <br> - states an appropriate and complete conclusion in context |


| $3$ <br> Substantial | - shows substantial understanding of the problem's statistical components <br> - synthesizes a relationship among these components, perhaps with minor gaps <br> - uses appropriate statistical techniques <br> - may have arithmetic errors, but answers are still reasonable | - provides a clear but not perfectly organized explanation, using correct terminology, of what was done and why, but explanation may be slightly incomplete <br> - may miss necessary assumptions or caveats <br> - uses diagrams or plots when appropriate to aid in describing the solution <br> - states a conclusion that follows from the analysis but may be somewhat incomplete |
| :---: | :---: | :---: |
| 2 <br> Developing | - shows some understanding of the problem's statistical components <br> - shows little in the way of a relationship among these components <br> - uses some appropriate statistical techniques, but misses or misuses others <br> - may have arithmetic errors that result in unreasonable answers | - provides some explanation of what was done, but explanation may be vague and difficult to interpret and terminology may be somewhat inappropriate <br> - uses diagrams in an incomplete or ineffective way, or diagrams may be missing <br> - states a conclusion that is incomplete |
| $\begin{aligned} & 1 \\ & \text { Minimal } \end{aligned}$ | - shows limited understanding of the problem's statistical components by failing to identify important components <br> - shows little ability to organize a solution and may use irrelevant information <br> - misuses or fails to use appropriate statistical techniques <br> - has arithmetic errors that result in unreasonable answers | - provides minimal or unclear explanation of what was done or why it was done, and explanation may not match the presented solution <br> - fails to use diagrams or plots, or uses them incorrectly <br> - states an incorrect conclusion or fails to state a conclusion |
| 0 | - shows little to no understanding of statistical components | - provides no explanation of a legitimate strategy |

Some important points that students should remember when answering free-response questions on the AP Statistics Exam are given below.

1. Read the questions carefully and answer them in context; for example, the results of a hypothesis test should always be followed by a conclusion in context, and a confidence interval should always be followed by an interpretation of the interval in context. Explanations and conclusions in context are always required for a complete answer.
2. Know the vocabulary of statistics, and use that vocabulary correctly in all written responses.
3. Remember to define all symbols. Specifically, remember to distinguish between population parameters and sample statistics.
4. Remember to state and check all necessary assumptions when performing hypothesis tests and constructing interval estimates.
5. Be able to interpret data displayed in a variety of ways, including graphs and computer outputs. Be able to represent data in a variety of forms and base sound statistical arguments on these representations.

AP Central contains free-response questions, scoring guidelines, and selected student responses from past AP Statistics Exams. This is an excellent place to become more familiar with the content of past free-response questions and how they were scored.
The following questions are examples of free-response questions. These questions were administered as part of a previous year's exam.

1. The summary statistics for the number of inches of rainfall in Los Angeles for 117 years, beginning in 1877, are shown below.

| N | MEAN | MEDIAN | TRMEAN | STDEV | SE MEAN |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 117 | 14.941 | 13.070 | 14.416 | 6.747 | 0.624 |


| MIN | MAX | Q1 | Q3 |
| :---: | :---: | :---: | :---: |
| 4.850 | 38.180 | 9.680 | 19.250 |

(a) Describe a procedure that uses these summary statistics to determine whether there are outliers.
(b) Are there outliers in these data?

Justify your answer based on the procedure that you described in part (a).
(c) The news media reported that in a particular year, there were only 10 inches of rainfall. Use the information provided to comment on this reported statement.
2. A department supervisor is considering purchasing one of two comparable photocopy machines, $A$ or $B$. Machine $A$ costs $\$ 10,000$ and machine $B$ costs $\$ 10,500$. This department replaces photocopy machines every three years. The repair contract for machine $A$ costs $\$ 50$ per month and covers an unlimited number of repairs. The repair contract for machine $B$ costs $\$ 200$ per repair. Based on past performance, the distribution of the number of repairs needed over any one-year period for machine $B$ is shown below.

| Number of Repairs | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: |
| Probability | 0.50 | 0.25 | 0.15 | 0.10 |

You are asked to give a recommendation based on overall cost as to which machine, $A$ or $B$, along with its repair contract, should be purchased. What would your recommendation be? Give a statistical justification to support your recommendation.
3. Every Monday a local radio station gives coupons away to 50 people who correctly answer a question about a news fact from the previous day's newspaper. The coupons given away are numbered from 1 to 50 , with the first person receiving coupon 1 , the second person receiving coupon 2 , and so on, until all 50 coupons are given away. On the following Saturday, the radio station randomly draws numbers from 1 to 50 and awards cash prizes to the holders of the coupons with these numbers. Numbers continue to be drawn without replacement until the total amount awarded first equals or exceeds $\$ 300$. If selected, coupons 1 through 5 each have a cash value of $\$ 200$, coupons 6 through 20 each have a cash value of $\$ 100$, and coupons 21 through 50 each have a cash value of $\$ 50$.
(a) Explain how you would conduct a simulation using the random number table provided below to estimate the distribution of the number of prize winners each week.
(b) Perform your simulation three times. (That is, run three trials of your simulation.) Start at the leftmost digit in the first row of the table and move across. Make your procedure clear so that someone can follow what you did. You must do this by marking directly on or above the table. Report the number of winners in each of your three trials.
$7274913347 \quad 65030 \quad 26128 \quad 49067 \quad 029044995374674 \quad 9461713317$
$81638365664270933717 \quad 599431202746547 \quad 613034669976423$
$38449464389157901907 \quad 721460576422400944904983309258$
4. Students are designing an experiment to compare the productivity of two varieties of dwarf fruit trees. The site for the experiment is a field that is bordered by a densely forested area on the west (left) side. The field has been divided into eight plots of approximately the same area. The students have decided that the test plots should be blocked. Four trees, two of each of the two varieties, will be assigned at random to the four plots within each block, with one tree planted in each plot.

The two blocking schemes shown below are under consideration.
For each scheme, one block is indicated by the white region and the other block is indicated by the gray region in the figures.

(a) Which of the blocking schemes, A or B , is better for this experiment? Explain your answer.
(b) Even though the students have decided to block, they must randomly assign the varieties of trees to the plots within each block. What is the purpose of this randomization in the context of this experiment?
5. A growing number of employers are trying to hold down the costs that they pay for medical insurance for their employees. As part of this effort, many medical insurance companies are now requiring clients to use generic brand medicines when filling prescriptions. An independent consumer advocacy group wanted to determine if there was a difference, in milligrams, in the amount of active ingredient between a certain "name" brand drug and its generic counterpart. Pharmacies may store drugs under different conditions. Therefore, the consumer group randomly selected ten different pharmacies in a large city and filled two prescriptions at each of these pharmacies, one for the "name" brand and the other for the generic brand of the drug. The consumer group's laboratory then tested a randomly selected pill from each prescription to determine the amount of active ingredient in the pill. The results are given in the following table.

## ACTIVE INGREDIENT

(in milligrams)

| Pharmacy | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Name brand | 245 | 244 | 240 | 250 | 243 | 246 | 246 | 246 | 247 | 250 |
| Generic brand | 246 | 240 | 235 | 237 | 243 | 239 | 241 | 238 | 238 | 234 |

Based on these results, what should the consumer group's laboratory report about the difference in the active ingredient in the two brands of pills? Give appropriate statistical evidence to support your response.
6. The statistics department at a large university is trying to determine if it is possible to predict whether an applicant will successfully complete the Ph.D. program or will leave before completing the program. The department is considering whether GPA (grade point average) in undergraduate statistics and mathematics courses (a measure of performance) and mean number of credit hours per semester (a measure of workload) would be helpful measures. To gather data, a random sample of 20 entering students from the past 5 years is taken. The data are given below.

Successfully Completed Ph.D. Program

| Student | A | B | C | D | E | F | G | H | I | J | K | L | M |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| GPA | 3.8 | 3.5 | 4.0 | 3.9 | 2.9 | 3.5 | 3.5 | 4.0 | 3.9 | 3.0 | 3.4 | 3.7 | 3.6 |
| Credit <br> hours | 12.7 | 13.1 | 12.5 | 13.0 | 15.0 | 14.7 | 14.5 | 12.0 | 13.1 | 15.3 | 14.6 | 12.5 | 14.0 |

Did Not Complete Ph.D. Program

| Student | N | O | P | Q | R | S | T |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| GPA | 3.6 | 2.9 | 3.1 | 3.5 | 3.9 | 3.6 | 3.3 |
| Credit <br> hours | 11.1 | 14.5 | 14.0 | 10.9 | 11.5 | 12.1 | 12.0 |

The regression output below resulted from fitting a line to the data in each group. The residual plots (not shown) indicated no unusual patterns, and the assumptions necessary for inference were judged to be reasonable.

Successfully Completed Ph.D. Program

| Predictor | Coef | StDev | T | P |
| :--- | :--- | :--- | :--- | :---: |
| Constant | 23.514 | 1.684 | 13.95 | 0.000 |
| GPA | -2.7555 | 0.4668 | -5.90 | 0.000 |
| $\mathrm{~S}=0.5658$ | $\mathrm{R}-\mathrm{Sq}=76.0 \%$ |  |  |  |

Did Not Complete Ph.D. Program

| Predictor | Coef | StDev | T | P |
| :--- | :---: | :---: | :---: | :---: |
| Constant | 24.200 | 3.474 | 6.97 | 0.001 |
| GPA | -3.485 | 1.013 | -3.44 | 0.018 |
| $\mathrm{~S}=0.8408$ | $\mathrm{R}-\mathrm{Sq}=70.3 \%$ |  |  |  |

(a) Use an appropriate graphical display to compare the GPA's for the two groups. Write a few sentences commenting on your display.
(b) For the students who successfully completed the Ph.D. program, is there a significant relationship between GPA and mean number of credit hours per semester? Give a statistical justification to support your response.
(c) If a new applicant has a GPA of 3.5 and a mean number of credit hours per semester of 14.0, do you think this applicant will successfully complete the Ph.D. program? Give a statistical justification to support your response.

## Teacher Support

## AP Central ${ }^{\circledR}$ (apcentral.collegeboard.com)

You can find the following Web resources at AP Central (free registration required):

- AP Course Descriptions, AP Exam questions and scoring guidelines, sample syllabi, and feature articles.
- A searchable Institutes and Workshops database, providing information about professional development events.
- The Course Home Pages (apcentral.collegeboard.com/coursehomepages), which contain insightful articles, teaching tips, activities, lab ideas, and other course-specific content contributed by colleagues in the AP community.
- Moderated electronic discussion groups (EDGs) for each AP course, provided to facilitate the exchange of ideas and practices.


## AP Publications and Other Resources

Free AP resources are available to help students, parents, AP Coordinators, and high school and college faculty learn more about the AP Program and its courses and exams. Visit apcentral.collegeboard.com/freepubs.

Teacher's Guides and Course Descriptions may be downloaded free of charge from AP Central; printed copies may be purchased through the College Board Store (store.collegeboard.com). Released Exams and other priced AP resources are available at the College Board Store.

## Teacher's Guides

For those about to teach an AP course for the first time, or for experienced AP teachers who would like to get some fresh ideas for the classroom, the Teacher's Guide is an excellent resource. Each Teacher's Guide contains syllabi developed by high school teachers currently teaching the AP course and college faculty who teach the equivalent course at colleges and universities. Along with detailed course outlines and innovative teaching tips, you'll also find extensive lists of suggested teaching resources.

## Course Descriptions

Course Descriptions are available for each AP subject. They provide an outline of each AP course's content, explain the kinds of skills students are expected to demonstrate in the corresponding introductory college-level course, and describe the AP Exam. Sample multiple-choice questions with an answer key and sample free-response questions are included. (The Course Description for AP Computer Science is available in PDF format only.)

## Released Exams

Periodically the AP Program releases a complete copy of each exam. In addition to providing the multiple-choice questions and answers, the publication describes the process of scoring the free-response questions and includes examples of students' actual responses, the scoring standards, and commentary that explains why the responses received the scores they did.

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