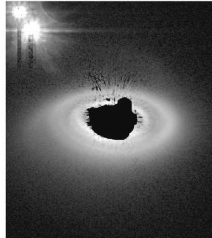
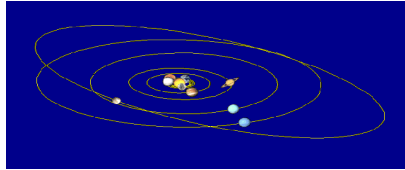


Planet Formation (in the Solar System)



Planets in the solar system were formed **in a disk**
 ---proto-planetary nebula (or, solar nebula)---
 ~4.6 Gyr ago.

We have an incomplete theory on how this worked.
 But improving as more extra-solar systems are discovered...

dust disk of HD141569A

- concepts:
- 1) Minimum-mass solar nebula.
 - 2) Planetesimal hypothesis.
 - 3) Frost line.

- application: 4) Story about giant & terrestrial planet formation.
 test: 5) Isotope dating results; possible problems.

Solar nebula: the **disk** surrounding the newly formed Sun

- High angular momentum, does not fall into the Sun directly
- Likely had the same elemental composition as the Sun
Sun: H 70% H, He 28%, C, N, O ~1.3%, Ne ~ 0.17%, Mg, Al, Si, S, Ca, Fe, Ni ~0.36%
 --- also seen in meteorites
- A substantial nebula likely existed for a few Myr,
 then, either accreted to the star or blown away by stellar winds & UV
 + a **small** fraction locked into planets

Minimum-mass solar nebula

Current mass sum: ~ 1.5 M_J ~ 0.0015 M_☉, originally must be a lot more

Reconstruction of a minimum disk (lower limit):

Replenish all planets back to solar abundance, add them all up
*(Mercury: *350, Earth: *235, Jupiter: *5, Saturn: *8, Uranus: *15...)*

Yields a minimum mass for the solar nebula

$$M_{\text{MMSN}} \sim 10 M_{\text{J}} \sim 0.01 M_{\odot}$$

density decreases outward

*at least 85% lost (preceding generations of planets?)
 used as starting points in theoretical modeling
 compatible with many other observed disks*

Evolution of the nebula depends on its initial mass (stability, temperature...)

2) Can planets form in the solar nebula by direct gravitational collapse, just like how stars are thought to form?

No. At least not likely in the case of M_{MMSN} (too low by a factor of ~20)

Tidal gravity from the Sun far exceeds the self-gravity of a sphere of gas
(tidal bulge > size of sphere that wants to collapse)

3) The planetesimal hypothesis

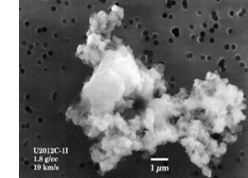
Planets are formed step-by-step, starting from dust particles as small as a virus

- 1) Disk cools, rock/icy grains condense, forming micron-sized dust grains (mass ~10⁻¹⁵ kg, micron)
- 2) Sticking together, these form pebbles (~1 g, cm)
- 3) Quick collisions lead to **planetesimals** (~10¹² kg, km) --> the asteroid belt?
- 4) A few planetesimals dominate -- planetary embryos (~ 10¹⁸ kg, 100 km)
- 5) Embryos slowly collide, form planetary cores (~ 10²¹ kg, 1000 km, *proto-Earth*)
- 6) Cores accrete gas and become gaseous planets (~10²² kg, *proto-Jupiter*)

steps 2 & 3: dust *somehow* builds up to **planetesimals** (*stickiness? grav. influence?*)

Many of these planetesimals survive to today

*an interplanetary dust particle
 (glass, carbon, silicates)*

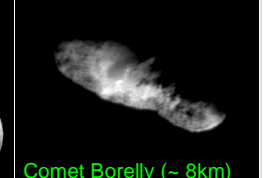


rocky planetesimals
 (< frost line)



Asteroid Eros (~35km)

icy planetesimals
 (> frost line)



Comet Borelly (~ 8km)

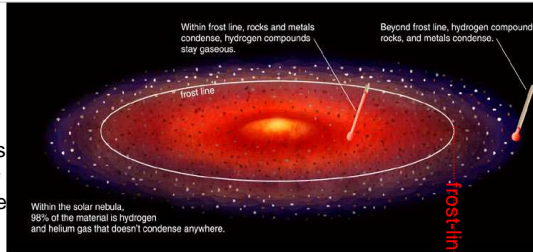
Not everything is collected into planets---there is left-over junk

- 1) Some irregular moons – captured planetesimals
- 2) Kuiper belt -- primordial planetesimals formed at ~30 AU
- 3) Oort cloud -- planetesimals ejected outward by Jupiter & co.
- 4) Early bombardment stage (first ~700 Myr)

These pristine (un-differentiated, un-processed) materials provide a window to the early solar system.

frost line

Distance from Sun where temperature was low enough for hydrogen compounds (H_2O, \dots) to condense into ices, between the present-day orbits of Mars and Jupiter



frost-line $\sim 4AU$

- 1) Rocky planetesimals inside frost-line
 $T_{melt} < 1300 K$, rocks & metals, **refractory**
 Asteroid belt, terrestrial planets, volatiles in gas phase
- 2) Icy planetesimals outside frost-line (H_2O : $T_{melt} \sim 150 K$ @ near vacuum pressure)
 $T_{melt} < 150 K$ (roughly), H_2O -ice, carbon-grains, **volatile**
 Cores of giant planets, Kuiper belt & Oort cloud (comets),
- 3) Higher mass-fraction in solids outside the frost-line (solid mass jumps by ~ 5)
 Carbon, oxygen \sim twice more abundant than heavier elements

Giant & terrestrial planet formation

5th step: planetesimals conglomerate into $10^3 km$ -sized **cores**

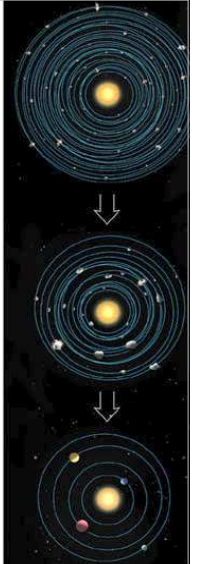
If core massive enough, H & He can be accreted
 ----> a **giant planet**

Jupiter, Saturn, Uranus & Neptune all have cores+gaseous env.

If core does not grow fast enough it cannot accrete gas
 ----> a **terrestrial planet**

Explains

- 1) Giant planets gas rich, terrestrial no gas.
- 2) Giant planets formed outside frost line.
 Enriched in metals + icy-rocky core of $10\text{-}20 M_{\oplus}$
Outside: more solid (ice), smaller velocity, gas easier to accrete
- 3) Terrestrial planets formed inside frost line.
 Contain rocky, refractory material.
- 4) seems to explain our system, but correct?



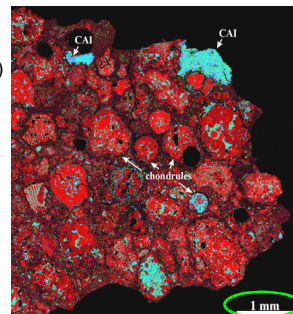
When was the Solar system formed?

---- Isotope dating

The **pristine, leftover junk** is useful: meteorites (asteroids, comets, Moon, Mars...)
(pristine: abundances of parent, daughter & non-radiogenic element un-altered)
not melted since condensation, no differential settling, trap some gas

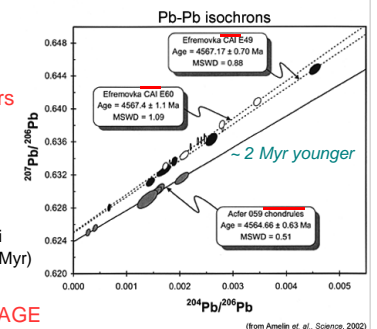
85% of all meteorite finds are **chondrites** (*meteoric stone containing chondrules*)

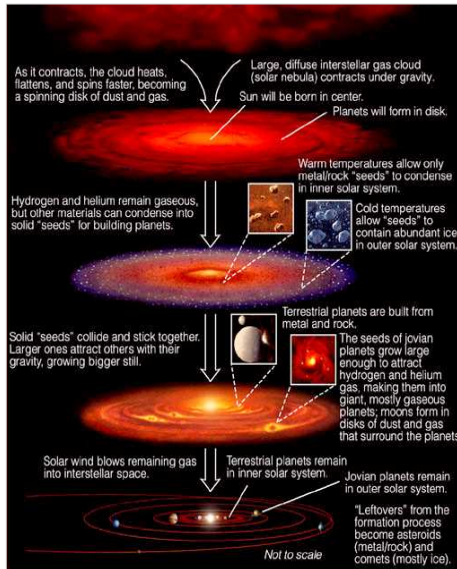
- Abundance pattern remarkably close to the Sun except for H & He, some volatiles, **primordial**
- Chondrules and CAI (calcium-aluminum-inclusion) appear to have been melted once: heating to $\sim 1700 K$ + a rapid cooling (~ 10 min)
Not melted since!



Isotope dating: results

1. The **AGE** of the solar system (from chondrites): **4567.2 ± 0.6 Myrs**
 Dated using long-lived radio-active nuclei (e.g., $^{238}U \rightarrow ^{206}Pb$, $t_{1/2} = 4.47$ Gyr)
2. There was a last supernova a few Myr **before AGE**
 Dating using short-lived radio-active nuclei (e.g. ^{60}Fe , $t_{1/2} = 1.5$ Myrs & ^{26}Al , $t_{1/2} = 0.7$ Myr)
 SS formation triggered by a supernova?
3. Earth formed within ~ 10 Myr **after AGE**
 Relative age dating can be rather accurate using short-lived nuclei (e.g. $^{182}Hf \rightarrow ^{182}W$, $t_{1/2} = 9$ Myr, Yin et. al, Klein et. al, Nature 2002)
TROUBLE FOR THEORISTS!
4. Moon formed within ~ 30 Myr **after AGE**
 Age of Moon (since last melt) ~ 4.5 Gyr, Apollo samples & lunar meteorites.
 Oldest rock on Earth ~ 4.28 Gyr (Nuvvuagittuq, Hudson Bay, QC)
 (rare, most old rock ~ 3.8 Gyr, after late heavy bombardment)
 Mars (since last melt) ~ 4.5 Gyr (Martian meteorites ALH84001 --life?)
 Age of oldest fossils ~ 3.5 Gyr (blue-green algae)





Open issues

have to form planets in ~ few Myrs

- 1) how did the gas disk disperse?
- 2) how are planetesimals made? Are dust grains sufficiently sticky?
- 3) what makes chondrules?
- 4) How do planetesimals survive collisions?
- 5) What is Jupiter's role in the fate of other planets?
- 6) Do giant planets only form outside frost lines? If so, how to explain the extra-solar hot Jupiters?
- 7)....

Origin of the Moon



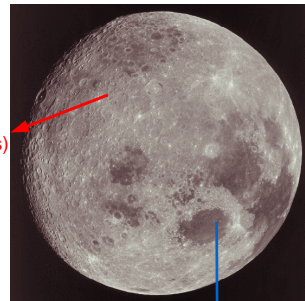
Earth is unique among terrestrial planets in having a large moon
 radius ~ 1737 km, mass ~ 10^{23} kg ~ 1% Earth mass ~ Mercury

- 1) largest satellite/planet mass ratio (except. Pluto/Charon)
- 2) Moon raises tide, lunar cycles
- 3) Moon always faces us with the same side (*nodding -> see 59% of Moon*)
- 4) Moon stabilizes Earth's spin axis/climate

Lunar Geology

no atmosphere, dominated by cratering

- 1) "land" is older & pock-marked
 early solar-system heavy-bombardment stage
 Terraes (lands) craters ~4 Gyr old
- 2) "sea" is younger, smoother
 huge impacts, molten lava (dark)
 end of bombardment stage
- 3) little cratering after the heavy stage,
 no re-surfacing
 surface pulverized by micro-meteorites
(Earth is constantly resurfaced; soil made by weathering & life)
- 4) clues to formation from comparison with Earth
 ~400 kg of lunar rocks returned in '70s
 lunar rock has little water and other volatiles (low boiling T material)
 iron-deficient (small iron core, < 200km)
 similar isotope pattern (e.g. Oxygen, different from meteorites)



Maria (seas) smooth
 3.1-3.8 Gyr old

Various hypothesis for the origins of Planetary Satellites – and of our Moon

capture



Phoebe (@S), Deimos/Phobos(@M)
 Moon: why oxygen isotopes?
 small initial separation?
 very massive?

fission



fast spinning planet
 if above break-up speed
 Moon: why volatiles gone?

accretion disk



primordial accretion disk
 Io, Europa... (@J)
 Moon: why ecliptic plane?
 why volatiles gone?

giant impact



molten ejecta re-collect
 also explain Pluto-Charon?
 Moon: iron-poor, volatile poor
 isotope ratios similar

Current Favourite --- impact

- i) How big was the impactor? (to melt a significant fraction of Earth)

$$\frac{1}{2} m v^2 \approx k_B T \frac{M_E}{\mu m_H}$$

$$v \sim 10 \text{ km/s}, T \sim 5000 \text{ K}, \mu \sim 10 \Rightarrow m \sim 0.05 M_E \sim M_{\text{Mars}}$$

some mass ejected by pressure gradient, formed a disk
In disk: volatiles: vaporized and lost; non-volatiles: molten and re-solidified quickly

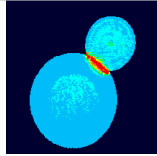
- ii) How fast does a 1 km-size piece of ejecta re-solidify?

$$k_B T \frac{4\pi}{3} R^3 \left(\frac{\rho}{\mu m_H} \right) \approx 4\pi R^2 \sigma T^4 \times t_{\text{solidify}}$$

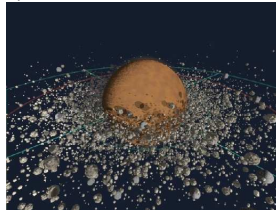
takes mere hours...
(but need to check conduction is not the bottleneck; still should be fast)

- iii) How do the boulders re-collect?
only one moon was formed in the disk
multiple moon-lets
accrete each other by mutual gravity

Kokubo et al.



Canup et al.



Extra Notes: Can planets form in the solar nebula by gravitational collapse -- just like how stars form?

No. At least not likely in our case.

Tidal gravity of the Sun too strong, prevents collapse.

Consider forces on a ball of gas of size d and mass M_{gas} at a distance a from the Sun

$$\text{Tidal force due the Sun: } f_{\text{tide}} \approx \frac{GM_s M_{\text{gas}}}{a^2} \left(\frac{d}{a} \right)$$

$$\text{Self-gravity of the gas ball: } f_{\text{self}} \approx \frac{GM_{\text{gas}}^2}{d^2} \approx \frac{G \rho d^3}{d^2} \approx G \rho d$$

$$f_{\text{self}} > f_{\text{tide}} \rightarrow \rho > \frac{M_s}{a^3} \sim 2 \times 10^{-4} \text{ kg/m}^3 \left(\frac{1 \text{ AU}}{a} \right)^3$$

-- the Toomre criterion for structure formation in a disk

$$\text{For comparison: } \rho_{\text{MMSN}} \sim 10^{-5} \text{ kg/m}^3 \left(\frac{1 \text{ AU}}{a} \right)^{5/2}$$

MMSN contains a mass too low by a factor ~ 20 .

