# Why Do People Learn Foreign Languages? ${ }^{1}$ 

Victor Ginsburgh, Ignacio Ortuño-Ortín and Shlomo Weber ${ }^{2}$

February 2005


#### Abstract

In this paper we adopt the Selten-Pool (1993) framework of language acquisition that is based on the notions of communicative benefits and learning costs. We consider a model with languages that serve as imperfect substitutes and show that, under supermodularity of the communicative benefit function and some other mild conditions, there exists a unique interior linguistic equilibrium. We then derive a demand function for foreign languages, that we estimate for English, French, German and Spanish in 13 European countries.


Key words: Languages, Communicative benefits, Learning costs, Linguistic distances, estimation of demand functions for languages, European Union.

JEL Classification Numbers: C72, O52, Z13.

[^0]
## 1 Introduction

In this paper we analyze the reasons that induce inhabitants of a country to learn other languages. Each individual's decision can be analyzed by examining the benefits and the costs that it generates. Economists who examine the benefits of acquiring an additional language link them with the increased earning potential, ${ }^{3}$ but these studies often focus on immigrants who acquire the native language of the country in which they live. We adopt the framework of Selten and Pool (1993) who consider a general model of learning - languages and do not limit their analysis to "earnings as a mechanism and to firms as a milieu of the incentive to learn languages." (Selten and Pool, 1993, p.66).

In their model every individual derives a gross benefit from the knowledge of a foreign language that depends on the number of other individuals with whom she can communicate. This "gross communicative benefit" is therefore positively correlated with the number of other individuals with whom she shares at least one common language. Naturally we assume that all languages are "communicative substitutes," and the communication between two individuals can take place in any common language they share. The substitution however, is, in general, imperfect, and the communicative benefits are different (larger) if communication is conducted in the languages native for both sides. Therefore, we distinguish advantages of communication in native and non-native languages. For any individual $t$ we represent the gross communication benefit by means of an increasing function with two arguments: the number of individuals who share a common native language with $t$, and the number of individuals who speak a language known by $t$ but do not share her native language. To reflect the fact that languages are substitutes, we assume that the benefit function is supermodular.

[^1]Selten and Pool also assume that an individual who learns a new language incurs a cost. We make the assumption of "cost heterogeneity," that is the cost and difficulty for $t$ of learning a new language depends on its linguistic proximity with her native language. ${ }^{4}$ Indeed, it is natural to assume that a native speaker of Portuguese would find it easier to learn Spanish than Swedish. The fact that learning a foreign language is easier if it is close to the native language will have an impact on the number of those who learn it. The net communicative benefit that determines the individuals' behavior is the difference between the gross communicative benefit and the cost of acquiring a new language.

Consider the case of two native languages $i$ and $j$ with two populations. The attractiveness of a foreign language for a population that may learn this non-native language depends on the sizes of both populations. If the population that speaks $i$ is large relatively to the other one, the incentive of an $i$-citizen to learn the other language is likely to be quite low, since she can trade and communicate with enough citizens in her own country. But a large population that speaks $j$ may also attract citizens who speak $i$. The intuition on the expected properties of demand functions for foreign languages is confirmed by the theoretical model that is the subject of Section 2. Section 3 describes the data that will be used to estimate such demand functions, while results are reported in Section 4. Section 5 is devoted to some concluding remarks.

## 2 Modelling the Learning of a Foreign Language

We consider two languages $i$ and $j$, spoken in two regions or countries $i$ and $j$, respectively by $N_{i}$ and $N_{j}$ citizens. For simplicity, we assume that all citizens are unilingual, but may consider learning the other language. We denote by $N_{i j}$ (resp. $N_{j i}$ ) the number of citizens of country $i$ (country $j$ )

[^2]who study language $j(i)$. The communicative benefit of each individual $t$ depends on the number of those who speak the same language. It is represented by the utility function $U_{t}(x, y)$, where $x$ is the (log of the) number of individuals who speak the same native language as $t$, while $y$ is the (log of the) number of individuals who share with $t$ a language that is not their native language. ${ }^{5}$ We assume that the utility function is common to all individuals, so that $U_{t}(x, y)=U(x, y)$. Let $n$ represent the logarithm of $N$.

More specifically, the communicative benefit of an $i$-speaker who learns $j$ is $U\left(n_{i}, n_{j}\right)$, since she will be able to communicate with all $j$-speakers. The benefit of an $i$-speaker who does not learn language $j$ is $U\left(n_{i}, n_{j i}\right)$ : she will communicate with those who know her language in country $j$. For $j$-speakers the levels of communicative benefit are $U\left(n_{j}, n_{i}\right)$ and $U\left(n_{j}, n_{i j}\right)$, respectively. An individual who learns another language incurs a cost $C\left(l_{i j}\right)$, where $l_{i j}=l_{j i}$ is the (log of the) linguistic distance $L_{i j}$ between languages $i$ and $j$.

We impose the following assumptions:
Assumption A1: $U(\cdot, \cdot)$ is continuous and increasing on $\Re_{+}^{2}$. Moreover, $U$ is supermodular, i.e., for every two pairs of positive numbers $\bar{n}_{i}, n_{i}$, $\bar{n}_{j}, n_{j}$ with $\bar{n}_{i}>n_{i}, \bar{n}_{j}>n_{j}$ the following inequality holds:

$$
U\left(\bar{n}_{i}, \bar{n}_{j}\right)-U\left(\bar{n}_{i}, n_{j}\right) \geq U\left(n_{i}, \bar{n}_{j}\right)-U\left(n_{i}, n_{j}\right) .
$$

Assumption A2: The cost function $C(\cdot)$ is continuous and increasing on $\Re_{+}$.

The first part of Assumption A1 and Assumption A2 are standard, whereas the second part of A1 simply reflects the fact that the two languages are substitutes. If the function $U$ is twice continuously differentiable, the condition amounts to the positivity of the cross derivative $U_{i j}$ (Topkis, 1979).

[^3]To state our first result, we need an additional condition that guarantees that learning costs are not prohibitively high with respect to communicative benefits. It requires that if no $j$-speaker studies $i$, an $i$-speaker would get a positive net benefit from studying $j$ so that his access to all $j$-speakers outweighs the language learning cost $C\left(l_{i j}\right)$. If this assumption is violated, than no citizen of country $i$ learns a foreign language. Similarly, we assume that it is worthwhile for a $j$-speaker to study $i$, if no $i$-speaker learns $j$. This very mild condition is formally stated as follows:

## Assumption A3:

$$
U\left(n_{i}, n_{j}\right)-U\left(n_{i}, 0\right)>C\left(l_{i j}\right) \text { and } U\left(n_{i}, n_{j}\right)-U\left(0, n_{j}\right)>C\left(l_{i j}\right) .
$$

These assumptions make it possible to state the following two propositions.
Proposition 1: Under A1 and A3, there exists a unique interior ${ }^{6}$ linguistic equilibrium, where all individuals are indifferent between learning the foreign language and incurring the cost of learning it, and not learning the language. This equilibrium is a solution of the following system of two equations:

$$
\begin{align*}
& U\left(n_{i}, n_{j}\right)-C\left(l_{i j}\right)-U\left(n_{i}, n_{j i}\right)=0,  \tag{1}\\
& U\left(n_{j}, n_{i}\right)-C\left(l_{j i}\right)-U\left(n_{j}, n_{i j}\right)=0 . \tag{2}
\end{align*}
$$

Proof: The proof follows immediately from Assumptions A1 and A2. Indeed, A2 together with the continuity of $U$ in the second argument yields the unique $n_{j i}$ that satisfies (1), whereas A2 together with the continuity of $U$ in the first argument guarantees the uniqueness of $n_{i j}$ that satisfies (2).

[^4]The interior linguistic equilibrium yields functions $n_{i j}\left(n_{i}, n_{j}, l_{i j}\right)$ and $n_{j i}\left(n_{j}, n_{i}, l_{j i}\right)$ for languages $j$ and $i$ of individuals whose native language is $i$ and $j$, respectively. Denote by $\log \left(N_{i j} / N_{i}\right)=D_{i}\left(n_{i}, n_{j}, l_{i j}\right)$, the equilibrium share (demand function) of individuals whose native language is $i$ and who learn language $j$. The properties of $D_{i}$ are described in the following proposition: ${ }^{7}$

Proposition 2: Suppose that Assumptions A1-A3 hold. Then:
(a) If, in addition, $U$ is concave in the second variable, $D_{i}\left(\cdot, n_{j}, l_{i j}\right)$ is decreasing in $n_{i}$;
(b) $D_{i}\left(n_{i}, \cdot, l_{i j}\right)$ is increasing in $n_{j}$;
(c) $D_{i}\left(n_{i}, n_{j}, \cdot\right)$ is increasing in $l_{i j}$.

Proof: (a) We can rewrite equation (2) as:

$$
\begin{equation*}
U\left(n_{j}, n_{i}\right)-C\left(l_{j i}\right)-U\left(n_{j}, n_{i}+D_{i}\left(n_{i}, n_{j}, l_{i j}\right)\right)=0 . \tag{3}
\end{equation*}
$$

Assume that $n_{i}$ increases to $\bar{n}_{i}$. Concavity of the $U$ in the second variable implies that

$$
U\left(n_{j}, \bar{n}_{i}\right)-C\left(l_{j i}\right)-U\left(n_{j}, \bar{n}_{i}+D_{i}\left(n_{i}, n_{j}, l_{i j}\right)\right)<0 .
$$

Since

$$
U\left(n_{j}, \bar{n}_{i}\right)-C\left(l_{j i}\right)-U\left(n_{j}, \bar{n}_{i}+D_{i}\left(\bar{n}_{i}, n_{j}, l_{i j}\right)\right)=0,
$$

and, by A1 ( $U$ is increasing), it follows that

$$
D_{i}\left(\bar{n}_{i}, n_{j}, l_{i j}\right)<D_{i}\left(n_{i}, n_{j}, l_{i j}\right) .
$$

(b) Consider (3) and assume that $n_{j}$ increases to $\bar{n}_{j}$. The supermodularity of $U$ implies that

$$
U\left(\bar{n}_{j}, n_{i}\right)-C\left(l_{j i}\right)-U\left(\bar{n}_{j}, n_{i}+D_{i}\left(n_{i}, n_{j}, l_{i j}\right)\right)>0 .
$$

[^5]But since

$$
U\left(\bar{n}_{j}, n_{i}\right)-C\left(l_{j i}\right)-U\left(\bar{n}_{j}, n_{i}+D_{i}\left(n_{i}, \bar{n}_{j}, l_{i j}\right)\right)=0,
$$

and, by A1 ( $U$ is increasing in the second argument), it follows that

$$
D_{i}\left(n_{i}, n_{j}, l_{i j}\right)<D_{i}\left(n_{i}, \bar{n}_{j}, l_{i j}\right) .
$$

(c) Follows from $A 1$ and $A 2$. Indeed, let $\bar{l}_{i j}>l_{i j}$, which, by $A 2$, yields $C\left(\bar{l}_{i j}\right)>C\left(l_{i j}\right)$. Since the function $U$ is increasing in the second argument, equation (2) immediately implies that the number of $j$-learners in country $i$ would decline under a higher value of the linguistic distance.

## 3 Data

We estimate the demand functions derived in Section 2 for English, French, German and Spanish by citizens from the European Union (EU) whose native languages are none of these. The data consist of knowledge of native and foreign languages in various EU countries, and distances between languages.

Language proficiency was the topic of a survey on languages ordered by the Directorate of Education and Culture of the EU in $2000 .^{8}$ In each of the 15 EU countries, 1,000 interviews ${ }^{9}$ were conducted on the use of languages. The information in which we are interested here is concerned with answers to the following two questions:
(a) What is your mother tongue? (note to the interviewer: do not probe; do not read [the list of languages] out; if bilingual, state both languages);

[^6](b) What other languages do you know? (show card [containing a list of languages]; ${ }^{10}$ read out; multiple answers possible).

There were four possible choices for (b), and we assumed that the first two choices that came to the mind of the person interviewed were the languages that she knew best.

There were also questions on whether the knowledge of each of the tongues mentioned was "very good," "good" or "basic," but we did not take these answers into account, since such assessments are often subjective and, therefore, not very informative.

The results of such surveys can be questioned, since what individuals claim to know is hard to verify without deeper but very costly and timeconsuming probing. We assume that there is some consistency across countries.

We restrict our attention to the "knowledge" in 13 EU countries ${ }^{11}$ of four non-native languages: English, French, German, and Spanish. The first three are the most widely languages spoken in the EU. Though Italy has a larger population than Spain, and the number of natives speakers of Italian is larger, the language is hardly spoken outside of Italy, ${ }^{12}$ which is of course not the case of Spanish. Table 1, which also includes Italian and Dutch gives a general overview of language use by native speakers in the EU and worldwide. Column (1) shows the number of native speakers, in fact the population in each country. ${ }^{13}$ Columns (2) and (3) show two estimates

[^7]of the worldwide use of each language as mother tongue. Though orders of magnitude are similar, there is some variation especially for English and Spanish. The last column gives estimates of worldwide knowledge as mother tongue and otherwise. ${ }^{14}$

Table 2 gives details about the knowledge of languages in the 13 EU countries that are dealt with here. Column (2) contains the world population that speaks the language of the country listed in column (1) as first language. ${ }^{15}$ The other four columns give the share of the total population in each country that (claims to) know English, French, German and Spanish.

Data on distances between languages among 95 Indo-European languages have been computed by Dyen, Kruskal and Black (1992). They are constructed on the basis of a set of cognition data. For each meaning in a list of 200 basic meanings, Dyen collected the words used in 95 Indo-European speech varieties, and classified these into cognate classes, that contain all the words for a given meaning that have an unbroken history of descendent from a common ancestral word. The distance between languages $i$ and $j$ is then computed as the ratio of "non-cognate" and "cognate" plus "non-cognate" meanings, ${ }^{16}$ and lies between 0 and 1 . The distances used in this paper are displayed in Table 3.

## 4 Estimation Results

We estimate the following demand function for languages $j$ ( $j=$ English, French, German, Spanish) by those whose native language is $i(i=$

## they migrated.

${ }^{14}$ Dalby (2002, p. 31) gives much higher estimates for English (1.8 billion) and Spanish (450 million). The French diplomatic service (website http://www.france.diplomatie.fr/francophonie/francais/carte.html) provides the estimation of 169 million people who use French.
${ }^{15}$ Following Ethnologue.com.
${ }^{16}$ See Dyen, Kruskal and Black (1992), and also Ginsburgh, Ortuño-Ortín and S. Weber (2003) for further details.

Austria, Denmark, Finland, France, Germany, Greece, Italy, Ireland, the Netherlands, Portugal, Spain, Sweden and the United Kingdom):

$$
\log \left(N_{i j} / N_{i}\right)_{E U}=\alpha_{0}+\alpha_{1} n_{i}+\alpha_{2} n_{j}+\alpha_{3} l_{i j}+u_{i j},
$$

where $\left(N_{i j} / N_{i}\right)_{E U}$ represents the proportion of inhabitants of EU country $i$ who are proficient in language $j$ (columns (3) to (6) in Table 2); $n_{i}$ and $n_{j}$ represent respectively the ( $\log$ of the) world populations whose native languages are $i$ and $j$ (column (2) in Table 2) and $l_{i j}$ is the (log of the) distance between languages $i$ and $j$ (Table 3).

The results of this equation appear in column (1) of Table 4. Though the signs of all three variables conform with theory, and both $\alpha_{2}$, the coefficient picked by the acquired language, and $\alpha_{3}$, the coefficient for distance are significantly different from zero, the adjustment is poor, as can be seen from the adjusted $R^{2}$, which is small. The reason for this appears in the equation reproduced in column (2), which separates the four acquired languages (world populations who speak English, French, German and Spanish are interacted with dummies for each of them). The results show that the four languages do not have the same attraction power, which is explained by factors that are not fully captured by the population that knows the language.

Spanish is obviously much less attractive than the three other languages. In column (3), we combined the three other languages, leaving Spanish separate. The fit deteriorates only very marginally with respect to the previous equation. The null hypothesis (using an $F$-test) that English, French and German are equally attractive, but that Spanish is less so, cannot be rejected at the $10 \%$ probability level, but is rejected at the $5 \%$ level.

The introduction of trade shares (which do not appear in the theoretical model) as possible determinants (or incentives) between the 13 EU countries and the regions in which English, French, German and Spanish are spoken, does not bring much change. The parameter picked by the trade shares
variable is almost significant at the $5 \%$ probability level, and the parameters for acquired languages are slightly reduced.

## 5 Concluding Comments

Our results show that three variables explain reasonably well the share of people who learn a foreign language, without taking into account the incentives every individual has to acquire a language. The larger the native population who speaks the language, the less speakers are prone to learn another language; the more the foreign language is spoken, the more it attracts others to learn it; the larger the distance between two languages, the smaller the proportion of people who will learn it. However, our results also show that the attraction powers of the four foreign languages are significantly different, and that other determinants, mostly historical, must be at play. Spanish, for instance, should attract Europeans much more than it does. With the exception of France, there is no country in which more that five percent of the population knows the language. The isolation of Spain until 1975, the year in which Franco died, explains partly this result, but the large population of native Spanish speakers (essentially in Mexico and South America, and increasingly so in the United States) does not seem to generate large incentives to learn the tongue. Dynamics, past as well as current cultural relations that are absent from our model should obviously be part of the story: Attractiveness of a foreign language depends on more than just the number of people who speak it worldwide. Therefore the questions of why English is becoming the lingua franca in Europe (and probably in the world), and why Spanish is relatively less spoken in Europe remain only partly captured by our model.

## 6 References

Chiswick, B. (1993), Hebrew language usage: determinants and effects on earnings among immigrants in Israel, manuscript, University of Illinois.

Church, J. and I. King (1993), Bilingualism and network externalities, Canadian Journal of Economics 26, 337-345.

Crystal, D. (2001), A Dictionary of Language, Chicago: Chicago University Press.

Dalby, A. (2002), Languages in Danger, London: Allen Lane-The Penguin Press.

Dyen, I. , J. B. Kruskal, and P. Black (1992), An Indo-European classification: A lexicostatistical experiment, Transactions of the American Philosophical Society 82 (5).

Ginsburgh, V., I. Ortuño-Ortín, and S. Weber (2003), Language disenfranchisement in linguistically diverse societies. The case of European Union, Journal of the European Economic Association, forthcoming.

Ginsburgh, V. and S. Weber (2003), Language disenfranchisement in the European Union, Journal of Common Market Studies, forthcoming.

Grenier, G. (1985), Bilinguisme, transferts linguistiques et revenus du travail au Québec, quelques éléments d'interaction, in Francois Vaillancourt, ed., Économie et Langue, Québec: Éditeur officiel, 243-287.

Lang, K. (1986), A language theory of discrimination, Quarterly Journal of Economics 100, 363-381.

MacManus, W. Gould, and F. Welsch (1978), Earnings of Hispanic men: The role of English language proficiency, Journal of Labor Economics, 1, 101-130.

Selten, R. and J. Pool (1991), The distribution of foreign language skills as a game equilibrium, in R. Selten, ed., Game Equilibrium Models, vol. 4, Berlin: Springer-Verlag, 64-84.

Topkis, D. (1979), Equilibrium points in non-zero sum $n$-person submodular games, SIAM Journal of Control and Optimization 17, 773-787.

Van Parijs, P (2003), Europe's three language problems, in R. Bellamy, D. Castiglione and C. Longman, eds., Multilingualism in Law and Politics, Oxford: Hart, forthcoming.

Table 1. Main Languages Used in the European Union (millions)

|  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
|  | Native speakers <br> in the EU <br> $(1)$ | Mother tongue <br> Ethnologue <br> $(2)$ | Crystal <br> $(3)$ | Woldwide use |
|  |  |  |  | $(4)$ |
|  |  |  |  |  |
| English | 62.3 | 341 | 400 | $1,000-1,500$ |
| French | 64.5 | 77 | 72 | 122 |
| German | 90.1 | 100 | 100 | 120 |
| Spanish | 39.4 | 340 | 270 | 350 |
| Italian | 57.6 | 62 | 63 | 63 |
| Dutch | 21.9 | 20 | 20 | 20 |
|  |  |  |  |  |

Column (1): English is the native language in Great Britain and Ireland. French is the native language in France and is spoken by 40 percent of Belgians. German is the native language in Germany and Austria. Spanish and Italian are the native languages in Spain and Italy, respectively. Finally, Dutch is the native language in the Netherlands and is spoken by 60 percent of Belgians.
Column (2): Number of first language speakers as given by www.ethnologue.com. For Spanish, the number is the average between the two estimates given by www.ethnologue.com. Column (3): Estimates by Crystal (2001).
Column (4): Estimates by Crystal (2001). Note that the 1 billion users of English is a conservative estimate. Crystal also gives a more "liberal" estimate of 1,5 billion users.

Table 2. Knowledge of Languages in the European Union (millions and percent)

|  |  |  | Percentage who know |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Country | Native language <br> known by <br> (millions) | English | French | German | Spanish |  |
| $(1)$ | $(2)$ | $(3)$ | $(4)$ | $(5)$ | $(6)$ |  |
|  |  |  |  |  |  |  |
| Austria (G) | 100.0 | 46 | 11 | 100 | 1 |  |
| Denmark (Dk) | 5.3 | 75 | 5 | 37 | 1 |  |
| Finland (Fi) | 6.0 | 61 | 1 | 7 | 1 |  |
| France (F) | 77.0 | 42 | 100 | 8 | 15 |  |
| Germany (G) | 100.0 | 54 | 16 | 100 | 2 |  |
| Greece (Gr) | 12.0 | 47 | 12 | 12 | 5 |  |
| Italy (I) | 62.0 | 39 | 29 | 4 | 3 |  |
| Ireland (E) | 341.0 | 100 | 23 | 6 | 2 |  |
| Netherlands (D) | 20.0 | 70 | 19 | 59 | 1 |  |
| Portugal (P) | 176.0 | 35 | 28 | 2 | 4 |  |
| Spain (S) | 340.0 | 36 | 19 | 2 | 100 |  |
| Sweden (Sw) | 9.0 | 79 | 7 | 31 | 4 |  |
| Un. Kingdom (E) | 341.0 | 100 | 22 | 9 | 5 |  |
|  |  |  |  |  |  |  |

The native language in each country is given between brackets (G: German, Dk: Danish, Fi: Finnish, F: French, G: German, Gr: Greek, I: Italian, E: English, D: Dutch, P: Portuguese, S: Spanish, Sw: Swedish). The numbers in the first column are from www. ethnologue.com. The percentages of people who know English, French, German and Spanish in each country are from Ginsburgh and Weber (2003).

Table 3. Distances Between Languages (x 1,000)

|  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
|  | English | French | German | Spanish |
|  |  |  |  |  |
|  |  |  |  |  |
| Danish | 407 | 759 | 293 | 750 |
| Dutch | 392 | 756 | 162 | 742 |
| English | 0 | 764 | 422 | 760 |
| Finnish | 1000 | 1000 | 1000 | 1000 |
| French | 764 | 0 | 756 | 266 |
| German | 422 | 764 | 0 | 747 |
| Greek | 838 | 843 | 812 | 833 |
| Italian | 753 | 197 | 735 | 212 |
| Portuguese | 760 | 291 | 753 | 126 |
| Spanish | 760 | 266 | 747 | 0 |
| Swedish | 411 | 756 | 305 | 747 |
|  |  |  |  |  |

Sources. Dyen et. al (1992) for further details.
See also Ginsburgh et. al (2003).

Table 4. Estimation Results

|  | (1) | (2) | (3) | (4) |
| :---: | :---: | :---: | :---: | :---: |
| Population speaking language $i\left(\alpha_{1}\right)$ | $\begin{gathered} -0.059 \\ (0.120) \end{gathered}$ | $\begin{gathered} -0.049 \\ (0.069) \end{gathered}$ | $\begin{gathered} -0.046 \\ (0.070) \end{gathered}$ | $\begin{aligned} & -0.055 \\ & (0.070) \end{aligned}$ |
| Population speaking language $j\left(\alpha_{2}\right)$ | $\begin{aligned} & 0.543^{*} \\ & (0.207) \end{aligned}$ |  | $\begin{aligned} & 0.760^{*} \\ & (0.123) \end{aligned}$ | $\begin{aligned} & 0.600^{*} \\ & (0.067) \end{aligned}$ |
| Dummy English ( $\alpha_{E}$ ) |  | $\begin{aligned} & 3.602^{*} \\ & (0.333) \end{aligned}$ |  |  |
| Dummy French ( $\alpha_{F}$ ) |  | $\begin{aligned} & 2.202^{*} \\ & (0.344) \end{aligned}$ |  |  |
| Dummy German $\left(\alpha_{G}\right)$ |  | $\begin{aligned} & 1.779^{*} \\ & (0.351) \end{aligned}$ |  |  |
| Dummy Spanish ( $\alpha_{S}$ ) |  | $\begin{gathered} 0.617 \\ (0.341) \end{gathered}$ | $\begin{gathered} -0.374^{*} \\ (0.041) \end{gathered}$ | $\begin{gathered} -0.340^{*} \\ (0.044) \end{gathered}$ |
| Distance between <br> languages $i$ and $j\left(\alpha_{3}\right)$ | $\begin{gathered} -0.876^{*} \\ (0.341) \end{gathered}$ | $\begin{aligned} & -0.942^{*} \\ & (0.199) \end{aligned}$ | $\begin{aligned} & -0.915^{*} \\ & (0.200) \end{aligned}$ | $\begin{aligned} & -0.789^{*} \\ & (0.205) \end{aligned}$ |
| Trade share $\left(\alpha_{4}\right)$ |  |  |  | $\begin{gathered} 0.249 \\ (0.134) \end{gathered}$ |
| Adjusted $R^{2}$ | 0.185 | 0.726 | 0.720 | 0.712 |

Standard errors are given between brackets, under the coefficients. Starred coefficients are significantly different from 0 at the $5 \%$ (or $1 \%$ ) probability level. The number of observations is equal to 46 in all equations. Intercepts are not reported.


[^0]:    ${ }^{1}$ This paper was motivated by some of the views held in Van Parijs (2003). We are grateful to Abdul Noury and Philippe Van Parijs for comments on a previous version.
    ${ }^{2}$ Ginsburgh: ECARES, Université Libre de Bruxelles and CORE, Louvain-la-Neuve; Ortuño-Ortín: Department of Economics and IVIE, University of Alicante; Weber: Department of Economics, SMU, Dallas, and CORE, Université Catholique de Louvain.

[^1]:    ${ }^{3}$ See e. g., MacManus, Gould and Welsch (1978), Granier (1985), Lang (1986), and Chiswick (1993)

[^2]:    ${ }^{4}$ See Dyen, Kruskal and Black (1992), and Ginsburgh, Ortuño-Ortín and Weber (2003).

[^3]:    ${ }^{5}$ Logarithms are used to link the model to the empirical results and this entails no loss of generality.

[^4]:    ${ }^{6}$ There also exist two "corner" equilibria, where one language is learnt by everybody in the foreign country whereas the other language is learnt by nobody (see Church and King, 1993). We do not examine these equilibria here.

[^5]:    ${ }^{7}$ Obviously, the same properties hold for $D_{j}$.

[^6]:    ${ }^{8}$ INRA, Eurobaromtre 54 Special, Les Europens et les Langues, February 2001.
    ${ }^{9}$ With some minor variations: 1,300 interviews in the UK, 2,000 in Germany, 600 in Luxembourg.

[^7]:    ${ }^{10}$ Danish, German, French, Italian, Dutch, English, Spanish, Portuguese, Greek, Irish, Swedish, Finnish, Luxembourgish, Arabic, Turkish, Chinese, Sign language, Other (specify first and second), None.
    ${ }^{11}$ Austria, Denmark, Finland, France, Germany, Greece, Italy, Ireland, The Netherlands, Portugal, Spain, Sweden and The United Kingdom. Belgium and Luxembourg are omitted because they are both bilingual and would be more difficult to treat (and Luxembourg's population- 0.4 million-is extremely small.)
    ${ }^{12}$ Italian is known by 9 percent of the population in Austria, 6 percent in Belgium and Greece, 5 percent in France, and one percent in other countries of the EU.
    ${ }^{13}$ To simplify, we assume that immigrants speak the language of the country to which

