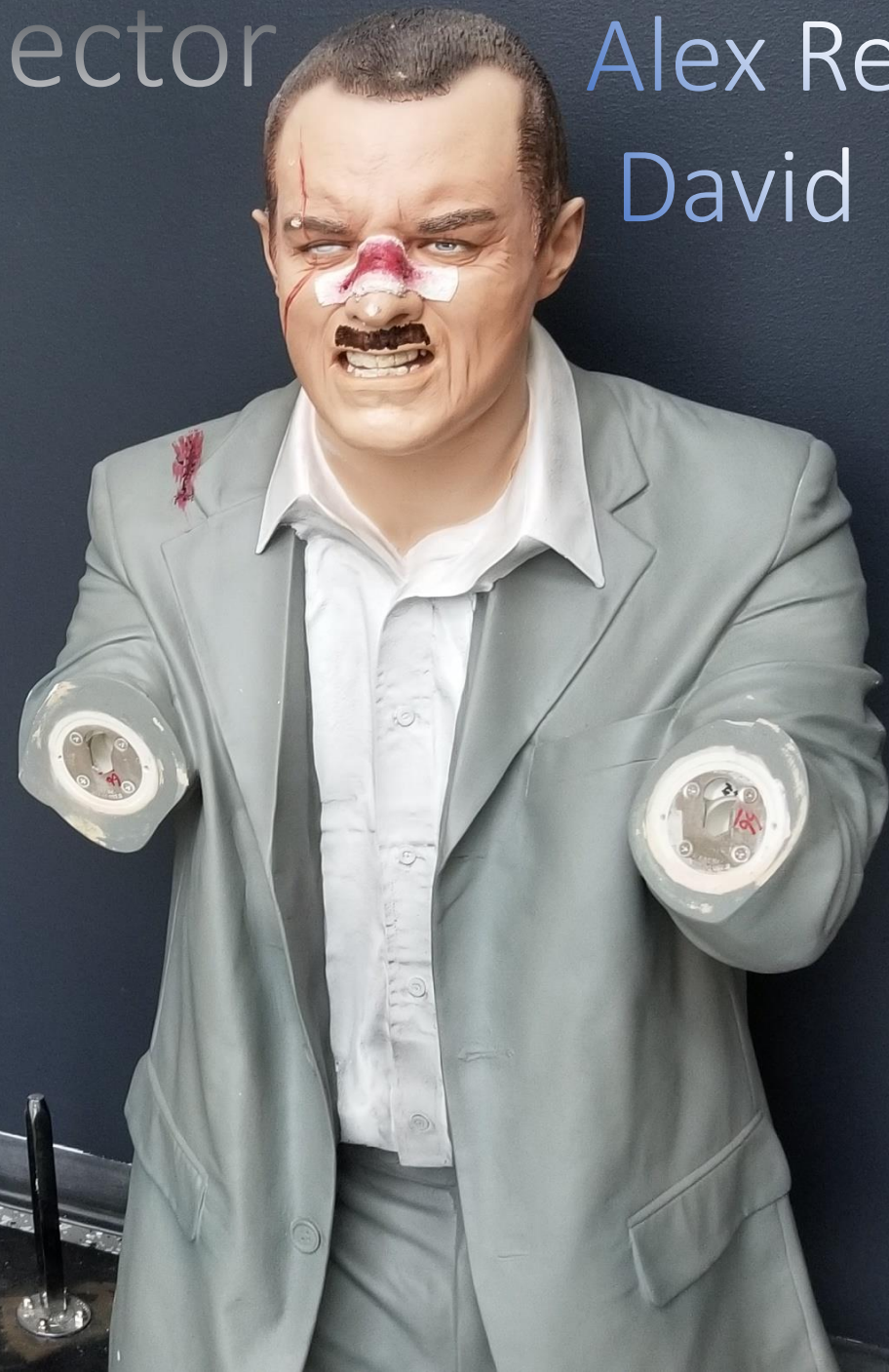
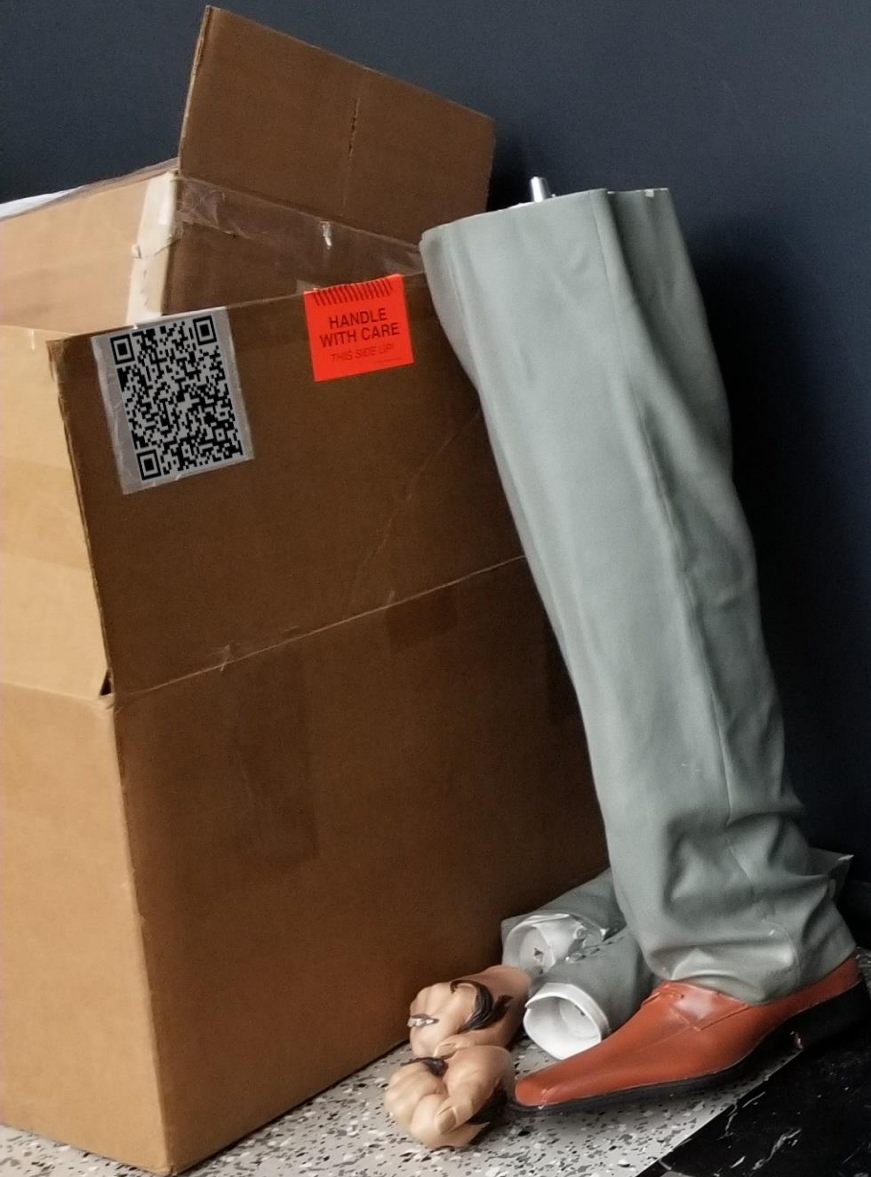


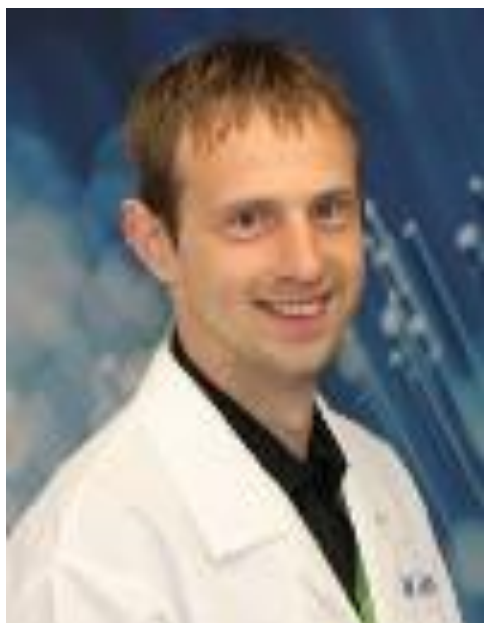
Phantom Ray-Hair Intersector

Alex Reshetov

David Luebke

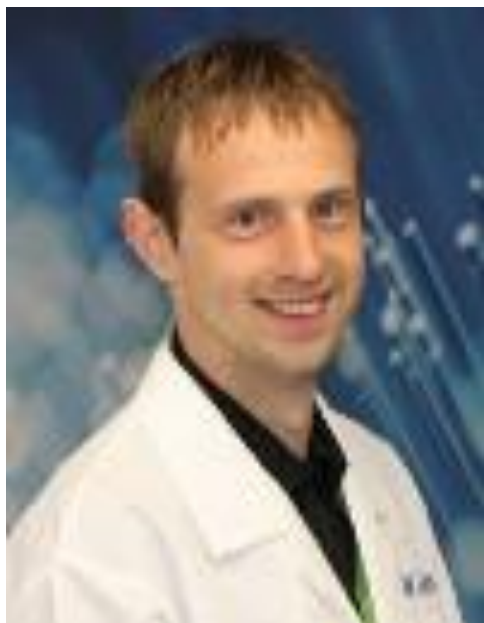
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Mailboxing. When using spatial splits, the resulting replication of references can lead to the same primitive being encountered multiple times during traversal. For highly optimized triangle tests this is often ok, and the cost and complexity of potentially adding mailboxing often outweighs its savings. However, even with our vectorized intersection test from Section 2, a hair segment intersection is significantly more expensive than a ray-triangle test.

Exploiting Local Orientation Similarity for Efficient Ray Traversal of Hair and Fur
Sven Woop, Carsten Benthin, Ingo Wald, Gregory S. Johnson, and Eric Tabellion
High Performance Graphics 2014

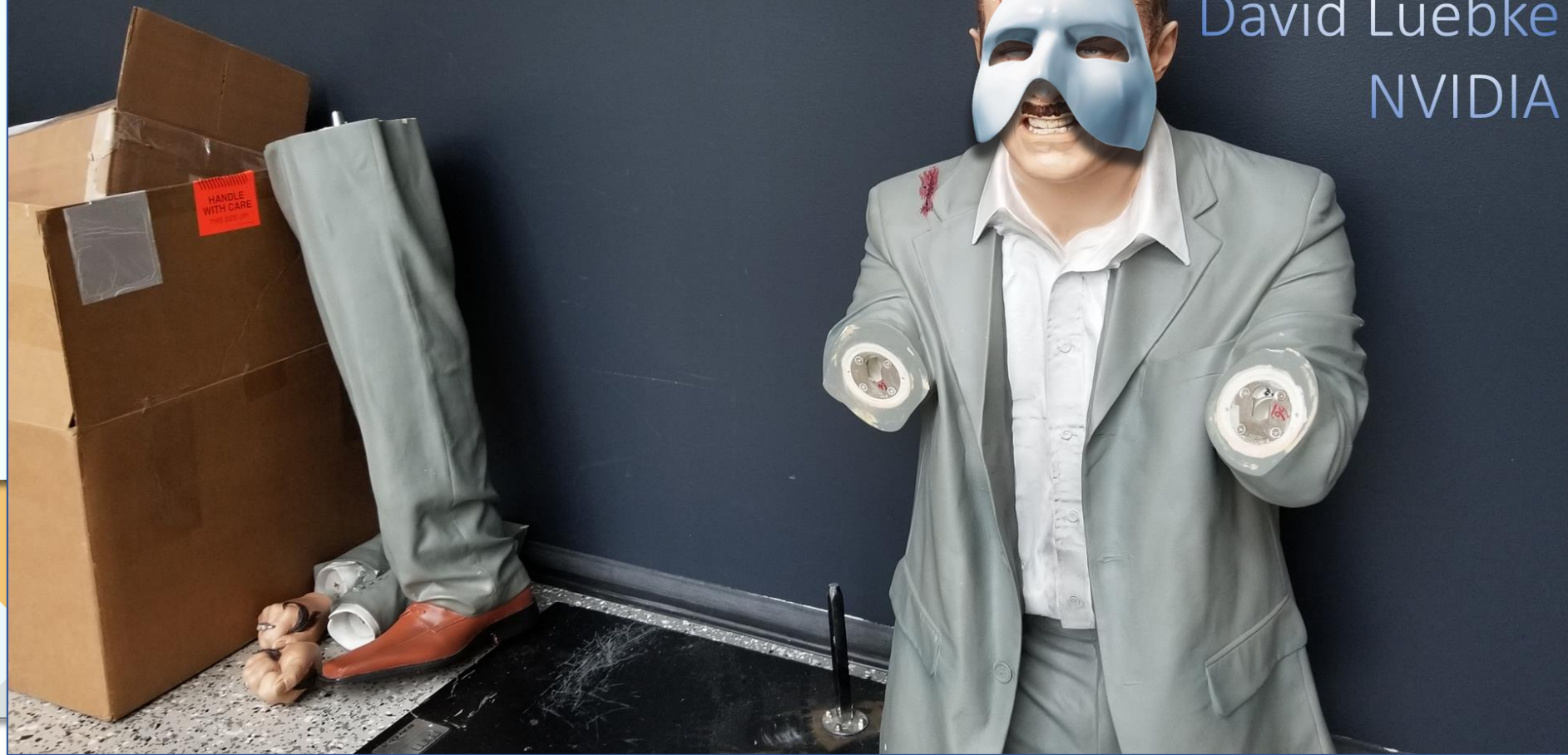


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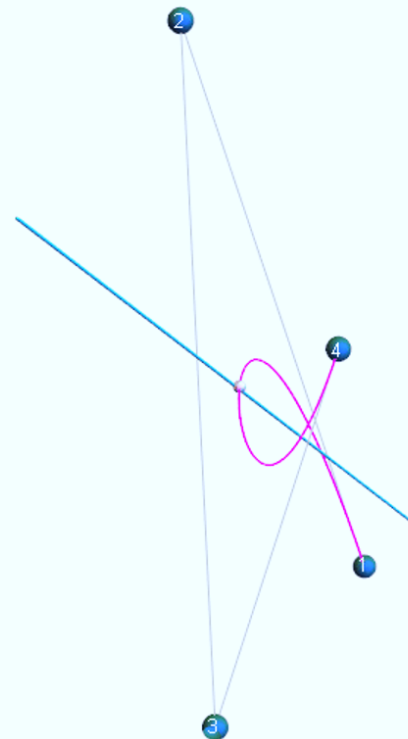
Alex Reshetov
David Luebke
NVIDIA



Exploiting Budan-Fourier and Vincent's Theorems for Ray Tracing 3D Bézier Curves

Alex Reshetov

NVIDIA



High-Performance Graphics 2017

Los Angeles | July 28-30, 2017



- › My awesome coolest totally-wicked strategy for producing many papers on the same topic (modification of an anonymous post - note: this is *supposed to be* a joke):
 - › Preparation - Discover some new application domain.
 - › Paper #1 - Introduce the problem. Model it as a ray tracing problem and render images using pbrt. Minimal implementation effort is needed.
 - › Paper #2 - Solve the problem with importance sampling. Because you know something about your application domain, you can find a good PDF to reduce variance a bit compared to #1.
 - › Paper #3 - Importance sampling is not working well in difficult cases. Now let's solve it with a Markov Chain Monte Carlo method such as the Metropolis-Hastings algorithm.
 - › Paper #4 - Speed is important. Implement the algorithm on a GPU.
 - › Paper #5 - #4 is still too slow. You've found an interactive application of the problem, so now you need to focus on speed rather than image quality. Rasterization.
 - › Paper #6 - You've analyzed your application domain, and found that 50-70% of all problem instances belong to a special class that can be rendered more efficiently. New paper.
 - › Paper #7 - It's time for an approximation algorithm. Another new paper.
 - › Now, repeat the process from the step 2 by slightly changing the topic.



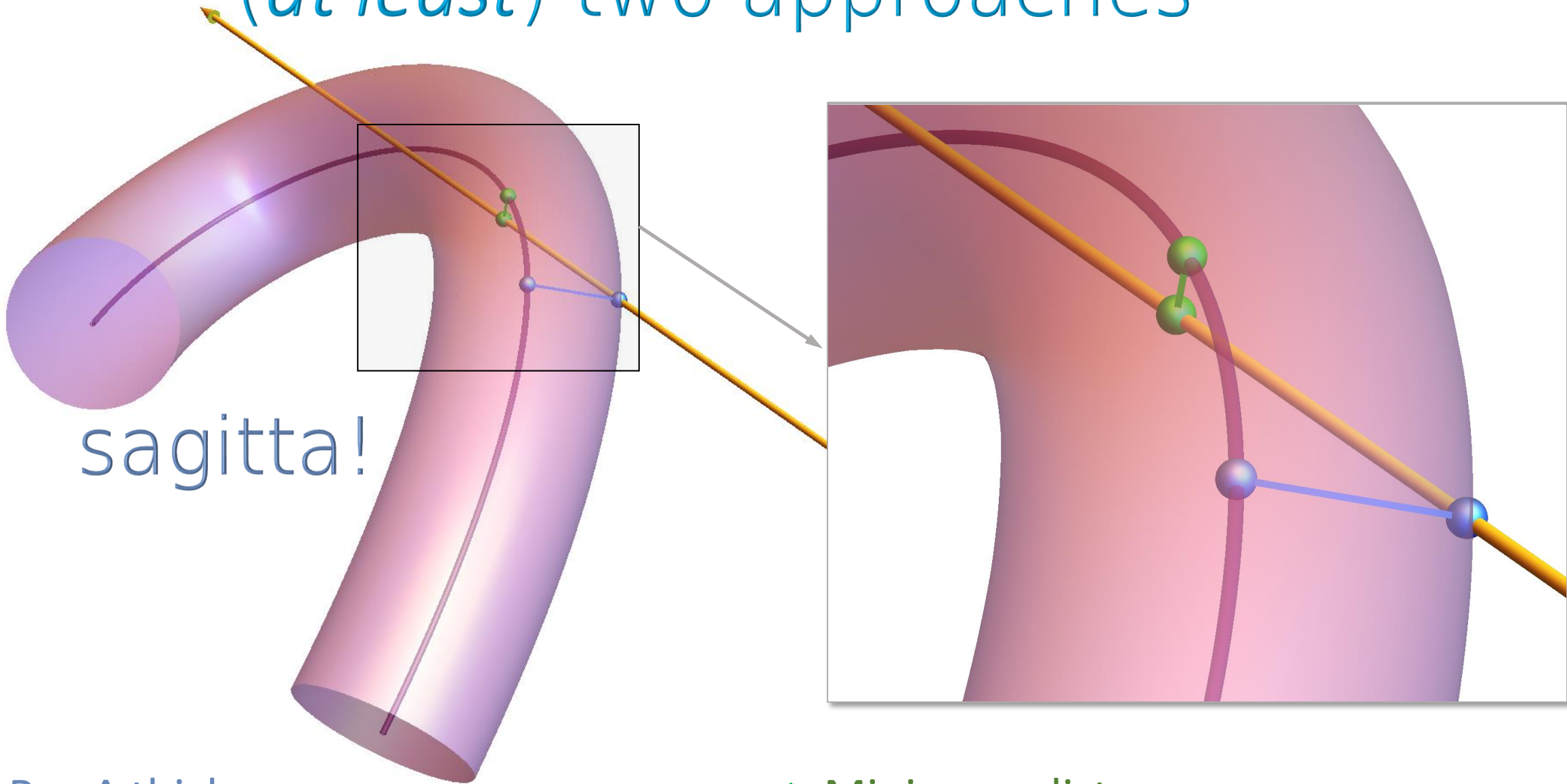
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Phantom \neq Budan 2.0

If you can't convince
them, confuse them.

Harry S. Truman

(at least) two approaches



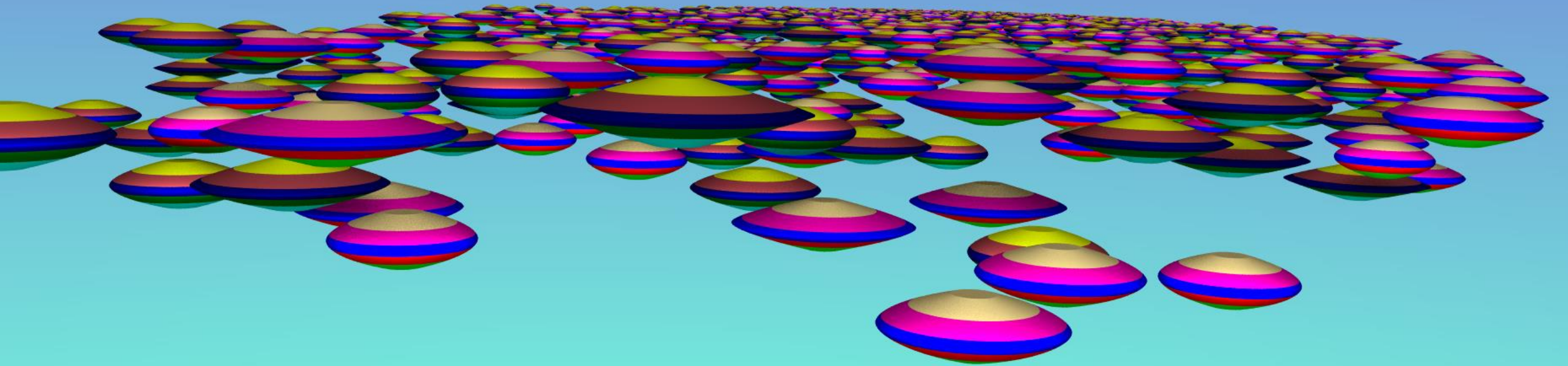
sagitta!

- Ray ^ thick curve
more thrilling

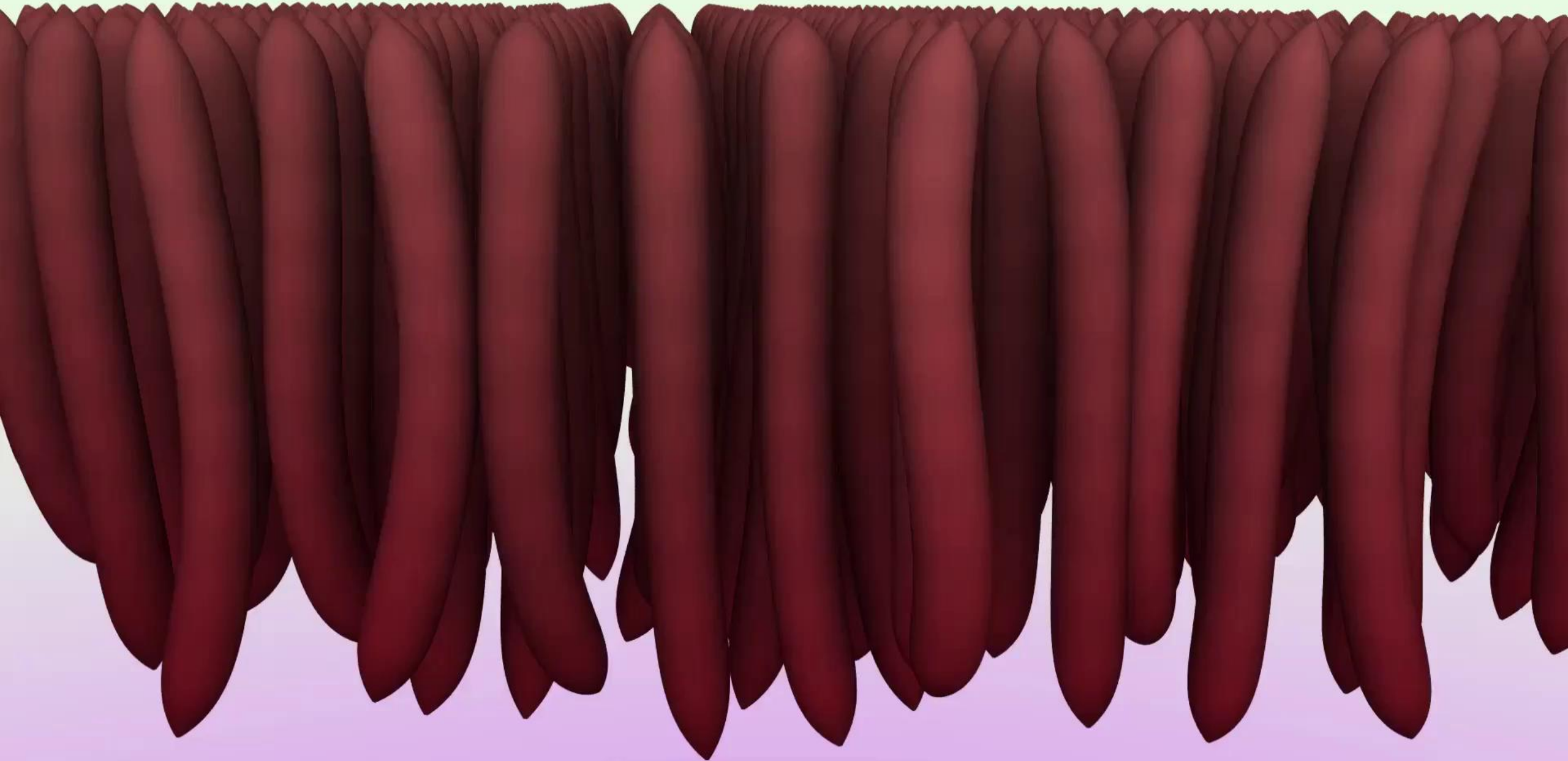


Minimum distance
more universal (and easier)

Invasion of Flying Saucers



Sausage Factory



~~Phantom Ray-Saucer Intersector~~

~~Phantom Ray-Sausage Intersector~~

Phantom Ray-Hair Intersector

The 'phantom' name according to the reviewers

- the title is a bit strange and confusing
- hard to follow the real "story"
- a bit confusing
- 'phathom intersector' is kind of confusing
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Phathom



Members

- Matthew Sikora - Vocals/Guitar
- Yannick d' Assgnies - Bass
- Anton Tilgren - Drums
- Jason Zielonka - Guitar

Phathom Links

- Facebook
- iTunes
- Last.FM
- MySpace
- PureVolume
- Reverb Nation
- Website

Phathom News

Twitter

PHATHOM's, (originally called Section 8), four members (Anton, Jason, Matt and Yannick)



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- Featured content
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- Help
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- Page information
- Wikidata item
- Cite this page

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- Create a book
- Download as PDF
- Printable version

Languages

- Català
- Deutsch
- Español
- فارسی
- Français
- 한국어
- हिन्दी
- Italiano
- עברית
- Magyar
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Article **Talk**

Read **Edit** View history


Search Wikipedia

Phantom

From Wikipedia, the free encyclopedia

Phantom may refer to:

- An **apparition**, more specifically a
 - Spirit
 - Ghost
- An **illusion**, a distortion of the senses

 Look up **phantom** in Wiktionary, the free dictionary.

Film [edit]

- Phantom*, a 1922 silent film directed by F. W. Murnau
- The Phantom* (1931), an American film directed by Alan James
- The Phantom*, a 1943 film serial based on the comic strip
- The Phantom* (1996), a film directed by Simon Wincer starring Billy Zane
- Phantoms*, a 1998 film adaptation of the Dean Koontz novel
- O Fantasma (The Phantom)*, a 2000 Portuguese film
- Phantom*, a 2002 Malayalam film
- The Belgrade Phantom*, a 2009 Serbian film
- The Phantom*, a 2010 science-fiction television miniseries inspired by the comic strip *The Phantom*
- Phantom*, a 2013 film about a submarine captain trying to prevent a war
- Phantom*, a 2015 Indian political thriller film directed by Kabir Khan
- The Phantom, a *Pink Panther* character
- The Phantom, main antagonist in the animated television series *Flying Rhino Junior High*
- Film productions in 1925, 1943, 1962, 1983, 1987, 1989, 1998, 2004, and 2011 of *The Phantom of the Opera*, see *The Phantom of the Opera (disambiguation)*

Music [edit]

- Phantom (band), a South Korea-based hip hop project trio
- Phantoms (band), a Los-Angeles based EDM duo
- Phantom* (musical), a 1991 musical
- The Phantom of the Opera* (1986 musical), by Andrew Lloyd Webber
- TXFM, a radio station formerly known as Phantom 105.2
- Phantom Records, a record label
- Phantom Regiment Drum and Bugle Corps
- Vox Phantom, a guitar
- Phantoms* (Toch), a choral work by Ernst Toch
- "The Phantom", a pseudonym used by Jerry Lott for the primal rockabilly song "Love Me"

Albums [edit]

- Phantom* (Khold album), a 2002 album by Khold
- Phantom (Betraying the Martyrs album), 2014

Contents [hide]

- 1 Film
- 2 Music
 - 2.1 Albums
 - 2.2 Songs
- 3 Literature
- 4 Gaming
- 5 Medical
- 6 Military
- 7 Sports
 - 7.1 Teams
 - 7.2 Individuals
- 8 Television
- 9 Other uses
- 10 See also

Rich history of a 'Phantom' name



Jacco Bikker aka 'Phantom'



phantom ray tracer



All

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More

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Tools

About 1,880,000 results (0.38 seconds)

Boeing Phantom Ray - Wikipedia

https://en.wikipedia.org/wiki/Boeing_Phantom_Ray ▼

The Boeing **Phantom Ray** is an American demonstration stealth unmanned combat air vehicle (UCAV) being developed by Boeing using company funds.

First flight: April 27, 2011

Number built: 1

Developed from: [Boeing X-45C](#)

Global Services Unlimited Support

 **BOEING**

Phantom Ray



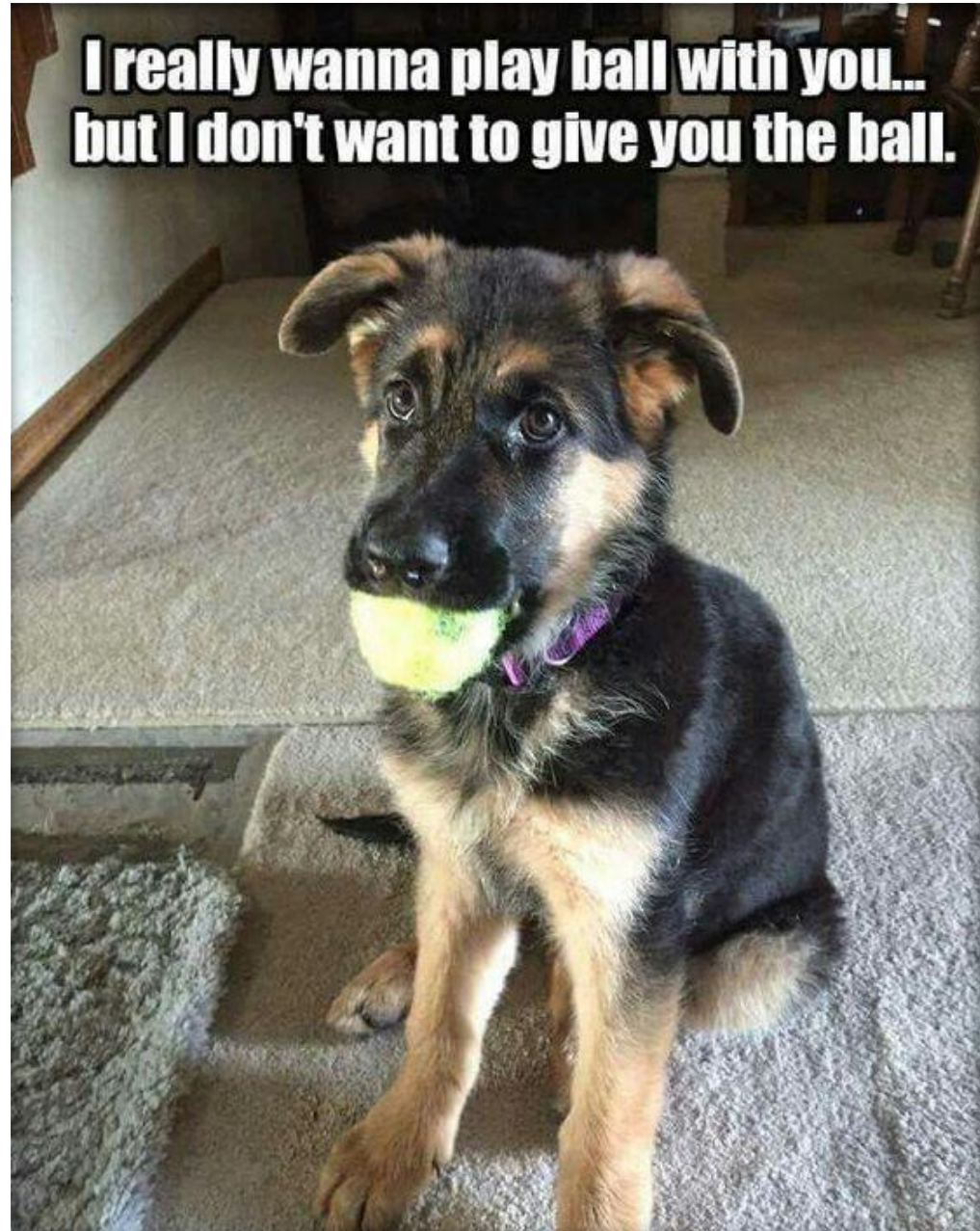
WOODWARD

Honeywell

Let's do an experiment...



Now we have a dilemma...



Now we have a dilemma...

- Any method works at intermediate distances
- (and something else has to be done @ far away)
- Accuracy matters at closeups
- If an 'accurate' intersector were significantly slower, we would have to resort to some complicated LOD scheme...

Taxonomy of ray-hair intersection methods

1. Texture approximations (2D and 3D)

[Andersen et al. 2016; Hadap et al. 2007; Kajiya and Kay 1989; Lengyel et al. 2001; Petrovic et al. 2005; Ren et al. 2010; Sintorn and Assarsson 2009]

2. Fixed 3D cylinders

[Sedaghat 2010; Martins 2016]

3. CPA (the closest point of approach) methods

[Barringer et al. 2012; Chiang et al. 2015; Nakamaru and Ohno 2002; Qin et al. 2014; Reshetov 2017; Woop et al. 2014]

4. Accurate geometric methods

[Wijk 1985; Bronsvoort and Klok 1985]



accuracy



speed

Fortunately...

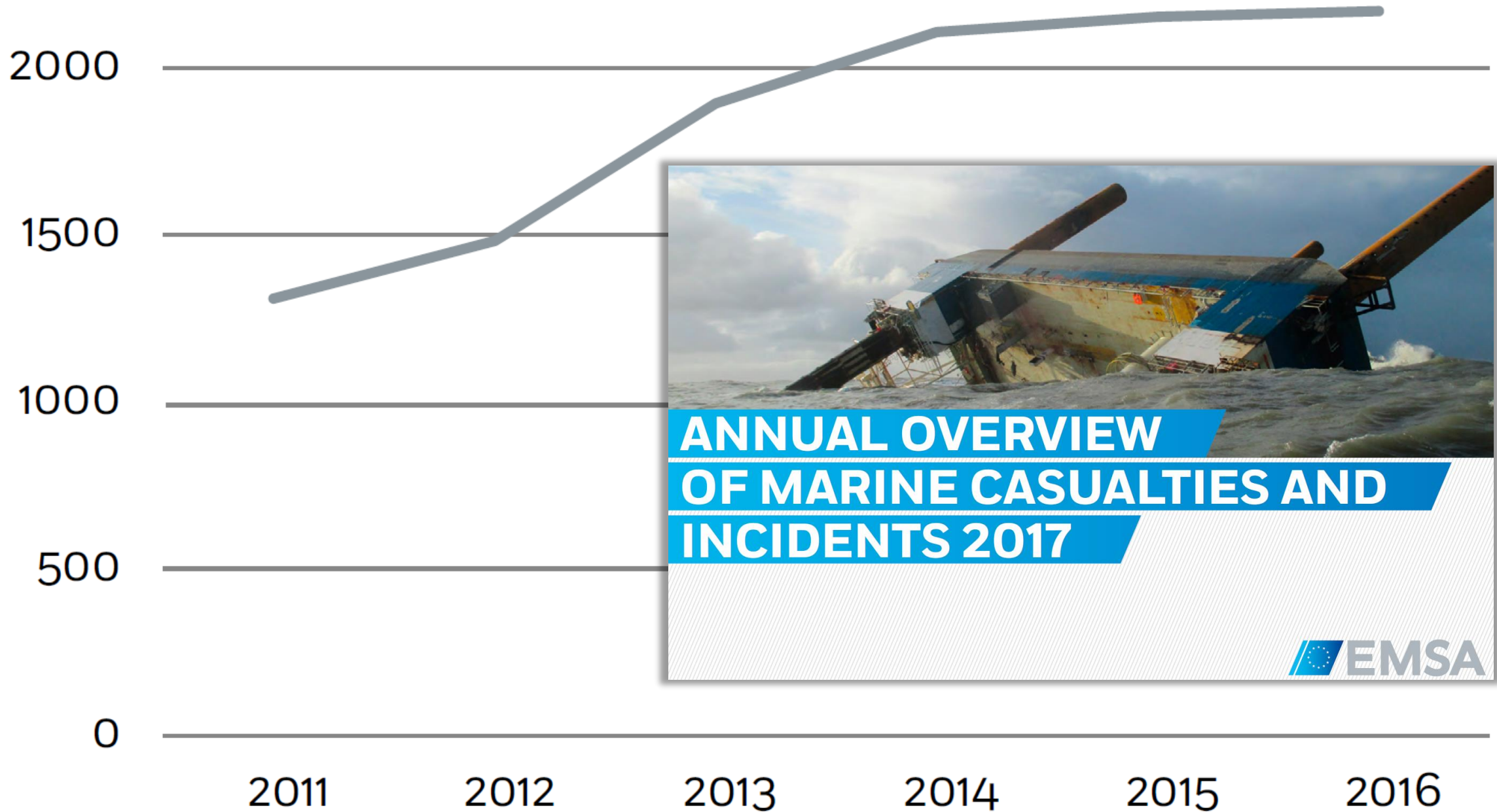
- Phantom intersector is 25% faster than the Budan one on CPU
- while Budan is 5X faster than the adaptive linearization methods
- and it is well suited for GPU implementation
- (I didn't try implementing Budan on GPU)
- fixed cylinders still about 5% faster though by itself, but it is not worth any LOD complications...

Yay for CPA

- We're talking only about CPA => bona fide ray/swept volume intersection
- CPA finds a minimum distance between a ray and a curve that might be useful in other applications (collisions)
- In fact, CPA was first proposed by Morell to reduce ship collisions
J. S. Morrel. 1961. The Physics of Collision at Sea. *Journal of Navigation* 14, 2 (1961), 163–184.



Casualty with a ship

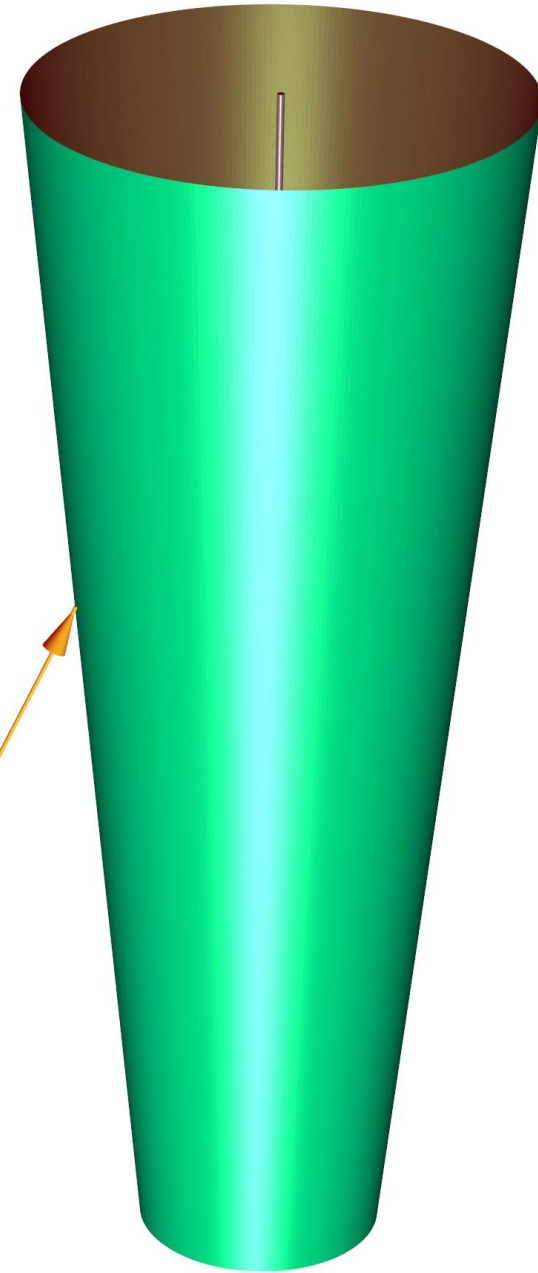


Phantom xsector: the main idea

- Instead of approximating geometry with cylinders (or cones),
- we'll use ray-cone intersection inside an iterative scheme.

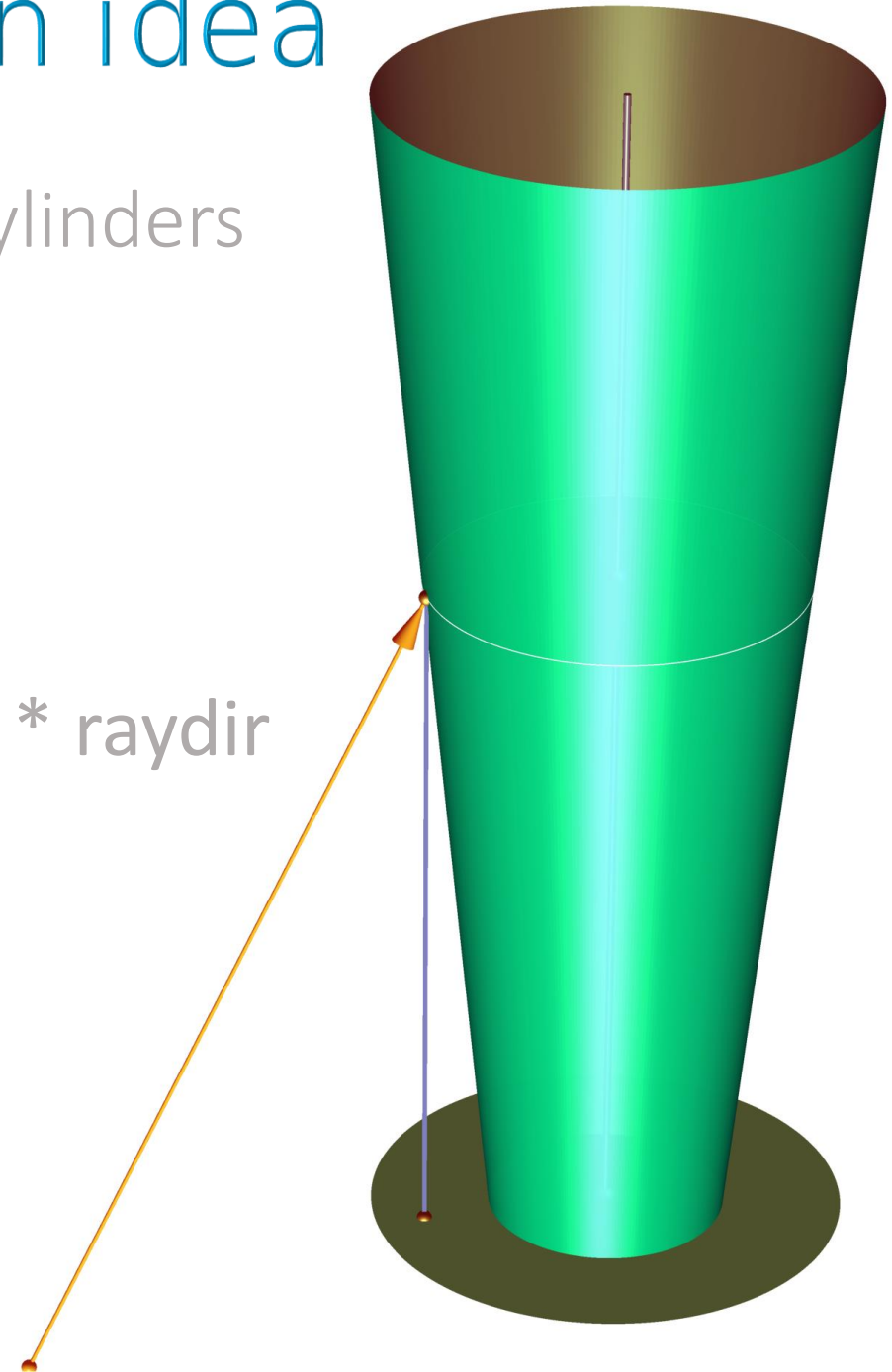
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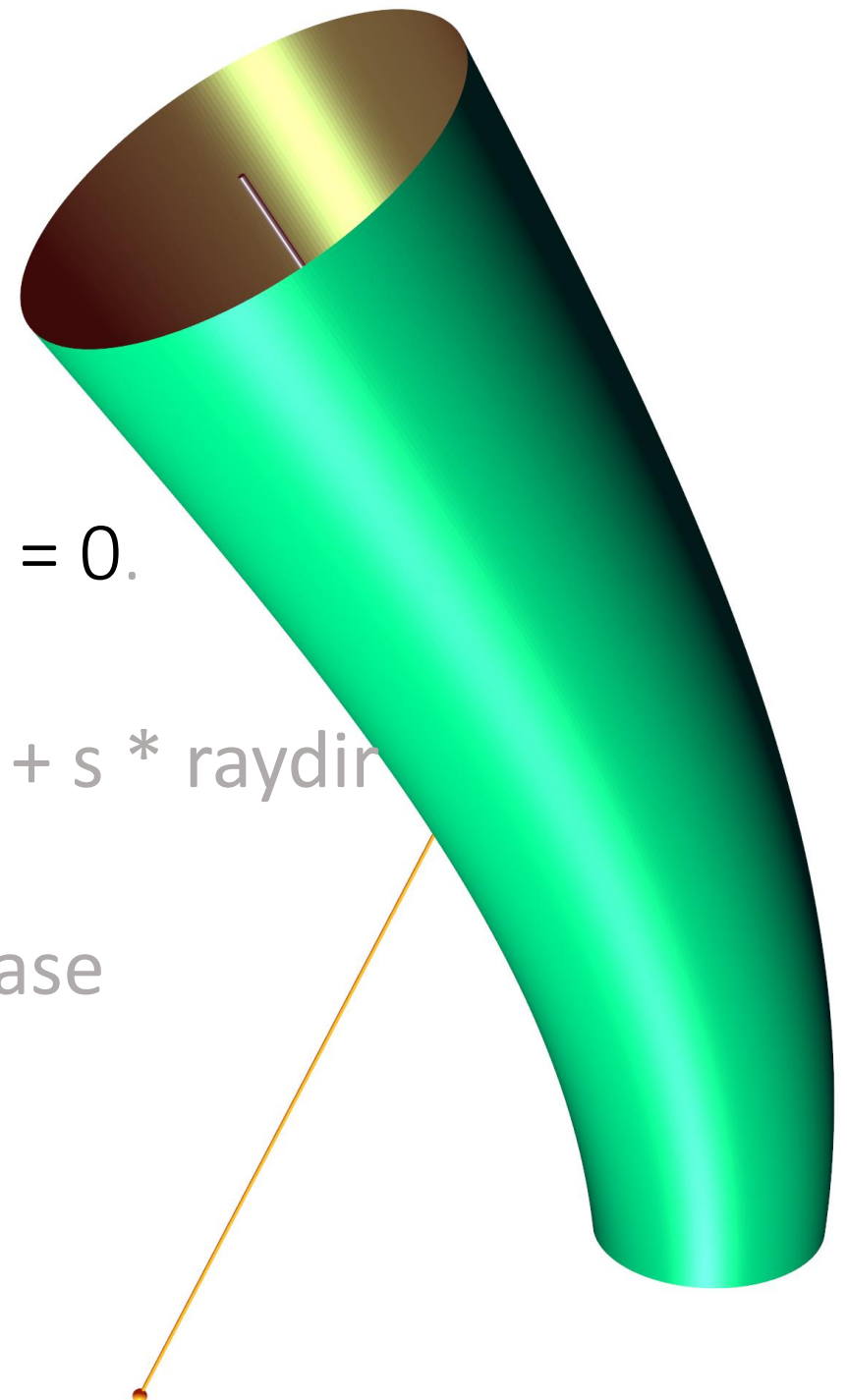
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- To find the surface normal, we will need a **distance to the cone's base**



General case

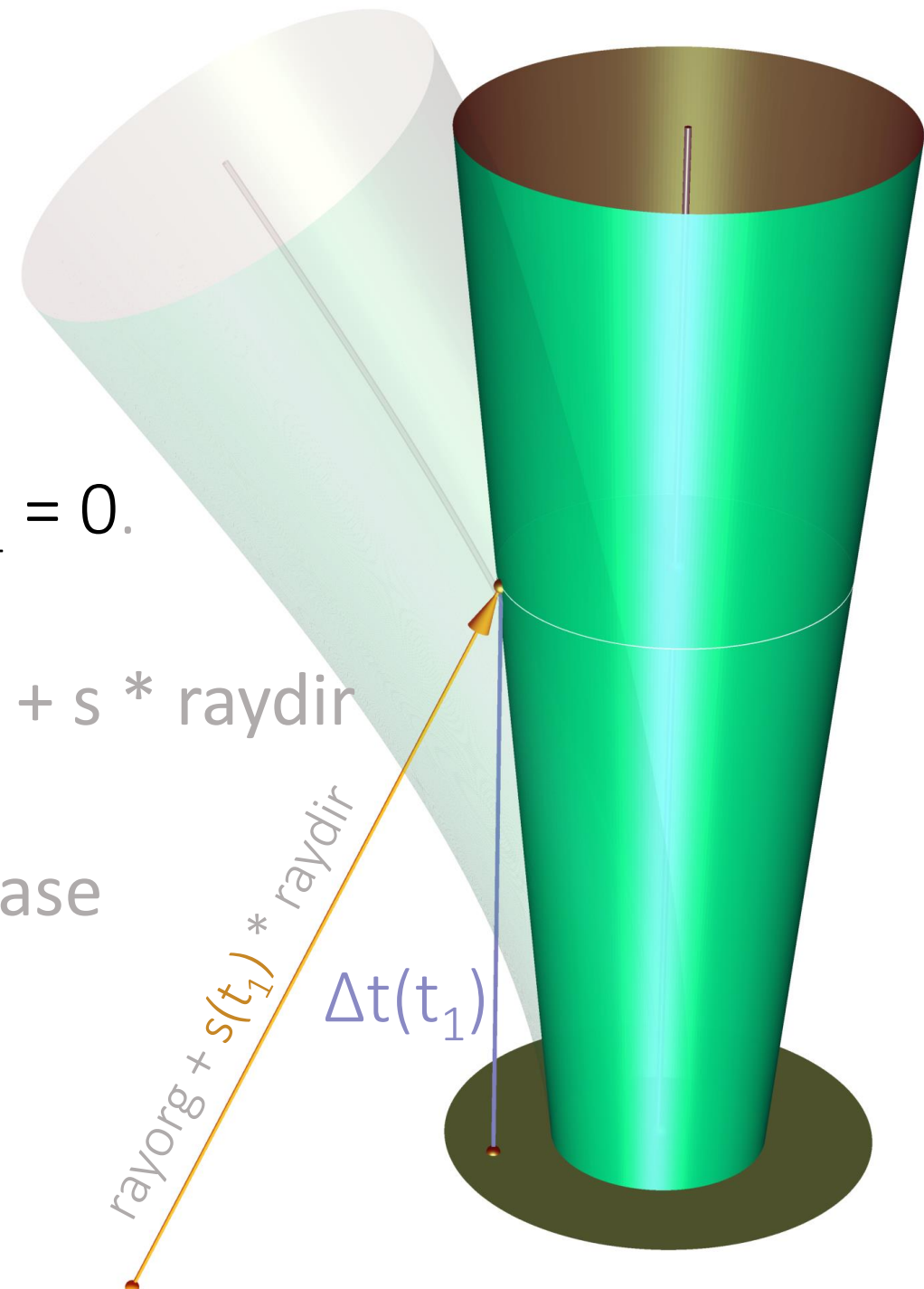
- Instead of approximating geometry,
- we'll use ray-cone intersection inside an iterative scheme starting at $t_1 = 0$.
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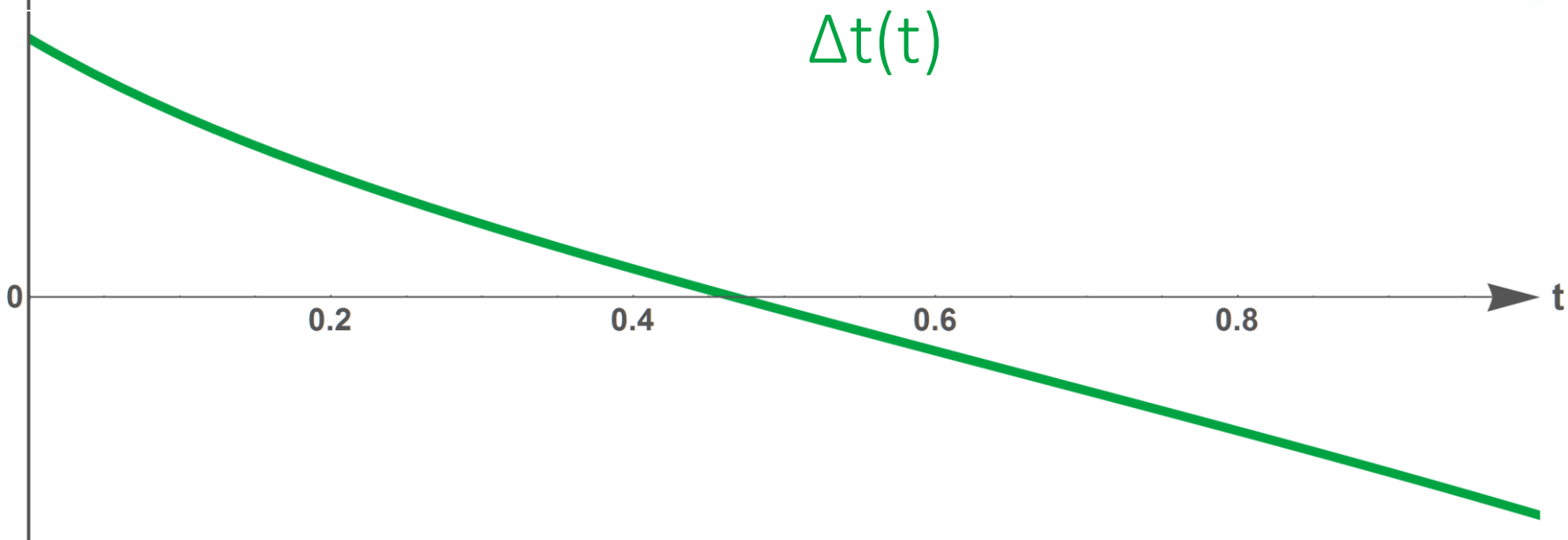
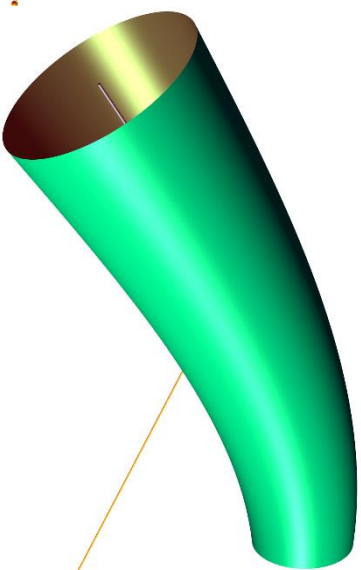
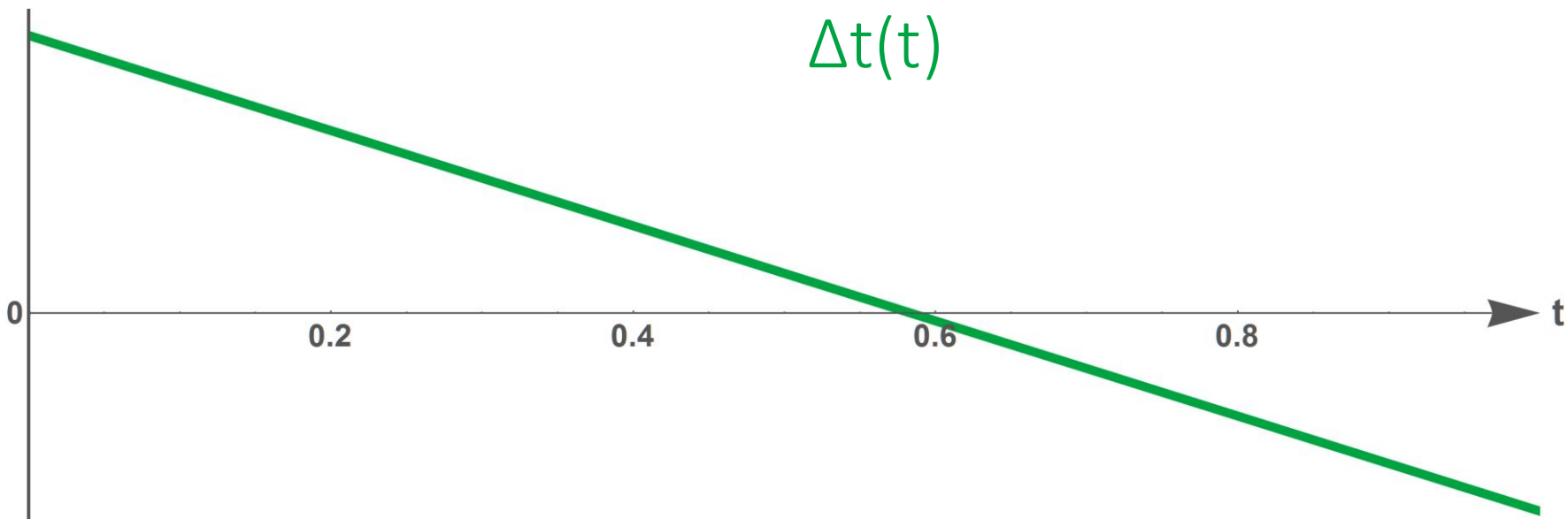
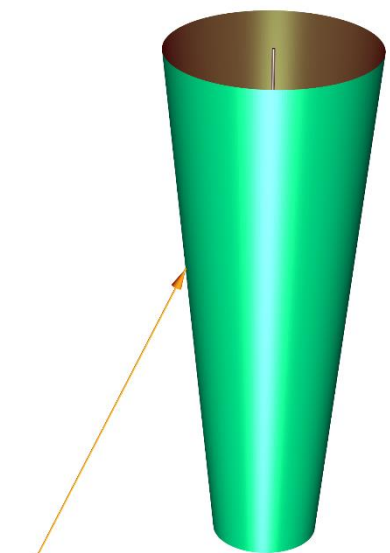
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- To find the surface normal, we will need a distance to the cone's base

1. find $\text{cone}(t_1) \rightarrow s(t_1) \rightarrow \Delta t(t_1)$
2. then set $t_2 = t_1 + \Delta t(t_1)$



It works (mostly) OK



There are two (minor) complications

1. There could be no ray/cone(t) intersections (especially for thin hair)
2. $\Delta t(t)$ function could have ∞ values (ray || cone)

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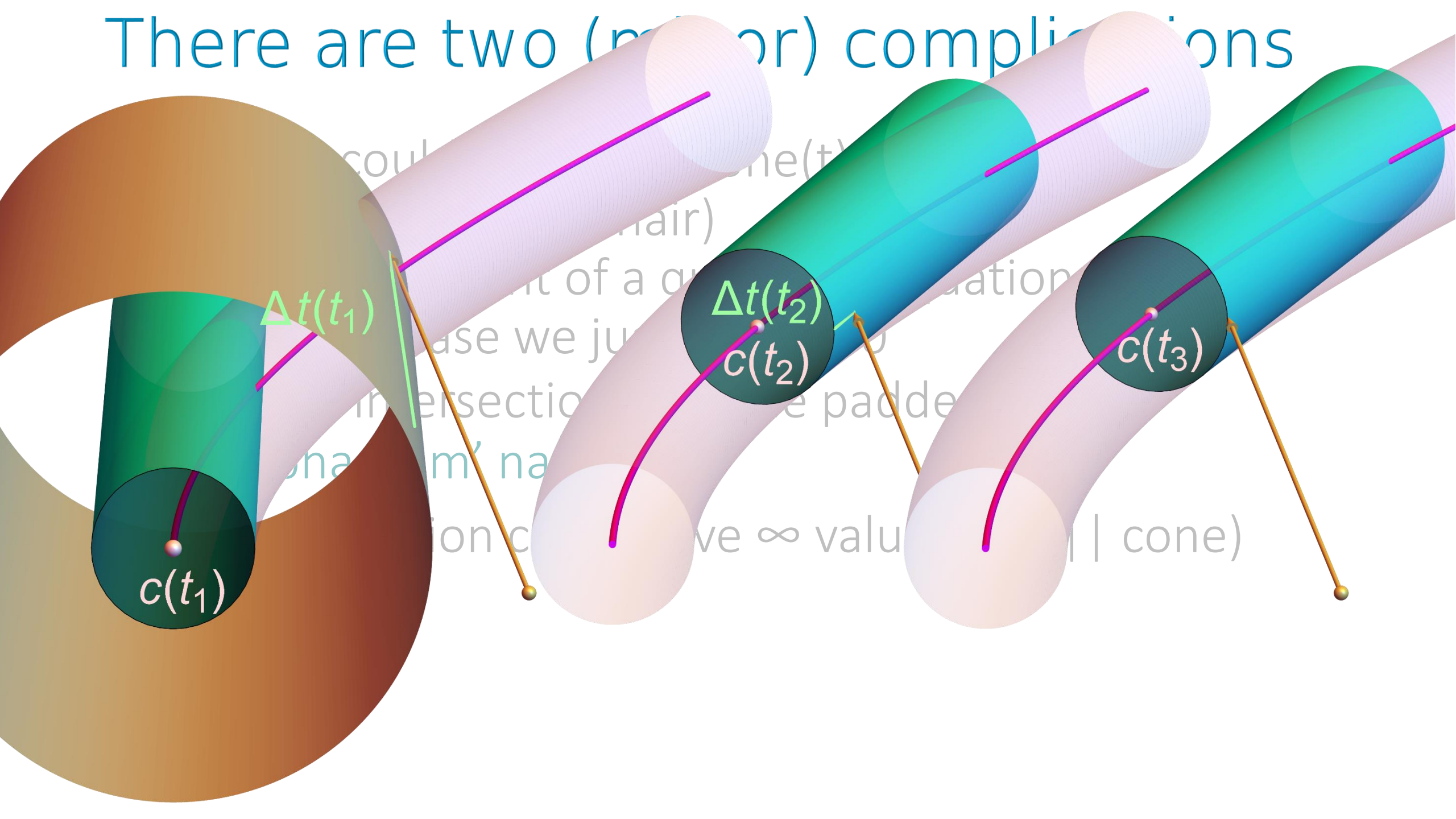
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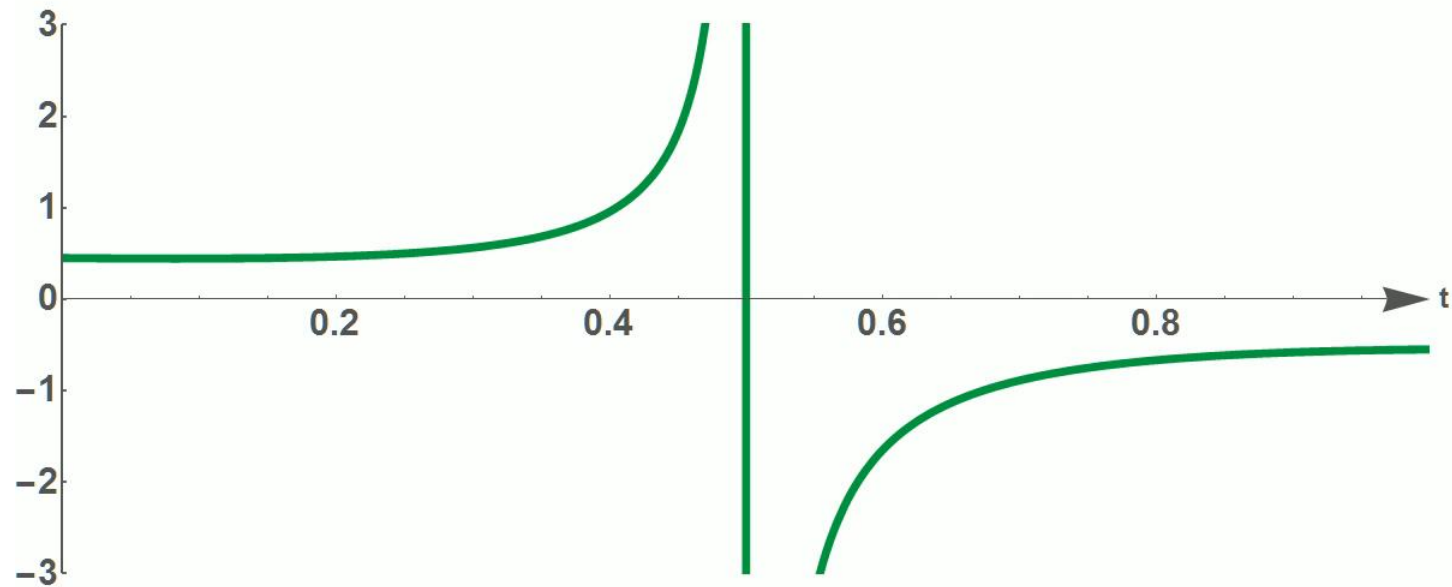


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in such a case we just set it to 0
≡ the intersection with the padded cone
≡ 'phantom' name
2. $\Delta t(t)$ function could have ∞ values (ray || cone)
we need some kind of procedure to address this issue

$$\Delta t(0.5) = \infty$$

single root
two roots



Proceedings of the 1988 Linear Accelerator Conference, Williamsburg, Virginia, USA

NEW FEATURES OF THE ΔT -PROCEDURE FOR AN INTENSIVE ION LINAC

G.A. Dubinsky, A.V. Reshetov, Yu.V. Senichev, E.N. Shaposhnikova

Institute of Nuclear Research of the
Academy of Science of the USSR
Moscow, USSR

Abstract

We investigate Δt -procedure features connected with using the longitudinal bunches instead of the single particle for the tuning of the ion linac. The Δt -procedure for longitudinal bunches is found to be correct from viewpoint of the minimal oscillation of the bunch center of gravity excluding the setting of the RF field amplitude too high. The error of the

ΔT -procedure

Δt -procedure is a method based on the time-of-flight measurements. It allows to set the design field amplitude (i.e. to form the capture region of the given sizes) and to put the particle into the determined phase with respect to the RF field. Let us briefly consider the scheme of Δt -procedure carried out with a single particle for N th cavity of the "ideal"

- Most commonly, Newton - Raphson method is used for root finding...



- Most commonly, Newton's method is used for root finding...
- He also invented cat doors

Newton's experiments were interrupted constantly by his cats scratching at his office door, so he summoned the Cambridge carpenter and had him saw two holes in his door: a large hole for the mother cat and a small one for her kittens.



Why we will not use Newton's method:

$D[dt[t, \{ \{c_{0x}, c_{1x}, c_{2x}, c_{3x}\}, \{c_{0y}, c_{1y}, c_{2y}, c_{3y}\}, \{c_{0z}, c_{1z}, c_{2z}, c_{3z}\} \}, r[t], r'[t]], t]$

```

inline bool intersect(float r, float dr) {
// cone is defined by base center c0, radius r,
// axis cd, and slant dr
float r2 = r * r; // dr could be either positive
float drr = r * dr; // or negative (0 for cylinder)

float ddd = cd.x*cd.x + cd.y*cd.y; // all possible
dp = c0.x*c0.x + c0.y*c0.y; // combinations
float cdd = c0.x*cd.x + c0.y*cd.y; // of x*y terms
float cxd = c0.x*cd.y - c0.y*cd.x; // (c0 x cd)_z

float c = ddd; // compute a,b,c in
float b = cd.z * (drr - cdd); // a - 2 b s + c s^2
float cdz2 = cd.z*cd.z; // (s for ray ∩ cone)
ddd += cdz2; // now it is cd·cd
float a = 2*drr*cdd + cxd*cxd - ddd*r2 + dp*cdz2;
#if defined(KEEP_DR2) // dr^2 adjustments
float qs = (dr*dr)/ddd; // (it does not help
a -= qs * cdd*cdd; // much with neither
b -= qs * cd.z*cdd; // performance nor
c -= qs * cdz2; // accuracy)
#endif
// We will add c0.z to s and sp latter if needed
float det = b*b - a*c; // for a - 2 b s + c s^2
s = (b - (det > 0? sqrt(det) : 0))/c; // c > 0
dt = (s*cd.z - cdd)/ddd; // wrt t
dc = s*s + dp; // |(ray ∩ cone) - c0|^2
sp = cdd/cd.z; // will add c0.z latter
dp += sp*sp; // |(ray ∩ plane) - c0|^2

return det > 0; // true (real) or false (phantom)
}

```

$$- \left(\frac{((c_x + 2t c_{0x} + 3t^2 c_{1x})(c_x - t c_{0x} - t^2 c_{1x} - t^3 c_{2x}) - (c_y + 2t c_{0y} + 3t^2 c_{1y})(c_y - t c_{0y} - t^2 c_{1y} - t^3 c_{2y}))(c_x + 2t c_{0x} + 3t^2 c_{1x}) r[t]^2}{(c_x + 2t c_{0x} + 3t^2 c_{1x})^2 + (c_y + 2t c_{0y} + 3t^2 c_{1y})^2 + (c_z + 2t c_{0z} + 3t^2 c_{1z})^2} \right) - \sqrt{t \left(\left((c_x + t c_{0x} + t^2 c_{1x} + t^3 c_{2x})(c_x - 2t c_{0x} - 3t^2 c_{1x}) - (c_y + 2t c_{0y} + 3t^2 c_{1y})(c_y - t c_{0y} - t^2 c_{1y} - t^3 c_{2y}) - r[t]^2 \right) - \left((c_x + t c_{0x} + t^2 c_{1x} + t^3 c_{2x})(c_x - 2t c_{0x} - 3t^2 c_{1x}) - (c_y + 2t c_{0y} + 3t^2 c_{1y})(c_y - t c_{0y} - t^2 c_{1y} - t^3 c_{2y}) - r[t]^2 \right) \right)} \left(\frac{2(c_x + 2t c_{0x} + 3t^2 c_{1x})(c_x - t c_{0x} - t^2 c_{1x} - t^3 c_{2x})}{(c_x + 2t c_{0x} + 3t^2 c_{1x})^2 + (c_y + 2t c_{0y} + 3t^2 c_{1y})^2 + (c_z + 2t c_{0z} + 3t^2 c_{1z})^2} \right) + \left(\frac{(c_x + 2t c_{0x} + 3t^2 c_{1x})^2 + (c_y + 2t c_{0y} + 3t^2 c_{1y})^2 + (c_z + 2t c_{0z} + 3t^2 c_{1z})^2}{(c_x + 2t c_{0x} + 3t^2 c_{1x})^2 + (c_y + 2t c_{0y} + 3t^2 c_{1y})^2 + (c_z + 2t c_{0z} + 3t^2 c_{1z})^2} \right) r[t]^2 \right)$$

$\Delta t'[t] =$

$$2 \left((c_x + t c_{0x} + t^2 c_{1x} + t^3 c_{2x})(2 c_{0y} + 6 t c_{1y} + 2 c_{2y} + 6 t^2 c_{3y}) - (2 c_{0x} + 6 t c_{1x} + 2 c_{2x} + 6 t^2 c_{3x})(c_y + 2 t c_{0y} + 3 t^2 c_{1y}) - (c_x + t c_{0x} + t^2 c_{1x} + t^3 c_{2x})(c_y + 2 t c_{0y} + 3 t^2 c_{1y}) - 2 \left((c_y + t c_{0y} + t^2 c_{1y} + t^3 c_{2y})(c_x - 2 t c_{0x} - 3 t^2 c_{1x}) - (c_y + 2 t c_{0y} + 3 t^2 c_{1y})(c_x - t c_{0x} - t^2 c_{1x} - t^3 c_{2x}) \right) - 2 t c_{0z} \left((c_x + 2 t c_{0x} + 3 t^2 c_{1x})(c_x - t c_{0x} - t^2 c_{1x} - t^3 c_{2x}) - (c_y + 2 t c_{0y} + 3 t^2 c_{1y})(c_y - t c_{0y} - t^2 c_{1y} - t^3 c_{2y}) \right) - 2 \left((c_x + 2 t c_{0x} + 3 t^2 c_{1x})(c_x - t c_{0x} - t^2 c_{1x} - t^3 c_{2x}) - (c_y + 2 t c_{0y} + 3 t^2 c_{1y})(c_y - t c_{0y} - t^2 c_{1y} - t^3 c_{2y}) \right) \right) r[t]^2 - \left(\frac{2(c_x + 2t c_{0x} + 3t^2 c_{1x})(c_x - t c_{0x} - t^2 c_{1x} - t^3 c_{2x})}{(c_x + 2t c_{0x} + 3t^2 c_{1x})^2 + (c_y + 2t c_{0y} + 3t^2 c_{1y})^2 + (c_z + 2t c_{0z} + 3t^2 c_{1z})^2} \right) r[t]^2$$

Instead, we use the *regula falsi* method

- credited to Babylonian Mathematics
- they had also invented sexagesimal (base 60) numeral system
- aka false position method
 1. Using 2 function values, find the abscissa crossing (as in the *secant* method)
 2. Adjust bounds to keep the root inside
- What we do: after first iteration $t_2 = t_1 + \Delta t(t_1)$
 1. use *regula falsi* if $\Delta t(t_1) * \Delta t(t_2) < 0$
 2. otherwise use $t_2 + \Delta t(t_2)$
 3. clamp Δt values to $[-0.5, 0.5]$ interval (it helps in ray || cone situations)
 4. switch to $(t_i + t_{i-1})/2$ every 4th iteration

OptiX triX

From: Detlef Roettger

Sent: Friday, October 27, 2017 2:12 AM

To: Alexander Reshetov <areshetov@nvidia.com>

Subject: RE: NVIDIA-OptiX-SDK-5.0.0-DEV-win64.exe

Your RSVI curve primitives look better than anything I've seen in papers so far. Very nice!

Are the different colors indicating separate AABBs or just visualizing the proper t interpolant along the curve?

For additional performance analysis with OptiX you can make use of an OptiX developer build and look at which device programs used how many clocks.

Normally intersection programs are inlined and the clocks of that appear inside the traversal as well, but you can switch off inlining for that with another OptiX knob.

The procedure is simple:

- Create an empty file named `optix.props` next to your OptiX DLL.
- Run your application, end it.
- Now the OptiX developer build should have written all available knobs into that `optix.props` file as comments (~43 kB)
- Open it in an editor and search for the knob `stats.timeVpcs` uncomment and set it to 1.
- If you start your OptiX program now from a command line, OptiX will print out a table per launch (to `stderr` by default) with information about how many rays you shot, how many clocks were used and which program spent how many of them in absolute values and percentages.

The last column in that table shows the occupancy where 32 is perfect.

My non-default `optix.props` settings

`acceleration.bvh.traversal_cost` 0.4

`deviceManager.forceSmVersion` 50

`log.colored` 0

`megakernel.loadBalancer.memoryWeight` 0.8

`megakernel.loadBalancer.smWeight` 0.2

`megakernel.register.attributeSwitch` 1

`megakernel.register.currentTmax` 1

also using `context->createAcceleration("Bvh8")`

Performance

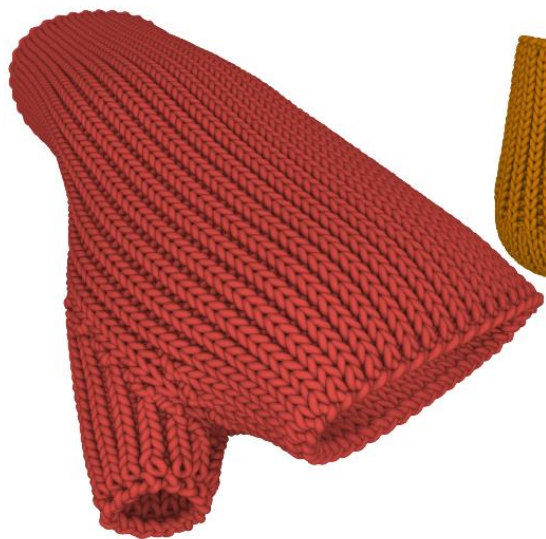


400K curves, 145M rays/s @ Titan Xp



1K snakes, 250M rays/s

© SNAKEB



a. 58537 curves
412M rays/s



b. 139506 curves
400M rays/s



c. 729628 curves
322M rays/s



d. 271902 curves
515M rays/s



e. 756453 curves
531M rays/s

*A Titan Xp performance for the different yarn models [Wu and Yuksel 2017; Yuksel et al. 2012]
for one primary and four ambient occlusion rays at 1000×1000 screen resolution*



a. 58537 curves

412M rays/s

*A Titan Xp performed
for one primary and*



curves

rs/s

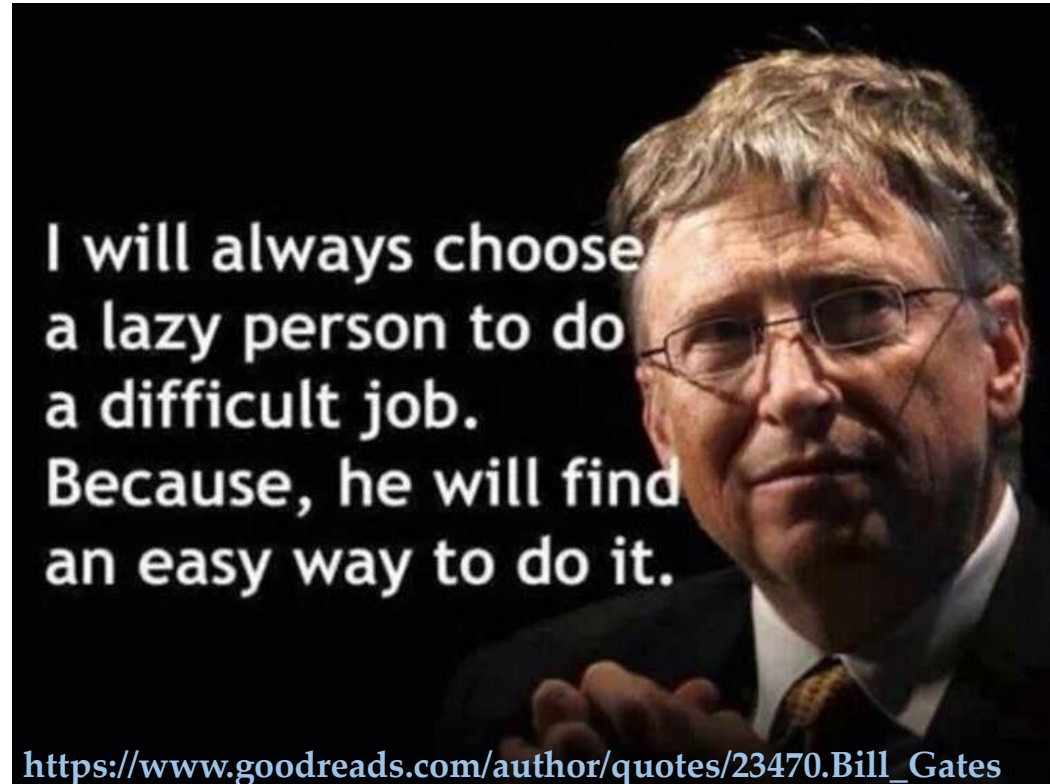
e. 756453 curves

531M rays/s

Yuksel et al. 2012]
ation

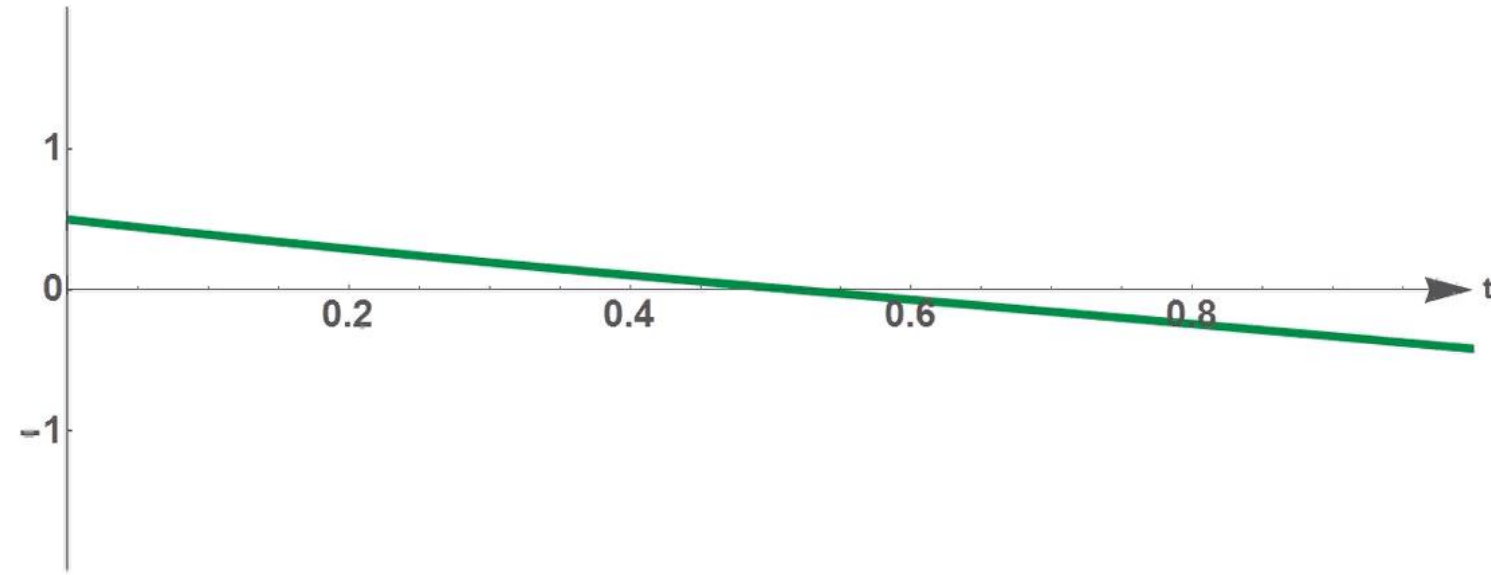
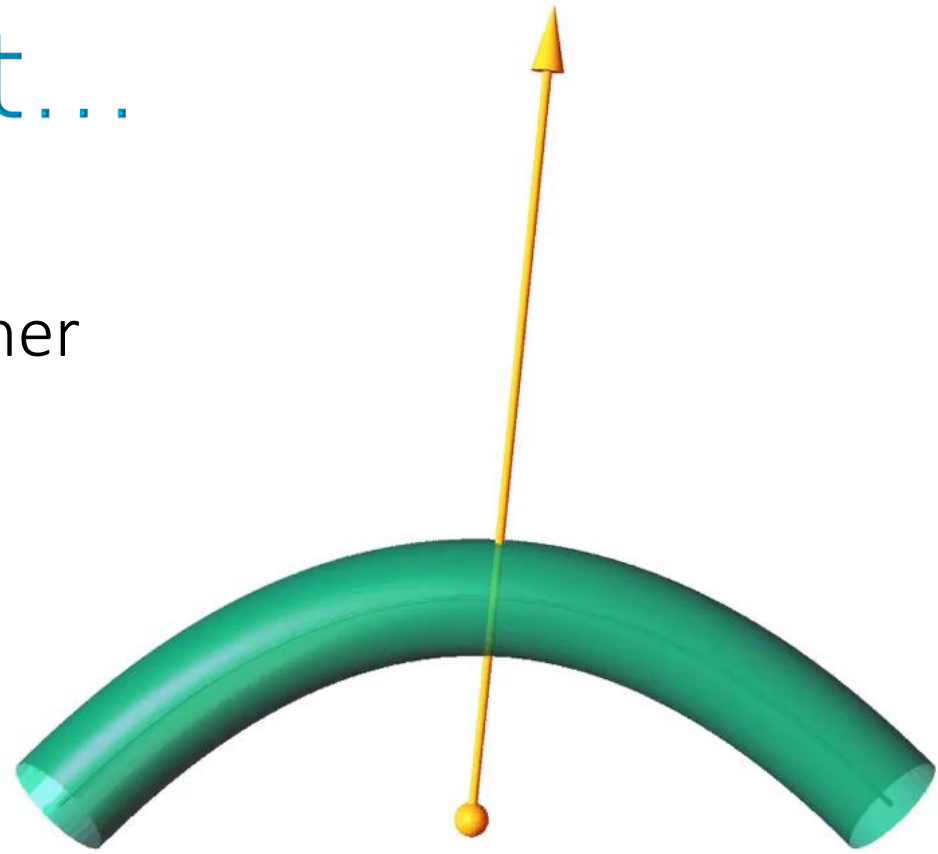
Limitations

- It is all applicable only for ray-tracing problems (“reverse rasterization”)
- By itself, “finding roots of $\Delta t(t)$ ” is just an algebra-speak for “finding ray – surface intersections”
- But we want to do it lazily...
- ... and it might cause problems

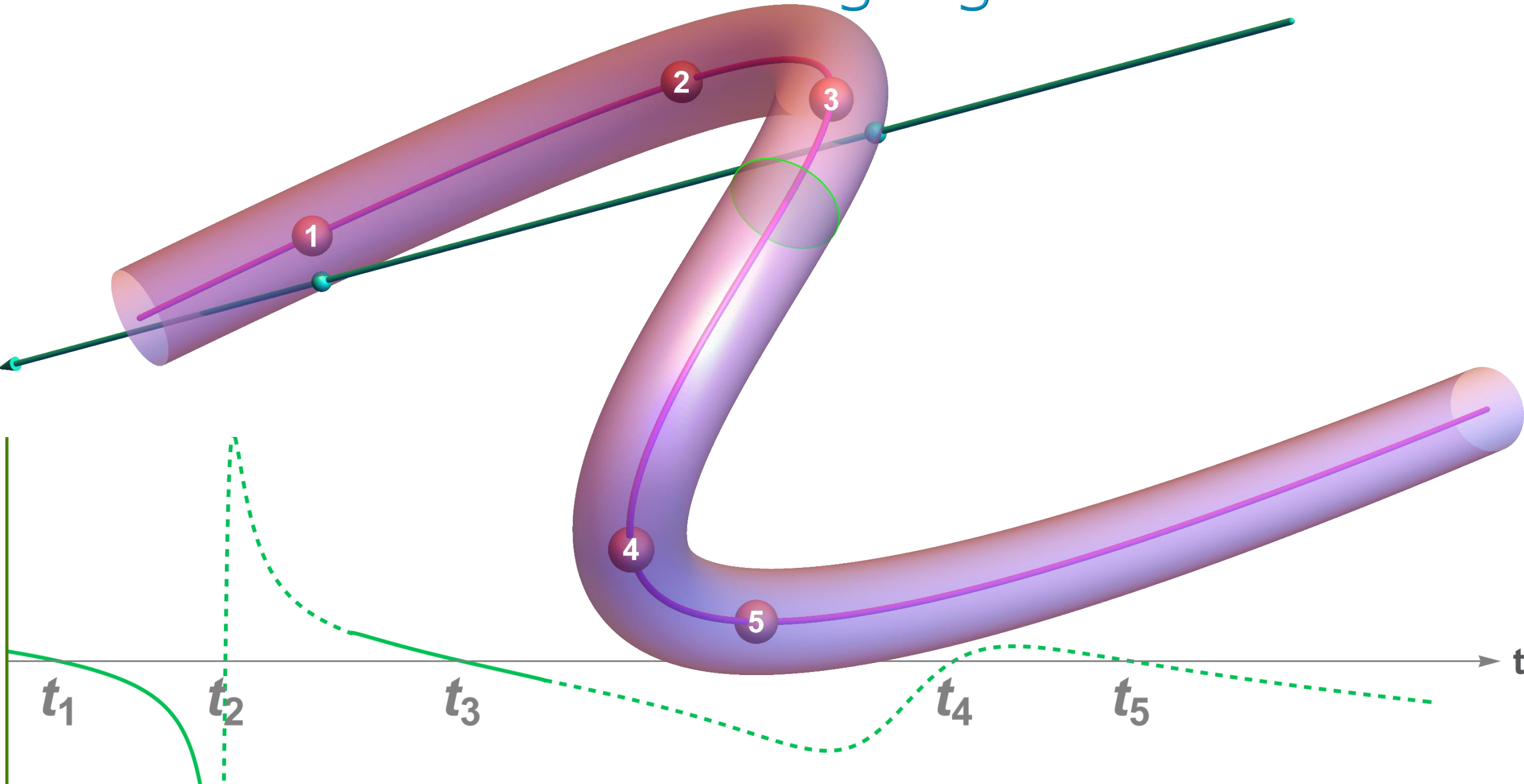


Another experiment...

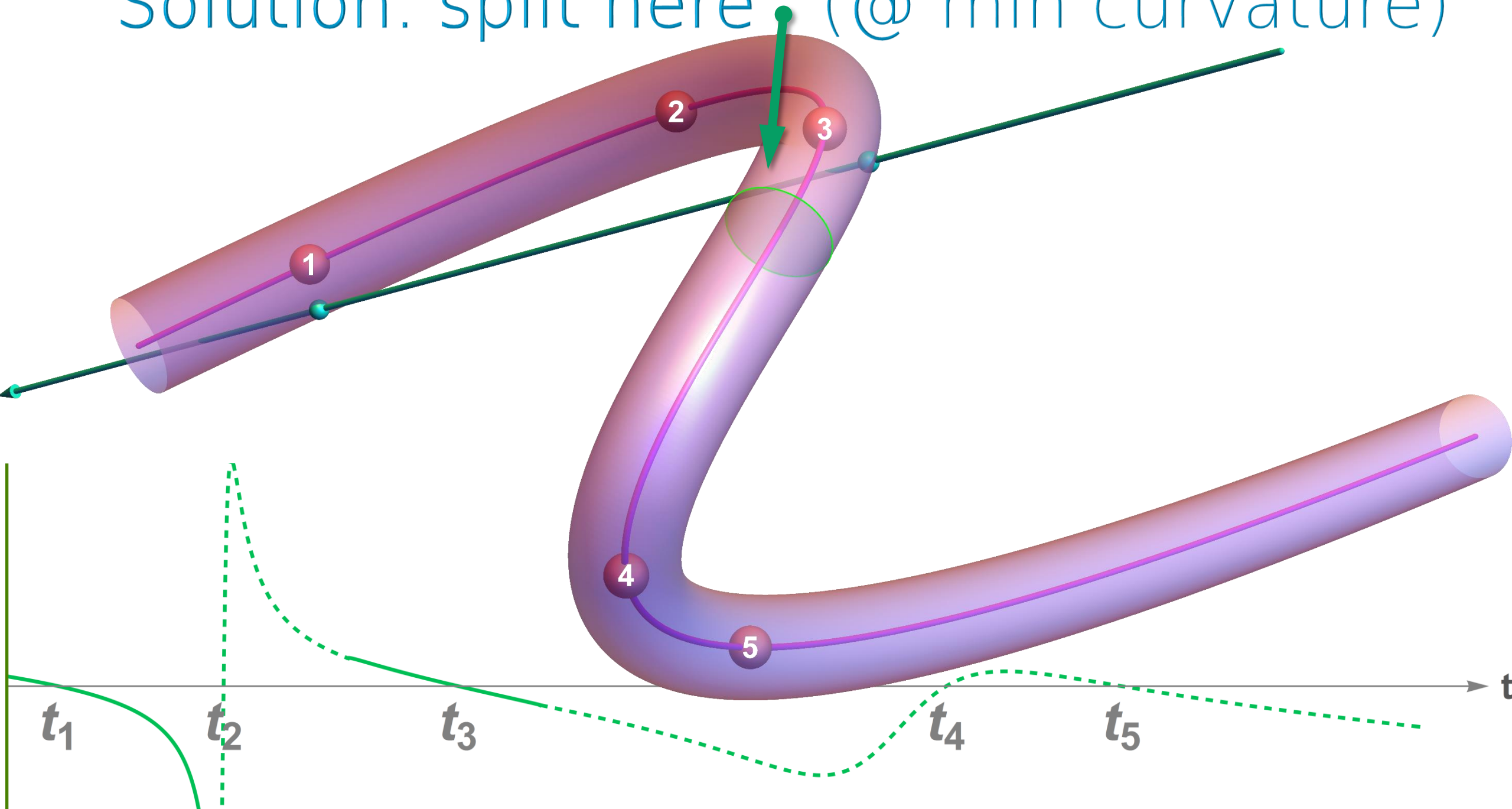
- $\Delta t(t)$ is almost linear;
root $t = 0.5$ can be found starting at either
 $t = 0$ or $t = 1$
- Phantom values near
 $t = 0$ or $t = 1$; $\Delta t(t)$ is still \approx linear
- root $t = 0.5$ got hidden by the phantom
values near $t = 0$ or $t = 1$



Problems with zigzag curves



Solution: split here (@ min curvature)



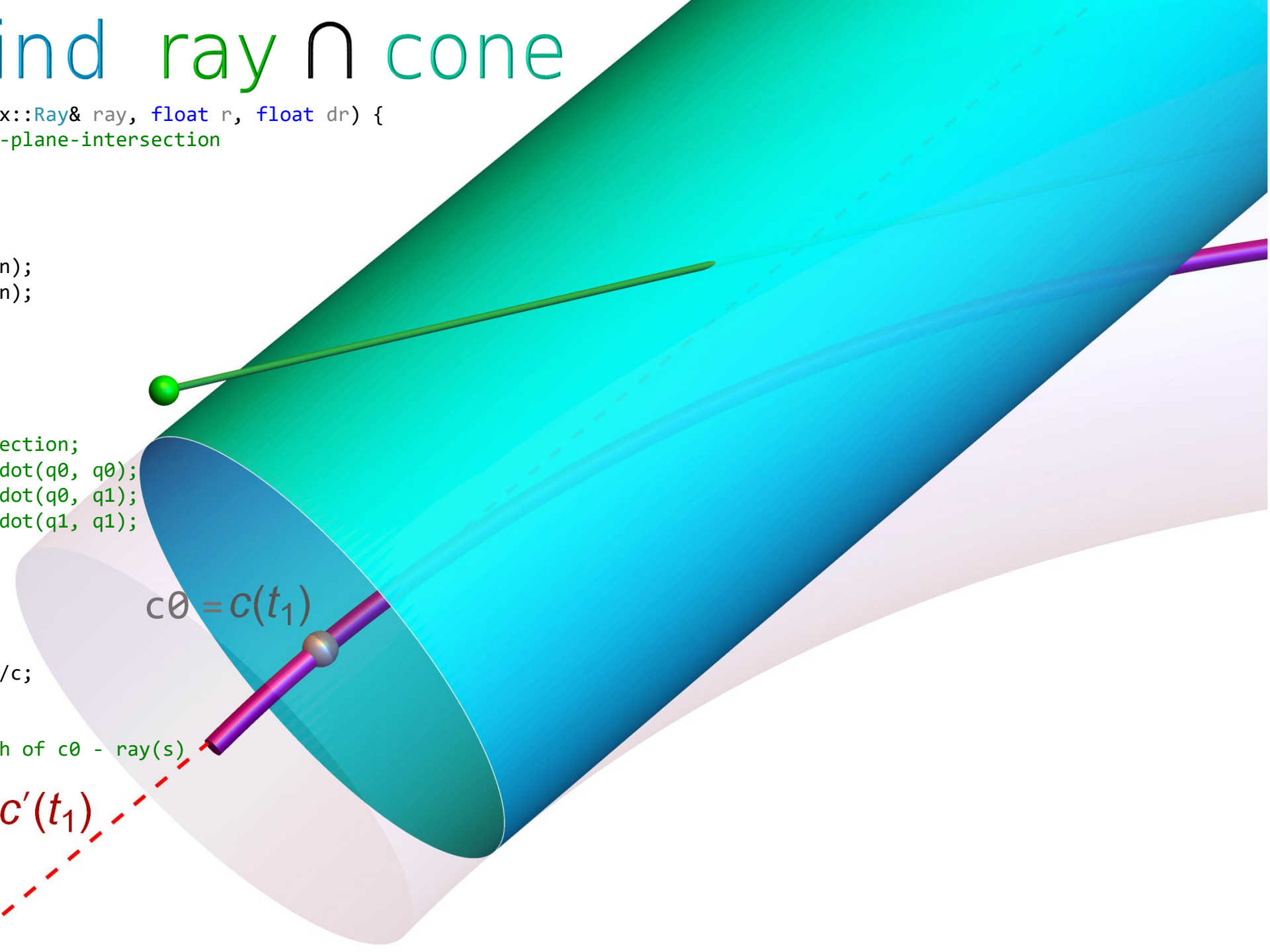
no splits



8 splits per curve

Step 1/3: find ray \cap cone

```
inline bool intersectCone(const optix::Ray& ray, float r, float dr) {  
    // d = q0 + q1*s = (c0+cd*t) - ray-plane-intersection  
    float3 cr = c0 - ray.origin;  
    float cdc = dot(cd, cd);  
    float crcd = dot(cr, cd);  
    float crcr = dot(cr, cr);  
    float crrd = dot(cr, ray.direction);  
    /* */ cdrd = dot(cd, ray.direction);  
    float cdrdn = cdrd/cdc;  
    float crcdn = crcd/cdc;  
    r = r - dr * crcdn;  
    dr = dr * cdrdn;  
    //float3 q0 = cr - cd * crcdn;  
    //float3 q1 = cd * cdrdn - ray.direction;  
    float q00 = crcr - crcd*crcdn; // dot(q0, q0);  
    float q01 = cdrd*crcdn - crrd; // dot(q0, q1);  
    float q11 = 1 - cdrd*cdrdn; // dot(q1, q1);  
  
    float a = q00 - r*r;  
    float b = q01 - r*dr;  
    float c = dr*dr - q11;  
    float det = b*b + a*c;  
    s = (b + (det < 0? 0 : sqrt(det)))/c;  
    dt = cdrdn * s - crcdn;  
  
    // Compute |cr - s rd|, i.e. length of c0 - ray(s)  
    dc = crcr - 2*crrd*s + s*s;  
  
    sp = crcd/cdrd;  
    dp = crcr - 2*crrd*sp + sp*sp;  
  
    return det > 0;  
}
```



Step 2/3: find $\Delta t(t_1)$

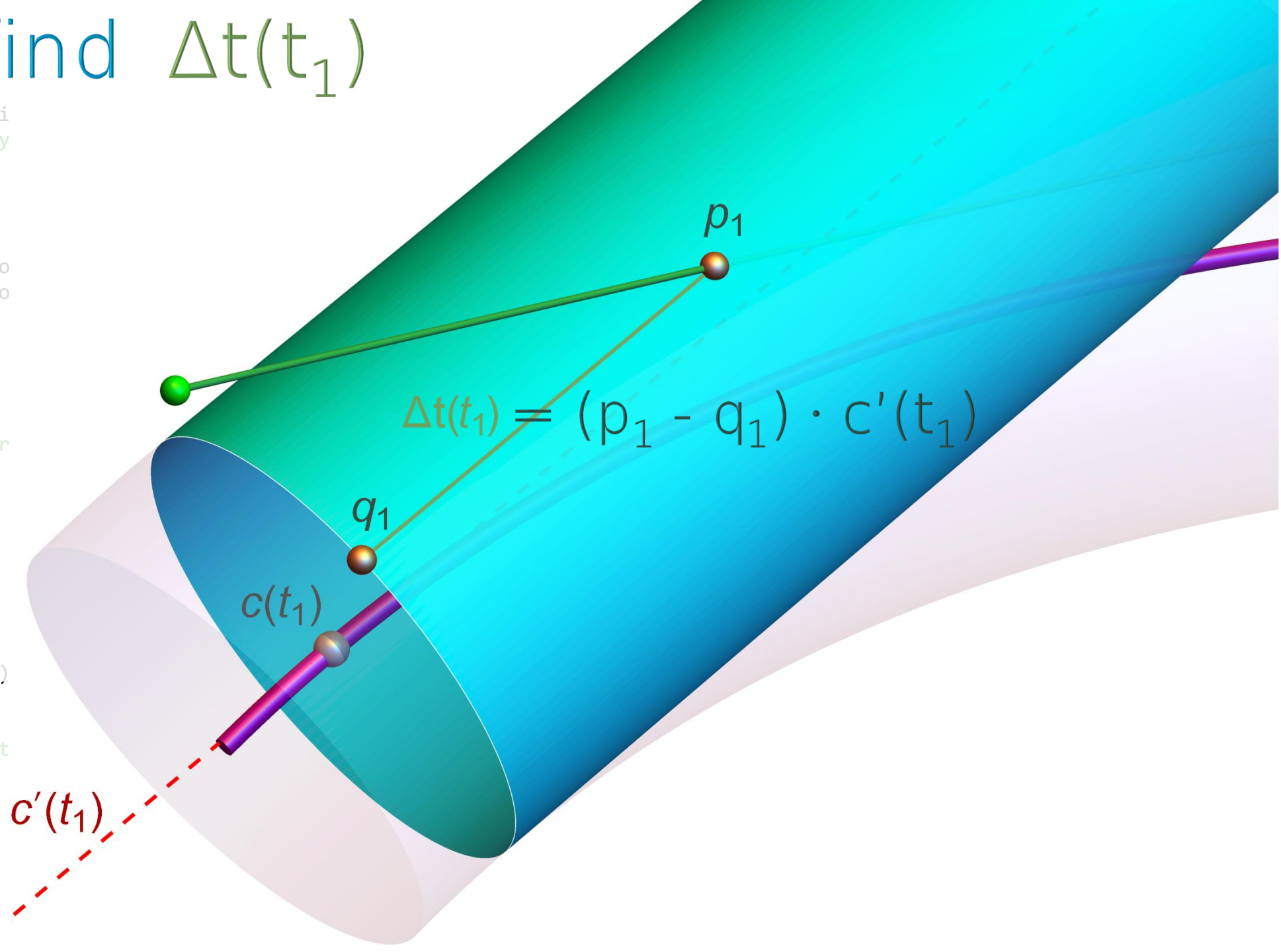
```
inline bool intersectCone(const opti
// d = q0 + q1*s = (c0+cd*t) - ray
float3   cr = c0 - ray.origin;
float   cdc = dot(cd, cd);
float   crcd = dot(cr, cd);
float   crcr = dot(cr, cr);
float   crrd = dot(cr, ray.directio
/* */   cdrd = dot(cd, ray.directio
float   cdrdn = cdrd/cdc;
float   crcdn = crcd/cdc;
r   = r - dr * crcdn;
dr = dr * cdrdn;
//float3 q0 = cr - cd * crcdn;
//float3 q1 = cd * cdrdn - ray.dir
float   q00 = crcr - crcd*crcdn; //
float   q01 = cdrd*crcdn - crrd; //
float   q11 = 1 - cdrd*cdrdn; //

float   a = q00 - r*r;
float   b = q01 - r*dr;
float   c = dr*dr - q11;
float   det = b*b + a*c;
s = (b + (det < 0? 0 : sqrt(det)))
dt = cdrdn * s - crcdn;

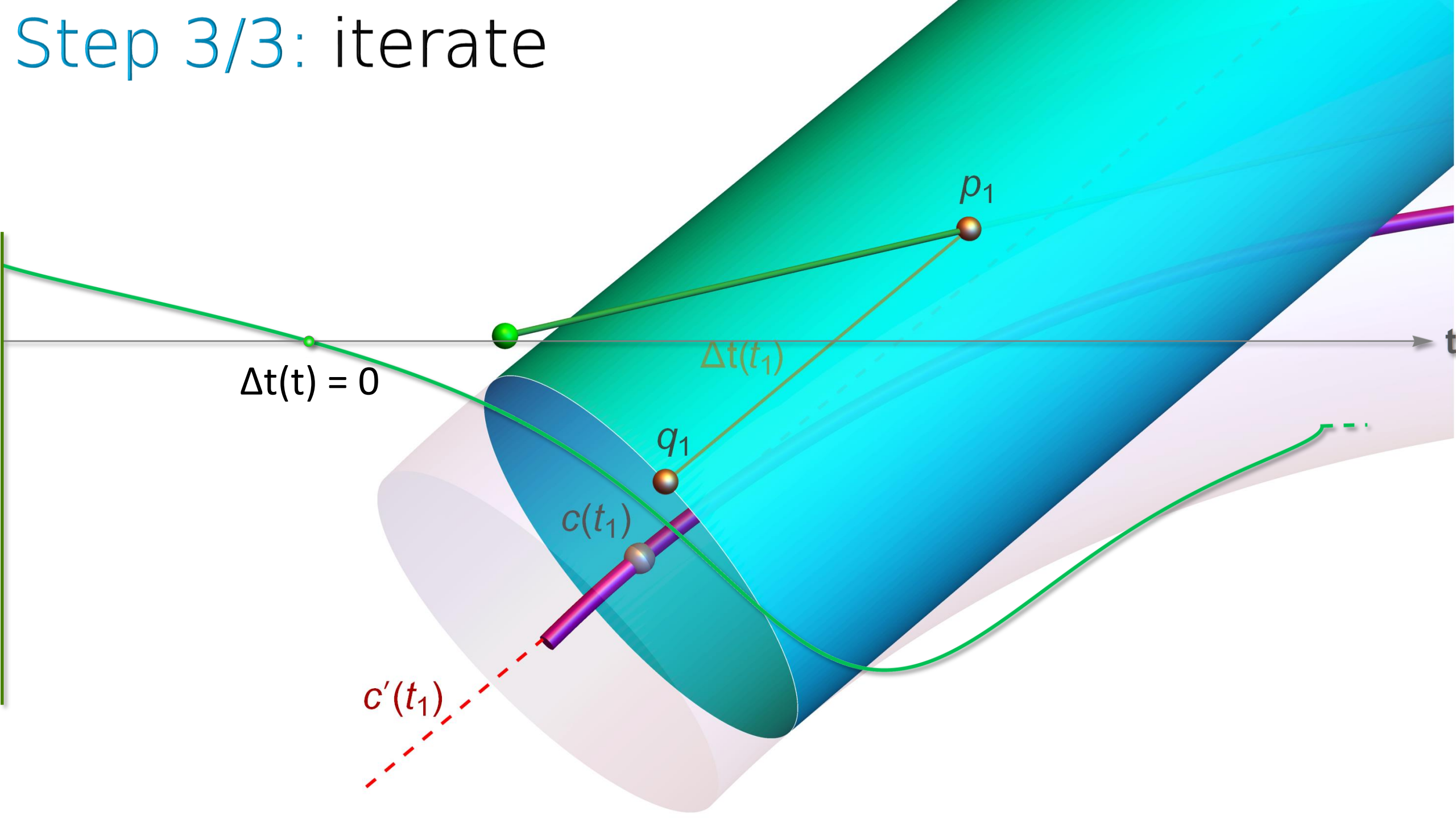
// Compute |cr - s rd|, i.e. lengt
dc = crcr - 2*crrd*s + s*s;

sp = crcd/cdrd;
dp = crcr - 2*crrd*sp + sp*sp;

return det > 0;
}
```



Step 3/3: iterate



The topics covered in this presentation

- Killer drones
- Newton's pets
- Bill Gate's pet peeves
- Daniel Day-Lewis' last movie
- Bender Bending Rodríguez' vocation
- Control systems for particle accelerators
- Star constellations
- Maritime science
- Rendering of flying saucers; sausage; snakes; hair/fur; yarn
- World Cup 2018
- Germany's population growth
- Hardline rock-n-roll
- Zombies invasion



pensive things





We saw this whole zombie thing coming from a mile away... we already have safe houses and are stocked up...

#zombielove

<http://www.purevolume.com/new/phathom>

Sagitta!

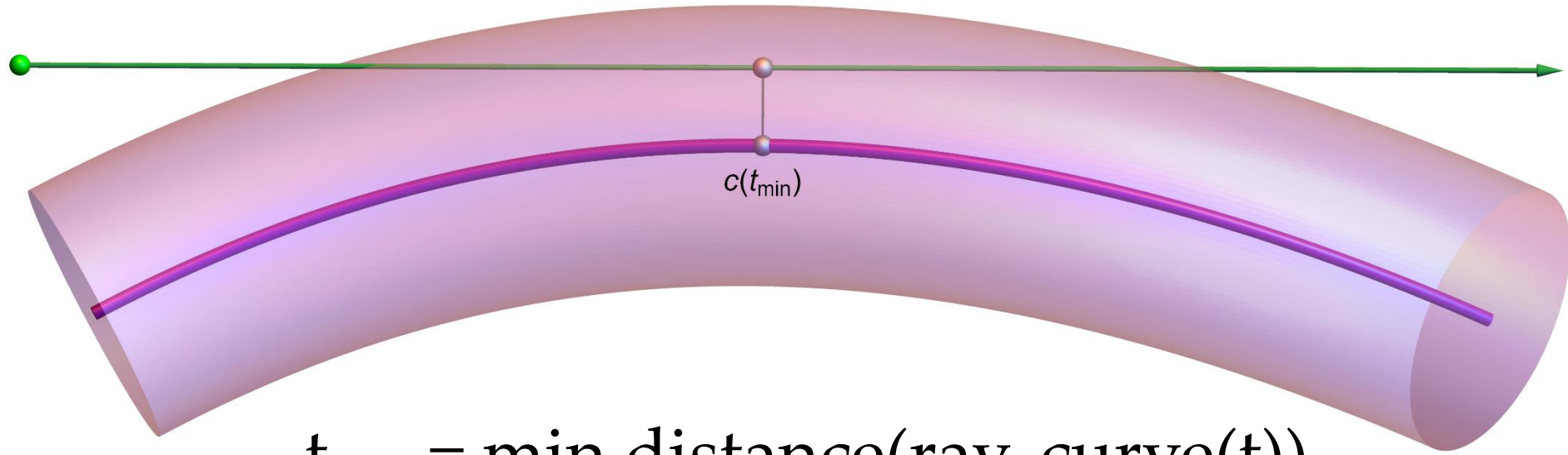
```
inline bool intersectCylindricalEnclosure(const optix::Ray& ray, float2& limits) const {
    // cylinder is defined by axis acyl, radius^2 = rcyl and point on the axis pcyl
    float3 nn = cross(ray.direction, acyl); // orthogonal to both
    float3 r2c = ray.origin - pcyl;
    float distance_from_ray_to_cylinder_axis = dot(r2c, nn);
    float innlen2 = 1.0f/dot(nn, nn);

    float d2 = distance_from_ray_to_cylinder_axis * distance_from_ray_to_cylinder_axis;
    float sagitta = rcyl - d2 * innlen2;

    // compute distance from ray.origin to the closest point between the ray and acyl
    float3 o2c = cross(r2c, acyl);
    float po2c = dot(o2c, nn);
    limits.x = limits.y = -po2c * innlen2;
    // now reproject 2D sagitta (in the plane orthogonal to the tangent) back into 3D
    sagitta = sagitta > 0? sqrt(sagitta * innlen2) : 0;
    limits.x = optix::fmaxf(limits.x - sagitta, ray.tmin);
    limits.y = optix::fminf(limits.y + sagitta, ray.tmax);

    return limits.y > 0 && limits.x < limits.y;
}
```

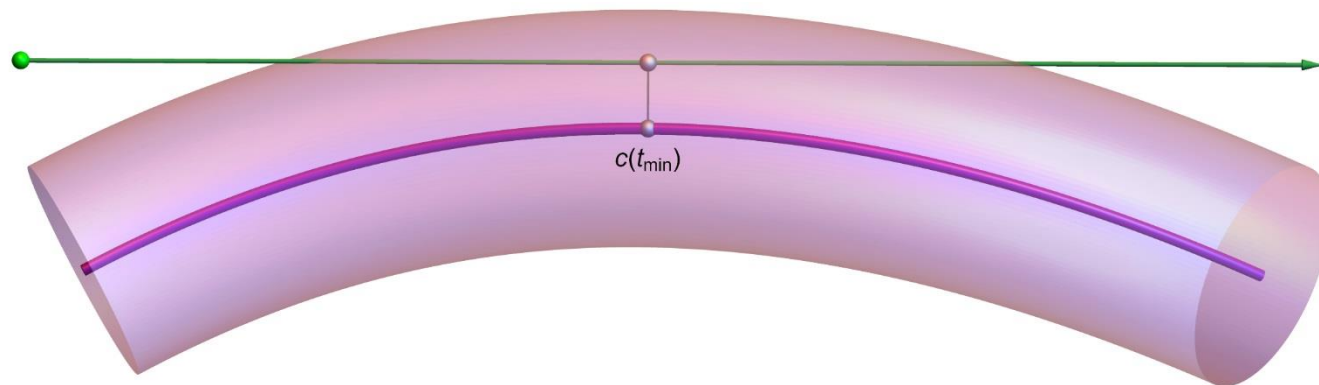
state-of-the-art = closest-point-of-approach



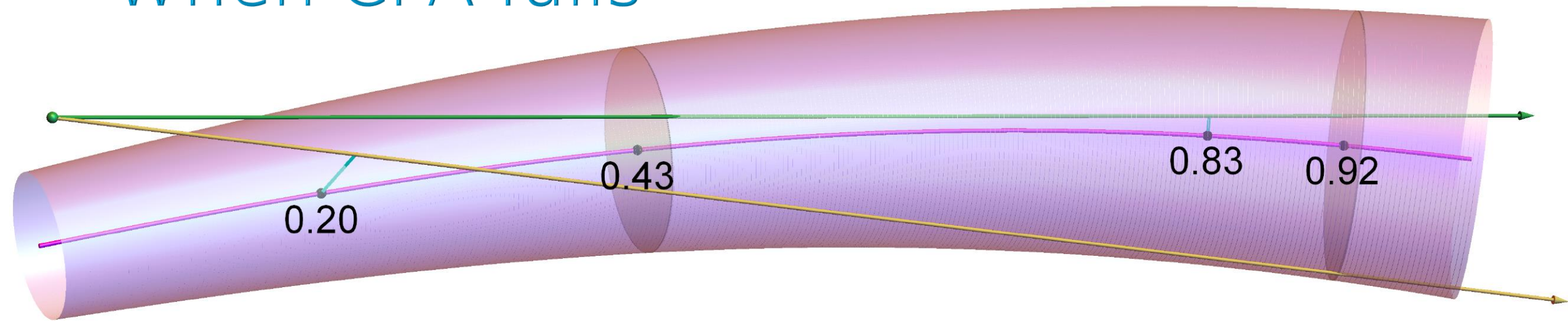
$$t_{\min} = \min_{t \in [0,1]} \text{distance}(\text{ray}, \text{curve}(t))$$

Aye and nay for CPA

- Pros
 - Simple; in practice: adaptive linearization
 - Might be useful for the collision detection and repulsion
- Cons
 - Non-physically based
 - What is the surface normal?
 - View-dependent results
 - Artificial high-order frequencies

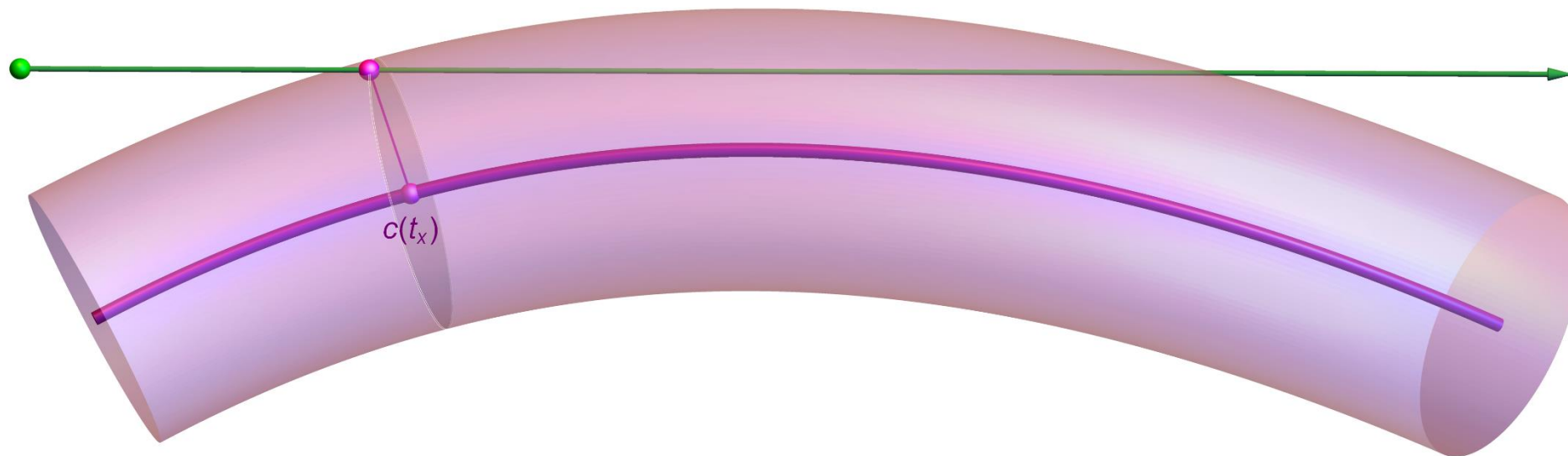


When CPA fails



- CPA root at $t = 0.2$
- $\text{Distance}[\text{curve}[0.2], \text{ray}] / \text{radius}[t] = 1.4$
- Ray-swept volume intersection at $t = 0.92$

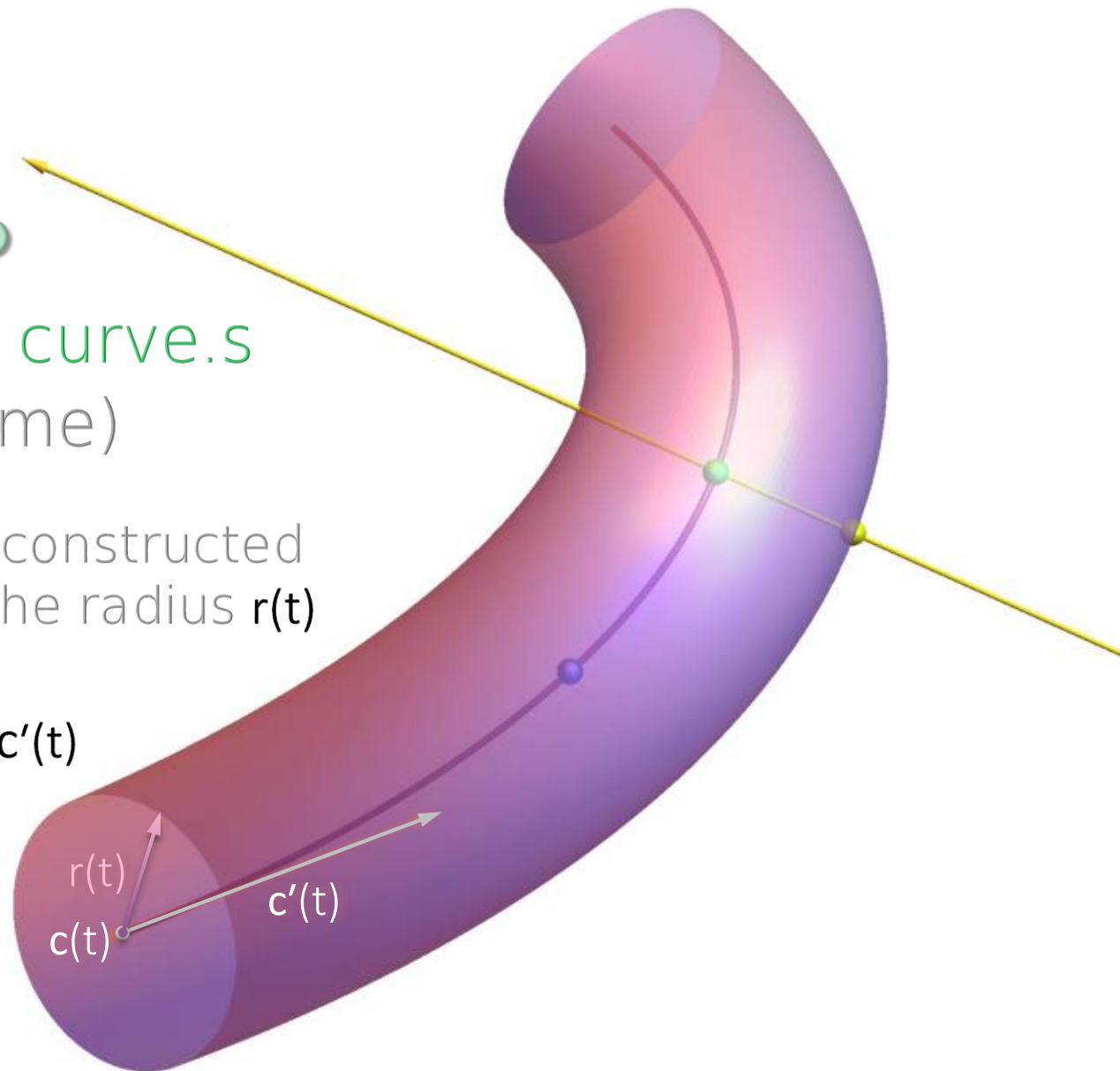
Instead, we search for ray \cap swept volume



We want ● and ●

(defined by ray.t and curve.s
for ray \cap swept volume)

Note: the swept volume is constructed
by extruding a circle with the radius $r(t)$
centered at $\mathbf{c}(t)$
in the plane orthogonal to $\mathbf{c}'(t)$
along the curve



● and ● properties

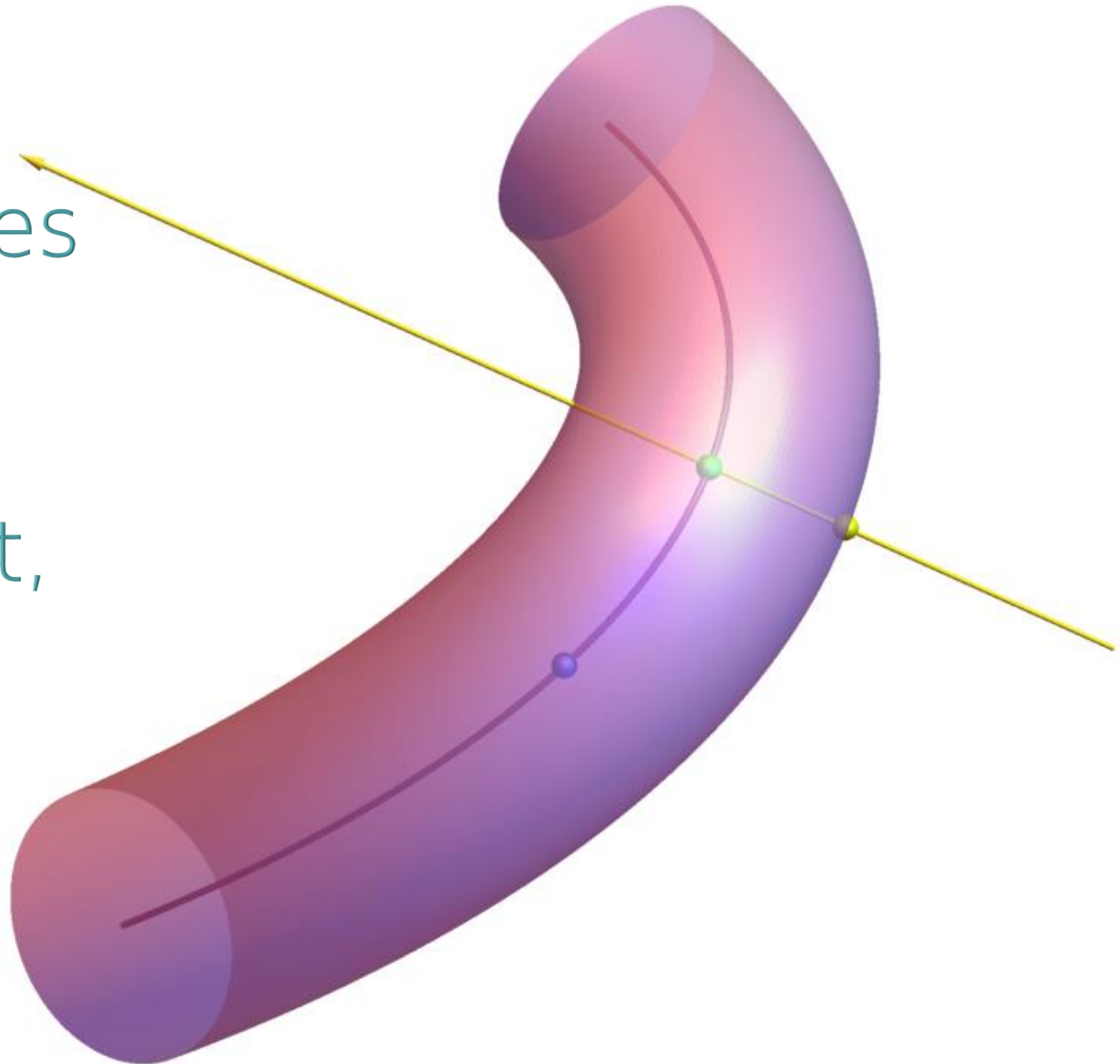
$$|\bullet - \bullet| == r(t_x)$$

$$(\bullet - \bullet) \cdot \mathbf{c}'(t_x) == 0$$

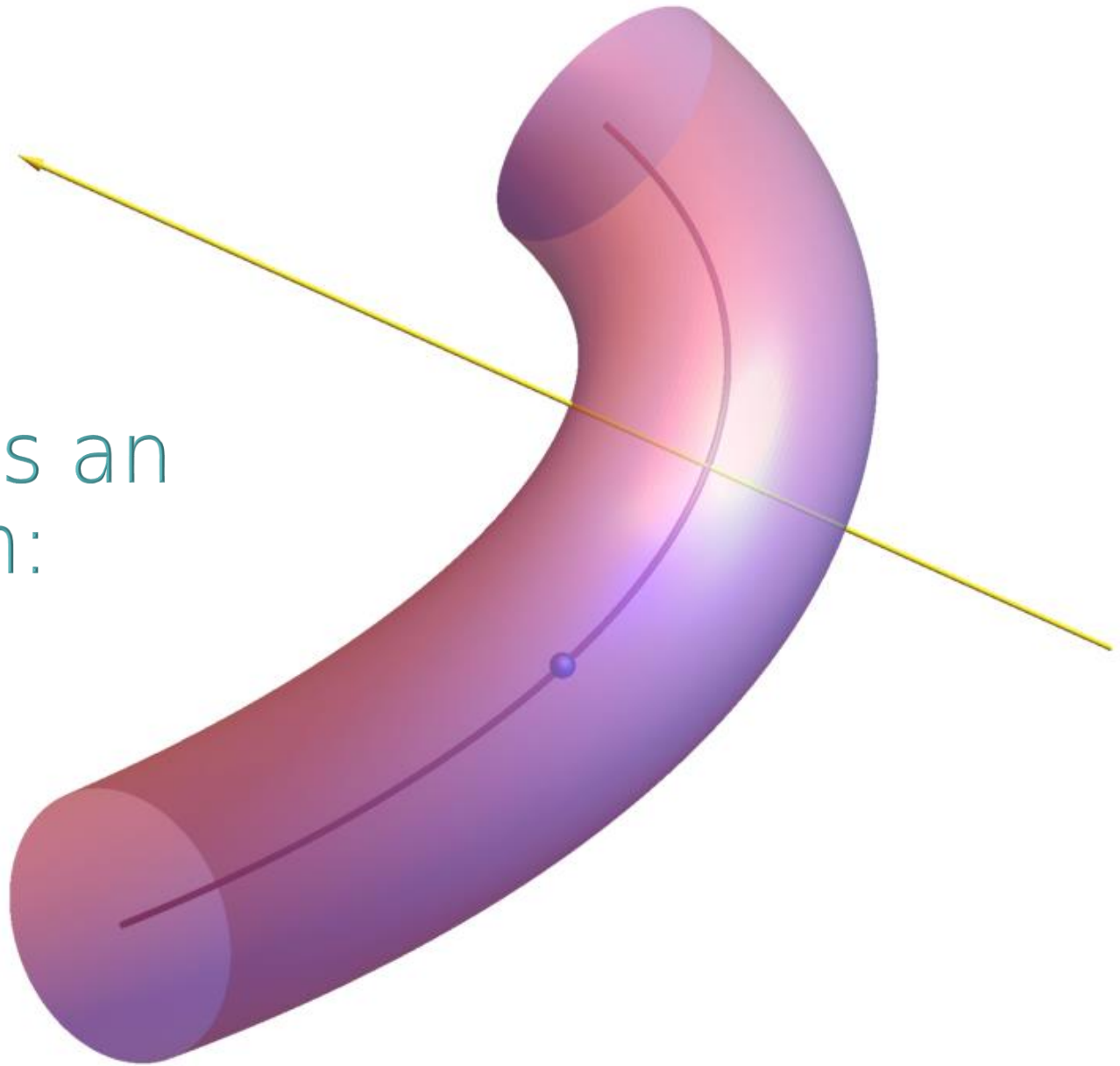
Once we found it,

● is the hit point

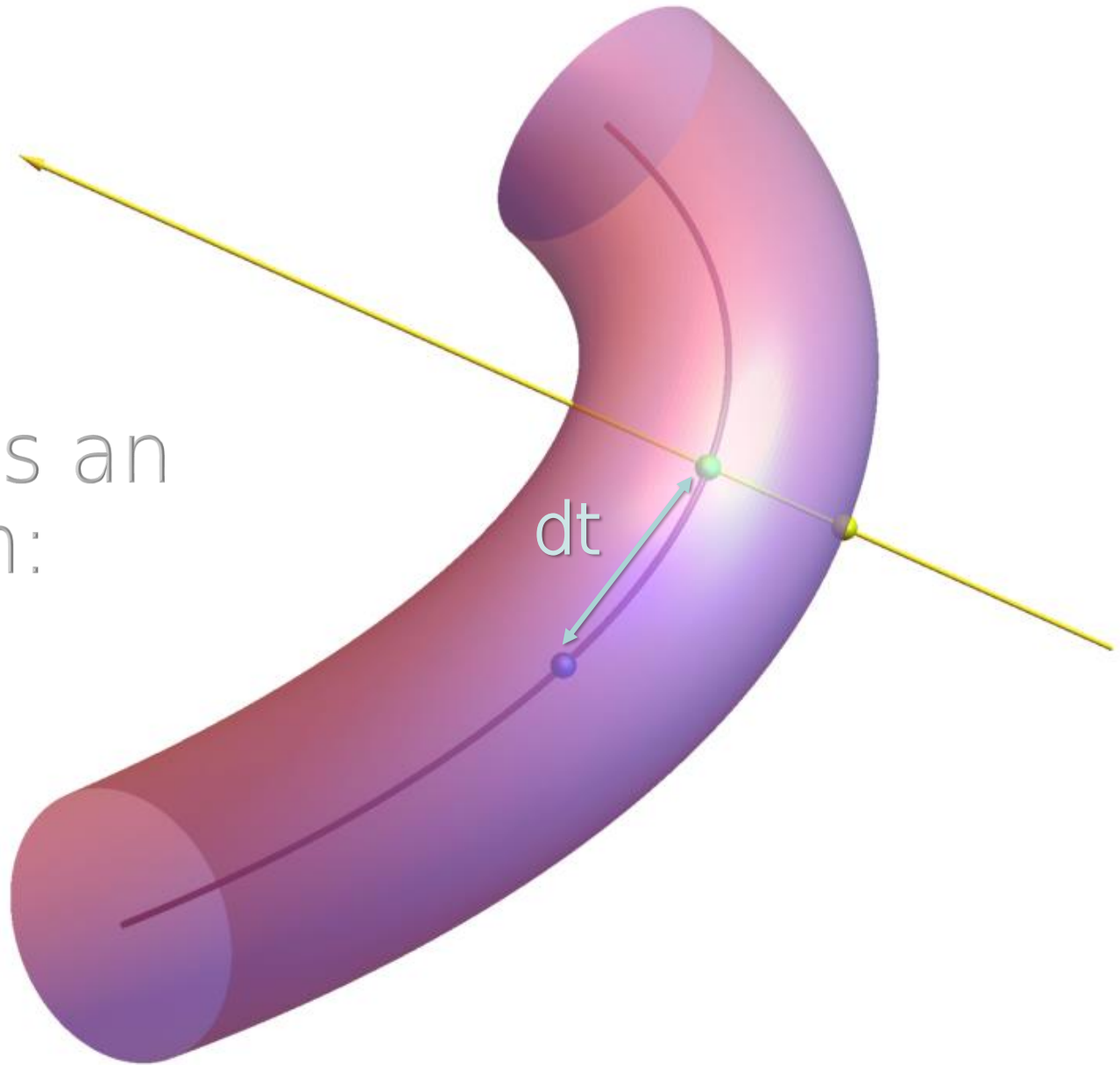
$(\bullet - \bullet) / |\bullet - \bullet|$ gives
the surface normal
(for cylinder; more
complex expression
for other profiles)



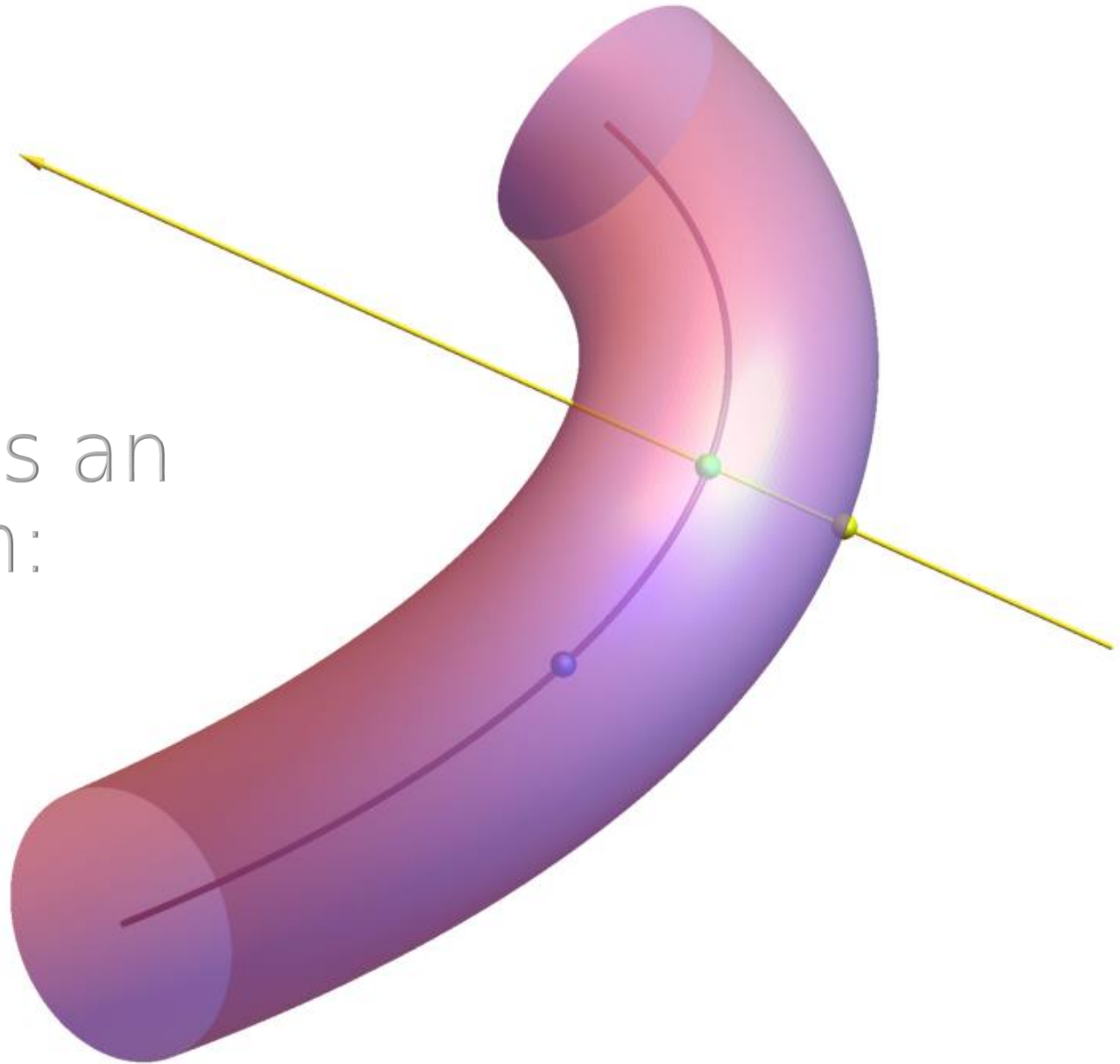
Phantom xsector is an
iterative algorithm:
for any initial ●



Phantom xsector is an
iterative algorithm:
for any initial \bullet
we will find
(the approximate)
 $dt = \bullet - \bullet$



Phantom xsector is an
iterative algorithm:
for any initial ●
we will find
(the approximate)
 $dt = \bullet - \bullet$
and also find ●
as a side effect



Because

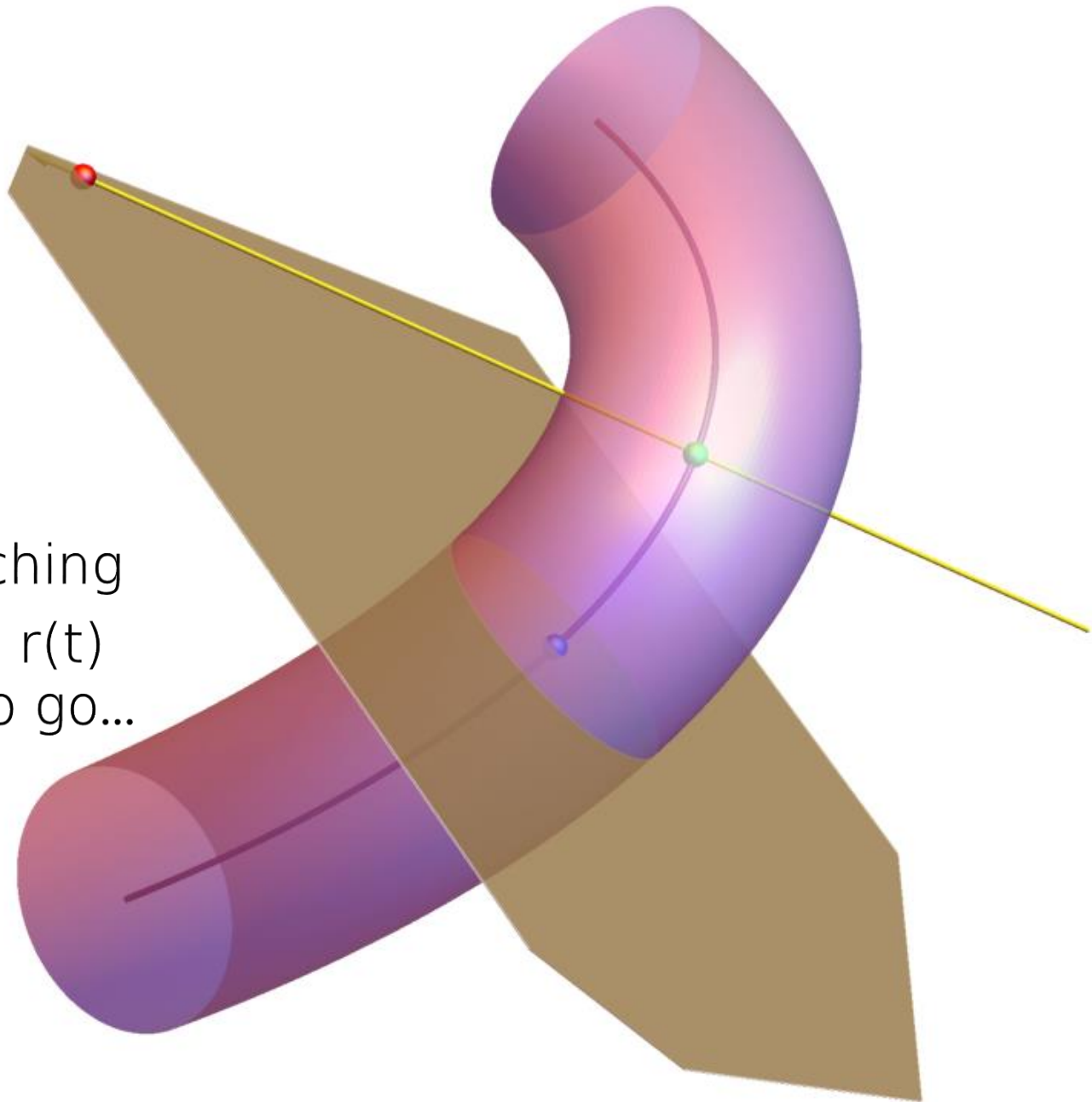
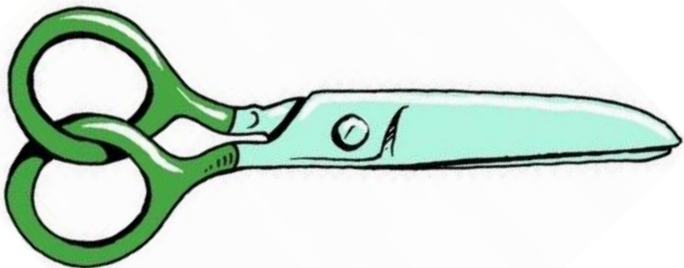
$$(\bullet - \bullet) \cdot \mathbf{c}'(t_x) == 0 \text{ and}$$

$$|\bullet - \bullet| == r(t_x)$$

@ ray \cap volume,

finding \bullet and then searching
for root(s) of $|\bullet - \bullet| == r(t)$
might seem like a way to go...

...yet it is a terrible idea

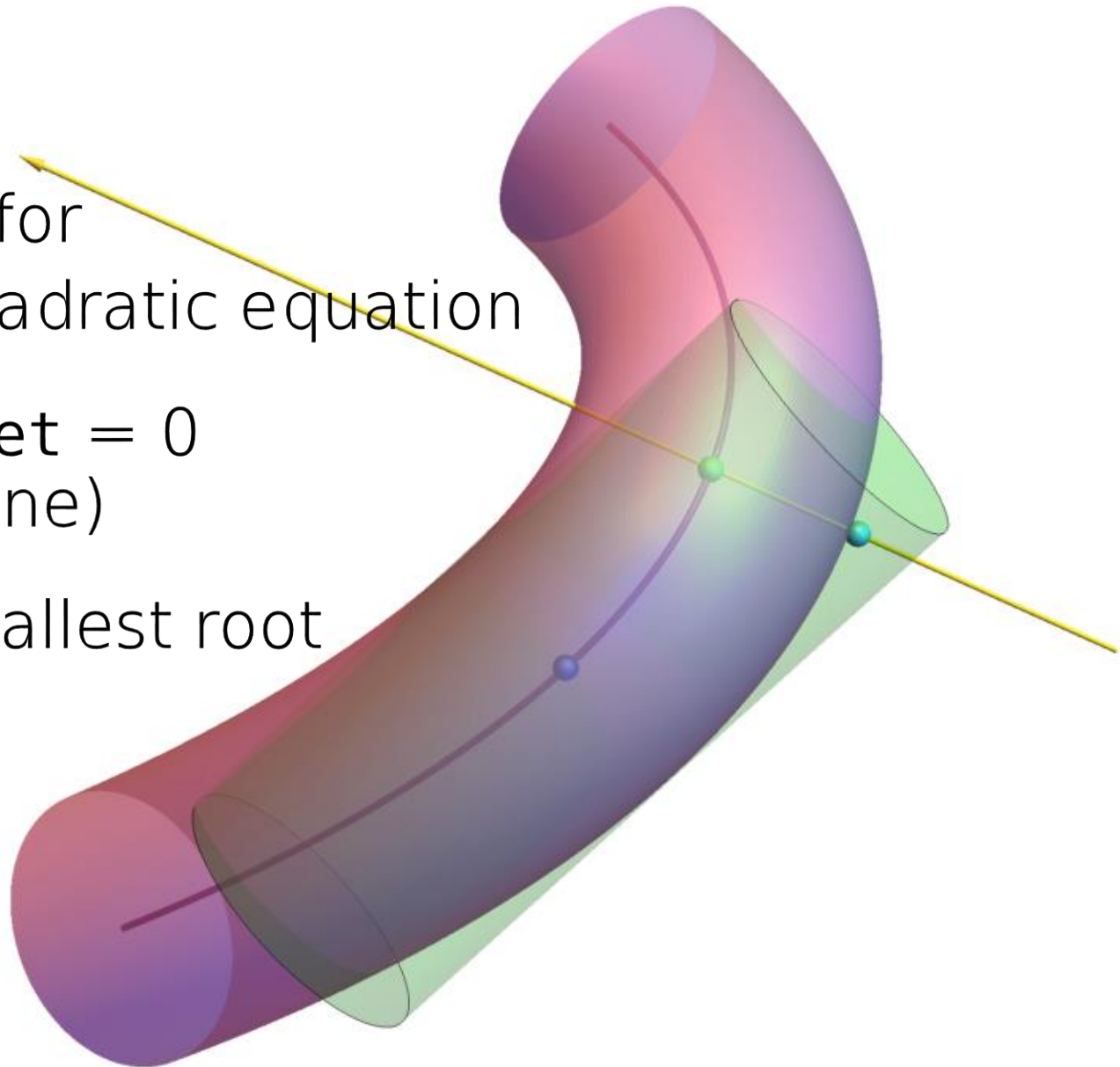


Instead, we will look for

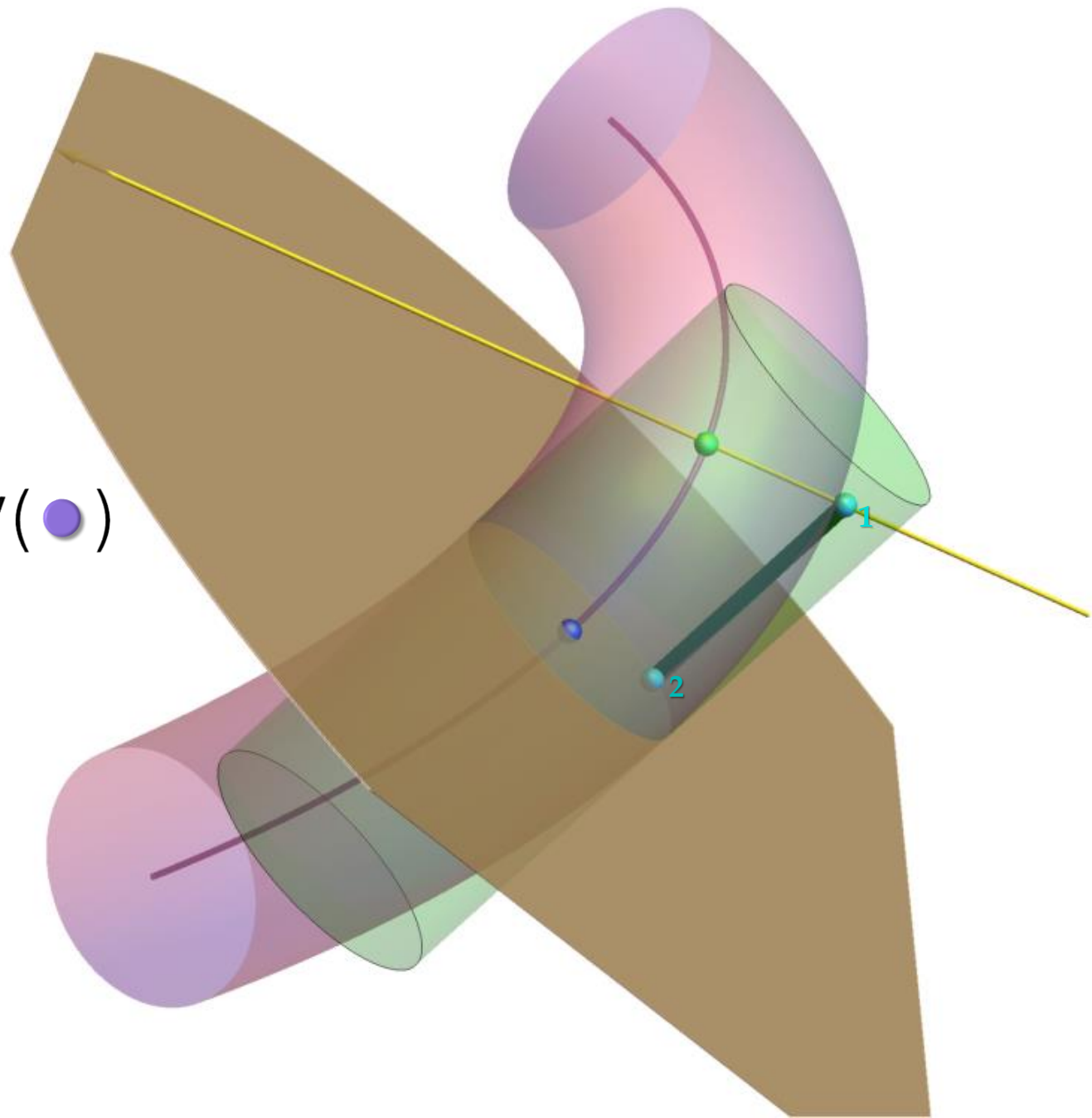
• (ray \cap cone) \leftarrow quadratic equation

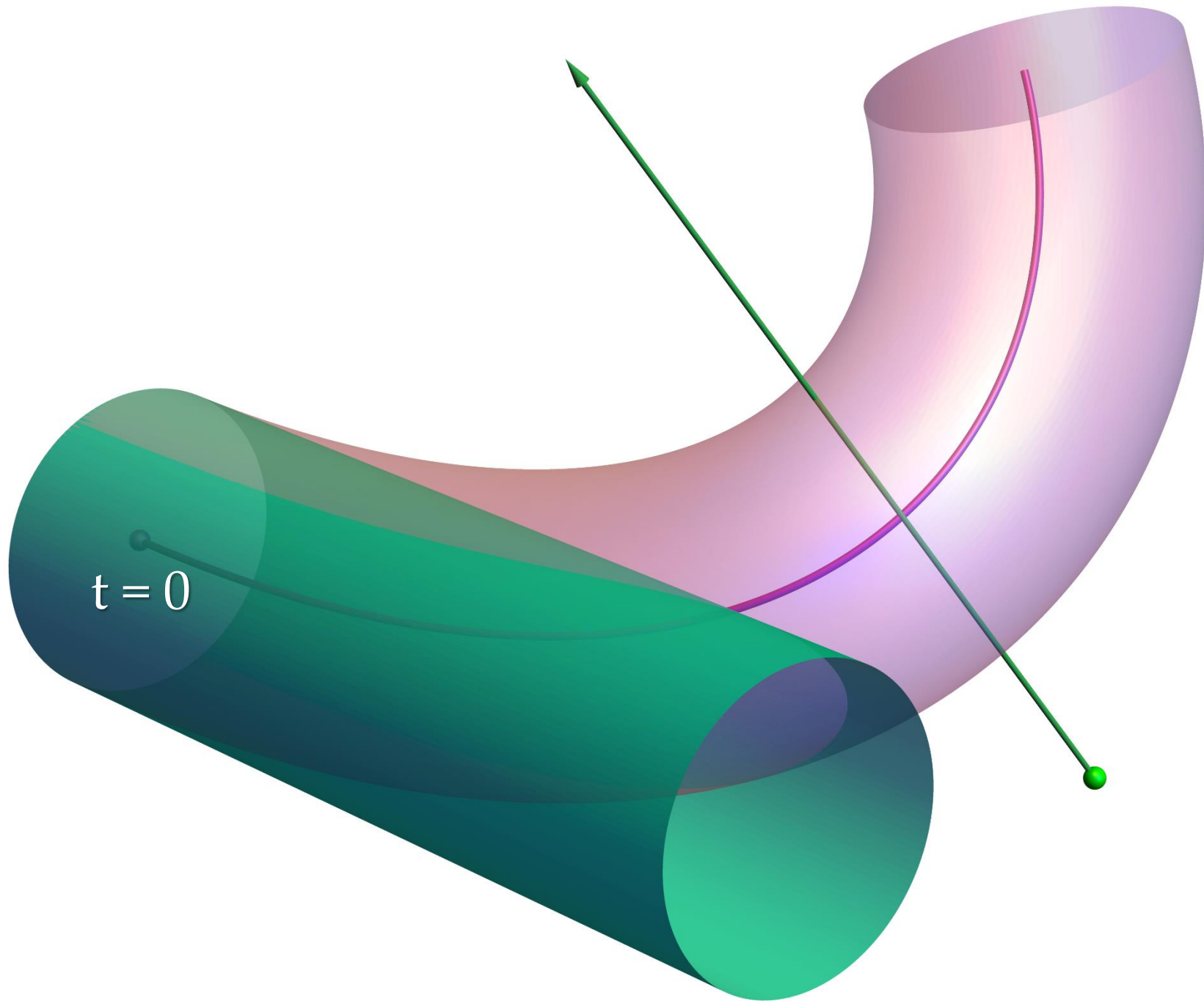
If $\det < 0$, we'll set $\det = 0$
(ray \cap the padded cone)

We need only the smallest root



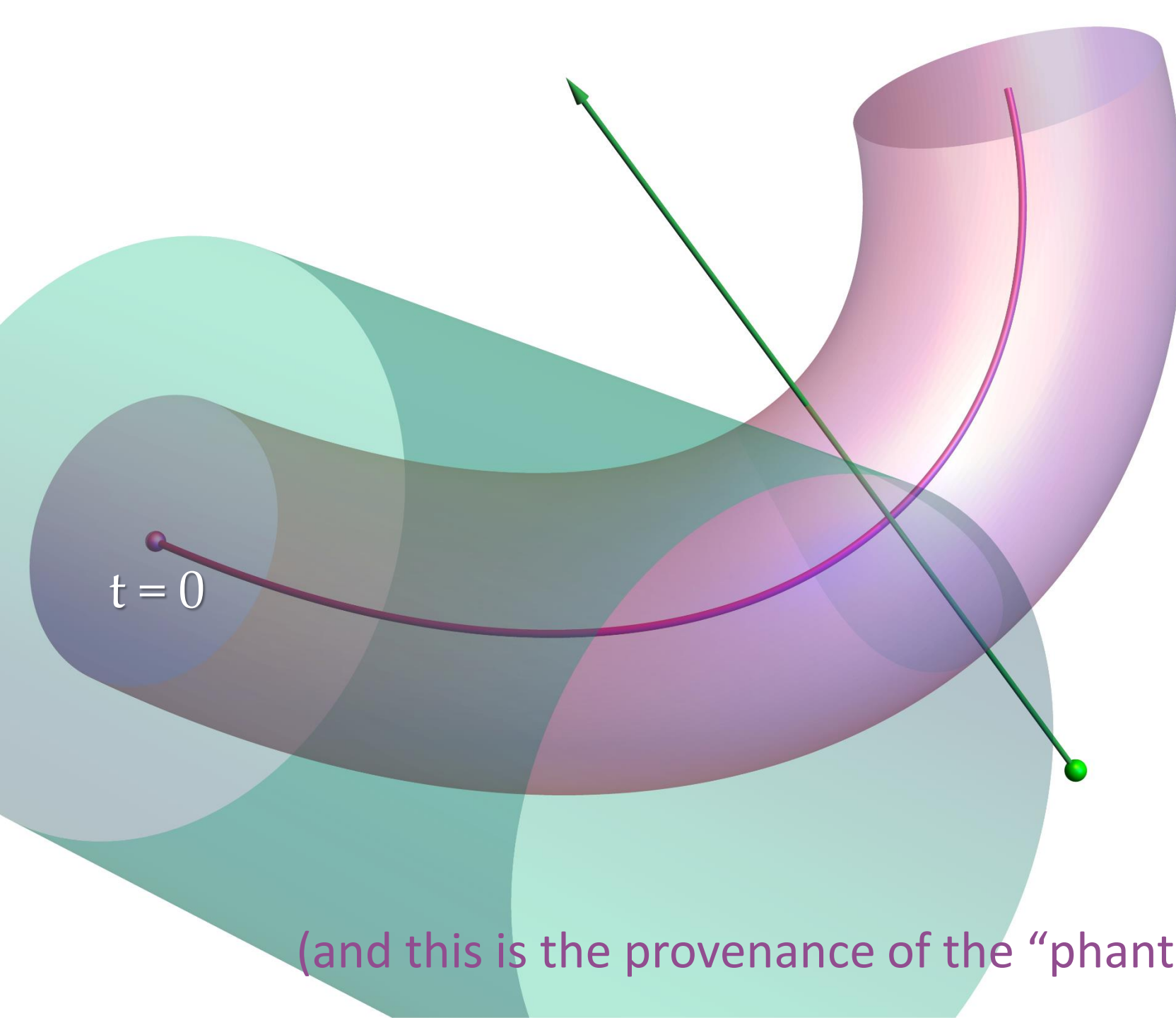
$$dt(\bullet) = (\bullet_1 - \bullet_2) \cdot \mathbf{c}'(\bullet)$$





Example of
dt function:

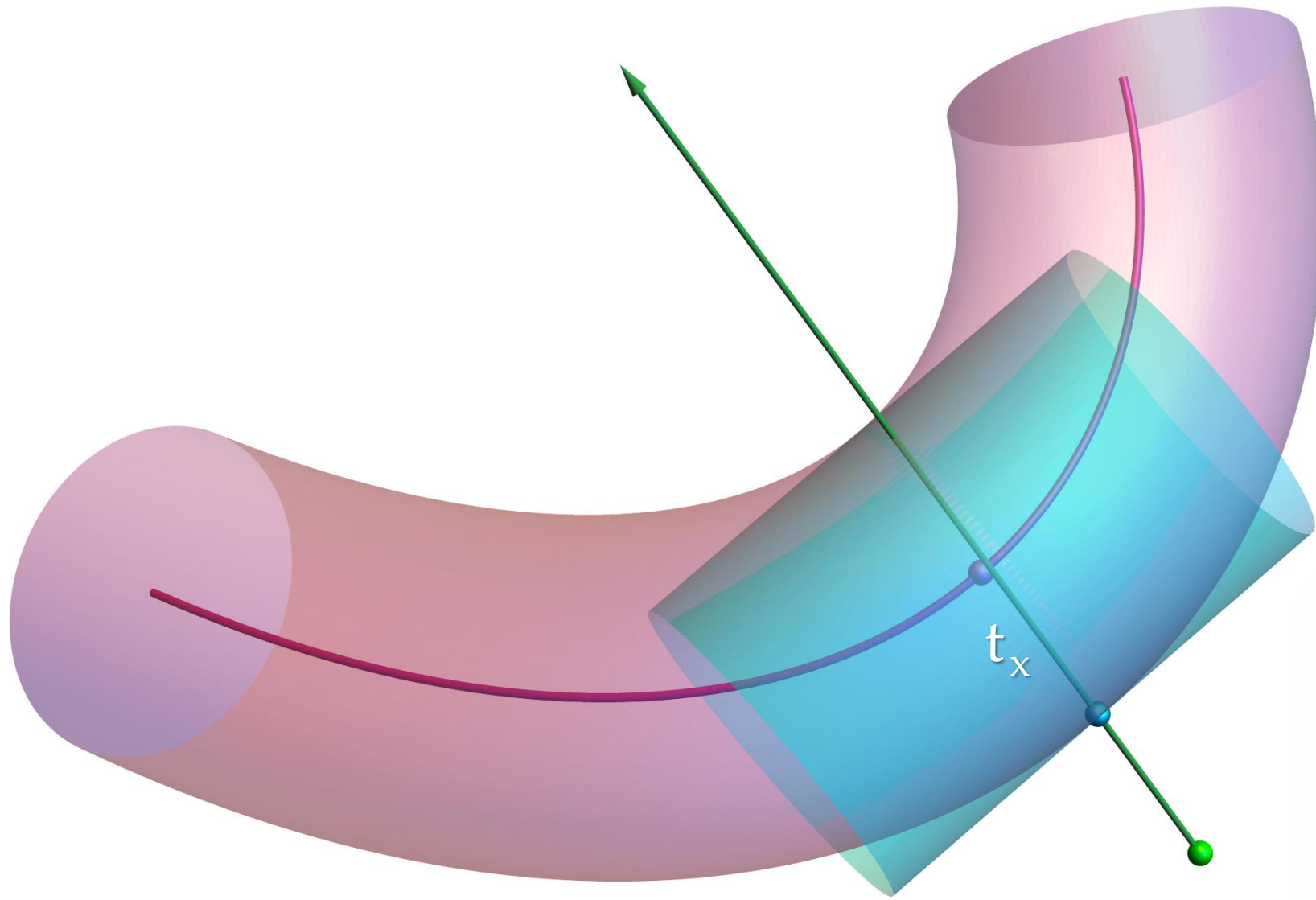
at $t = 0$, the ray does
not intersect $\text{cone}(t)$.



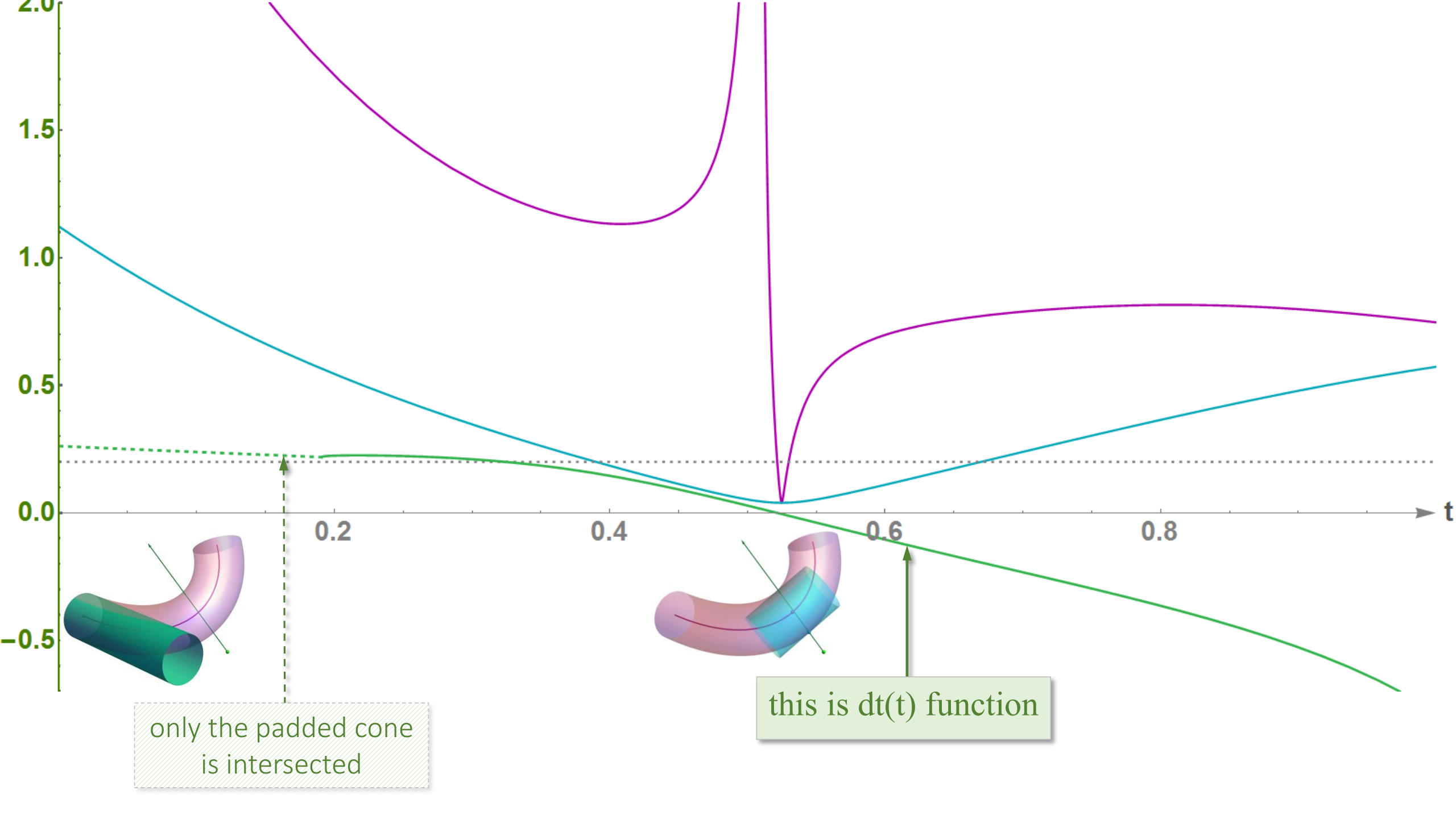
Example of
dt function:

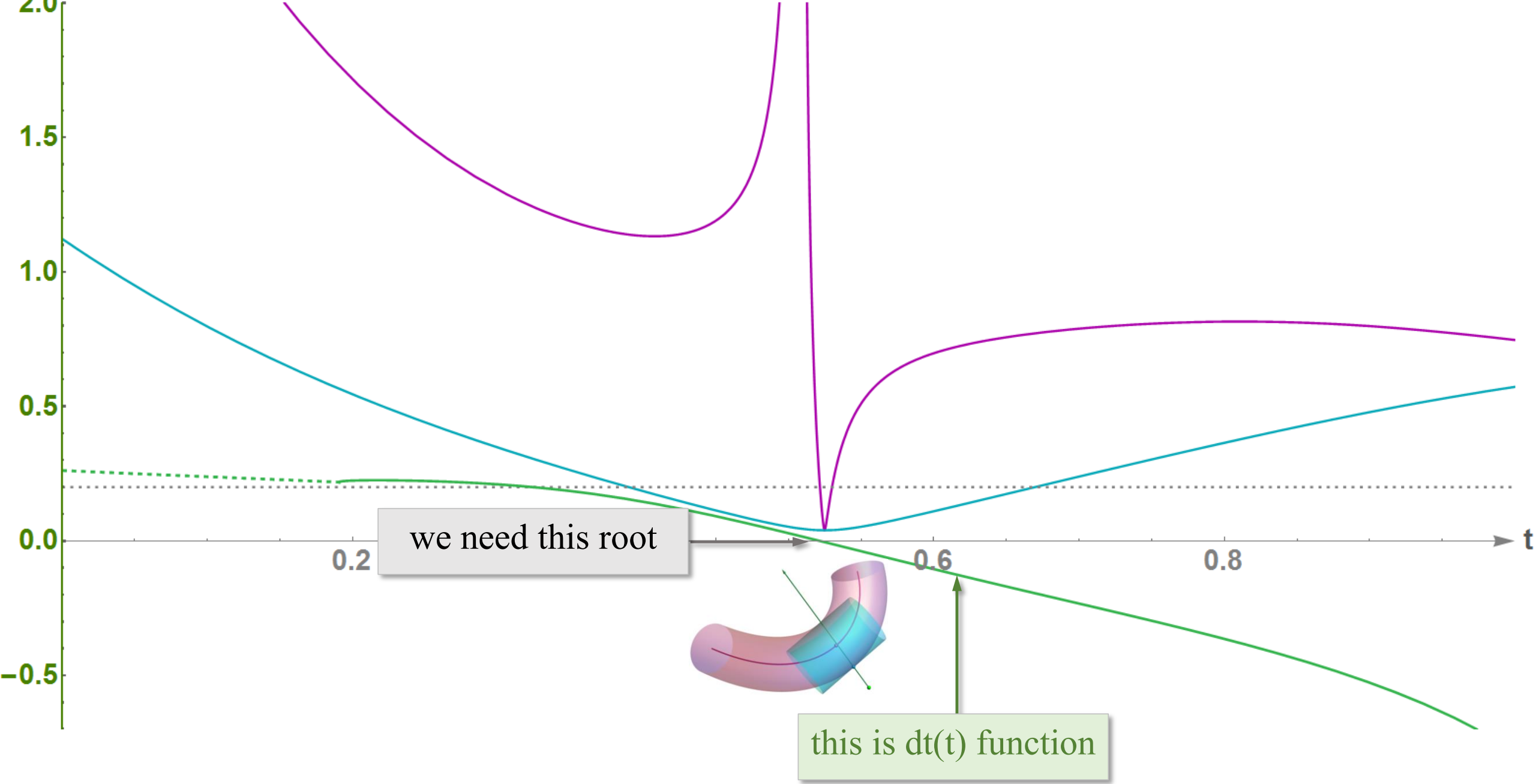
at $t = 0$, the ray does
not intersect $\text{cone}(t)$.
Yet, it touches
the padded cone,
allowing to find $\text{dt}(0)$

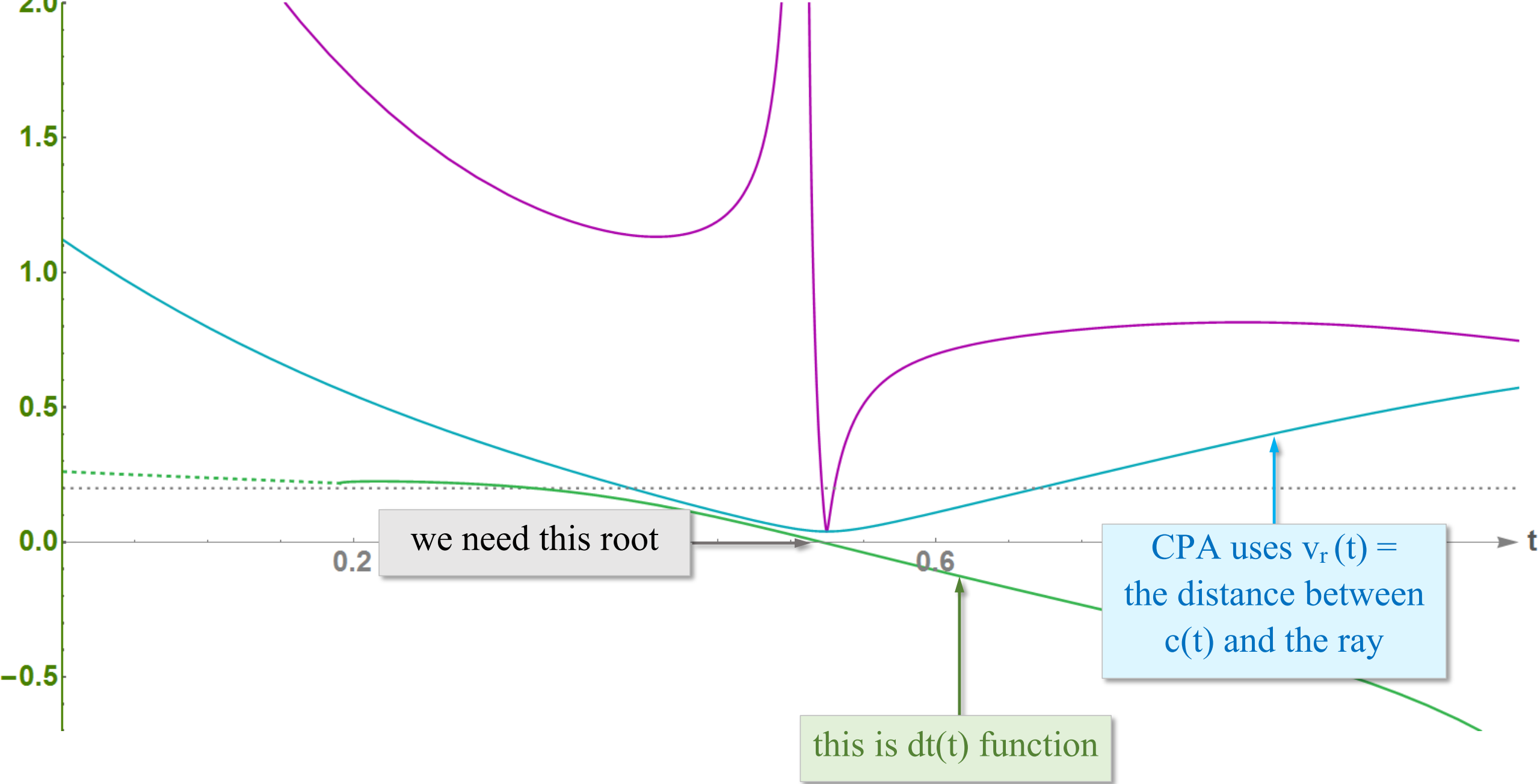
(and this is the provenance of the “phantom” name)

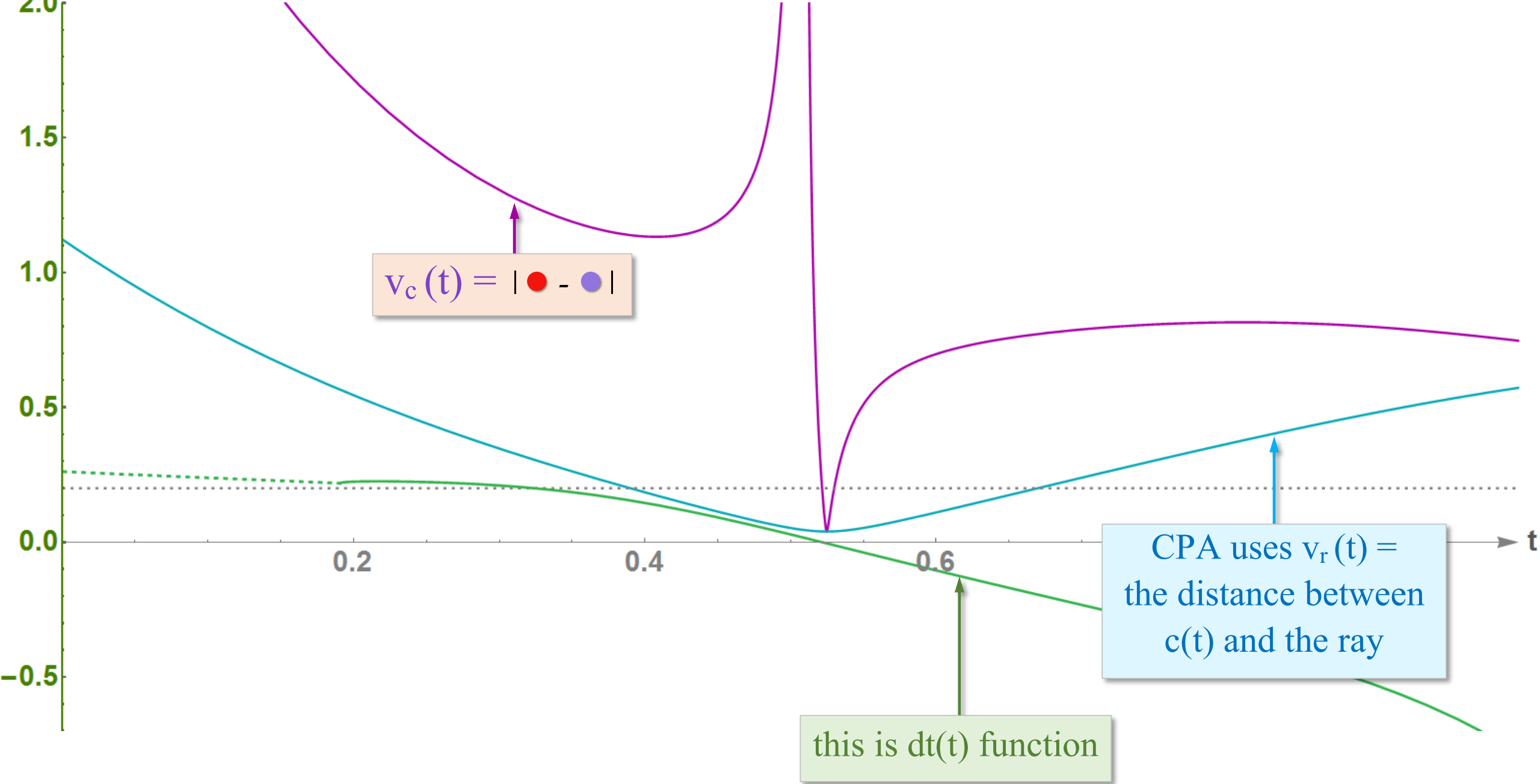


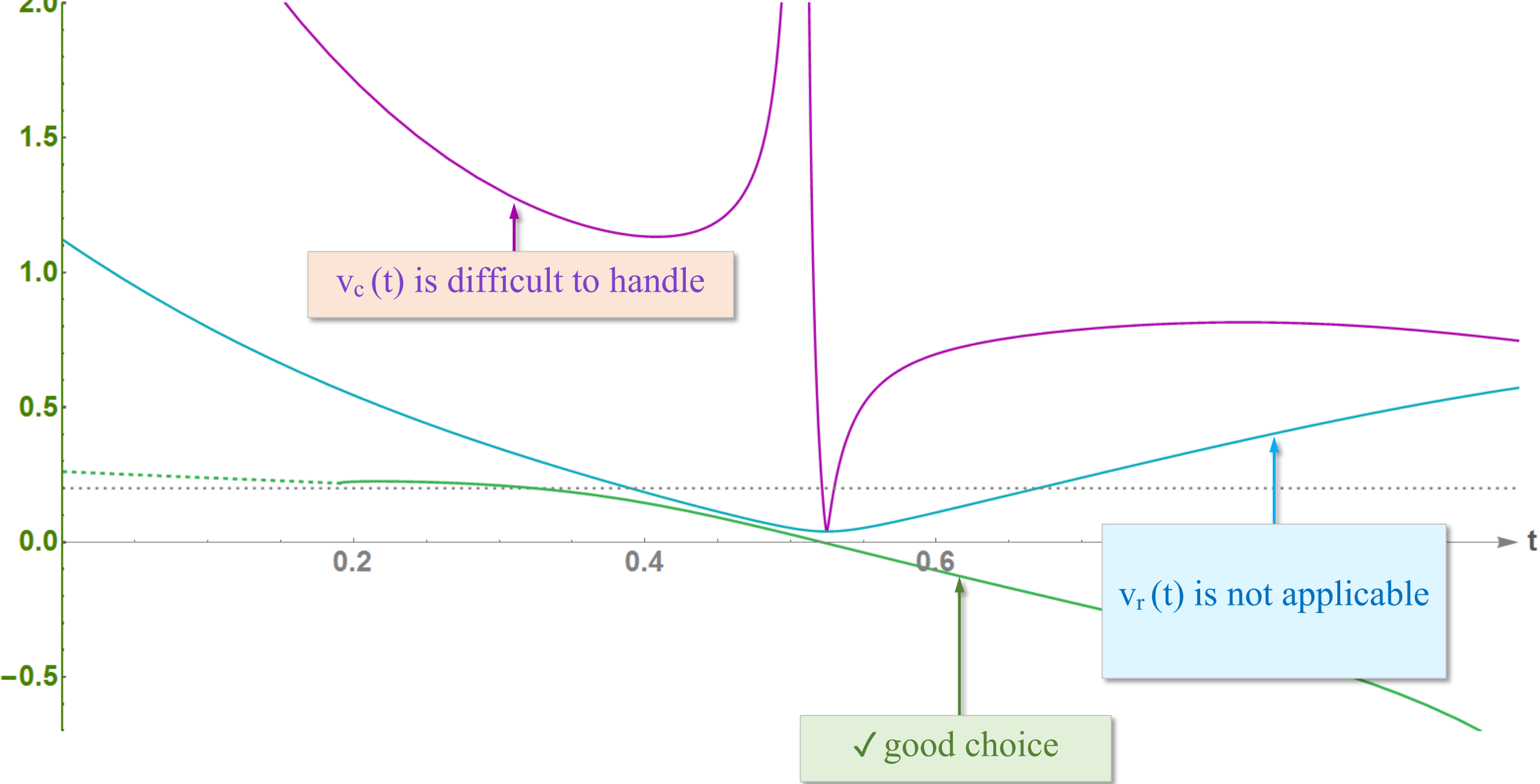
when $dt(t) == 0$,
ray intersects
the cone and
the swept volume
@ the same point ●

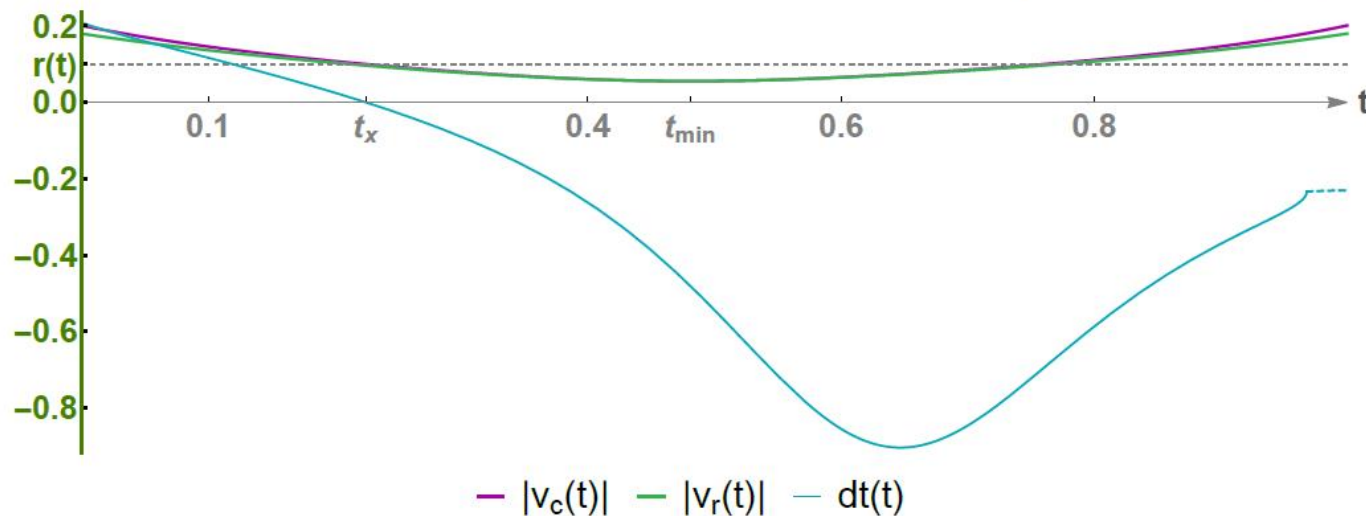
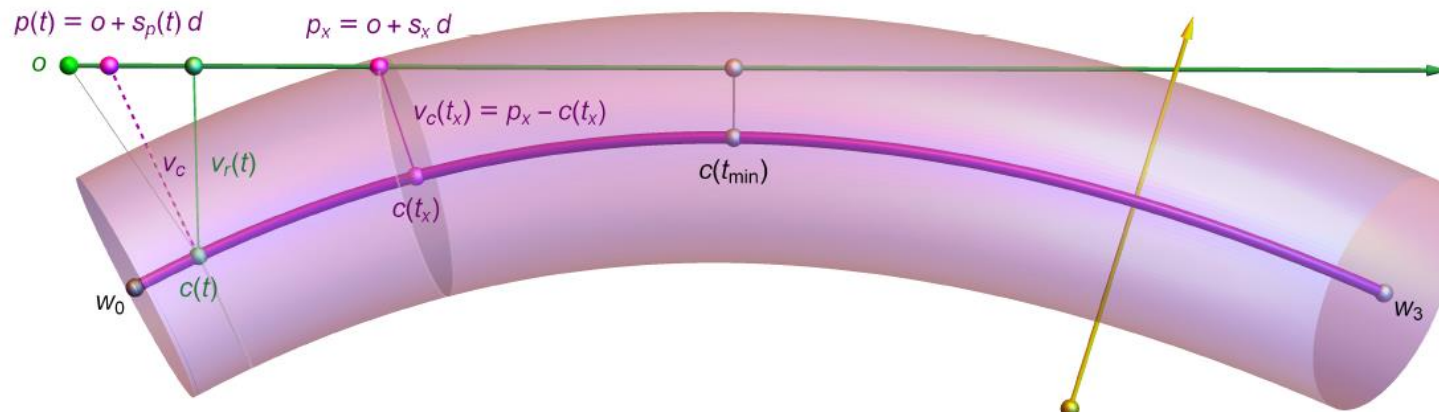




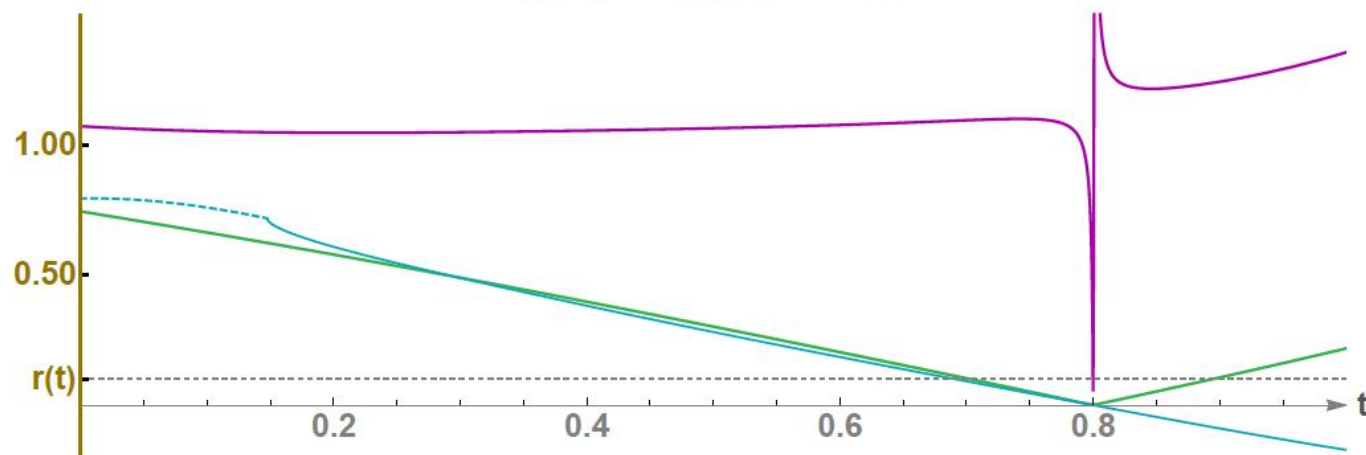






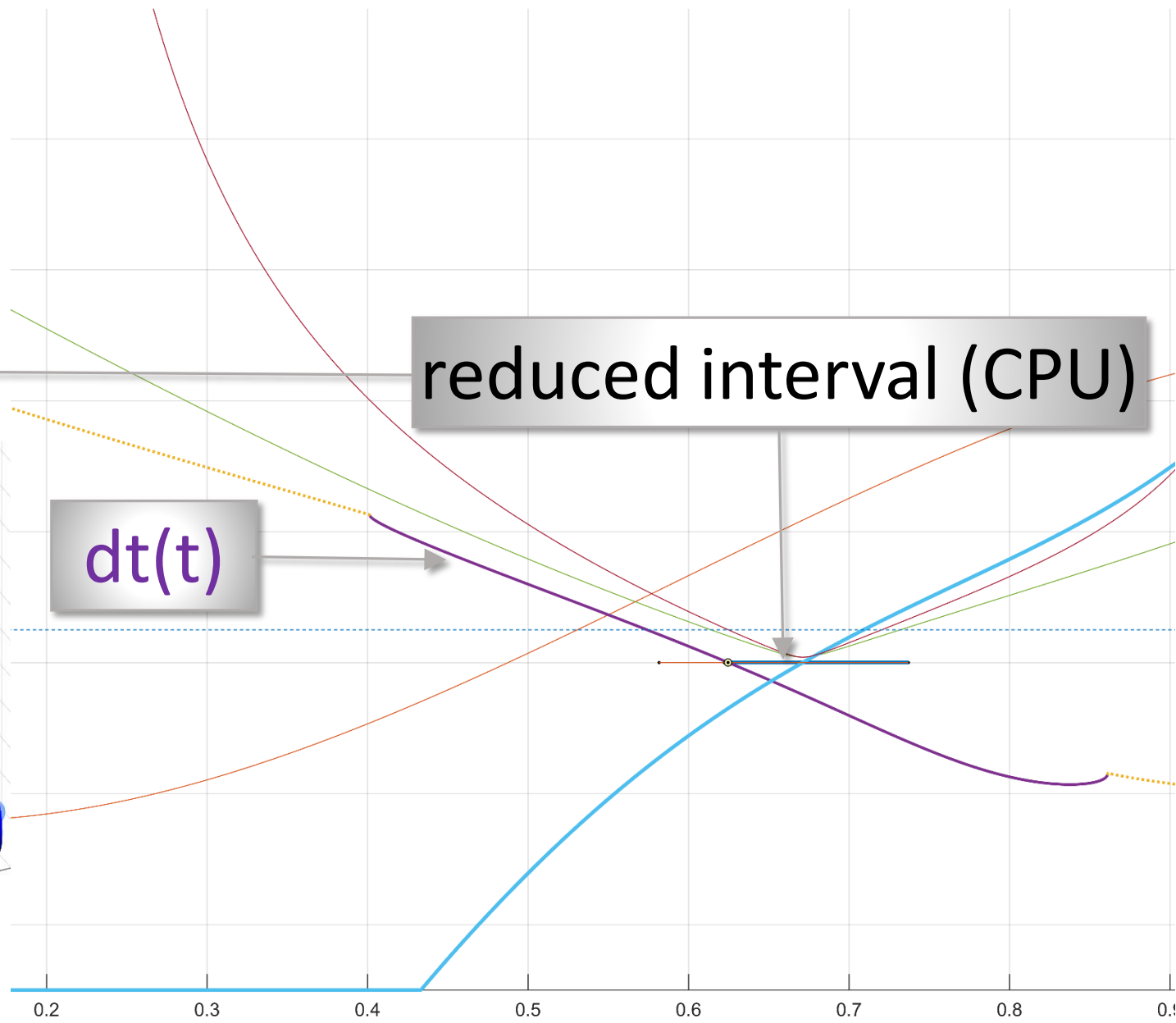
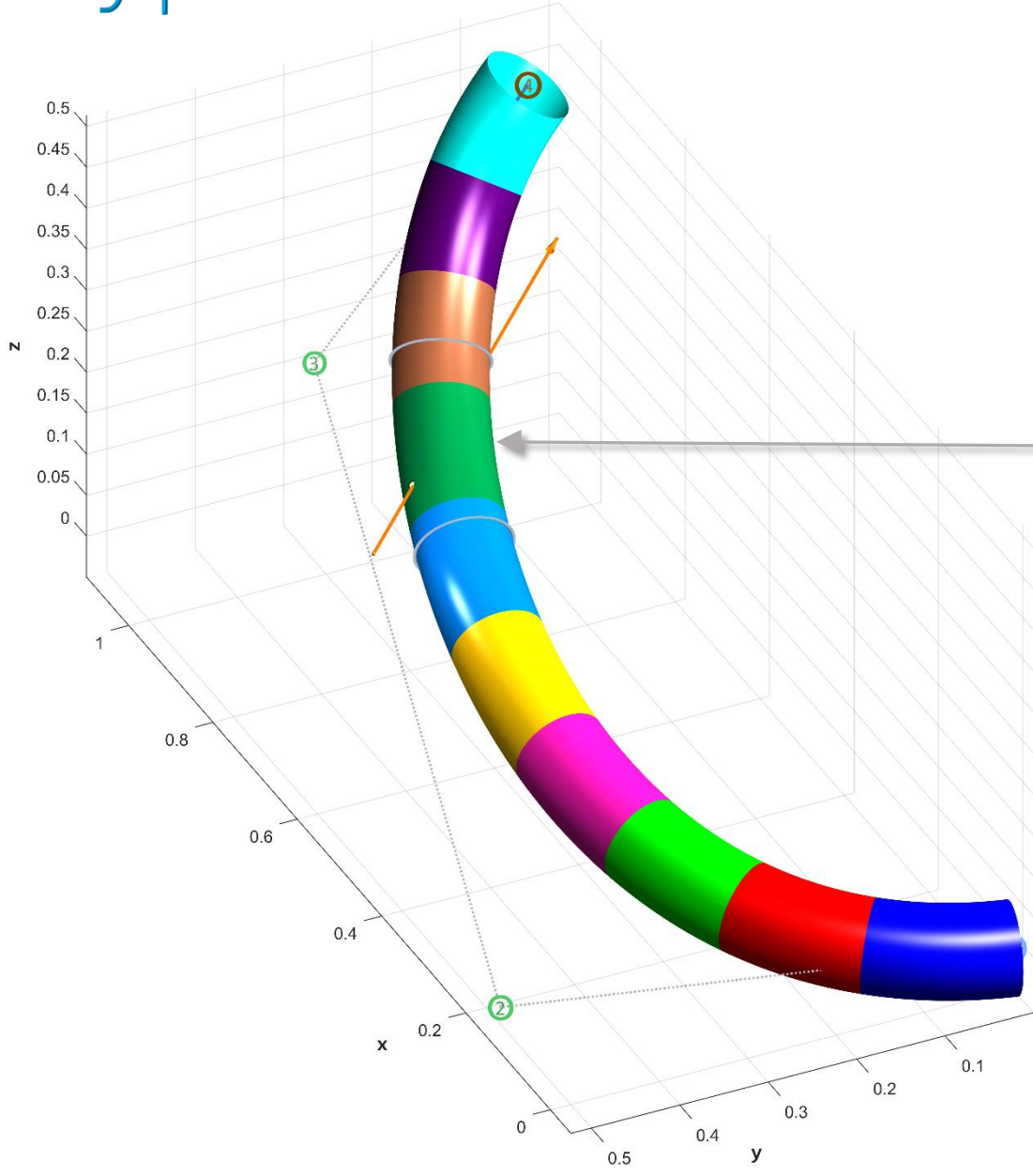


ray || curve
(more or less)

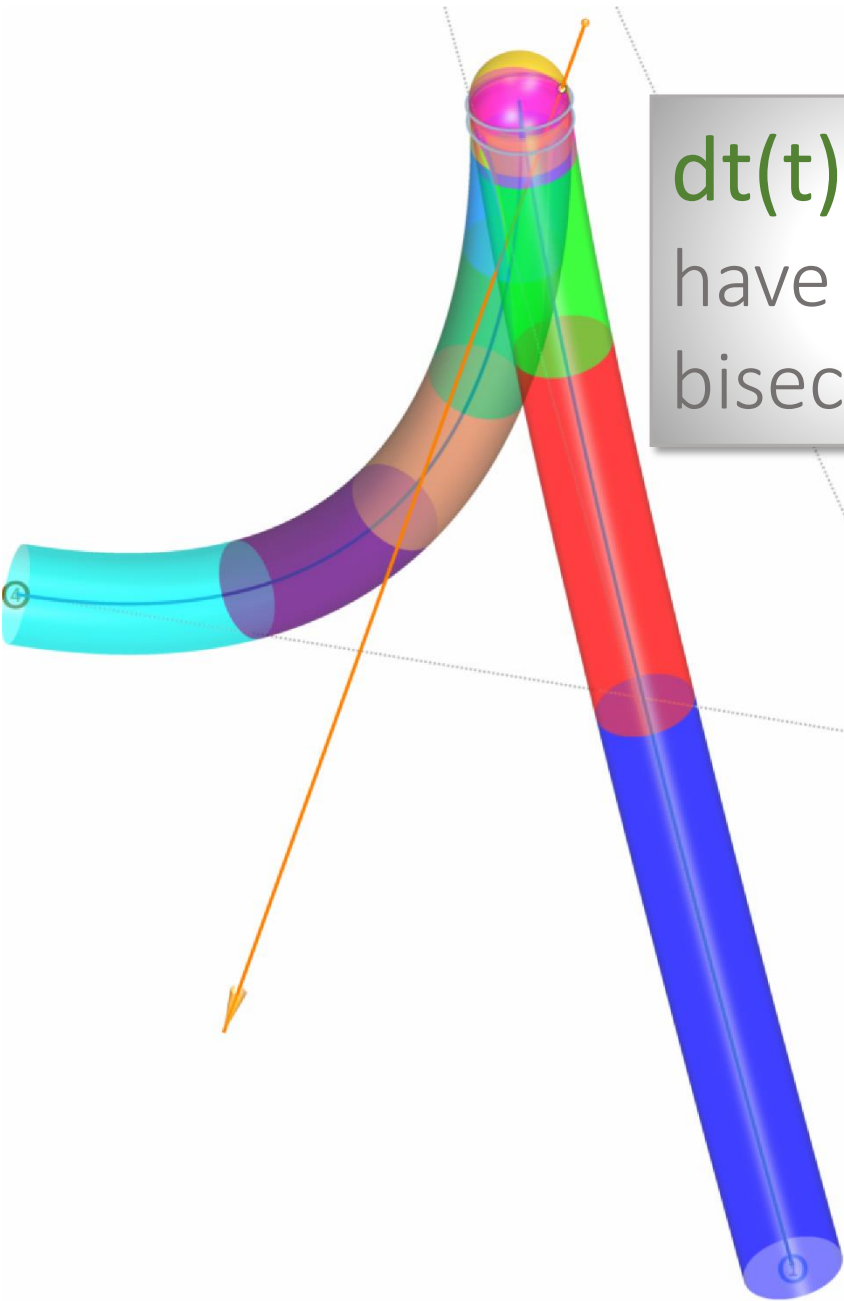


ray \perp curve

Typical situation: 3 iterations with *regula falsi*

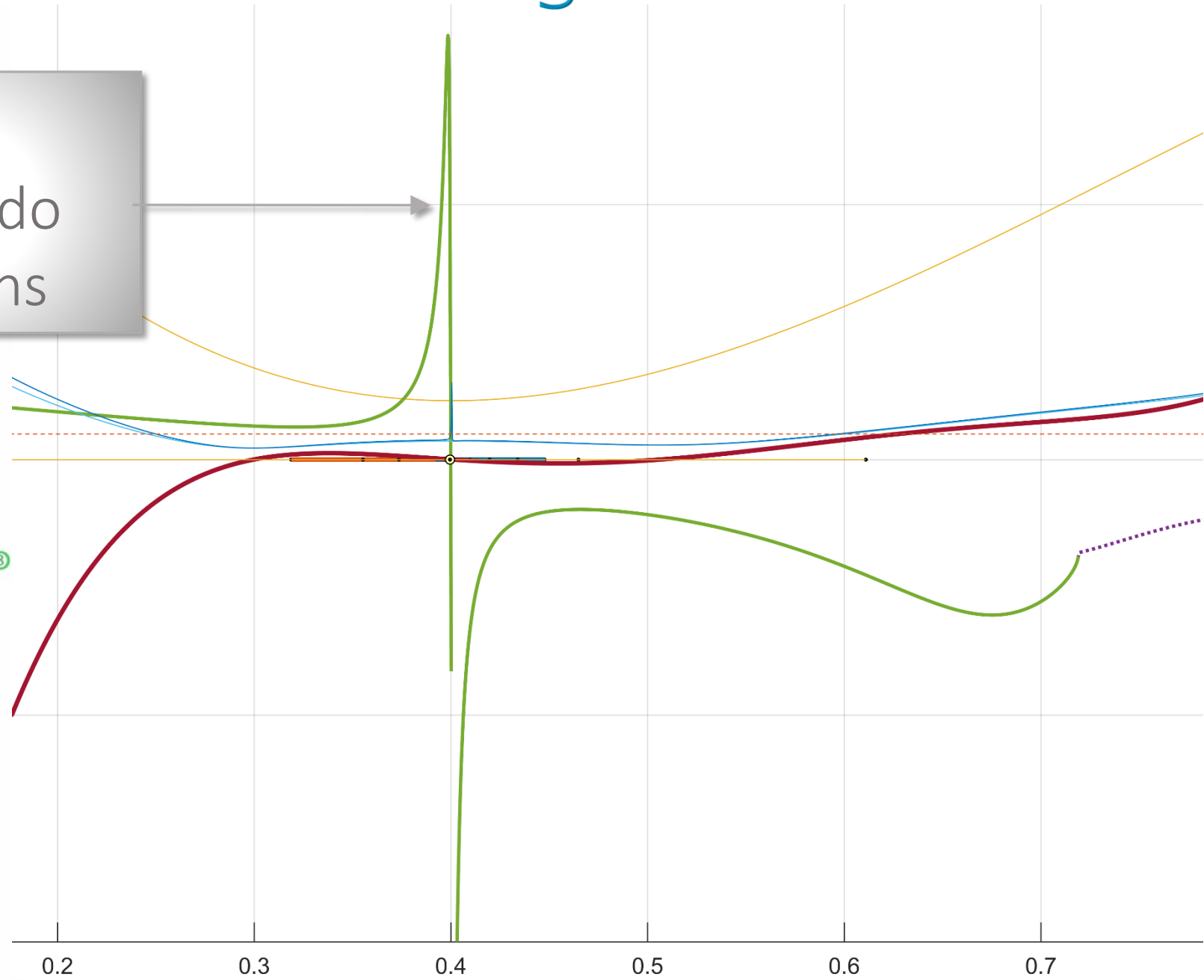


Difficult case for finding dt roots



$dt(t)$

have to do
bisections



Details



Steps of the Phantom Intersector

1. Find (the exact) bounding box for the Bézier curve + padding during BVH building.
2. Check the ray against the curve's enclosing cylinder. Exit if no such intersection exists.
3. Transform the curve into the ray-centric coordinate system.
4. Split big intervals.
5. For each subinterval $[t_1, t_2]$
 1. If $dt(t_1) < 0$ and $dt(t_2) > 0$, ignore the interval
 2. Start iterations at the endpoint that is closer to the ray origin
 3. Test for convergence. If the intersection is found, report it, otherwise start at the other endpoint.

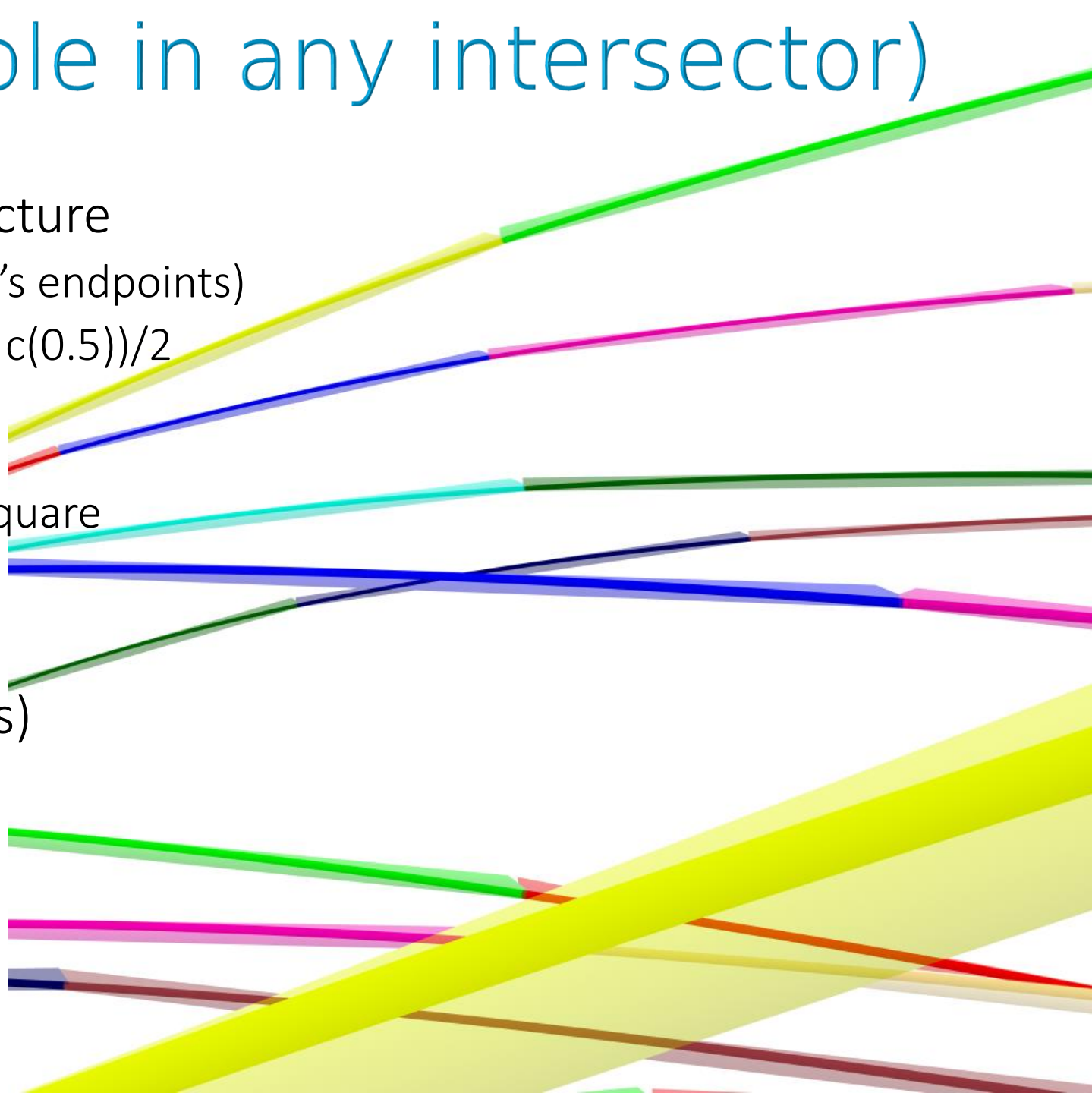
Steps of the Phantom Intersector

1. Find (the exact) bounding box for the Bézier curve + padding during BVH building.
2. Check the ray against the curve's enclosing cylinder.
Exit if no such intersection exists.
3. Transform the curve into the ray-centric coordinate system.
4. Split big intervals.
5. For each subinterval $[t_1, t_2]$
 1. If $dt(t_1) < 0$ and $dt(t_2) > 0$, ignore the interval
 2. Start iterations at the endpoint that is closer to the ray origin
 3. Test for convergence. If the intersection is found, report it, otherwise start at the other endpoint.

Enclosures (usable in any intersector)

- While building the acceleration structure
 - (normalized) axis $acy1 = w_3 - w_0$ (curve's endpoints)
 - point on the axis $pcy1 = ((w_3 + w_0)/2 + c(0.5))/2$
 - find a conservative maximum distance $rcy1$ from the points on the curve to this axis; add r_{max} to it and square
- Intersection is ruled out if the ray and the padded cylinder do not intersect (considered as infinite lines)

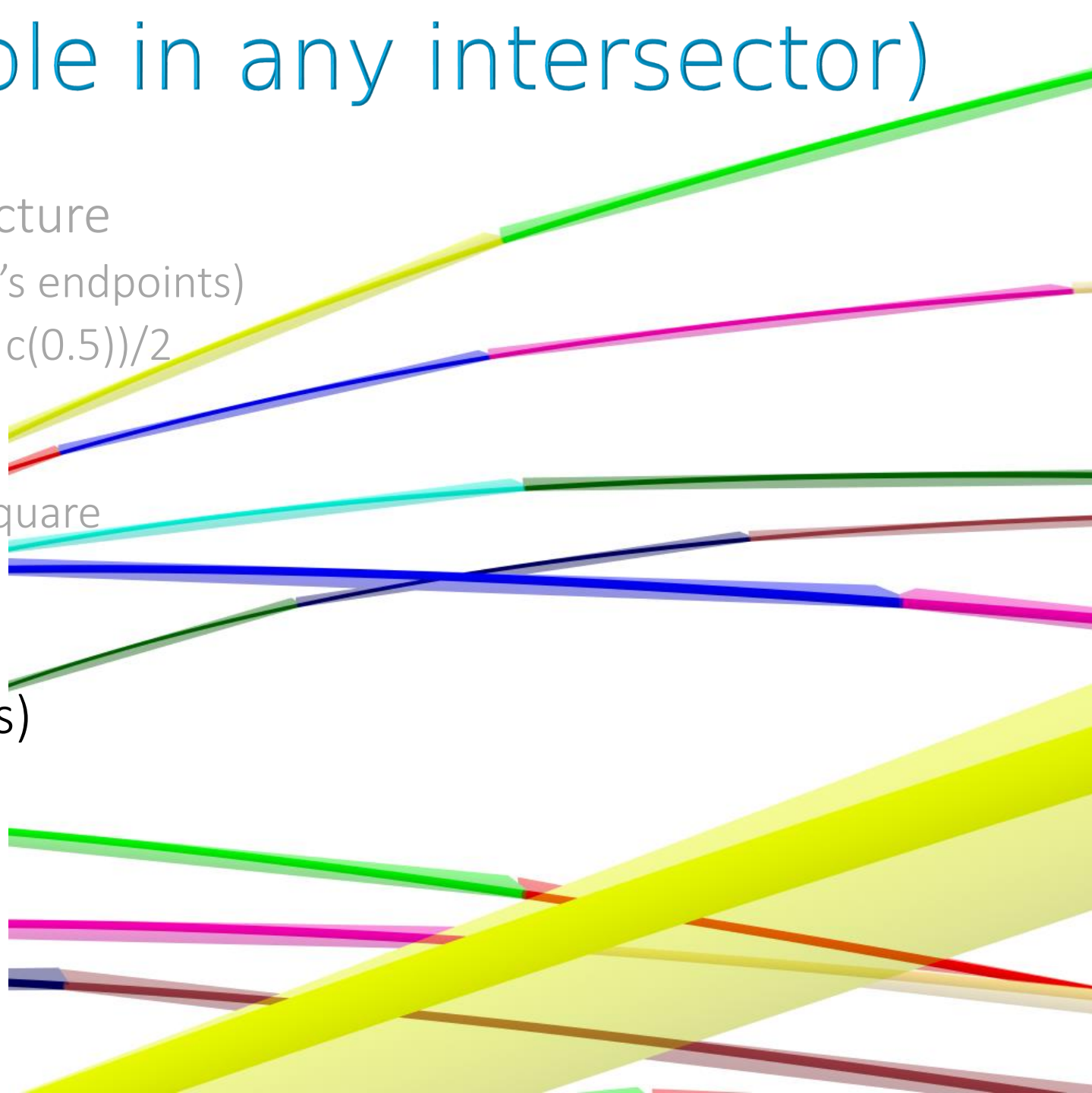
```
float3 dxc = cross(ray.direction, acy1);  
float3 r2c = ray.origin - pcy1;  
float d1 = dot(r2c, dxc);  
return d1 * d1 > rcy1 * dot(dxc, dxc);
```



Enclosures (usable in any intersector)

- While building the acceleration structure
 - (normalized) axis $acy1 = w_3 - w_0$ (curve's endpoints)
 - point on the axis $pcy1 = ((w_3 + w_0)/2 + c(0.5))/2$
 - find a conservative maximum distance $rcy1$ from the points on the curve to this axis; add r_{max} to it and square
- Intersection is ruled out if the ray and the padded cylinder do not intersect (considered as infinite lines)

```
float3 dxc = cross(ray.direction, acyl);  
float3 r2c = ray.origin - pcy1;  
float d1 = dot(r2c, dxc);  
return d1 * d1 > rcyl * dot(dxc, dxc);
```



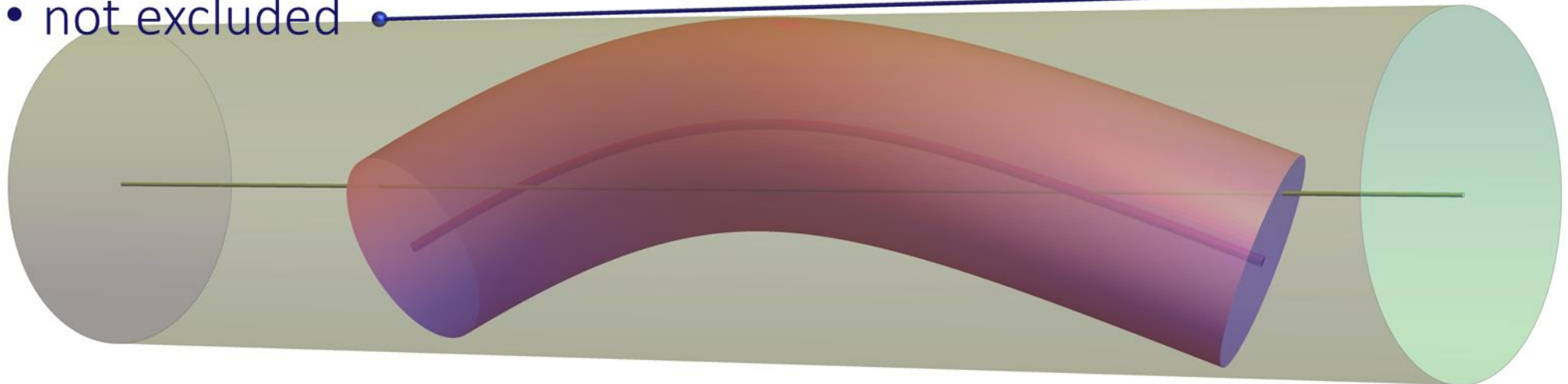
- excluded



- not excluded



- not excluded



slabs slightly slower than cylinders

```
bool intersectEnclosure(const optix::Ray& ray, float2& limits) const {
    float d0 = dot(ray.direction, pn0); // pn0 = plane0.normal
    float d1 = dot(ray.direction, pn1); // pn1 = plane1.normal
    float3 pr = pcy1 - ray.origin;      // pcy1 is a point on slab's axis
    float p0 = dot(pr, pn0);           // pcy1.pn0 could be precomputed
    float p1 = dot(pr, pn1);           // pcy1.pn1 could be precomputed
    float pd0, ed0, min0, max0;
    pd0 = p0 / d0;
    ed0 = ext0 / abs(d0);
    min0 = pd0 - ed0;
    float pd1, ed1, min1, max1;
    pd1 = p1 / d1;
    ed1 = ext1 / abs(d1);
    min1 = pd1 - ed1;
    max0 = pd0 + ed0;
    max1 = pd1 + ed1;

    float tmin = fmaxf(min0, min1); tmin = fmaxf(ray.tmin, tmin);
    float tmax = fminf(max0, max1); tmax = fminf(ray.tmax, tmax);
    limits.x = tmin;
    limits.y = tmax;
    return tmax > 0 && tmin < tmax;
}
```

```
bool intersectEnclosure(const optix::Ray& ray, float2& limits) const {
    float3 dxc = cross(ray.direction, acyl);
    float3 r2c = ray.origin - pcy1;
    float d1 = dot(r2c, dxc);
    float innlen2 = 1.0f/dot(dxc, dxc);

    float d2 = d1 * d1;
    float sagitta = r2c - d2 * innlen2;

    float3 o2c = cross(r2c, acyl);
    float po2c = dot(o2c, dxc);
    limits.x = limits.y = -po2c * innlen2;
    sagitta = sagitta > 0? sqrt(sagitta * innlen2) : 0;
    limits.x = optix::fmaxf(limits.x - sagitta, ray.tmin);
    limits.y = optix::fminf(limits.y + sagitta, ray.tmax);

    return limits.y > 0 && limits.x < limits.y;
}
```