## The TOP-C Parallel Model and Symbolic Algebra

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**Software name:** TOP-C (and ParGAP, ParGCL, ParGeant4, Marshalgen)

**Short description:** Parallelization features of TOP-C:

- minimal modifications to sequential code (using 'raw mode')
- small footprint (30 KB stripped library under Linux)
- self-contained (including MPI subset)
- extensive manual (approximately 50 pages)
- compiles into distributed or shared memory architecture
- optionally compiles into sequential emulation for easy debugging

Public access: http://www.ccs.neu.edu/home/gene/XXX for XXX one of topc.html, pargap.html, pargcl.html, or pargeant4.html

## **Abstract**

The TOP-C parallel model was specifically designed to be optimal for many symbolic algebra algorithms. Symbolic algebra problems are irregular and differ from typical problems of numerical analysis in two respects.

- 1. They have large amounts of intermediate swell.
- 2. They are usually not able to make good use of data parallelism.

The TOP-C model was developed on the basis of experience over ten years. The model was first implemented for distributed memory for GCL (GNU Common LISP), and is currently available as ParGCL [1]. That work was extended to ParGAP [3], a binding to the interactive language GAP (Groups, Algorithms and Programming). Finally, a C/C++ version, Task Oriented Parallel C/C++, lent its acronym to the TOP-C model [2].

A sign of the maturity of TOP-C is the parallelization of Geant4 (Geometry and Tracking) [4]. Geant4 is a million-line program for the simulation

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of particle-matter interaction used in the design of collider experiments at CERN. Current issues facing parallelization include the slowness of RAM [5] and the need for semi-automated marshalling (serialization of objects) [6].

- A. The Task: tasks executed by each slave process, in parallel
- B. The Action: control of parallel strategy for TOP-C
- C. The Shared Data: shared data, read-only by all processes

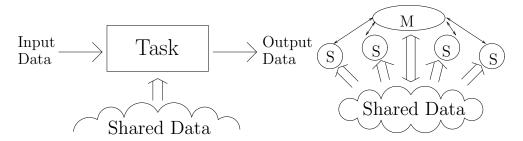


Figure 1: TOP-C model (distributed memory): For Gröbner bases, the *shared data* is the current basis of the polynomial ideal, the *task input* is an S-pair, and the *task output* is a reduced polynomial. For a non-trivial reduction, the master declares an UPDATE action, and each node reduces its replicate of the current basis.

## References

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