Instance-based learning

(a.k.a. memory-based) (a.k.a. nonparametric regression) (a.k.a. casebased) (a.k.a kernel-based)

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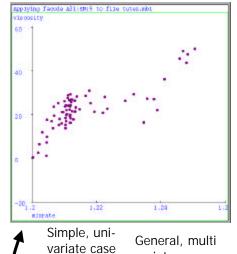
Oct 25th, 2001

Overview

- What do we want a regressor to do?
- Why not stick with polynomial regression? Why not just "join the dots"?
- · What's k-nearest-neighbor all about?
- And how about kernel regression, locally weighted regression?
- Hmm. But what about multivariate fitting?
- And how do you compute all that stuff? And why should I care?

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This Tutorial's Starting Point



variate case

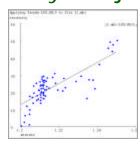
We've obtained some numeric data.

How do we exploit it?

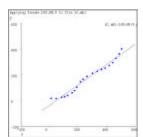
Steel	Line	Slab	Temp	Cool	Cool
Temp	Speed	Width	Stage2	Setpt	Gain
-0.4788	0.3849	0.0357	0.8384	0.6620	-0.9512
0.3470	-0.6488	0.6629	-0.5087	0.6845	-0.0647
0.8622	-0.5367	-0.2459	-0.1438	-0.7267	-0.6119
-0.2099	-0.5975	0.0614	-0.7648	0.0222	-0.7623
-0.4627	0.6218	0.9254	0.6081	-0.8739	-0.6439
0.7341	0.0745	-0.2650	-0.4510	-0.4548	0.5753
0.4237	-0.5143	-0.0731	0.0385	-0.8068	0.3098
-0.1267	0.8105	-0.6619	-0.0768	-0.8738	-0.3367
0.0332	0.7754	0.7718	-0.5440	0.6237	0.5113
0.2668	0.8777	-0.5690	-0.5151	0.6493	0.7705
-0.5682	0.8457	0.5669	-0.7359	-0.3394	0.5880

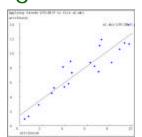
Instance-based learning: Slide 3

Why not just use Linear Regression?



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Here, linear regression manages to capture a significant trend in the data, but there is visual evidence of bias.

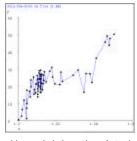
Here, linear regression better fit, but the bias is thing. very clear.

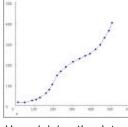
Here, linear regression appears to have a much may indeed be the right

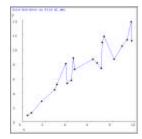
Bias: the underlying choice of model (in this case, a line) cannot, with any choice of parameters (constant term and slope) and with any amount of data (the dots) capture the full relationship.

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Why not just Join the Dots?







clearly fitting noise.

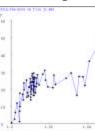
Here, joining the dots is Here, joining the dots looks very sensible.

Again, a clear case of noise fitting.

Why is fitting the noise so bad?

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Instance-based learning: Slide 5



- You will tend to make somewhat bigger prediction errors on new data than if you filtered the noise perfectly.
- You don't get good gradient estimates or noise estimates.
- You can't make sensible confidence intervals.
- It's morally wrong.
- · Also: Join the dots is much harder to

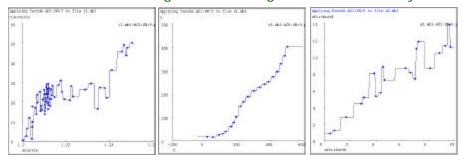
Here, joining the coimplement for multivariate inputs case sensible. clearly fitting noise. noise fitting.

Why is fitting the noise so bad?

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One-Nearest Neighbor

...One nearest neighbor for fitting is described shortly...



Similar to Join The Dots with two Pros and one Con.

- PRO: It is easy to implement with multivariate inputs.
- CON: It no longer interpolates locally.
- PRO: An excellent introduction to instance-based learning...

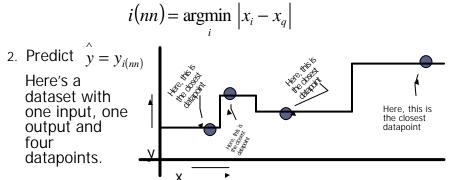
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Instance-based learning: Slide 7

Univariate 1-Nearest Neighbor

Given datapoints (x_1, y_1) (x_2, y_2) .. (x_N, y_N) , where we assume $y_i = f(s_i)$ for some unknown function f. Given query point x_{q_i} your job is to predict $\hat{y} = \hat{f}(x_q)$. Nearest Neighbor:

1. Find the closest x_i in our set of datapoints



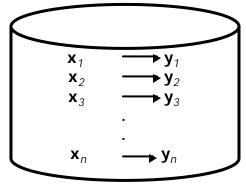
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1-Nearest Neighbor is an example of....

Instance-based learning

A function approximator that has been around since about 1910.

To make a prediction, search database for similar datapoints, and fit with the local points.



Four things make a memory based learner:

- A distance metric
- How many nearby neighbors to look at?
- A weighting function (optional)
- How to fit with the local points?

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Instance-based learning: Slide 9

Nearest Neighbor

Four things make a memory based learner:

1. A distance metric

Euclidian

2. How many nearby neighbors to look at?

One

3. A weighting function (optional)

Unused

4. How to fit with the local points?

Just predict the same output as the nearest neighbor.

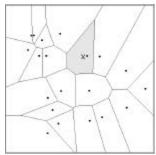
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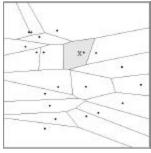
Multivariate Distance Metrics

Suppose the input vectors x1, x2, ...xn are two dimensional:

$$\mathbf{x}_1 = (x_{11}, x_{12}), \mathbf{x}_2 = (x_{21}, x_{22}), \dots \mathbf{x}_N = (x_{N1}, x_{N2}).$$

One can draw the nearest-neighbor regions in input space.





$$Dist(\mathbf{x}_{i}, \mathbf{x}_{i}) = (x_{i1} - x_{i1})^{2} + (x_{i2} - x_{i2})^{2} \quad Dist(\mathbf{x}_{i}, \mathbf{x}_{i}) = (x_{i1} - x_{i1})^{2} + (3x_{i2} - 3x_{i2})^{2}$$

Dist
$$(\mathbf{x}_{i}, \mathbf{x}_{i}) = (x_{i1} - x_{i1})^{2} + (3x_{i2} - 3x_{i2})^{2}$$

The relative scalings in the distance metric affect region shapes.

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Instance-based learning: Slide 11

Euclidean Distance Metric

$$D(x, x') = \sqrt{\sum_{i} s_{i}^{2} (x_{i} - x'_{i})^{2}}$$

Or equivalently,

$$D(x, x') = \sqrt{(x - x')^T \sum_{x} (x - x')}$$

where

$$\Sigma = \begin{bmatrix} s_1^2 & 0 & \cdots & 0 \\ 0 & s_2^2 & \cdots & 0 \\ \cdots & \cdots & \cdots & \cdots \\ 0 & 0 & \cdots & s_N^2 \end{bmatrix}$$

Other Metrics...

 Mahalanobis, Rank-based, Correlation-based (Stanfill+Waltz, Maes' Ringo system...)

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The Zen of Voronoi Diagrams

CNN Article

Mystery of renowned zen garden revealed

Thursday, September 26, 2002 Posted: 10:11 AM EDT (1411 GMT)

LONDON (Reuters) -- For centuries visitors to the renowned Ryoanji Temple garden in Kyoto, Japan have been entranced and mystified by the simple arrangement of rocks.

The five sparse clusters on a rectangle of raked gravel are said to be pleasing to the eyes of the hundreds of thousands of tourists who visit the garden each year.

Scientists in Japan said on Wednesday they now believe they have discovered its mysterious appeal.

"We have uncovered the implicit structure of the Ryoanji garden's visual ground and have shown that it includes an abstract, minimalist depiction of natural scenery," said Gert Van Tonder of Kyoto University.

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The researchers discovered that the empty space of the garden evokes a hidden image of a branching tree that is sensed by the unconscious mind.

"We believe that the unconscious perception of this pattern contributes to the enigmatic appeal of the garden," Van Tonder added.

He and his colleagues believe that whoever created the garden during the Muromachi era between 1333-1573 knew exactly what they were doing and placed the rocks around the tree image.

By using a concept called medial-axis transformation, the scientists showed that the hidden branched tree converges on the main area from which the garden is viewed.

The trunk leads to the prime viewing site in the ancient temple that once overlooked the garden.

It is thought that abstract art may have a similar impact.

"There is a growing realisation that scientific analysis can reveal unexpected structural features hidden in controversial abstract paintings," Van Tonder said Instance-based learning: Slide 13

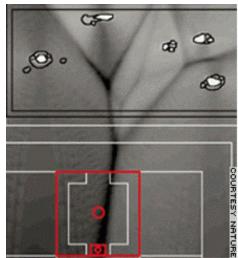
Zen Part Two



Ryoanji Temple garden in Kyoto

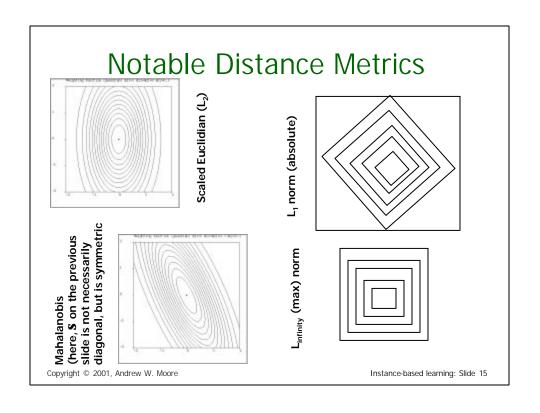
(Photos and article extracted from $\underline{\text{www.cnn.com}}$)

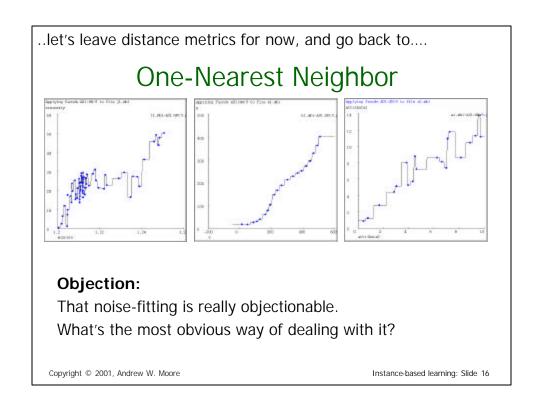
Ouestion: what set of five rocks placed at a distance would have <u>not</u> produced a tree-like voronoi diagram?



Layout shows the rock clusters (top) and the preferred viewing spot of the garden from the main hall (the circle in the middle of the square).

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k-Nearest Neighbor

Four things make a memory based learner:

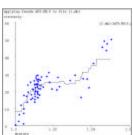
- 1. A distance metric
 - Euclidian
- 2. How many nearby neighbors to look at? **k**
- 3. A weighting function (optional) **Unused**
- 4. How to fit with the local points?

Just predict the average output among the k nearest neighbors.

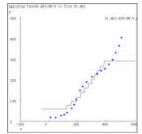
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Instance-based learning: Slide 17

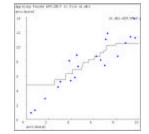
k-Nearest Neighbor (here k=9)



A magnificent job of noisesmoothing. Three cheers for 9-nearest-neighbor. But the lack of gradients and the jerkiness isn't good.



Appalling behavior! Loses all the detail that jointhe-dots and 1-nearestneighbor gave us, yet smears the ends.



Fits much less of the noise, captures trends. But still, frankly, pathetic compared with linear regression.

K-nearest neighbor for function fitting smoothes away noise, but there are clear deficiencies.

What can we do about all the discontinuities that k-NN gives us?

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Kernel Regression

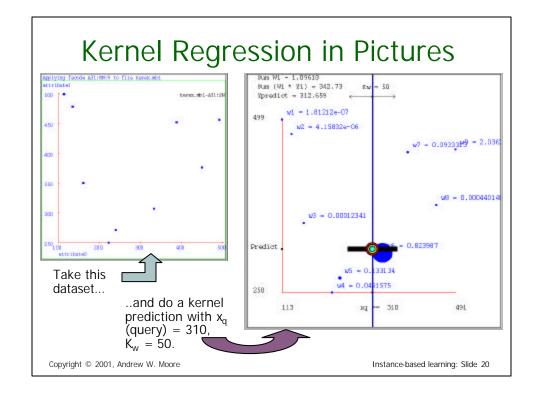
Four things make a memory based learner:

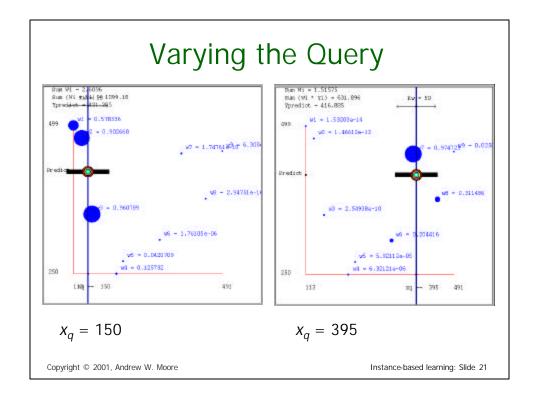
- A distance metric
 Scaled Euclidian
- How many nearby neighbors to look at?All of them
- 3. A weighting function (optional) $w_i = \exp(-D(x_i, \text{ query})^2 / K_w^2)$

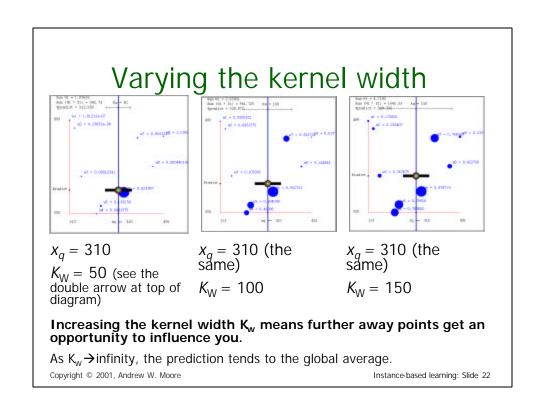
Nearby points to the query are weighted strongly, far points weakly. The K_W parameter is the **Kernel Width**. Very important.

4. How to fit with the local points? Predict the weighted average of the outputs: $predict = Sw_iy_i / Sw_i$

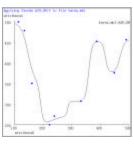
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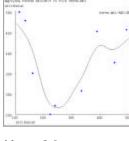


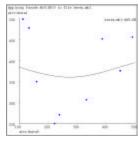




Kernel Regression Predictions







$$K_W = 10$$

$$K_W=20$$

$$K_{W} = 80$$

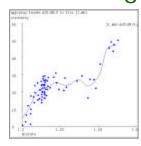
Increasing the kernel width $\mathbf{K}_{\mathbf{w}}$ means further away points get an opportunity to influence you.

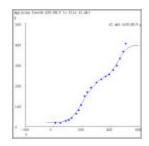
As $K_w \rightarrow$ infinity, the prediction tends to the global average.

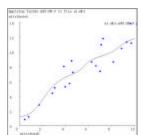
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Instance-based learning: Slide 23

Kernel Regression on our test cases







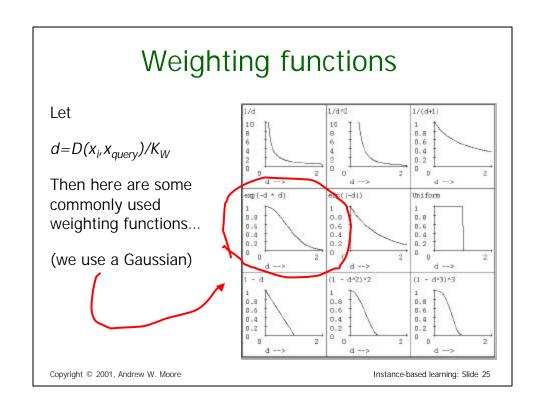
KW=1/32 of x-axis width. It's nice to see a smooth curve at last. But rather bumpy. If Kw gets any higher, the fit is poor.

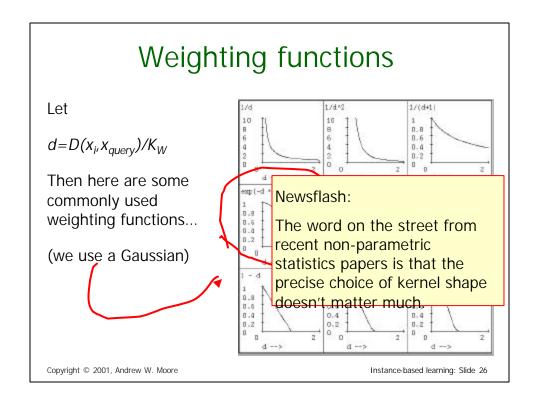
KW=1/32 of x-axis width. Quite splendid. Well done, kernel regression. The author needed to choose the right K_W to achieve this.

KW=1/16 axis width. Nice and smooth, but are the bumps justified, or is this overfitting?

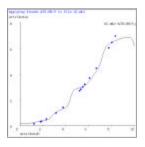
Choosing a good K_w is important. Not just for Kernel Regression, but for all the locally weighted learners we're about to see.

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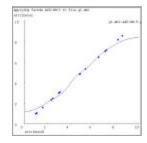


Kernel Regression can look bad



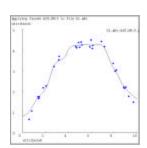


Clearly not capturing the simple structure of the data.. Note the complete failure to extrapolate at edges.



KW = Best.

Also much too local. Why wouldn't increasing Kw help? Because then it would all be "smeared".



KW = Best.

Three noisy linear segments. But best kernel regression gives poor gradients.

Time to try something more powerful...

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Instance-based learning: Slide 27

Locally Weighted Regression

Kernel Regression:

Take a very very conservative function approximator called AVERAGING. Locally weight it.

Locally Weighted Regression:

Take a conservative function approximator called LINEAR REGRESSION. Locally weight it.

Let's Review Linear Regression....

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Unweighted Linear Regression

You're lying asleep in bed. Then Nature wakes you.

YOU: "Oh. Hello, Nature!"

NATURE: "I have a coefficient ß in mind. I took a bunch of real numbers called $x_1, x_2 ... x_N$ thus: $x_1 = 3.1, x_2 = 2, ... x_N = 4.5$.

For each of them (k=1,2,...N), I generated $y_k = \beta x_k + e_k$ where e_k is a Gaussian (i.e. Normal) random variable with mean 0 and standard deviation s. The e_k 's were generated independently of each other.

Here are the resulting y_i 's: y_1 =5.1, y_2 =4.2, ... y_N =10.2"

You: "Uh-huh."

Nature: "So what do you reckon ß is then, eh?"

WHAT IS YOUR RESPONSE?

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Instance-based learning: Slide 29

Global Linear Regression: $y_k = \beta x_k + e_k$

 $\operatorname{prob}(y_k || x_k, \beta) \sim \operatorname{Gaussian}, \operatorname{mean} \beta x_k, \operatorname{std.dev}.s$

$$\operatorname{prob}(y_{k} | x_{k}, \beta) = \operatorname{Kexp}\left(\frac{-(y_{k} - \beta x_{k})^{2}}{2s^{2}}\right)$$

$$\operatorname{prob}(y_{1}, y_{2}, ..., y_{N} || x_{1}, x_{2}, ..., x_{N}, \beta) = \prod_{k=1}^{N} K \exp\left(\frac{-(y_{k} - \beta x_{k})^{2}}{2s^{2}}\right)$$

Which value of ß makes the y_1 , y_2 .. y_N values most likely?

$$\hat{\beta} = \frac{\arg \max}{\beta} \operatorname{prob}(y_1, y_2, ..., y_N || x_1, x_2, ..., x_N, \beta)$$

$$= \frac{\arg \max}{\beta} \log \operatorname{prob}(y_1, y_2, ..., y_N || x_1, x_2, ..., x_N, \beta)$$

$$= \underset{\beta}{\operatorname{arg\,max}} N \log K - \frac{1}{2s^2} \sum_{k=1}^{N} (y_k - \beta x_k)^2$$

$$= \frac{\arg\min}{\beta} \sum_{k=1}^{N} (y_k - \beta x_k)^2$$

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Least squares unweighted linear regression

Write
$$E(\beta) = \sum_{k} (y_k - \beta x_k)^2$$
, so $\hat{\beta} = \frac{\arg \min}{\beta} E(\beta)$

To minimize $E(\beta)$, set

$$\frac{\partial}{\partial \mathbf{B}} E(\mathbf{B}) = 0$$

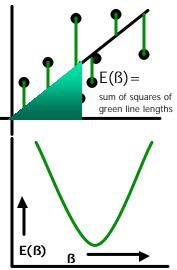
SO

$$0 = \frac{\partial}{\partial \beta} E(\beta) = -2\sum_{k} x_{k} y_{k} + 2\beta \sum_{k} x_{k}^{2}$$

giving

$$\hat{\mathbf{B}} = \left(\sum_{k} x_{k}^{2}\right)^{-1} \sum_{k} x_{k} y_{k}$$

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Instance-based learning: Slide 31

Multivariate unweighted linear regression

Nature supplies N input vectors. Each input vector x_k is *D*-dimensional: $\mathbf{x}_k = (x_{k1}, x_{k2} ... x_{kD})$. Nature also supplies N corresponding output values $y_1 ... y_N$.

$$X = \begin{bmatrix} x_{11} & x_{12} & \cdots & x_{1D} \\ x_{21} & x_{22} & \cdots & x_{2D} \\ \vdots & \vdots & & \vdots \\ x_{N1} & x_{N2} & \cdots & x_{ND} \end{bmatrix} \qquad Y = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_N \end{bmatrix} \text{ we are told } y_k = \left(\sum_{j=1}^{D} \boldsymbol{b}_j x_{kj}\right) + \boldsymbol{e}_k$$

We must estimate $\beta = (\beta_1, \beta_2 \dots \beta_D)$. It's easily shown using matrices instead of scalars on the previous slide that

$$\hat{\boldsymbol{b}} = (X^T X)^{-1} X^T Y$$

Note that X^TX is a D x D positive definite symmetric matrix, and X^TY is a D x 1 vector:

 $(X^T X)_{ij} = \sum_{k=1}^{N} x_{ki} x_{kj} \qquad (X^T Y)_i = \sum_{k=1}^{N} x_{ki} y_i$ Instance-based learning: Slide 32

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The Pesky Constant Term

Now: Nature doesn't guarantee that the line/hyperplane passes through the origin.

In other words: Nature says

$$y_k = \beta_0 + \left(\sum_{j=1}^D \beta_j x_{kj}\right) + e_k$$

"No problem," you reply. "Just add one extra input variable, x_{k0} , which is always 1"

$$\begin{bmatrix} x_{11} & x_{12} & \cdots & x_{1D} \\ x_{21} & x_{22} & \cdots & x_{2D} \\ \vdots & \vdots & & \vdots \\ x_{N1} & x_{N2} & \cdots & x_{ND} \end{bmatrix} \rightarrow \begin{bmatrix} 1 & x_{11} & x_{12} & \cdots & x_{1D} \\ 1 & x_{21} & x_{22} & \cdots & x_{2D} \\ \vdots & \vdots & & \vdots \\ 1 & x_{N1} & x_{N2} & \cdots & x_{ND} \end{bmatrix}$$

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Instance-based learning: Slide 33

Locally Weighted Regression

Four things make a memory-based learner:

1. A distance metric

Scaled Euclidian

2. How many nearby neighbors to look at?

All of them

3. A weighting function (optional)

$$W_k = \exp(-D(x_k, x_{auerv})^2 / K_w^2)$$

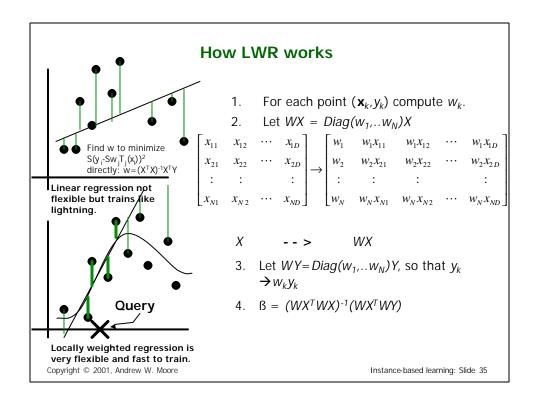
Nearby points to the query are weighted strongly, far points weakly. The K_w parameter is the **Kernel Width**.

4. How to fit with the local points?

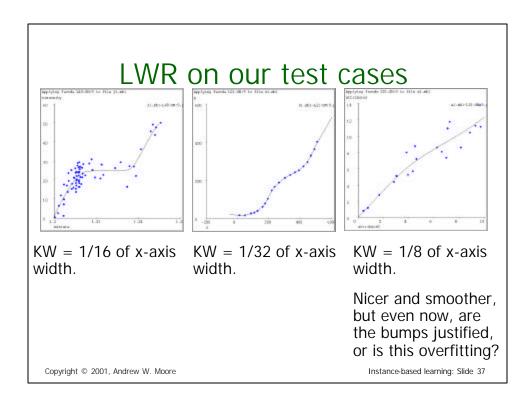
First form a local linear model. Find the $\underline{\beta}$ that minimizes the locally weighted sum of squared residuals:

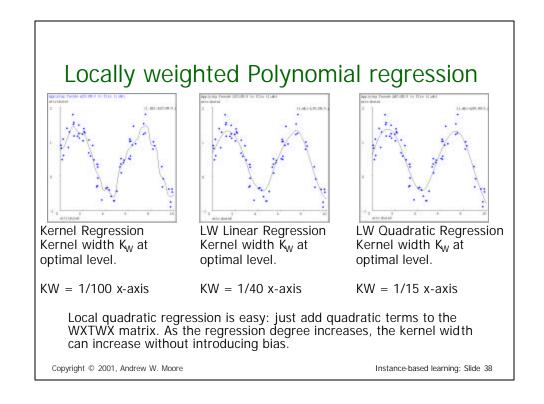
$$\hat{\mathbf{B}} = \underset{\mathbf{B}}{\operatorname{argmin}} \sum_{k=1}^{N} w_k^2 (\mathbf{y}_k - \mathbf{B}^T \mathbf{x}_k)^2$$
 Then predict $y_{predict} = \underline{\mathbf{B}}^T x_{query}$

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```
Input X matrix of inputs: X[k][i] = i'th component of k'th input point.
Input Y matrix of outputs: Y[k] = k'th output value.
Input xq = query input. Input kwidth.
WXTWX = empty (D+1) x (D+1) matrix
WXTWY = empty (D+1) \times 1
for (k = 1; k \le N; k = k + 1)
   /* Compute weight of kth point */
   wk = weight_function( distance( xq , X[k] ) / kwidth )
    /* Add to (WX) ^T (WX) matrix */
    for (i = 0; i < D; i = i + 1)
          for (j = 0; j <= D; j = j + 1)
                    if (i == 0) xki = 1 else xki = X[k] [i]
                    if (j == 0) xkj = 1 else xkj = X[k][j]
                    WXTWX [i] [j] = WXTWX [i] [j] + wk * wk * xki * xkj
    /* Add to (WX) ^T (WY) vector */
   for (i = 0; i <= D; i = i + 1)
           if (i == 0) xki = 1 else xki = X[k][i]
           WXTWY [i] = WXTWY [i] + wk * wk * xki * Y[k]
/* Compute the local beta. Call your favorite linear equation solver. Recommend Cholesky
    Decomposition for speed. Recommend Singular Val Decomp for Robustness. */
beta = (WXTWX)^{-1} (WXTWY)
ypredict = beta[0] + beta[1]*xq[1] + beta[2]*xq[2] + ... beta[D]*xq[D]
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                                                                  Instance-based learning: Slide 36
```





When's Quadratic better than Linear?

- It can let you use a wider kernel without introducing bias.
- Sometimes you want more than a prediction, you want an estimate of the local Hessian. Then quadratic is your friend!
- But in higher dimensions is appallingly expensive, and needs a lot of data. (Why?)
- Two "Part-way-between-linear-and-quadratic" polynomials:
 - "Ellipses": Add x_i^2 terms to the model, but not cross-terms (no $x_i x_i$ where i=j)
 - "Circles": Add only one extra term to the model:

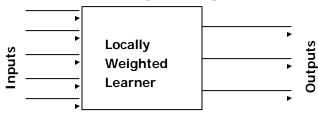
$$x_{D+1} = \sum_{i=1}^{D} x_j^2$$

 Incremental insertion of polynomial terms is well established in conventional regression (GMDH,AIM): potentially useful here too

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Multivariate Locally weighted learning



All the methods described so far can generalize to multivariate input and output. But new questions arise:

- What are good scalings for a Euclidean distance metric?
- What is a better Euclidean distance metric?
- Are all features relevant?
- Do some features have a global rather than local influence?

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A Bivariate Fit Example

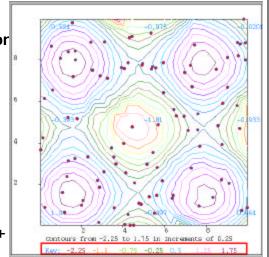
LWQ Regression

Let's graph the prediction surface given 100 noisy datapoints: each with 2 inputs, one output

Kernel Width, Number of fully weighted Neighbors, Distance Metric Scales all optimized. Kw = 1/16 axis width 4 nearest neighs full weight Distance metric scales each axis equally.

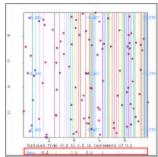
$$f(x,y) = \sin(x) + \sin(y) + \cos(x)$$

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Two more bivariate fits



Kernel Regression.

KW, num neighs, metric scales all optimized.

KW=1/100 x-axis width. 1-NN fully weighted. y not included in distance metric.

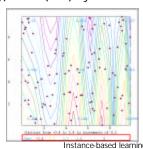
$$f(x,y) = \sin(x^*x)$$

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Locally weighted linear regression. KW, num neighs, metric scales all optimized.

KW=1/50 x-axis width. No neighbors fully weighted. y not included in distance metric, but is included in the regression.

$$f(x,y) = \sin(x^*x) + y + \text{noise}$$



Fabricated Example

 $f(x_1,x_2,x_3,x_4,x_5,x_6,x_7,x_8,x_9) = noise + x_2 + x_4 + 4sin(0.3x_6 + 0.3x_8).$ (Here we see the result of searching for the best metric, feature set, kernel width, polynomial type for a set of 300 examples generated from the above function) Recommendation.

Based on the search results so far, the recommended function approximator encoding is L20:SN:-0-0-9-9. Let me explain the meaning:

Locally weighted regression. The following features define the distance metric:

x6 (full strength). x8 (full strength).

A gaussian weighting function is used with kernel width 0.0441942 in scaled input space. We do a weighted least squares with the following terms:

Term 0 = 1Term 1 = x2/10Term 2 = x4/10Term 3 = x6/10

Term 4 = x8/10

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Locally Weighted Learning: Variants

- Range Searching: Average of all neighbors within a given range
- Range-based linear regression: Linear regression on all points within a given range
- Linear Regression on K-nearest-neighbors
- Weighting functions that decay to zero at the kth nearest neighbor
- Locally weighted Iteratively Reweighted Least Squares
- Locally weighted Logistic Regression
- Locally weighted classifiers
- Multilinear Interpolation
- Kuhn-Triangulation-based Interpolation
- Spline Smoothers

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Using Locally Weighted Learning for Modeling

- "Hands-off" non-parametric relation finding
- Low Dimensional Supervised Learning
- Complex Function of a subset of inputs
- Simple function of most inputs but complex function of a few
- Complex function of a few features of many input variables

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Use (1): "Hands-off" non-parametric relation finding.

You run an HMO (or a steel tempering process) (or a 7-dof dynamic robot arm)

You want an intelligent assistant to spot patterns and regularities among pairs or triplets of variables in your database...

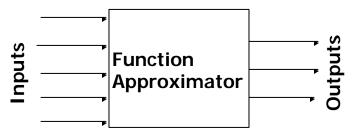
-HMO variables:	Steel Variables:	Robot Variables:
-Physician Age	Line Speed	Roll
-Patient Age	Line Spd 10mins	DRoll
-Charge/Day	Line Spd 20mins	DDRoll
-Charge/Discharge	Slab width	Pitch
-Discharges/100	Slab height	DPitch
-ICD-9 Diagnosis	Slab Temp Stg1	DDPitch
- Market Share	Slab Temp Stg2	SonarHeight
-Mortality/100	CoolTunn2 Setp	LaserHeight
Patient ZIP	CoolTunn5 Sep	FlightTime
-Zip Median Age	CoolTunn2 Temp	ThrustRate

You especially want to find more than just the linear correlations....

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Use (2): Low Dimensional Supervised Learning

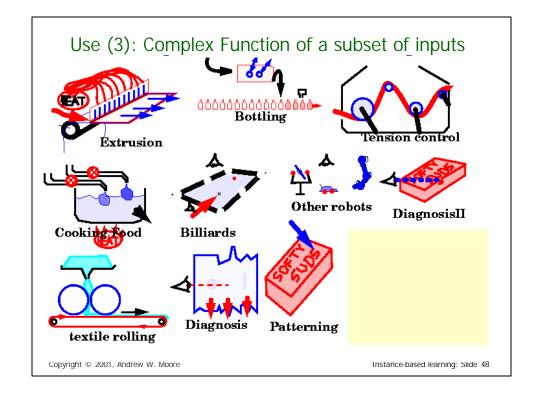
You have lots of data, not many input variables (less than 7, say) and you expect a very complex non-linear function of the data.



Examples:

- · Skin Thickness vs t,f for face scanner
- Topographical Map
- Tumor density vs (x,y,z)
- Mean wasted Aspirin vs (fill-target, mean-weight, weight -sdev, rate) for an aspirin-bottle filler
- Object -ball collision-point vs (x,y,?) in Pool

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Use (4): Simple function of most inputs but complex function of a few.

Examples:

- $f(x) = x_1 + 3x_2 x_4 + \sin(\log(x_5) x_6) x_7^2 + x_8 x_9 + 8x_{10}$
- Car Engine Emissions
- Food Cooling Tunnel

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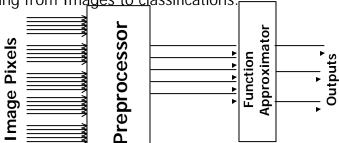
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Use (5): Complex function of a few features of many input variables.

Examples:

- Mapping from acoustic signals to "Probability of Machine Breakdown".
- Time series data analysis.

Mapping from Images to classifications.



(e.g. Product inspection, Medical imagery, Thin Film imaging..)

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Local Weighted Learning: Pros & Cons vs Neural Nets

Local weighted learning has some advantages:

- Can fit low dimensional, very complex, functions very accurately. Neural nets require considerable tweaking to do this.
- You can get meaningful confidence intervals, local gradients back, not merely a prediction.
- · Training, adding new data, is almost free.
- "One-shot" learning---not incremental
- · Variable resolution.
- Doesn't forget old training data unless statistics warrant.
- · Cross-validation is cheap

Neural Nets have some advantages:

- With large datasets, MBL predictions are slow (although kdtree approximations, and newer cache approximations help a lot).
- Neural nets can be trained directly on problems with hundreds or thousands of inputs (e.g. from images). MBL would need someone to define a smaller set of image features instead.
- · Nets learn incrementally.

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What we have covered

- Problems of bias for unweighted regression, and noisefitting for "join the dots" methods
- Nearest Neighbor and k-nearest neighbor
- · Distance Metrics
- Kernel Regression
- Weighting functions
- Stable kernel regression
- Review of unweighted linear regression
- Locally weighted regression: concept and implementation
- Multivariate Issues
- Other Locally Weighted variants
- Where to use locally weighted learning for modeling?
- Locally weighted pros and cons

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