Gecco 2006 Grammatical Evolution Tutorial

Conor Ryan

Biocomputing and Developmental Systems Group Department of Computer Science and Information Systems University of Limerick

8th July 2006

(University of Limerick)

Grammatical Evolution

8th July 2006 1 / 81

Outline



- 2 Grammatical Evolution
- 3 Genetic Operators









Issues with GP

• Function/terminal set must have "closure"

Single types only

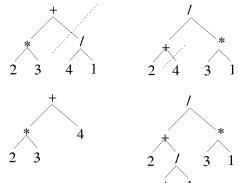
• Trees grow, or "bloat"

(University of Limerick)

Sac

Issues with GP

• Function/terminal set must have "closure"



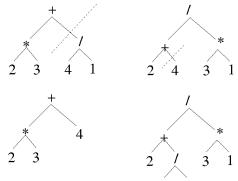
• Single types only

• Trees grow, or "bloat"

- E 🕨

Issues with GP

• Function/terminal set must have "closure"



- Single types only
- Trees grow, or "bloat"

Biological Phenomena

- No simple one to one mapping
 - Genes produce proteins
 - Proteins combine to create phenotype
- Linear strings
 - Genomes are always held on strings
- Unconstrained search
 - Repair not performed

< 17 ≥

Biological Phenomena

- No simple one to one mapping
 - Genes produce proteins
 - Proteins combine to create phenotype
- Linear strings
 - Genomes are always held on strings
- Unconstrained search
 - Repair not performed

Biological Phenomena

- No simple one to one mapping
 - Genes produce proteins
 - Proteins combine to create phenotype
- Linear strings
 - Genomes are always held on strings
- Unconstrained search
 - Repair not performed

• Grammatical Evolution (GE)

- GA to evolve programs
- Morphogenetic Effect:
 - Genotype mapped to phenotype
- Phenotype is a compilable program
- Genome governs mapping of a BNF/attribute grammar definition to the program

< 17 ≥

→ Ξ → +

• Grammatical Evolution (GE)

- GA to evolve programs
- Morphogenetic Effect:
 - Genotype mapped to phenotype
- Phenotype is a compilable program
- Genome governs mapping of a BNF/attribute grammar definition to the program

< 17 ≥

.∃ ▶ ∢

• Grammatical Evolution (GE)

- GA to evolve programs
- Morphogenetic Effect:
 - Genotype mapped to phenotype
- Phenotype is a compilable program
- Genome governs mapping of a BNF/attribute grammar definition to the program

∃ ► ∢

- Here genome (a binary string) is mapped to compilable C code
- Can potentially evolve programs in any language, with arbitrary complexity
- Any structure than be specified with a grammar, e.g. graphs, neural networks, etc.

Language Definition

- Backus Naur Form (BNF)
 - Notation for expressing a languages grammar as Production Rules
- BNF Grammar consists of the tuple < T,N,P,S > where
 - T is Terminals set
 - N is Non-Terminals set
 - P is Production Rules set
 - S is Start Symbol (a member of N)

BNF Example

 $T = {Sin, Cos, Tan, Log, +, -, /, *, X, (,)}$

S = < expr >

Grammars

Language Definition

- Backus Naur Form (BNF)
 - Notation for expressing a languages grammar as Production Rules
- BNF Grammar consists of the tuple < T,N,P,S > where
 - T is Terminals set
 - N is Non-Terminals set
 - P is Production Rules set
 - S is Start Symbol (a member of N)

BNF Example

 $T = \{Sin, Cos, Tan, Log, +, -, /, *, X, (,)\}$

$$S = < expr >$$

Grammars

Language Definition

- Backus Naur Form (BNF)
 - Notation for expressing a languages grammar as Production Rules
- BNF Grammar consists of the tuple < T,N,P,S > where
 - T is Terminals set
 - N is Non-Terminals set
 - P is Production Rules set
 - S is Start Symbol (a member of N)
- BNF Example

$$T = \{Sin, Cos, Tan, Log, +, -, /, *, X, (,)\}$$

$$S = < expr >$$

・ 同 ト ・ ヨ ト ・ ヨ ト

BNF Definition

۲

$N = \{expr, op, pre_op\}$

• And P can be represented as:

DQC

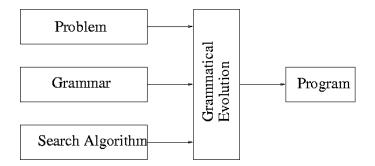
BNF Definition

• A Genetic Algorithm is used to control choice of production rule

ъ

・ロト ・日 ・ ・ ヨ ・ ・

Architecture



æ

DQC

<ロト < 回ト < 回ト < 回ト

Related GP Systems

Name	Genome	Representation
Koza	Tree	Direct
Banzhaf et al	Linear	Direct
Gruau	Tree	Graph Grammar
Whigham	Tree	Derivation Tree
Wong & Leung	Tree	Logic Grammars
Paterson	Linear	Grammar

• Repair mechanisms..

- Koza none needed
- Banzhaf required for syntactically legal individuals
- Gruau none needed
- Whigham all crossovers subject to repair
- Wong & Leung all crossovers subject to repair
- Paterson under/overspecification.

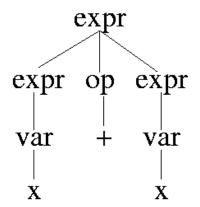
(University of Limerick)

Related GP Systems

Name	Genome	Representation
Koza	Tree	Direct
Banzhaf et al	Linear	Direct
Gruau	Tree	Graph Grammar
Whigham	Tree	Derivation Tree
Wong & Leung	Tree	Logic Grammars
Paterson	Linear	Grammar

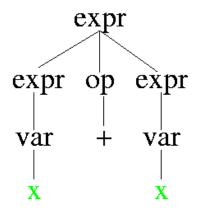
- Repair mechanisms..
- Koza none needed
- Banzhaf required for syntactically legal individuals
- Gruau none needed
- Whigham all crossovers subject to repair
- Wong & Leung all crossovers subject to repair
- Paterson under/overspecification.





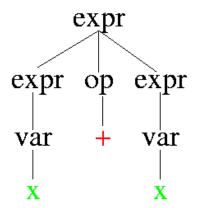
DQC





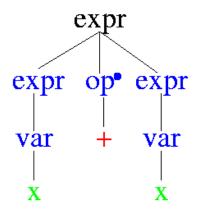
DQC





DQC

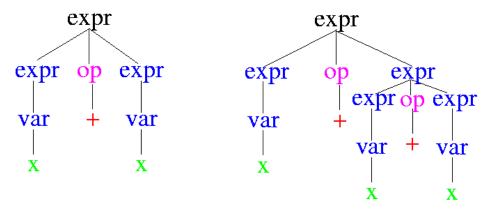




(1 Im.)	in rait	1 061	10000	(als)
(Univ	/ersit	V OI L	_imer	ICK)

DQC

Repair



æ

590

In contrast GE uses

- BNF Paterson/Whigham/Wong etc.
- Variable Length Linear Chromosomes Koza/Gruau/Banzhaf
- Genome encodes pseudo-random numbers
- Degenerate Genetic Code
 - Several genes map to same phenotype
- Wrap individuals

• Use 8 bit codons

- Each codon represents at least one Production Rule
- Gene contains many codons
- Pseudo-random numbers determine what production rule will be used

< 回 ト < 三 ト < 三

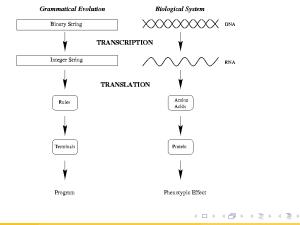
In contrast GE uses

- BNF Paterson/Whigham/Wong etc.
- Variable Length Linear Chromosomes Koza/Gruau/Banzhaf
- Genome encodes pseudo-random numbers
- Degenerate Genetic Code
 - Several genes map to same phenotype
- Wrap individuals
- Use 8 bit codons
 - Each codon represents at least one Production Rule
 - Gene contains many codons
- Pseudo-random numbers determine what production rule will be used

くぼう くほう くほう

- Expression of a *Codon* results in an *Amino Acid* (choice in the derivation sequence)
 - *Amino acids* can combine to form a functional protein (i.e. Terminals such as +, *X* or *Sin*, can combine)

- Expression of a *Codon* results in an *Amino Acid* (choice in the derivation sequence)
 - *Amino acids* can combine to form a functional protein (i.e. Terminals such as +, *X* or *Sin*, can combine)



Example Individual

• To complete BNF definition for a function written in a subset of C we include.....

```
<func> ::= <header>
<header> ::= float symb(float X) <body>
<body> ::= <declarations><code><return>
<declarations> ::= float a;
<code> ::= a = <expr>;
<return> ::= return (a);
```

- Note implementation details.....
 - Function is limited to a single line of code

Example Individual

• To complete BNF definition for a function written in a subset of C we include.....

```
<func> ::= <header>
<header> ::= float symb(float X) <body>
<body> ::= <declarations><code><return>
<declarations> ::= float a;
<code> ::= a = <expr>;
<return> ::= return (a);
```

- Note implementation details.....
 - Function is limited to a single line of code
 - If required can get GE to generate multi-line functions.....modify

```
<code> ::= <line>;
| <line>; <code>
```

Example

Example Individual

In this subset of C all individuals of the form

```
float symb(float x)
ł
  float a;
  a = \langle expr \rangle;
  return(a);
}
```

- Only < expr > will be evolved
- Each non-terminal is mapped to a terminal before any others undergo a mapping process

- 4 E b

< 🗇 🕨 < 🖃 🕨

Example

Example Individual

Given the individual

220	203	51	123	2	45	what will happen?
-----	-----	----	-----	---	----	-------------------

<expr> has 4 production rules to choose from

- Taking first codon 220 we get 220 MOD 4 = 0
- Gives <expr>< op >< expr >
- Next choice for the first <expr>
 - Taking next codon 203 we get 203 MOD 4 = 3
 - Gives < var>< op >< expr >

・ 同 ト ・ ヨ ト ・ ヨ ト

Example Individual

Given the individual

220	203	51	123	2	45	what will happen?
-----	-----	----	-----	---	----	-------------------

<expr> has 4 production rules to choose from

- Taking first codon 220 we get 220 MOD 4 = 0
- Gives <expr>< op >< expr >
- Next choice for the first <expr>
 - Taking next codon 203 we get 203 MOD 4 = 3
 - Gives <var>< op >< expr >

Example Individual

• Given the individual

220	203	51	123	2	45	what will happen?
-----	-----	----	-----	---	----	-------------------

<expr> has 4 production rules to choose from

- Taking first codon 220 we get 220 $MOD \ 4 = 0$
- Gives <expr>< op >< expr >

```
    Next choice for the first <expr>
```

- Taking next codon 203 we get 203 MOD 4 = 3
- Gives <<u>var</u>>< op >< expr >

Example

Example Individual

Given the individual

220	203	51	123	2	45	what will happen?
-----	-----	----	-----	---	----	-------------------

<expr> has 4 production rules to choose from

- Taking first codon 220 we get 220 MOD 4 = 0
- Gives <expr>< op >< expr>
- Next choice for the first <expr>
 - Taking next codon 203 we get 203 MOD 4 = 3
 - Gives <var>< op >< expr >

Example

Example Individual

- <var> involves no choice
 - Mapped to X...only one production
 - Now have X < op>< expr >

- Read next codon to choose <op>
 - Next is third codon, value 51, so get 51 MOD 4 = 3
 - Now have X < < expr >
- Next choice for <expr>
 - Next codon is 123 so get 123 MOD 4 = 3
 - Now have X * < var>
- Again <var> involves no choice
 - Finally we get X * X
- The extra codons at end of genome are simply ignored in mapping

イロト イポト イヨト イヨ

Example Individual

- <<u>var</u>> involves no choice
 - Mapped to X...only one production
 - Now have X <op>< expr >

220 203 <u>51</u> 123 2 45

- Read next codon to choose <op>
 - Next is third codon , value 51, so get 51 MOD 4 = 3
 - Now have X* <expr>
- Next choice for <expr>
 - Next codon is 123 so get 123 MOD 4 = 3
 - Now have *X** <<u>var</u>>
- Again <<u>var</u>> involves no choice
 - Finally we get *X* * *X*
- The extra codons at end of genome are simply ignored in mapping the genotype to phenotype

イロト イポト イヨト イヨ

Example Individual

- <<u>var</u>> involves no choice
 - Mapped to X...only one production
 - Now have X <op>< expr >

220 203 <u>51</u> 123 2 45

- Read next codon to choose <op>
 - Next is third codon , value 51, so get 51 MOD 4 = 3
 - Now have X* <expr>
- Next choice for <expr>
 - Next codon is 123 so get 123 MOD 4 = 3
 - Now have X* <<u>var</u>>
- Again < <u>var</u>> involves no choice
 - Finally we get X * X
- The extra codons at end of genome are simply ignored in mapping the genotype to phenotype

Example Mapping Overview

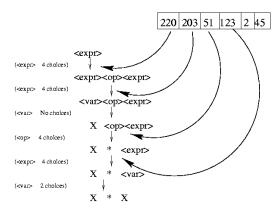


Figure: Example Mapping Outline

<expr> :: = <expr><op><expr> |(<expr><op><expr>) <var> ₹ 990

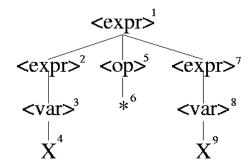
(University of Limerick)

イロト イ団ト イヨト イヨト

Mapping

Derivation Tree Structure

1	2	5	7		
220	203	51	123	2	45



• Not all nodes require a choice!

(University o	f Limerick)
---------------	-------------

ъ

Codons are polymorphic

• When mapping < *expr* >, we calculate

220 mod 4

 However, if we were mapping with 220, we would calculate

220 mod 3

because there are just three choices

• Meaning of a codon depends on its context

イロト イポト イヨト イヨ

Codons are polymorphic

• When mapping < *expr* >, we calculate

220 mod 4

• However, if we were mapping with 220, we would calculate

220 mod 3

because there are just three choices

Meaning of a codon depends on its context

- E - b

4 D b 4 B b 4

- B - 5

Mapping Process

- No simple one to one mapping in GE
- Mapping Process to generate programs
 - Separate Search and Solution Spaces
 - Ensure validity of individuals
 - Remove language dependency
 - Maintain diversity

< 回 ト < 三 ト < 三

Genetic Code Degeneracy

GENETIC CODE PARTIAL PHENOTYPE

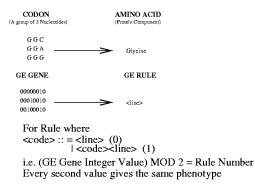


Figure: The Degenerate Genetic Code

э

イロト イポト イヨト イヨト

Genetic Code Degeneracy

Neutral Mutations

- Mutations having no effect on Phenotype Fitness
- Help preserve individual validity
- Gradual accumulation of mutations without harming functionality
 - Revisit later

Initialisation

- Individuals are strings of random numbers
 - No guarantee that they will terminate
 - Individuals can be very short.

Production

<expr>-><var>

always leads to termination

- expr>
 is the start symbol
 - On average, a quarter of all individuals are just one point

イロト イポト イヨト イヨト

Initialisation

- Individuals are strings of random numbers
 - No guarantee that they will terminate
 - Individuals can be very short.

```
<expr> ::= <expr> <op> <expr>
| ( <expr> <op> <expr> )
| <pre-op> ( <expr> )
| <var>
```

Production

```
<expr>-><var>
```

always leads to termination

- expr>
 is the start symbol
 - On average, a quarter of all individuals are just one point

イロト イポト イヨト イヨト

Sensible Initialisation

Generate a spread of individual sizes.

- Based on Ramped Half and Half initialisation in GP
 - For all tree depths from 2 to maximum size
 - Generate an equal number of trees of that size
 - Use full for 50%
 - Use grow for 50%

Similar in GE, but generate derivation trees of equivalent size

< 同 ト < 三 ト < 三

Sensible Initialisation - 2

- Record which number choice was made for each step
- Perform an "unmod" on list of choices
 - Produce a number between 0 and 255 that produces the original number when moded by the number of choices for that productionrule
- Reduces the number of clones (easier to detect)
- Eliminates single point individuals (if desired)

500

Sensible Initialisation - 2

- Record which number choice was made for each step
- Perform an "unmod" on list of choices
 - Produce a number between 0 and 255 that produces the original number when moded by the number of choices for that productionrule
- Ensures that all individuals are valid
- Reduces the number of clones (easier to detect)
- Eliminates single point individuals (if desired)

Genetic Operators

- Perform unconstrained Evolutionary Search
- GE employs standard operators of Genetic Algorithms
 - Point mutation, one-point crossover etc.
- Sometimes modified version of one-point crossover, Sensible Crossover, is used:
 - Effective length
 - Actual length

Genetic Operators

- Perform unconstrained Evolutionary Search
- GE employs standard operators of Genetic Algorithms
 - Point mutation, one-point crossover etc.
- Sometimes modified version of one-point crossover, Sensible Crossover, is used:
 - Effective length
 - Actual length



- What actually happens in crossover?
- Preliminary : Visualisation.

• Crossover is performed at genotypic level



Crossover

- What actually happens in crossover?
- Preliminary : Visualisation.



• Crossover is performed at *genotypic* level

(University of Limerick)

Grammatical Evolution

8th July 2006 30/81

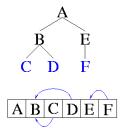
ъ

< 47 ▶



Crossover

- What actually happens in crossover?
- Preliminary : Visualisation.

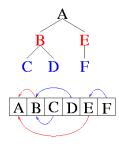


< 47 ▶

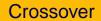


Crossover

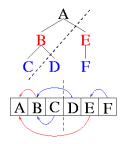
- What actually happens in crossover?
- Preliminary : Visualisation.



Crossover is performed at genotypic level



- What actually happens in crossover?
- Preliminary : Visualisation.



• Crossover is performed at genotypic level

- Analyse 1-point crossover in terms of derivation & syntax trees
- Use a *closed* grammar

$$E::= (+ E E) \{0\}$$
$$|(- E E) \{1\}$$
$$|(- E E) \{2\}$$
$$|(- E E) \{3\}$$
$$|X \{4\}$$
$$|Y \{5\}$$

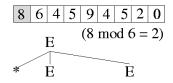
• No polymorphism, because there is only one non-terminal, i.e. one *context*

- Analyse 1-point crossover in terms of derivation & syntax trees
- Use a closed grammar

$$E::= (+ E E) \{0\}$$
$$|(- E E) \{1\}$$
$$|(- E E) \{2\}$$
$$|(- E E) \{3\}$$
$$|X \{4\}$$
$$|Y \{5\}$$

• No polymorphism, because there is only one non-terminal, i.e. one *context*

Different Views of Crossover





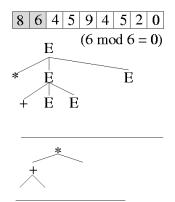
(University of Limerick)

3

DQC

<ロト < 回ト < 回ト < 回ト

Different Views of Crossover

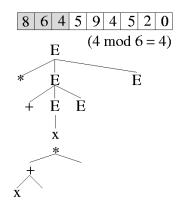


3

DQC

<ロト < 回ト < 回ト < 回ト

Different Views of Crossover

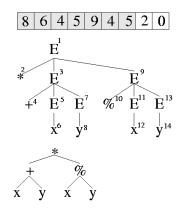


3

DQC

イロト イロト イヨト イヨト

Different Views of Crossover

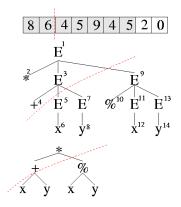


3

DQC

. 1

Different Views of Crossover



э

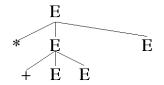
DQC

ъ

I > <
 I >
 I

Rebuilding individuals

• Parent left with "spine"

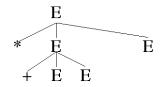


- *Tail* swapped with other parent 4 5 9 4 5 2 0 5 2 2
- Unmapped *E* terms must be mapped
- Use tail from other parent

4 A 1

Rebuilding individuals

• Parent left with "spine"



- Tail swapped with other parent 4594520522
- Unmapped E terms must be mapped
- Use tail from other parent

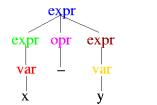
• With more than one non-terminal, a codon could be used differently in the offspring

1 0 0 2 0 1 1 0 0 2 0 1 1 0 0 2 0 1

expr ::= var | expr op expr
opr ::=
$$+ |*| - |\%$$

var ::= x | y

• With more than one non-terminal, a codon could be used differently in the offspring



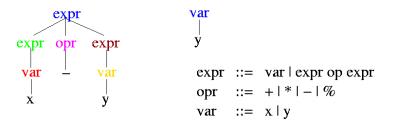
expr ::= var | expr op expr
opr ::=
$$+ |*| - |\%$$

var ::= $x | y$

4 A 1

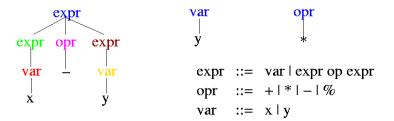
• With more than one non-terminal, a codon could be used differently in the offspring

1 0 0 2 0 1 1 0 0 2 0 1 1 0 0 2 0 1



 With more than one non-terminal, a codon could be used differently in the offspring

1 0 0 2 0 1 1 0 0 2 0 1 1 0 0 2 0 1



Effects of Ripple Crossover

 Symbolic Regression Grammars Closed Grammar

E ::= x| (+ E E) | (* E E) | (- E E) | (/ E E)

And the context free grammar:

Exp ::= Var | Exp Op Exp Var ::= xOp ::= + | * | - | /

Effects (contd.)

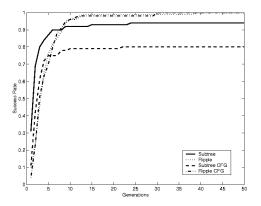
 Santa Fe ant trail grammars Closed grammar

Context free grammar:

```
Code ::= Line | prog2(Line, Code)
Line ::= Condition | Action
Action ::= move() | right() | left()
Condition ::= iffoodahead(Code, Code)
```

・ 同 ト ・ ヨ ト ・ ヨ ト

Symbolic Regresssion Success Rates



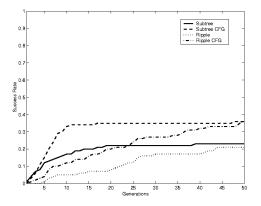
Both ripple crossovers start more slowly, but reach higher fitness.

(1	Jnive	rsitv	of	Lime	rick)
	211140	JOILY	01		illoity

프 🖌 🖌 프

Image: A matrix

Santa Fe Success Rates



Both ripple crossovers again start more slowly, but reach similar fitness.

(Universit	v of I	imer	ick)
Conversit	y 01 L		ion)

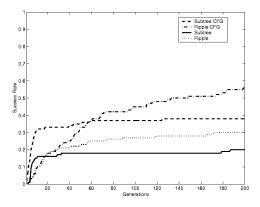
→ Ξ → → Ξ →

I > <
 I >
 I

Genetic Operators

Ripple Crossover

Santa Fe - Extended Run



Success rates on the Santa Fe ant trail problem, averaged over 100 runs, for 250 generations. Ripple crossovers start slowly, but reach higher fitness.

(University of Limerick)

Other types of Crossover?

Homologous Crossover

- Try not to cross in identical areas
- Uniform
- Same size homologous
- Same size two point

-

4 A 1

Homologous Crossover - First point

• Record rule histories for each individual

Rules

Codon Integers	2	13	40	1	3	240	100	23	PARENT 1
Rules	0	1	0	1	1	3	0	3	TARENT I
Codon Integers	2	13	40	7	4	5	1 .	100	PARENT 2

0 1 0 4 0 2 1 0

• Align rule histories of parents

Homologous Crossover - First point

• Record rule histories for each individual

Codon Integers	2	13	40	1	3	240	100	23	PARENT 1
Rules	0	1	0	1	1	3	0	3	TARENT
Codon Integers	2	13	40	7	4	5	1	100	PARENT 2
Rules	0	1	0	4	0	2	1	0	TAKENT 2

• Align rule histories of parents



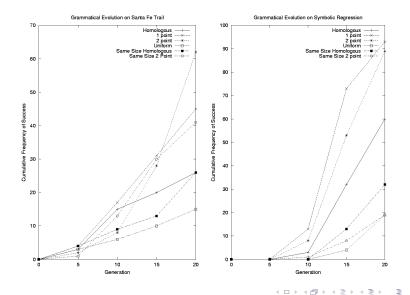
Homologous Crossover - Second Point

• Choose second point outside of area of similarity



Genetic Operators Alternative Crossovers

Crossover comparisons (Cumulative Freq. Success)

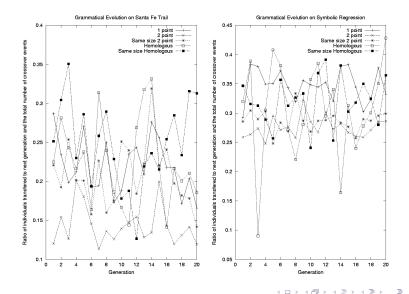


(University of Limerick)

Grammatical Evolution

8th July 2006 43 / 81

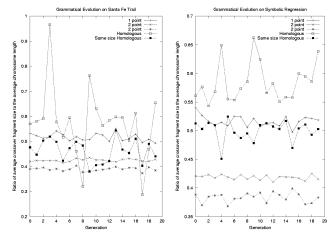
Productivity of Operators (Ratio of successes)



(University of Limerick)

8th July 2006 44 / 81

Relative size of crossover fragments

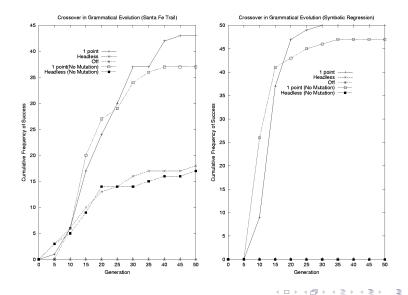


Ratio of the average fragment size being swapped and the average chromosome length at each generation averaged over 20 runs.

Headless Chicken - Crossover or Macromutation

- Appears Crossover works
- 50% material exchange with 1-point over entire runs
- If useful material exchanged then swapping random fragments should degrade performance?

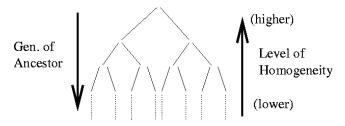
Headless Chicken Comparison



Explanation

Why does crossover work?

- Take a cue from GP crossover The "Eve" Effect :
 - All individuals in the final generation tend to evolve from the same ancestor



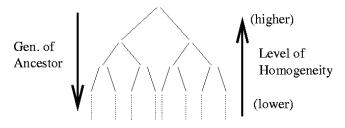
→ Ξ → +

4 A 1

Explanation

Why does crossover work?

- Take a cue from GP crossover The "Eve" Effect :
 - All individuals in the final generation tend to evolve from the same ancestor

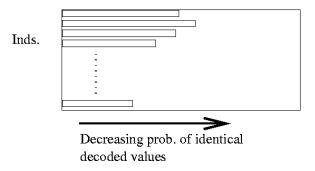


 The upper parts of individuals tend to come from the same individual

(University of Limerick)

GE View of Eve Effect?

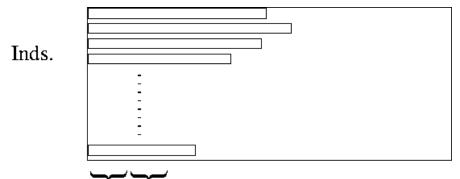
• Individuals grow from left to right



- 同ト - ヨト - ヨ

Size of region of similarity increases over time

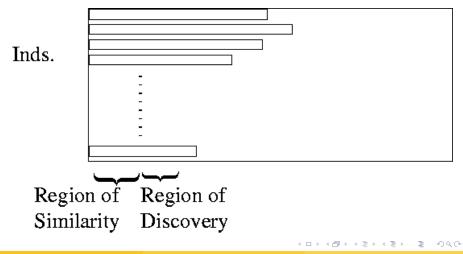
Area immediately beyond region of similarity is "region of discovery":



Region of Region of Similarity Discovery

Size of region of similarity increases over time

Area immediately beyond region of similarity is "region of discovery":

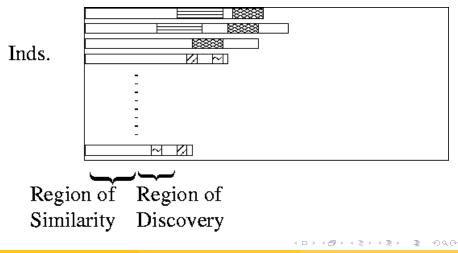


(University of Limerick)

8th July 2006 50 / 81

Size of region of similarity increases over time

Area immediately beyond region of similarity is "region of discovery":



The GAuGE System

Genetic Algorithms using Grammatical Evolution

Purpose:

- Position independent genetic algorithm;
- No under- or over-specification;
- Independent of search engine.

Based on mapping process (similar to GE):

- Specify position and value of each variable at genotypic level;
- Map genotype strings into functional phenotype strings.

4 A 1 1 4

The GAuGE System

Genetic Algorithms using Grammatical Evolution

Purpose:

- Position independent genetic algorithm;
- No under- or over-specification;
- Independent of search engine.

Based on mapping process (similar to GE):

- Specify position and value of each variable at genotypic level;
- Map genotype strings into functional phenotype strings.

Transform binary string into integer string:

- Problem has 4 variables ($\ell = 4$), with range 0...7;
- Choose position field size (pfs = 2);
- Choose value field size (vfs = 4);
- Calculate binary string length:

$$L = (pfs + vfs) \times \ell = (2+4) \times 4 = 24$$
 bits

< ロト < 同ト < ヨト < ヨト

Transform binary string into integer string:

- Problem has 4 variables ($\ell = 4$), with range 0...7;
- Choose position field size (pfs = 2);
- Choose value field size (vfs = 4);

• Calculate binary string length:

 $L = (pfs + vfs) \times \ell = (2+4) \times 4 = 24$ bits

Transform binary string into integer string:

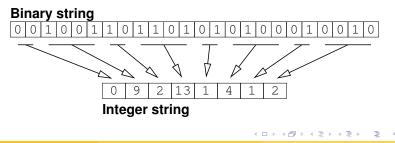
- Problem has 4 variables ($\ell = 4$), with range 0...7;
- Choose position field size (pfs = 2);
- Choose value field size (vfs = 4);
- Calculate binary string length:

$$L = (pfs + vfs) \times \ell = (2 + 4) \times 4 = 24$$
 bits

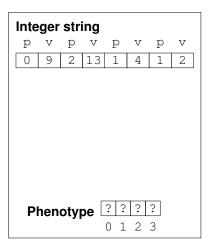
Transform binary string into integer string:

- Problem has 4 variables ($\ell = 4$), with range 0...7;
- Choose position field size (pfs = 2);
- Choose value field size (vfs = 4);
- Calculate binary string length:

$$L = (pfs + vfs) \times \ell = (2 + 4) \times 4 = 24$$
 bits



Calculating Phenotype

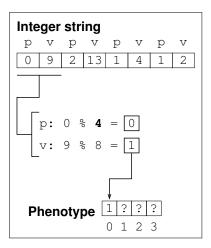


(University of Limerick)

3

Mapping

Calculating Phenotype

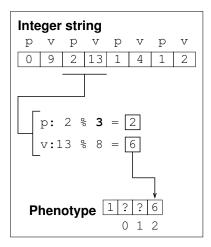


(University of Limerick)

3

Mapping

Calculating Phenotype



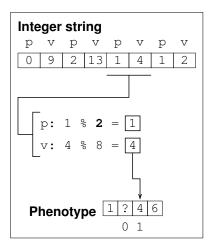
(University of Limerick)

8th July 2006 55 / 81

3

Mapping

Calculating Phenotype

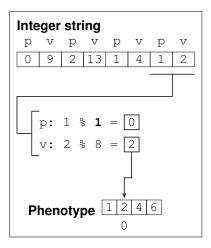


(University of Limerick)

8th July 2006 56 / 81

3

The GAuGE System



(University of Limerick)

3

Where is Gauge useful?

- GAuGE adapts the representation to the problem
 - Useful where interactions between genes not known
- GAuGE is cheap
 - Far less complicated than algorithms that try to model gene interactions/relationships
- GAuGE discovers saliency
 - Most important genes end up on left side of strings



- Mapping Independent Codons no ripple effect
- Codon % Total number of rules in the grammar
- Competition between the Genes
- Concentration Table
- Variable length binary strings
- 8 bit codons

Grammar specification

```
S= <expr>
(0)
    <expr> ::= <expr> <op> <expr>
(1)
   ( <expr> <op> <expr> )
(2)
     <pre-op> ( <expr> )
(3)
      <var>
(4) <op> ::= +
(5)
(6)
      *
(7)
(8)
   <pre-op>::= Sin
(9)
      Cos
(A)
      Exp
(B)
      Loq
(C) <var> ::= 1.0
(D)
    X
```

3

Mapping - 1

Four non-terminals:

 $\bullet \ <\!expr\!> 0..3, <\!op\!> 4..7, <\!pre-op\!> 8..B, <\!var\!> C..D$

209 102 190 55 65 15 255 87 D 4 8 D 9 1 3 3

 0
 1
 2
 3
 4
 5
 6
 7
 8
 9
 A
 B
 C
 D

 <e>
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0

3

Mapping - 2

Four non-terminals:

• <expr> 0..3, <op> 4..7, <pre-op> 8..B, <var> C..D

209 102 190 55 65 15 255 87 D 4 8 D 9 1 3 3

イロト イポト イヨト 一日

Mapping - 3

Four non-terminals:

• <expr> 0..3, <op> 4..7, <pre-op> 8..B, <var> C..D

209 102 190 55 65 15 255 87 D 4 8 D 9 1 <mark>3</mark> 3

6 7 Α В С D $\langle e \rangle$ 1 0 0 0 1 0 2 0 0 0 <e><0><e> <v><o>e>

(University of Limerick)

Four non-terminals:

• <expr> 0..3, <op> 4..7, <pre-op> 8..B, <var> C..D

209 102 190 55 65 15 255 87 D 4 8 D 9 1 <u>3</u> 3

	0	1	2	3	4	5	6	7	8	9	А	В	C	D
													0	
<e><0><e></e></e>	0	0	0	0	1	0	0	0	1	1	0	0	0	2
<v><0><e></e></v>	0	0	0	0	1	0	0	0	1	1	0	0	0	2
X <o><e></e></o>														

▲□▶ ▲圖▶ ▲ 臣▶ ▲ 臣▶ ― 臣 … の々(?)

Four non-terminals:

• <expr> 0..3, <op> 4..7, <pre-op> 8..B, <var> C..D

209 102 190 55 65 15 255 87 D 4 8 D 9 1 <u>3</u> 3

	0	1	2	3	4	5	6	7	8	9	А	В	C	D
<e></e>	0	0	0	0	0	0	0	0	0	0	0	0	0	0
<e><0><e></e></e>	0	0	0	0	1	0	0	0	1	1	0	0	0	2
<v><0><e></e></v>	0	0	0	0	1	0	0	0	1	1	0	0	0	2
X < o > < e >	0	0	0	0	1	0	0	0	1	1	0	0	0	1
X+ <e></e>	0	0	0	0	0	0	0	0	1	1	0	0	0	1

▲□▶ ▲圖▶ ▲ 臣▶ ▲ 臣▶ ― 臣 … の々(?)

Four non-terminals:

 $\bullet \ <\!expr\!> 0..3, <\!op\!> 4..7, <\!pre-op\!> 8..B, <\!var\!> C..D$

209 102 190 55 65 15 255 87 D 4 8 D 9 1 3 3

	0	1	2	3	4	5	6	7	8	9	А	В	C	D
<e></e>	0	0	0	0	0	0	0	0	0	0	0	0	0	0
<e><0><e></e></e>	0	0	0	0	1	0	0	0	1	1	0	0	0	2
<v><0><e></e></v>	0	0	0	0	1	0	0	0	1	1	0	0	0	2
X <o><e></e></o>	0	0	0	0	1	0	0	0	1	1	0	0	0	1
X+ <e></e>	0	0	0	0	0	0	0	0	1	1	0	0	0	1
X+ <v></v>	0	0	0	0	0	0	0	0	1	1	0	0	0	1

▲ロ▶ ▲周▶ ▲ヨ▶ ▲ヨ▶ - ヨ - めぬゆ

Four non-terminals:

 $\bullet \ <\!\!expr\!> 0..3, <\!\!op\!> 4..7, <\!\!pre\text{-}op\!> 8..B, <\!\!var\!> C..D$

209 102 190 55 65 15 255 87 D 4 8 D 9 1 3 <u>3</u>

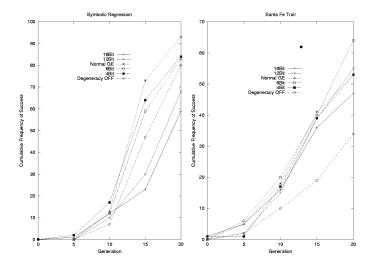
	0	1	2	3	4	5	6	7	8	9	А	В	С	D
<e></e>	0	0	0	0	0	0	0	0	0	0	0	0	0	0
<e><0><e></e></e>	0	0	0	0	1	0	0	0	1	1	0	0	0	2
<v><0><e></e></v>	0	0	0	0	1	0	0	0	1	1	0	0	0	2
X <o><e></e></o>	0	0	0	0	1	0	0	0	1	1	0	0	0	1
X+ <e></e>	0	0	0	0	0	0	0	0	1	1	0	0	0	1
X+ <v></v>	0	0	0	0	0	0	0	0	1	1	0	0	0	1
X+X	0	0	0	0	0	0	0	0	1	1	0	0	0	0

▲□▶ ▲圖▶ ▲ 臣▶ ▲ 臣▶ ― 臣 … の々(?)

Degeneracy Pe

Performance

Cumulative Freq. with and without degeneracy



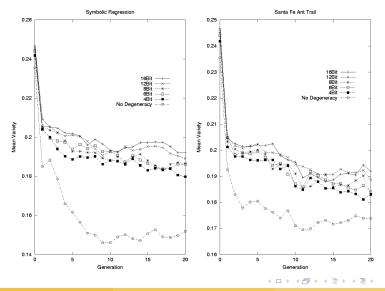
• No huge difference : Normal, 4- and 6-bit top three in both

(University of Limerick)

Degeneracy

Variety

Mean Variety - Any degeneracy helps!



(University of Limerick)

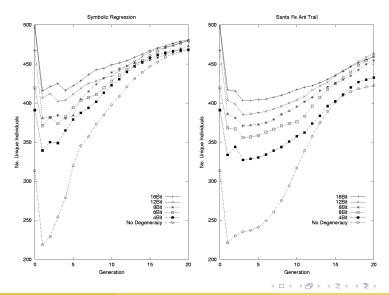
Grammatical Evolution

8th July 2006 69 / 81

Sac

Variety

Unique Individuals



(University of Limerick)

Grammatical Evolution

æ 8th July 2006 70/81

DQC

Conclusions

Conclusions:

- Improves genetic diversity
- Improves frequency of success on Santa Fe ant trail
- Tuneable/Evolvable Degeneracy a good idea?

- 同ト - ヨト - ヨ

Number of individuals wrapped

• Wrap Count & Invalid Individuals

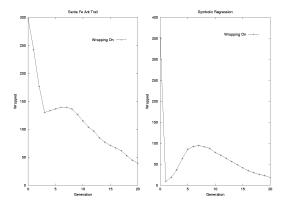


Figure: Number of individuals wrapped on the symbolic regression and Santa Fe trail problems.

(Universit	y of Limerick)
Conversit	y of Linenck)

∃ ⊳

Wrapping Number of individuals wrapped

Wrapping and Invalid Individuals

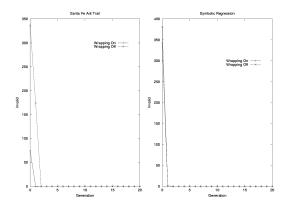


Figure: The number of invalid individuals for each generation in the presence and absence of wrapping.

			0			

∃ ► 4 Ξ

I > <
 I >
 I

Performance

Freq. of Success

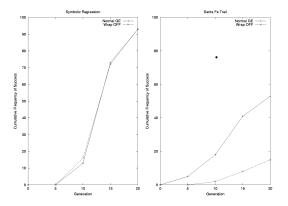


Figure: Figure shows the cumulative frequency of success measures on both problems with and without the presence of wrapping.

	4	□►	< ⊡ >	$\in \Xi \rightarrow$	< ≣ >	3	$\mathcal{O} \land \mathcal{O}$
(University of Limerick)	Grammatical Evolution			8th	July 2006	6	74 / 81

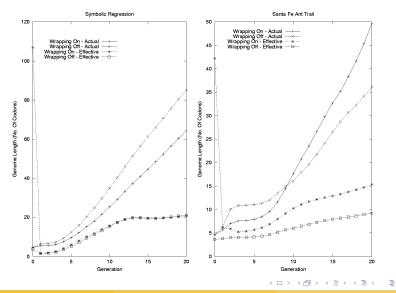
Lengths (Some Definitions)

- Actual length
 - Entire length of individual
- Effective length
 - Number of codons used
 - (Note! Can be less than or greater than actual length)

< 回 ト < 三 ト < 三

Wrapping Genome Lengths

Genome Lengths



(University of Limerick)

Grammatical Evolution

8th July 2006 76 / 81



- For SR (left) wrapping off has the longest actual length
- Effective length virtually the same
- For SF (right) wrapping on longer in both cases.
- Conclusions:
 - Wrapping improves frequency of success on Santa Fe ant trail
 - No effect on Symbolic Regression cumulative frequency
 - Provides some constraint on genome lengths

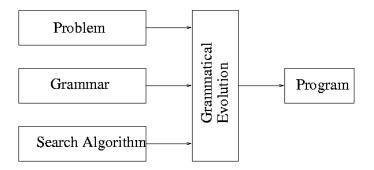
< ロト < 同ト < ヨト < ヨト

Wrapping & Degeneracy

- Removing both....
 - Cumulative frequency of success degrades
 - Genome lengths increase over 60% on Symbolic Regression
 - Genetic diversity no worse than without degeneracy alone

Other Algorithms

Search Techniques



• Other techniques

- Simulated Annealing
- Hill Climbing
- Random Search

э

Sac

∃ >

Comparison

• Three standard GP problems

- Santa Fe trail
- Symbolic Integration (integrate Cos(x) + 2x + 1)
- Symbolic regression $x^4 + x^3 + x^2 + x$

	Metaheuristic								
Problem	RS	HC	SA	GA					
Santa Fe	54%	7%	14%	81%					
Symbolic Integration	66%	4%	3%	100%					
Symbolic Regression	0%	0%	0%	59%					

The Future

- The Grammar (Attribute Grammars)
- Search & Evolutionary Dynamics
- Applications
- Newest Code Release
 - http://waldo.csisdmz.ul.ie/libGE/

< ロト < 同ト < ヨト < ヨト