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Alternative Methods of Evaluating and Achieving Progressive Collapse Resistance

National Steel Construction Conference

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Simpson Gumpertz & Heger Inc.
Consulting Engineers
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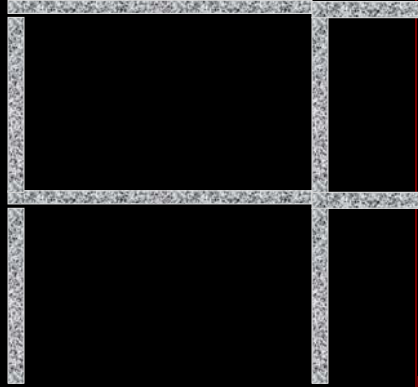
What is Progressive Collapse?

- A small, localized initiating event
- leads to a chain of failures
- resulting in large scale failure and collapse

- Since nearly all collapse is progressive in nature
- Any structure will collapse if subjected to a sufficiently large event
- Design goal is to prevent small events from initiating large scale failures
 - "disproportionate failure"

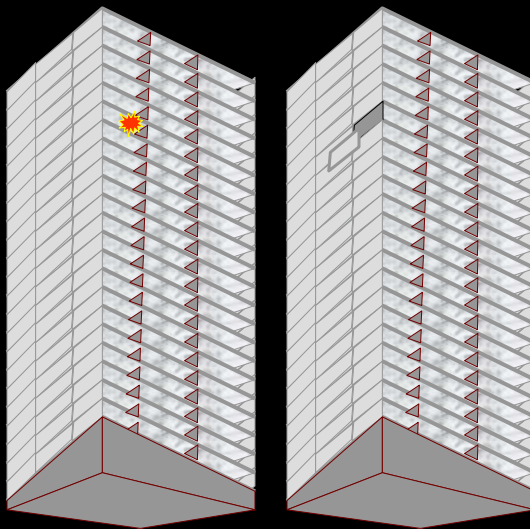
Ronan Point - 1968

- 23 story apartment building in London
- Precast concrete panel construction



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Ronan Point - 1968



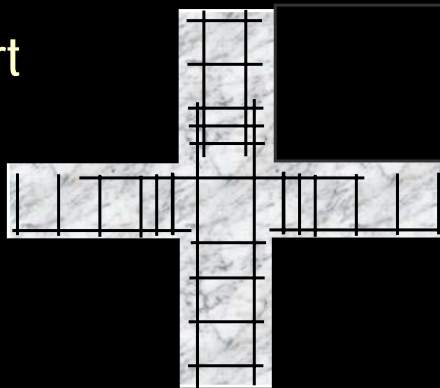
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Alfred P. Murrah Building



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ASCE Report



- Incorporation of seismic detailing would have provided the Murrah Building with greater resistance to the progression of collapse
 - Continuity of reinforcing
 - Confinement of members for ductility

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Steel Moment Frames are an Excellent System for Arresting Collapse



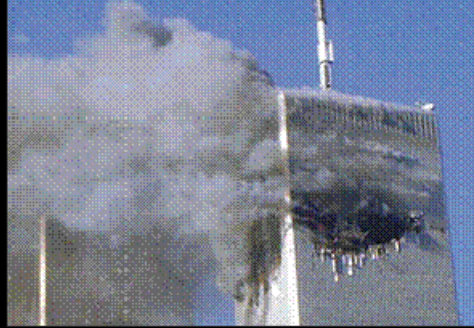
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Steel Moment Frames are an Excellent System for Arresting Collapse



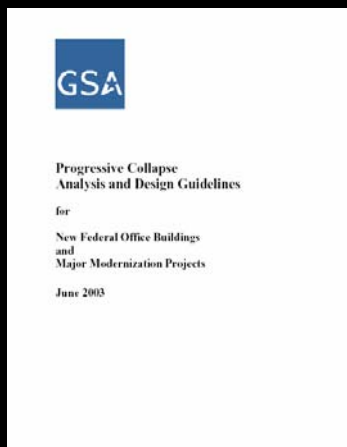
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Steel Moment Frames are an Excellent System for Arresting Collapse



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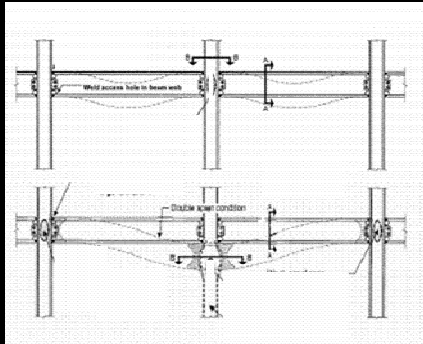
Design Criteria for Progressive Collapse



- Provide frame redundancy & continuity
- Evaluate adequacy of continuous framing for column removal condition
 - Linear static procedure
 - Nonlinear static procedure
 - Nonlinear dynamic procedure

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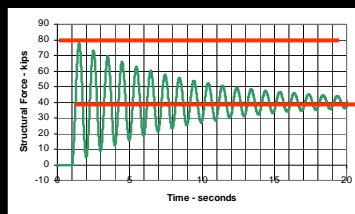
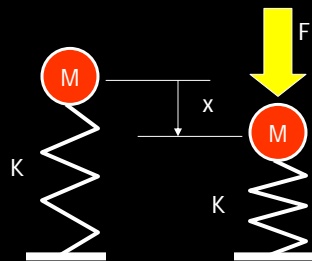
Linear Static Procedure



- Structure evaluated for element removal
 - Demand taken as:
 - $2(D+0.25L)$
 - Capacity taken as ZF_{ye}
 - Demand/Capacity Ratios evaluated against acceptable values from seismic guidelines (FEMA 356)
 - Compact sections – 3
 - Noncompact sections - 2

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Basis



- Structure evaluated for element removed
 - Demand taken as:
 - $2(D+0.25L)$
 - Basis:
 - Expected load actually present is dead load D and 25% of live load L
 - Peak deflection and stress on an elastic, lightly damped structure is twice the static value
 - Presumption is made that this is a conservative bound on collapse behavior

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Basis

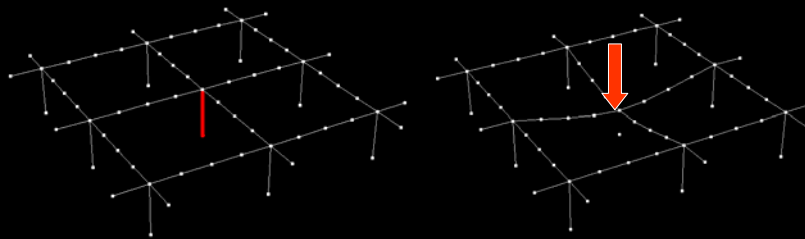
Component/Action	Values for Linear Procedures	
	DCR	
Beams - flexure		
a. $\frac{M_u}{\phi_b F_y S_x} \leq \frac{M_n}{\phi_b F_y S_x}$ and $\frac{M_u}{\phi_b F_y S_x} \leq \frac{M_n}{\phi_b F_y S_x}$	3	3
b. $\frac{M_u}{\phi_b F_y S_x} \leq \frac{M_n}{\phi_b F_y S_x}$ or $\frac{M_u}{\phi_b F_y S_x} \leq \frac{M_n}{\phi_b F_y S_x}$	2	2
c. Other	Linear interpolation between the values on lines a and b for both Range and Demand (first term) and web slenderness (second term) shall be performed, and the lowest resulting value shall be used.	
Columns - flexure		
For $\phi_c \geq 0.8$		
a. $\frac{M_u}{\phi_c F_y S_x} \leq \frac{M_n}{\phi_c F_y S_x}$ and $\frac{M_u}{\phi_c F_y S_x} \leq \frac{M_n}{\phi_c F_y S_x}$	2	
b. $\frac{M_u}{\phi_c F_y S_x} \leq \frac{M_n}{\phi_c F_y S_x}$ or $\frac{M_u}{\phi_c F_y S_x} \leq \frac{M_n}{\phi_c F_y S_x}$	1.25	
c. Other	Linear interpolation between the values on lines a and b for both Range and Demand (first term) and web slenderness (second term) shall be performed, and the lowest resulting value shall be used.	

■ Demand – capacity ratios obtained from FEMA 356

- Intended to represent modestly conservative estimates of ductility available in elements under seismic loading
- Presumption is made that similar ductility is available under collapse conditions

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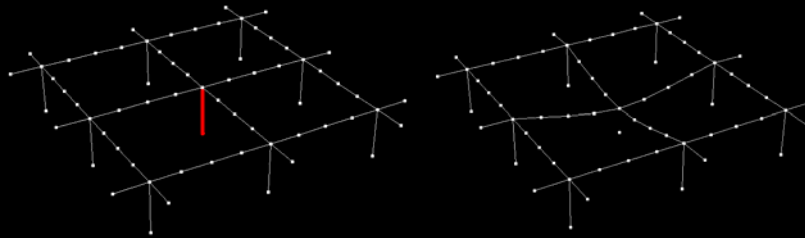
Nonlinear Static Procedure



- Structure modeled with removed element “missing”
- Gravity load pattern applied and scaled to produce first yield
- Model modified to reflect yield hinge
- Load incremented until next hinge predicted
- Process repeated until mechanism forms or $2(D + .25L)$ resisted
- Maximum ductility demands evaluated against seismic capacities
 - Plastic rotations comparable to linear acceptance criteria

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Nonlinear Dynamic Procedure

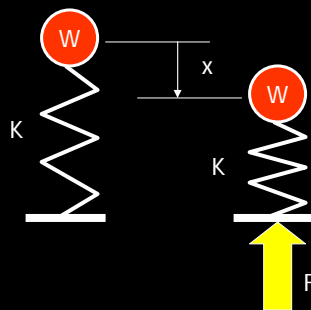


- Structure modeled
- Element removed
- Nonlinear time history analysis performed to determine response
- Maximum ductility demands evaluated against seismic capacities
 - Catenary tensile behaviors can be accounted for
 - Plastic rotations comparable to linear acceptance criteria

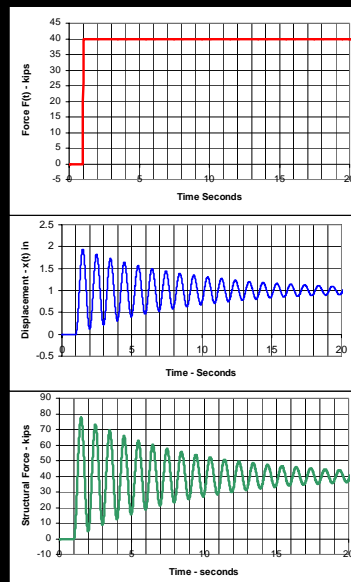
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Problems with linear method

- "Impact" load increase value of 2 is based on elastic behavior

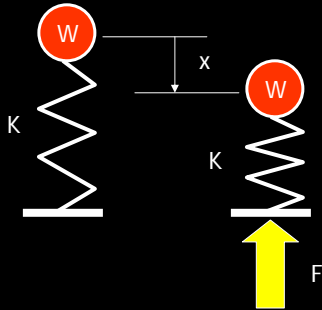


Linear Behavior
 $W = 40k$ $F_{max} = 80k$

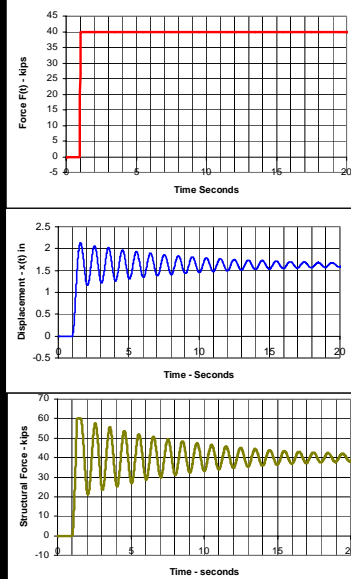


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Is Impact Factor of 2 Appropriate?

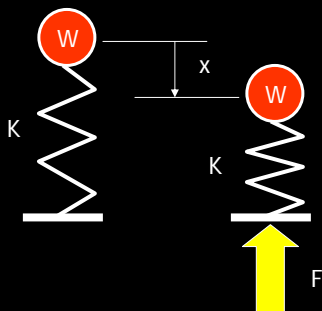


Mild Non-Linear Behavior
 $W=40k$, $F_y=60k$
 $SR=60/40=1.5$

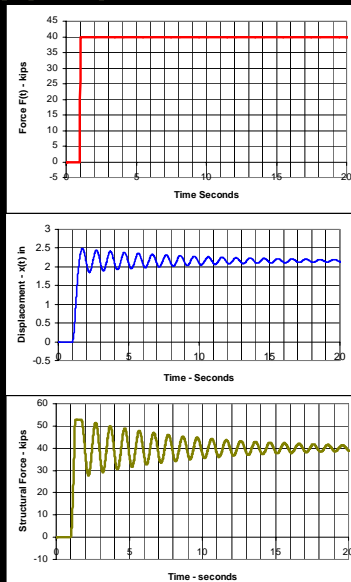


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Is Impact Factor of 2 Appropriate?

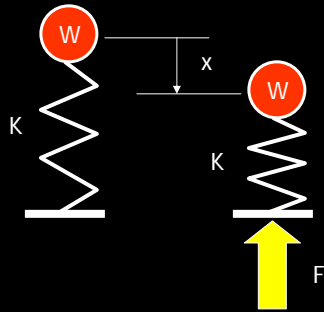


Mild Non-Linear Behavior
 $W=40$, $F_y=53k$,
 $SR=53/40=1.33$

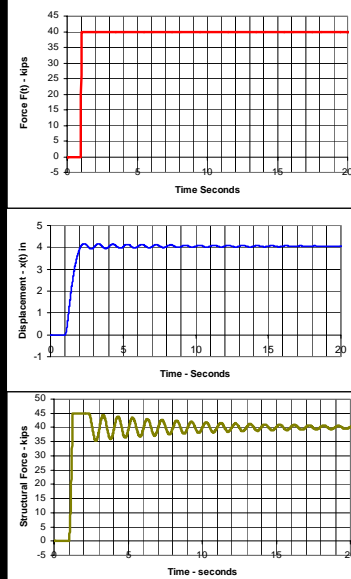


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Is Impact Factor of 2 Appropriate?

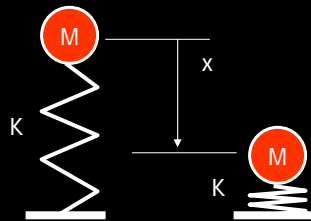


Mild Non-Linear Behavior
 $W=40k$, $F_y=45k$
 $SR=45/40=1.13$

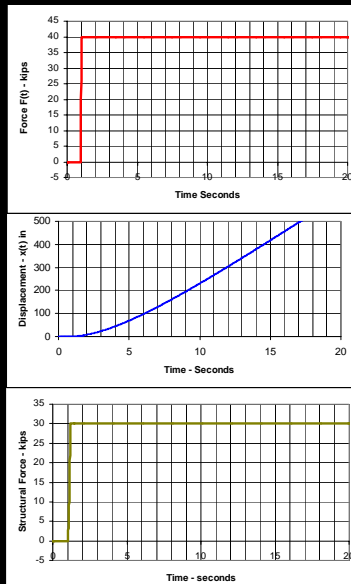


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Is Impact Factor of 2 Appropriate?

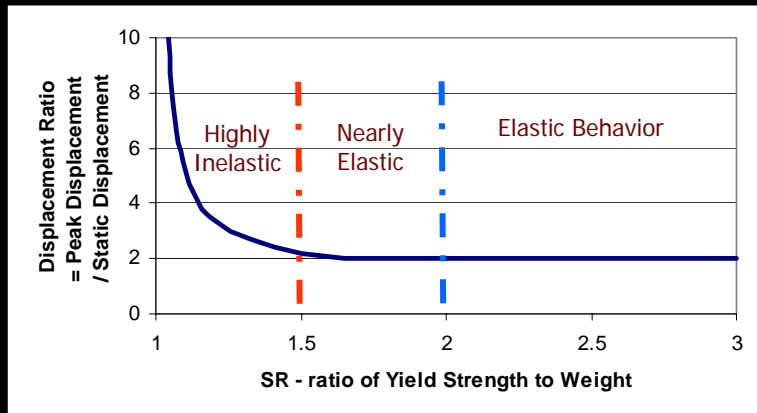


Significant Nonlinear Behavior
 $SR \leq 1$



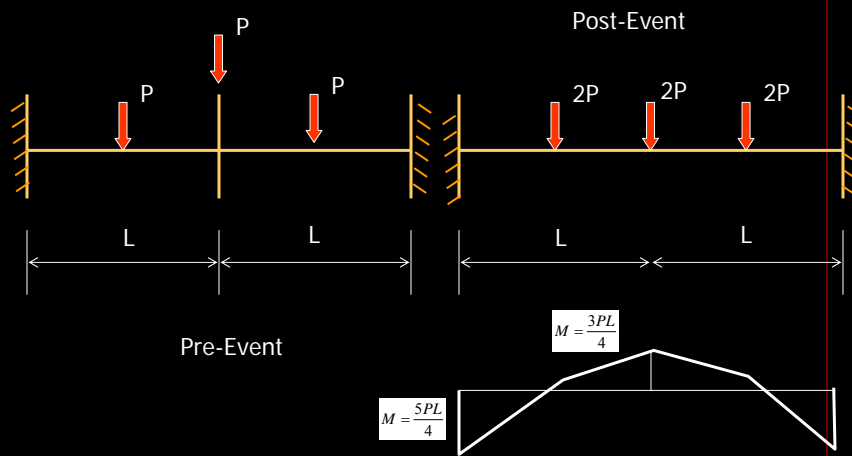
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Displacement & Strength Ratios



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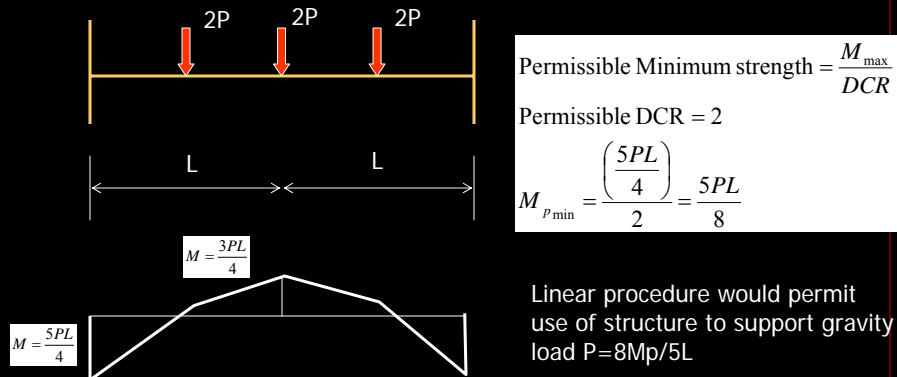
Linear Procedures Can Result in Structures that are too weak



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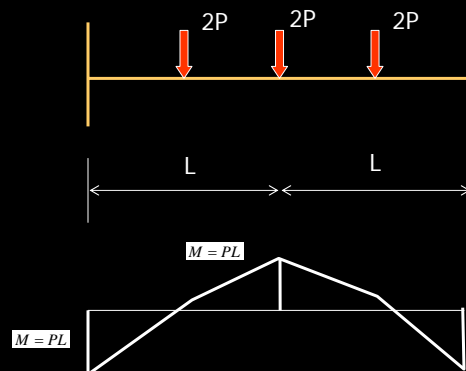
Linear Procedures Can Result in Structures that are too weak

Post-Event



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Linear Procedures Can Result in Structures that are too weak



Fully plastic condition achieved at $P=M_p/L$

Value of $P=8M_p/5L$ has strength ratio of $5/8$ and would collapse

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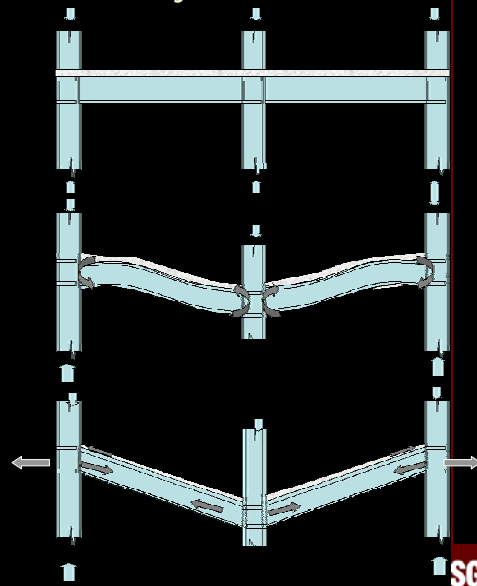
Nonlinear static procedure is also incorrect

- Impact factor of 2 is excessively conservative when nonlinear behavior is directly accounted for

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Neither Procedure Accounts for Catenary Behavior

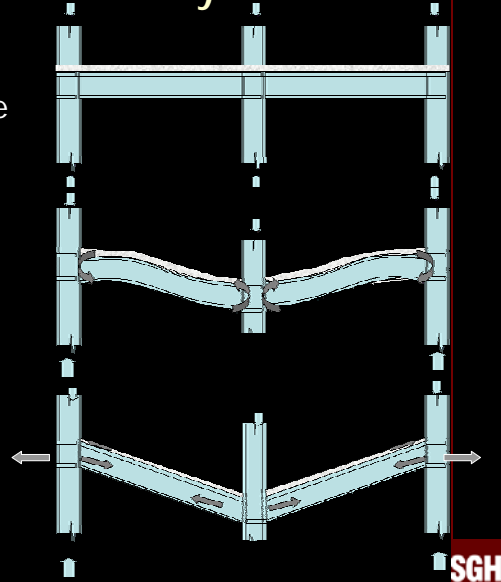
- Following development of full plastic flexural capacity of framing, beams fall into large deflection and catenary tensile behavior may develop, greatly increasing plastic capacity



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Catenary Behavior Will Not Always Work

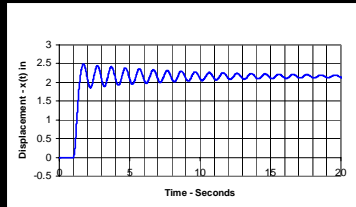
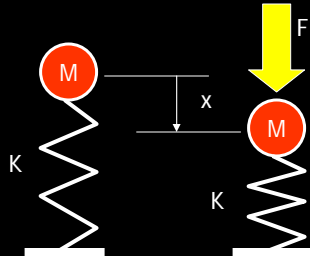
- Can not develop unless structure can resist large tensile forces that develop at edge of collapsed area
- Behavior is not predictable by linear methods of analysis
- Catenary behavior typically can not be developed effectively at building edges and corners



Energy-based Pushdown Analysis Procedure

- Adapted from pushover procedures currently used in earthquake engineering
- Can be performed as a series of sequential linear analyses
- Cannot account for catenary behavior
- Can more realistically model plastic flexural behavior of structure and ability to arrest collapse than linear methods

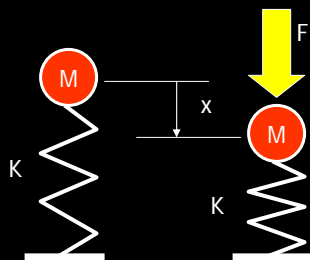
Base Theory



- As a mass supported by a spring (or damaged structure) drops under the action of gravity forces:
 - Mass loses potential energy (PE)
 - Mass gains kinetic energy (KE)
 - Spring gains strain energy (SE)
- At any instant of time (t)
 - $KE = PE - SE$
- As long as kinetic energy continues to increase, mass continues to fall
- If kinetic energy becomes negative (stored strain energy exceeds loss in potential energy) this indicates mass has reversed direction of travel and begun safe oscillation

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Base Theory

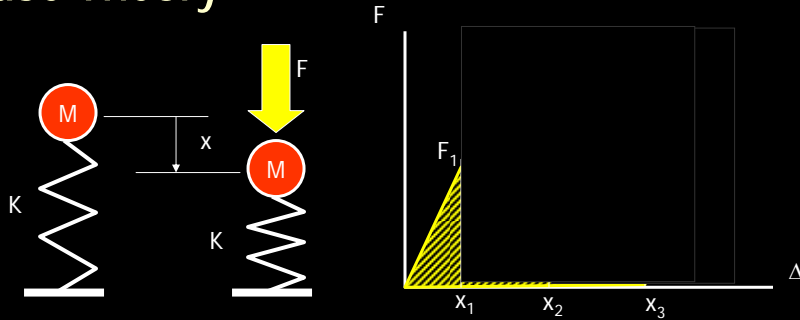


- At displaced position, x the potential energy lost by the falling mass is given by:

$$PE = Wx = Mgx$$

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Base Theory



- At any displaced position x_i , strain energy is given by the area under the force – displacement curve

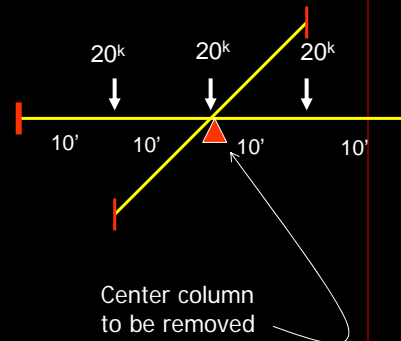
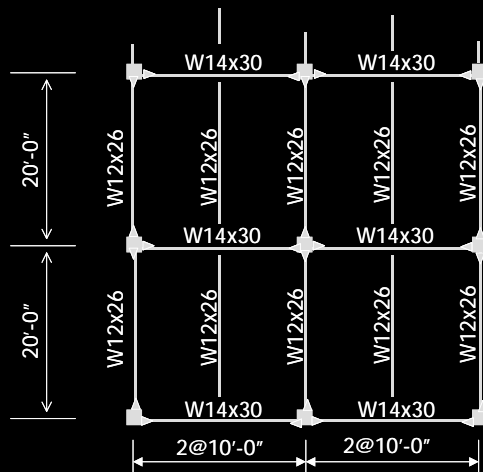
$$SE_1 = \frac{F_1 x_1}{2}$$

$$SE_2 = SE_1 + \frac{1}{2}(F_1 + F_2)(x_2 - x_1)$$

$$SE_3 = SE_2 + \frac{1}{2}(F_2 + F_3)(x_3 - x_2)$$

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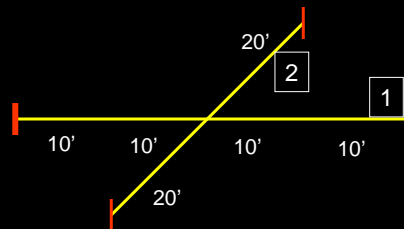
Illustration of Procedure Using Simple Structure



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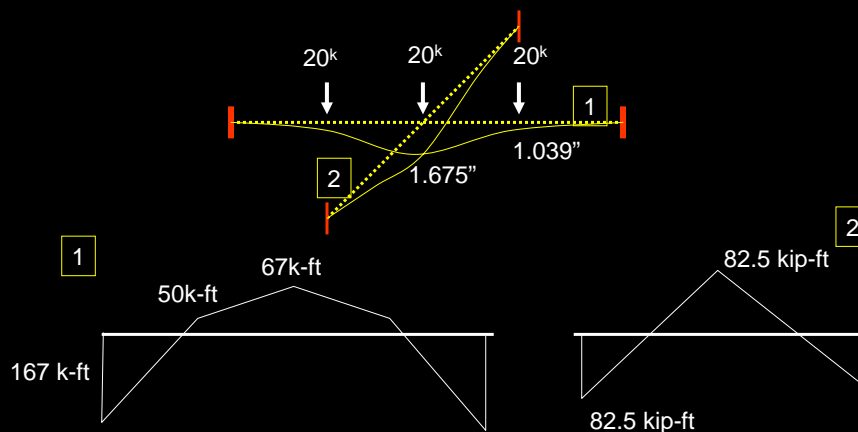
Procedure

1. Develop elastic model of structure, with "damaged" element removed



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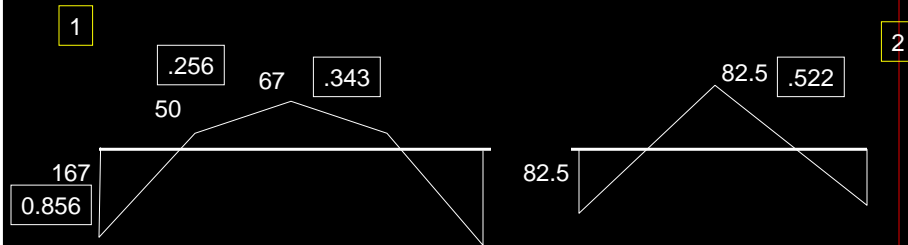
2. Apply weight W ($D + .25 L$) to model, calculate forces in all the elements and deflections at all loads



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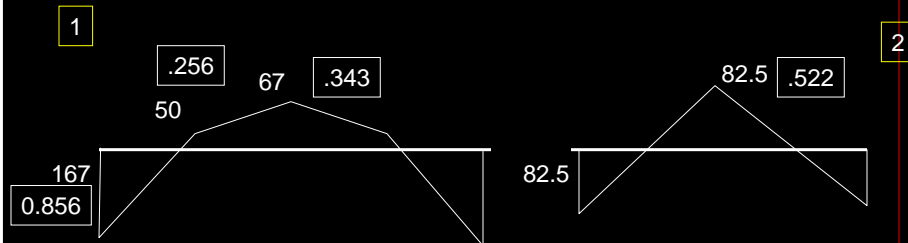
3. Calculate Demand to Capacity Ratios (DCRs) for all elements

W14x30 $M_p = 195$ kip-ft, W12x26 $M_p = 158$ kip-ft



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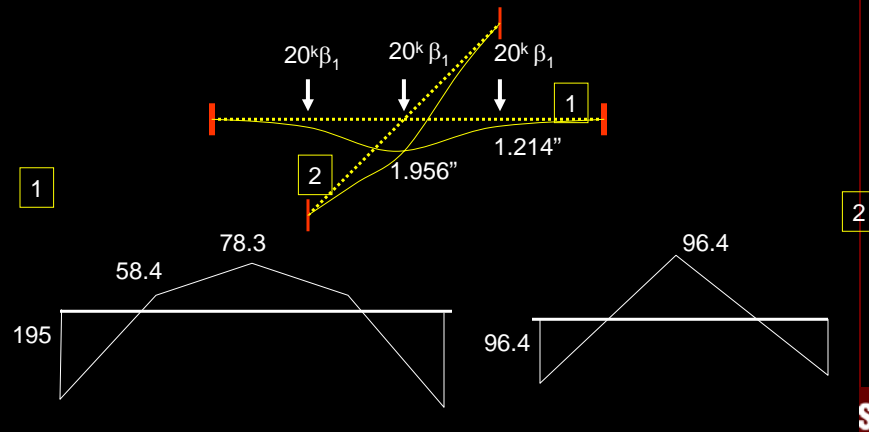
4. Find the factor on the applied static loading W that causes first yielding of structure as $\beta_1 = 1/DCR_{max}$



$$\beta_1 = 1/0.856 = 1.168$$

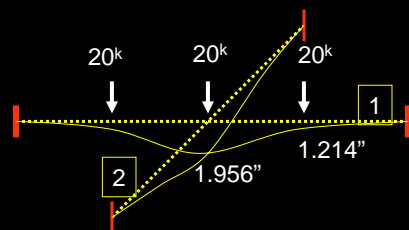
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5. Find the forces in all elements, and the deflections under all loads at applied load $\beta_1 W$



6. Calculate the total loss in Potential Energy as the structure deflects to a position β_1 times the static deflection under weight W

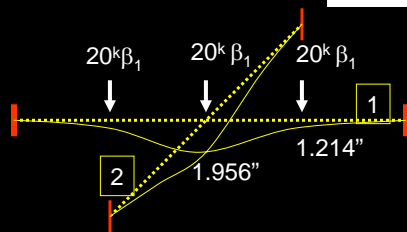
$$PE_1 = \sum_{i=1}^n W_i \Delta_i$$



Node "I"	W _i	Δ _i	W _i Δ _i
1	20	1.214	24.28 kip-in
2	20	1.956	39.12 kip-in
3	20	1.214	24.28 kip-in
Total			87.68 kip-in

7. Calculate the total gain in Strain Energy as the structure deflects to a position β_1 times the static deflection under weight W

$$SE_1 = \frac{1}{2} \sum_{i=1}^n \beta_1 W_i \Delta_i$$



Node "I"	$\beta_1 W_i$	Δ_i	$0.5 W_i \Delta_i$
1	23.36	1.214	14.18 kip-in
2	23.36	1.956	22.85 kip-in
3	23.36	1.214	14.18 kip-in
Total			51.21 kip-in

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8. Perform energy balance to determine Kinetic Energy

$$KE_1 = PE_1 - SE_1$$

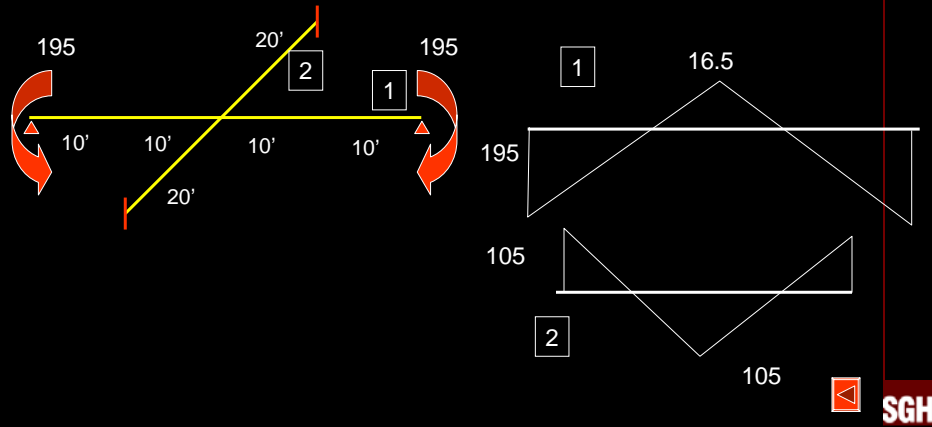
$$KE_1 = 87.68 - 51.21$$

$$KE_1 = 36.47 \text{ kip-in}$$

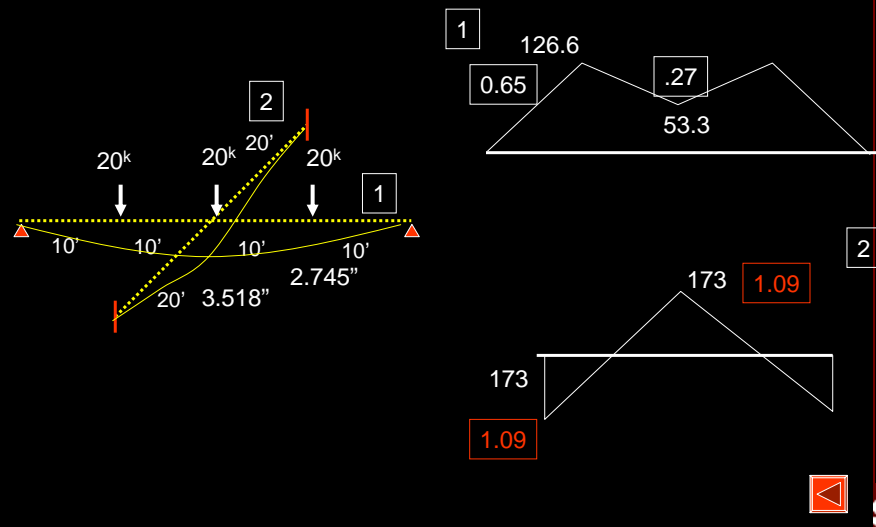
Conclusion: Kinetic energy is positive, structure has not been able to arrest collapse at deflection of β_1 times static deflection of structure under weight

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9. Place releases in model at point(s) where yielding occurs under $\beta_1 W$ forces. Apply plastic capacity of structure at this point(s) to represent yielding behavior of structure. Calculate forces, F_{1i} .



10. Calculate forces and DCRs in "released" model with applied load W

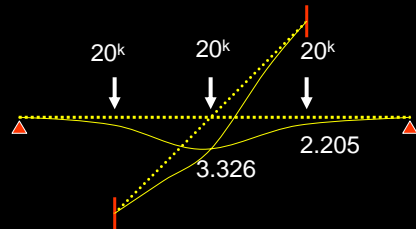


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13. Calculate potential energy lost at this applied deflection

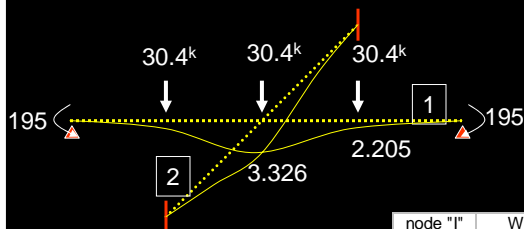
$$PE_2 = \sum_{i=1}^n W_i \Delta_i$$



Node "I"	W _i	Δ _i	W _i Δ _i
1	20	2.205	44.1 kip-in
2	20	3.326	66.52 kip-in
3	20	2.205	44.1 kip-in
Total			154.72 kip-in

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14. Calculate Strain Energy gained at this applied deflection



$$SE_2 = SE_1 + \frac{\beta_1 + \beta_2}{2} \sum_{i=1}^n W_i (x_2 - x_1)$$

node "I"	W _i	Δ _{2i}	Δ _{1i}	W _i (Δ _{2i} -Δ _{1i})
1	20	2.205	1.214	19.82 kip-in
2	20	3.326	1.956	27.4 kip-in
3	20	2.205	1.214	19.82 kip-in
Total				67.04 kip-in
	β ₁	1.168		
	β ₂	1.527		
SE1	51.21 kip-in			
SE2	141.55 kip-in			

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15. Compute Kinetic Energy at this displacement

$$KE_2 = PE_2 - SE_2$$

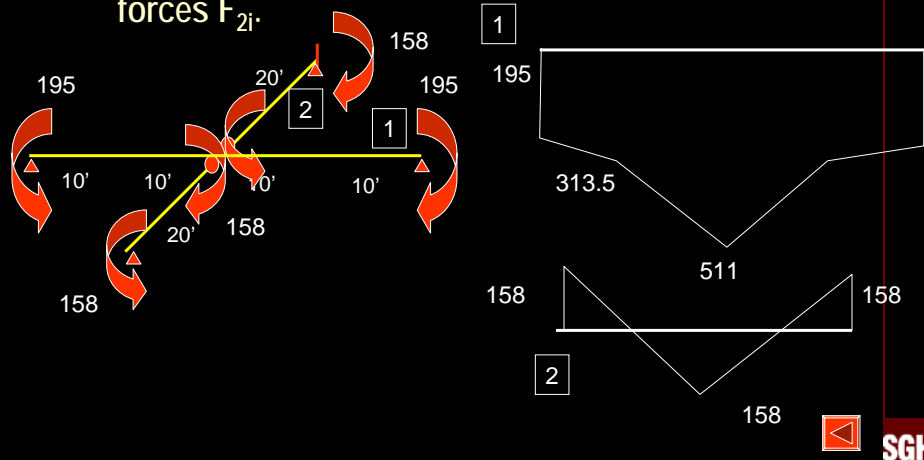
$$KE_2 = 154.72 - 141.55$$

$$KE_2 = 13.17 \text{ kip-in}$$

Conclusion: Kinetic energy is still positive, structure has not been able to arrest collapse at deflection of β_1 times static deflection of structure under weight

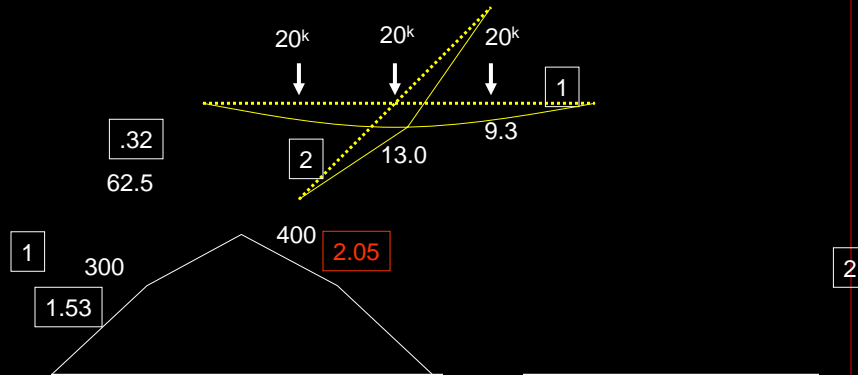
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16. Place releases in model at point(s) where yielding occurs under $\beta_2 W$ deflections. Apply plastic capacity of structure at yielded point(s). Calculate forces F_{2i} .



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17. Apply weight W to structure with all releases and calculate DCRs



18. Find the fraction of the deflection under static loading, W, that produces the next yield event in the structure, β_3 .

Where:

$$\beta_3 = \frac{1 - \frac{F_{2i}}{M_{pi}}}{DCR_{3i}} = \frac{1 - \frac{-511}{195}}{2.05} = 1.77$$

$DCR_{3i \max}$

Is the maximum DCR in the "released" structure under applied loading W (2.05)

"i"

Is the element degree of freedom at which this maximum DCR occurs

M_{pi}

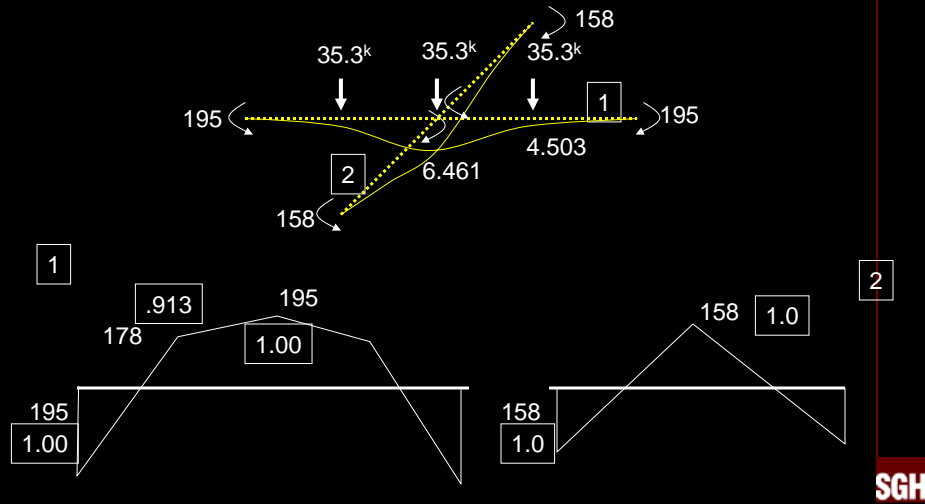
Is the plastic capacity of the structure at the degree of freedom with the maximum DCR (195 kip-ft)

F_{2i}

Is the force at the degree of freedom resulting from the application of prior release forces (511 kip-ft)

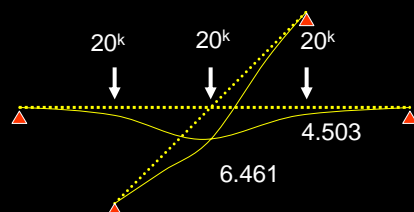


19. Evaluate structure for $\beta_3 W$ plus release forces, simultaneously applied



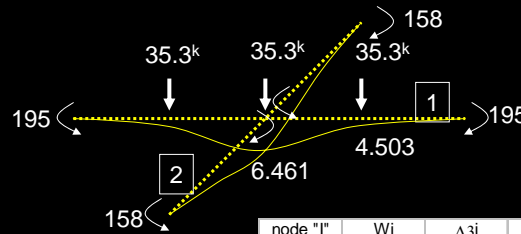
20. Calculate potential energy lost at this applied deflection

$$PE_3 = \sum_{i=1}^n W_i \Delta_i$$



Node "I"	W _i	Δ _i	W _i Δ _i
1	20	4.503	90.06 kip-in
2	20	6.461	129.22 kip-in
3	20	4.503	90.06 kip-in
Total			309.34 kip-in

21. Calculate Strain Energy gained at this applied deflection



$$SE_3 = SE_2 + \frac{\beta_2 + \beta_3}{2} \sum_{i=1}^n W_i (x_3 - x_2)$$

node "I"	Wi	$\Delta 3i$	$\Delta 2i$	$Wi(\Delta 3i - \Delta 2i)$
1	20	4.503	2.205	45.96 kip-in
2	20	6.461	3.326	62.7 kip-in
3	20	4.503	2.205	45.96 kip-in
Total				154.62 kip-in
	β_2	1.527		
	β_3	1.77		
SE2	141.55 kip-in			
SE3	396.44 kip-in			

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22. Compute Kinetic Energy at this displacement

$$KE_3 = PE_3 - SE_3$$

$$KE_2 = 309.34 - 396.44$$

$$KE_2 = -87.1 \text{ kip-in}$$



Conclusion: Kinetic energy is now negative, structure has been able to arrest collapse at a deflection less than β_3 times static deflection under the applied weight and initiate safe oscillation and damping out



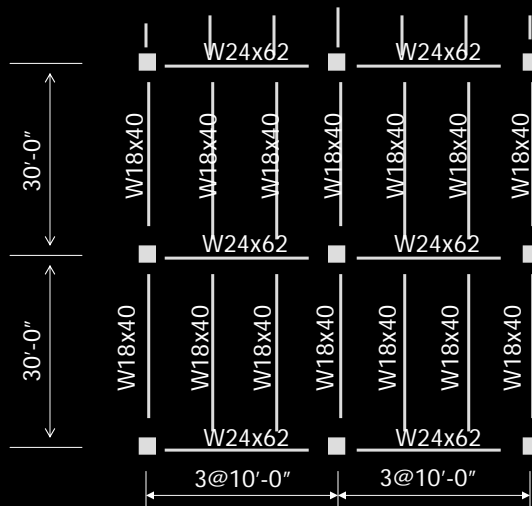
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Summary

- The same types of pushover techniques used in performance-based earthquake engineering can be used to more accurately characterize the risk of progressive collapse than standard linear procedures
- The procedure does not require sophisticated software
- It can not account for catenary action – nonlinear dynamic analysis is required to evaluate this effect

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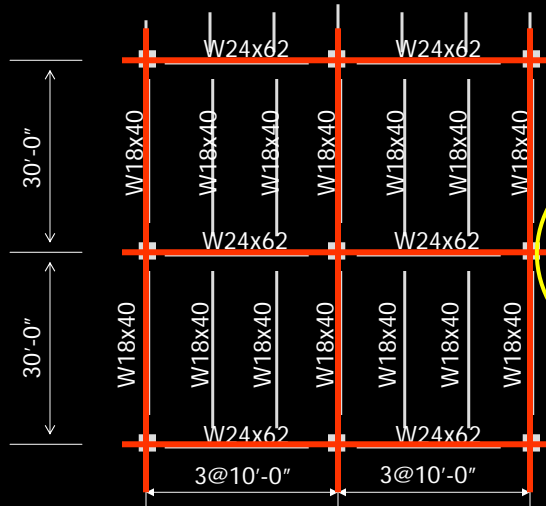
Does Design for Collapse Avoidance Add Substantial Cost?



- 50 psf live load
- 20 psf partition
- 5 psf mech & electrical
- 3" 20 gauge deck w/ 2-1/2" lightweight conc
- Steel designed non-composite, using LRFD
- 6 psf floor framing

SGH

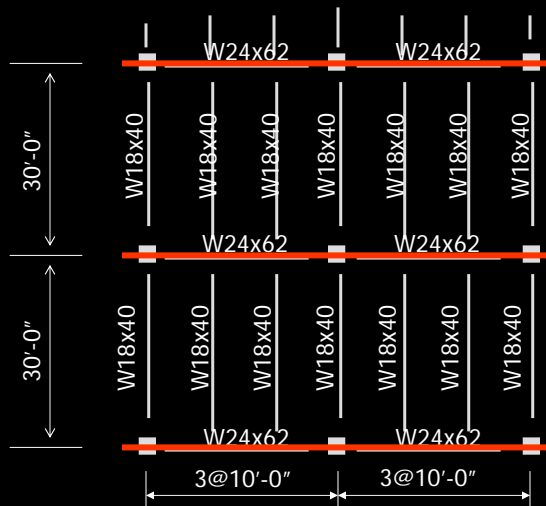
Does Design for Collapse Avoidance Add Substantial Cost?



- Moment-connect all beams and girders on column lines
- No change in member sizes
- Applying "pushdown" procedure – structure comes to rest after formation of hinges at girder ends, but before formation of any other hinges
- Conclusion – collapse avoidance can be achieved without weight increase but with significant additional connection costs

SGH

Does Design for Collapse Avoidance Add Substantial Cost?



- By observation:
 - Moment-connect girders only
 - No change in member sizes
- Conclusion – collapse avoidance can be achieved without weight increase but with some additional connection costs

SGH

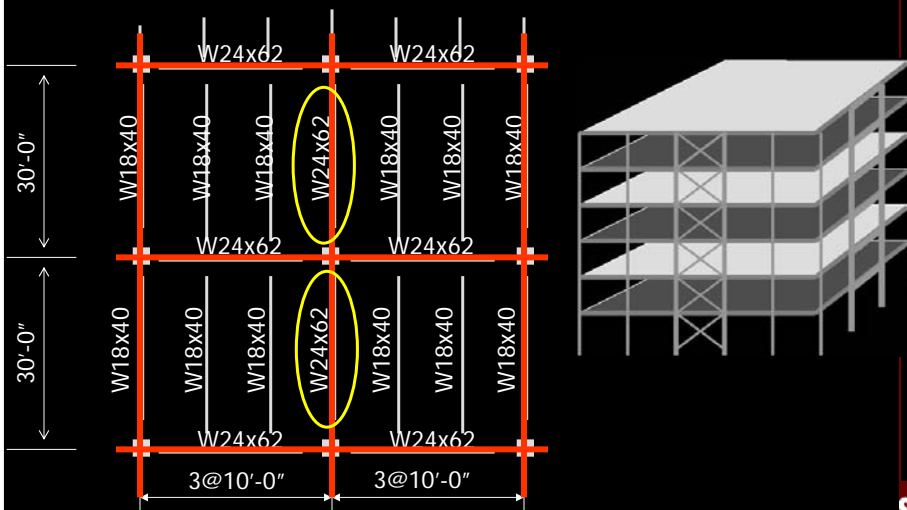
The Cost of Collapse Avoidance

- Steel weight
 - 6 pounds/ft² (flat)
 - 3 pounds/ft² (columns)
- Estimated cost –framing (\$2,500/ton) \$11.25/ft²
- Estimated cost of moment connections (\$500 connection) \$1.11/ft²
- Total Steel Cost \$12.36/ft²

- Premium for collapse prevention 10%
- Some significant schedule impact

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Can these impacts be reduced?



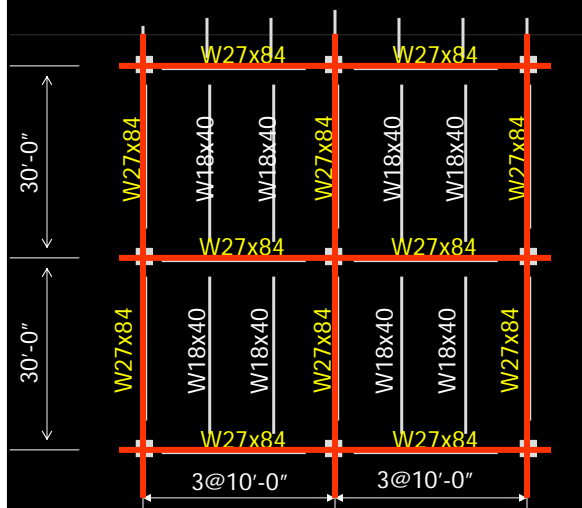
SGH

The Cost of Collapse Avoidance

- Steel weight
 - 6.4 pounds/ft² (flat)
 - 3 pounds/ft² (columns)
- Estimated cost –framing (\$3,000/ton) \$11.75/ft²
- Estimated cost of moment connections (\$500 connection) \$1.11/ft²
- Total steel cost - \$12.86/ft²
- Premium for collapse prevention 14%
- Same schedule impact

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Can impacts be reduced?



- What change to framing is required to allow moment connections to be made only on each third floor?
- Girders and beams must change to W27x84 on strong floor only

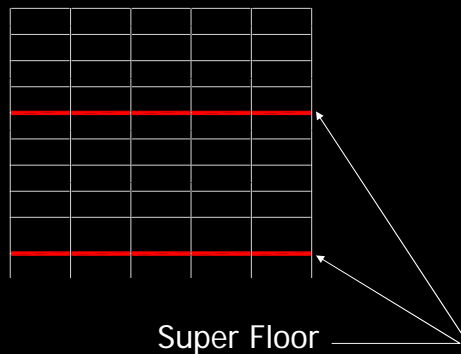
SGH

The Cost of Collapse Avoidance

- Steel weight
 - 6.8 pounds/ft² (flat)
 - 3 pounds/ft² (columns)
- Estimated cost –framing \$2,500/ton) \$12.25/ft²
- Estimated cost of moment connections (\$500 connection) \$0.75/ft²
- Total steel cost - \$13.00/ft²
- Premium for collapse prevention 15%
- Schedule impacts reduced (fewer moment connectinos)

SGH

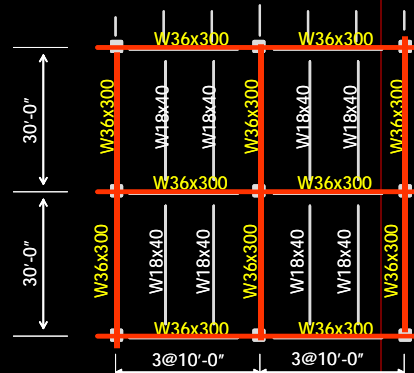
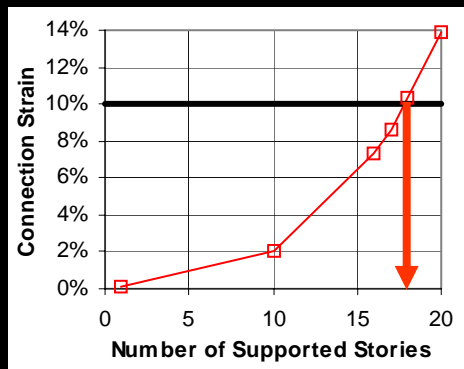
How many floors can be supported by one floor?



- Limits are:
 - Ability of connections to resist inelastic straining
 - Tolerance to deflection of floors in collapse avoidance condition

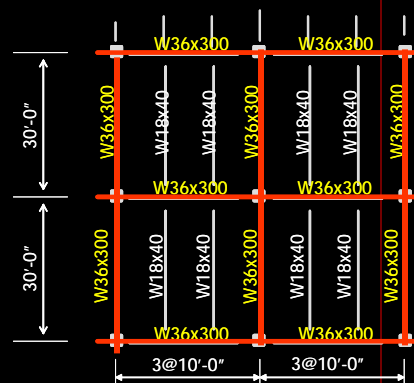
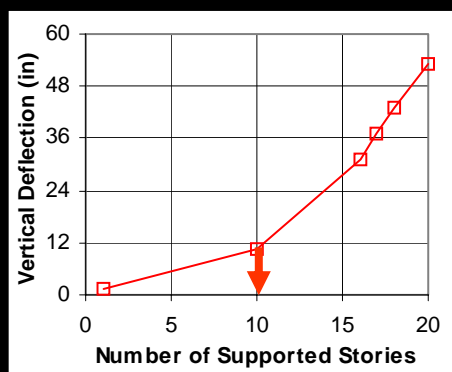
SGH

How many floors can be supported by one floor?



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How many floors can be supported by one floor?



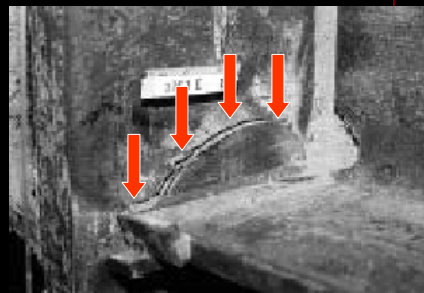
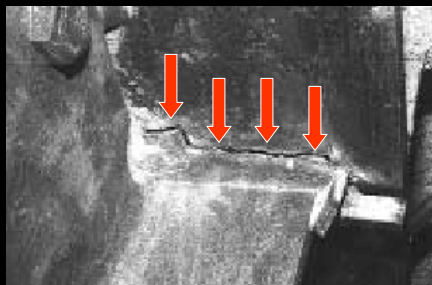
SGH

Summary

- The “strong floor concept” can be used to economically provide collapse resistant structures without substantial cost or schedule premium
- The Devil is in the Details (connections)
- As an industry, we still do not have good understanding of the vulnerability of various types of connections to impact induced fracture

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Connections are the critical issue



Welded, bolted flange moment-resisting connections fractured in the 1994 Northridge earthquake at modest demands

- yield level stresses
- negligible tension

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Similar and more severe damage has occurred in collapse conditions



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Similar and more severe damage has occurred in collapse conditions



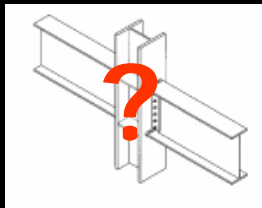
SGH

Bolted Connections are also vulnerable

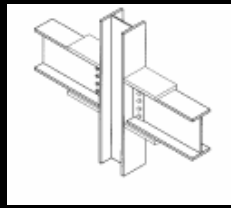


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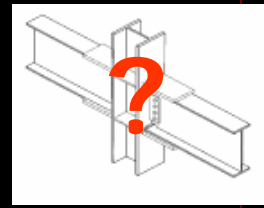
Guidelines permit use of a wide range of "approved connections"



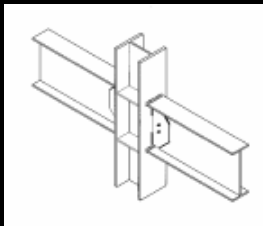
WUF-B



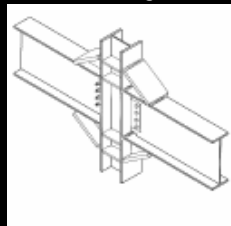
Welded Flange Plate



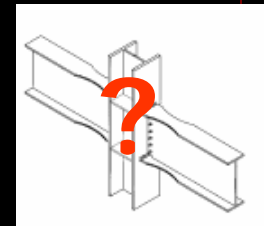
Welded Cover Plate



Free Flange



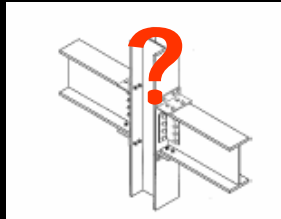
Haunched



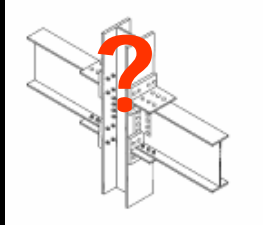
RBS

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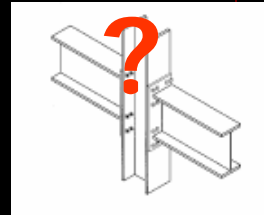
Guidelines permit use of a wide range of "approved connections"



Bolted Angle



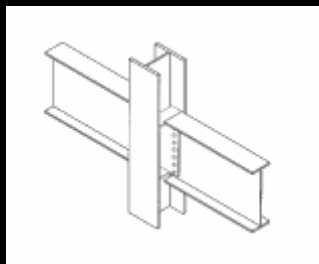
Double Tee



End Plate

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Moment-connections may not be necessary



- Catenary behavior is an effective method of resisting collapse
- Moment development at girder ends is not required for this
- Robust tensile connections may be sufficient to provide collapse avoidance capability

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Conclusions

- Steel framing has excellent ability to provide collapse resistance in structures
- The most common method of analysis used today is not adequate, but simple design approaches can be used to evaluate collapse resistance
- Collapse resistance can be provided with negligible increase in steel tonnage, cost or schedule.
- Connections are key
 - Ability of frame to provide collapse resistance
 - Relative cost of collapse resistance
- Testing of various connection technologies to demonstrate adequate robustness is urgently needed