

15-826: Multimedia Databases and Data Mining

Lecture#2: Primary key indexing – B-trees

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Reading Material

[Ramakrishnan & Gehrke, 3rd ed, ch. 10]

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Problem

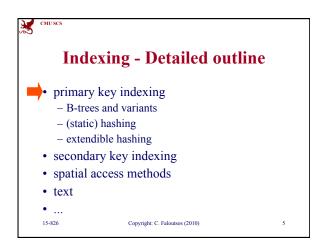
Given a large collection of (multimedia) records, find similar/interesting things, ie:

- Allow fast, approximate queries, and
- Find rules/patterns

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Primary key indexing

• find employee with ssn=123

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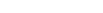


B-trees

- the **most successful** family of index schemes (B-trees, B*-trees, B*-trees)
- Can be used for primary/secondary, clustering/non-clustering index.
- balanced "n-way" search trees

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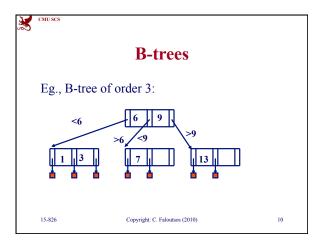


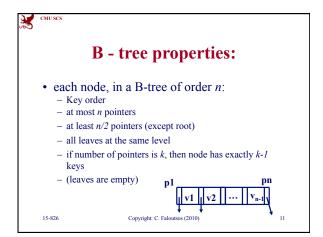


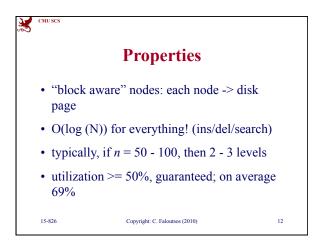
- Rudolf Bayer and Edward M. McCreight, *Organization and Maintenance of Large Ordered Indices*, Acta Informatica, 1:173-189, 1972.
- Received the 2001 SIGMOD innovations award
- among the most cited db publications
 - $\hbox{-}www.informatik.uni-trier.de/} \hbox{-}ley/db/about/top.html}$

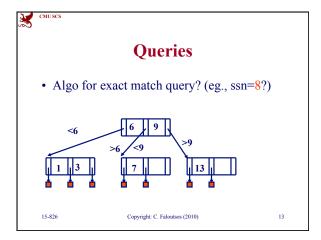
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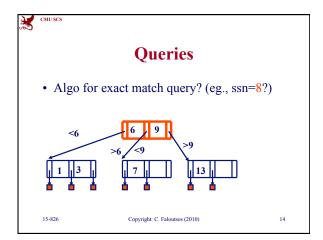
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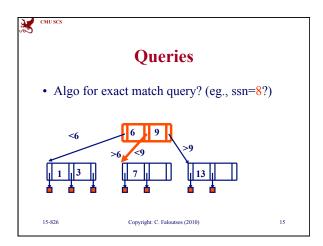


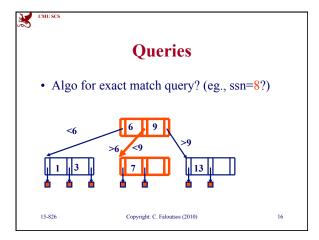


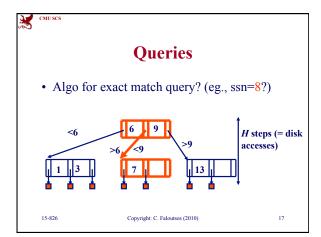


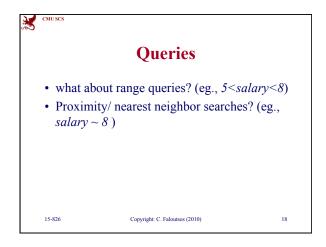


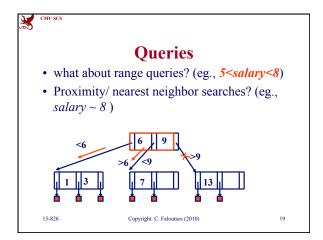


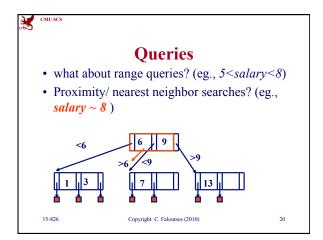


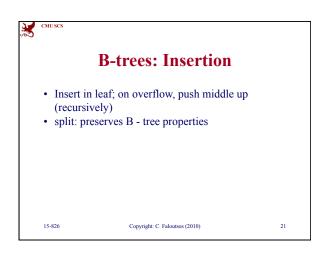


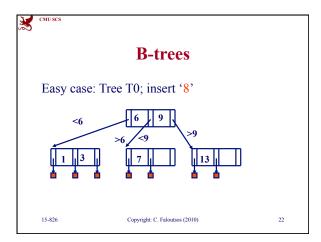


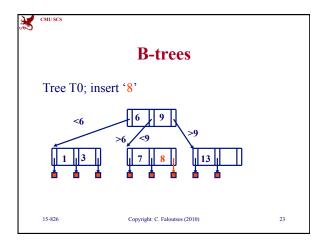


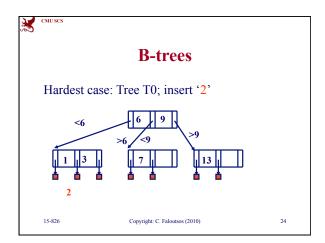


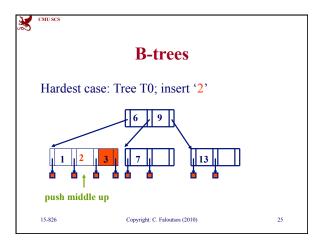


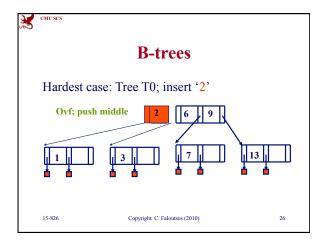


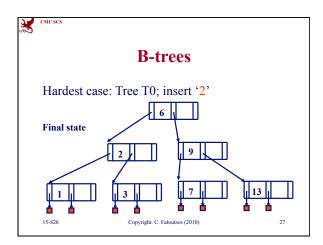


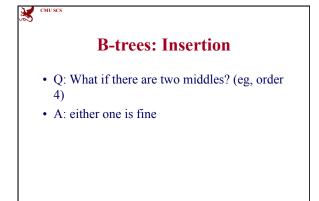












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B-trees: Insertion

- Insert in leaf; on overflow, push middle up (recursively 'propagate split')
- split: preserves all B tree properties (!!)
- notice how it grows: height increases when root overflows & splits
- Automatic, incremental re-organization

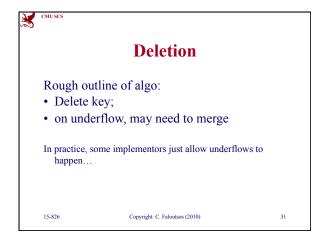
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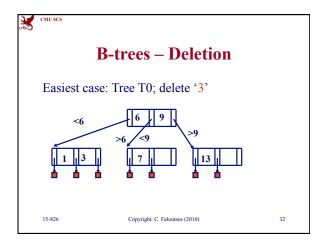
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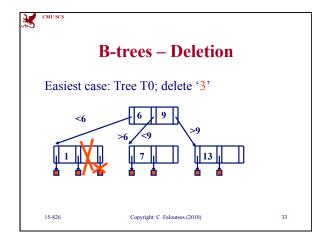
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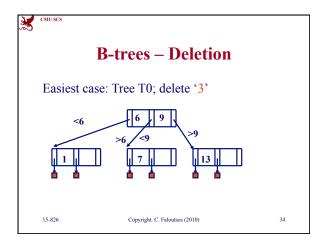


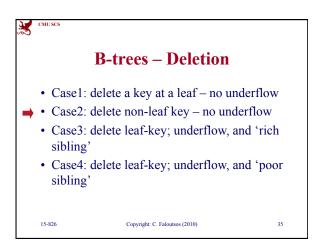
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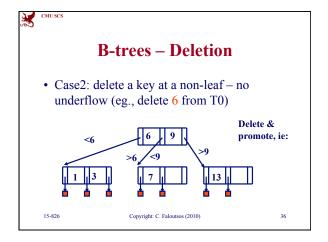


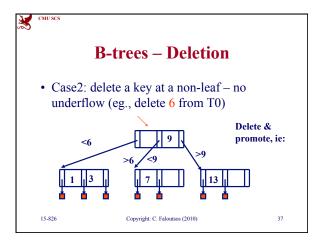


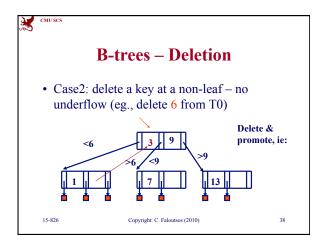


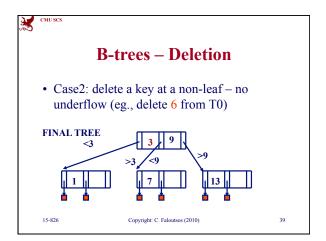














B-trees – Deletion

- Case2: delete a key at a non-leaf no underflow (eg., delete 6 from T0)
- Q: How to promote?
- A: pick the largest key from the left sub-tree (or the smallest from the right sub-tree)
- Observation: every deletion eventually becomes a deletion of a leaf key

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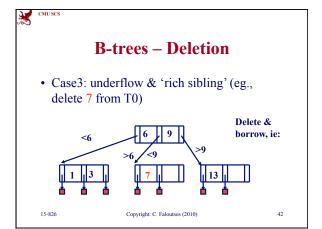
B-trees – Deletion

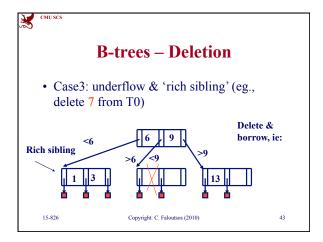
- Case1: delete a key at a leaf no underflow
- Case2: delete non-leaf key no underflow
- → Case3: delete leaf-key; underflow, and 'rich sibling'
 - Case4: delete leaf-key; underflow, and 'poor sibling'

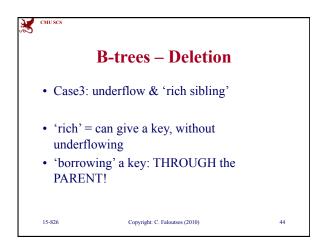
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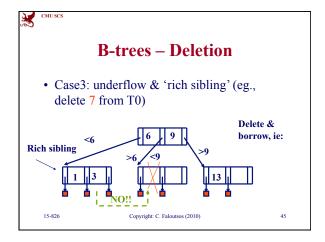
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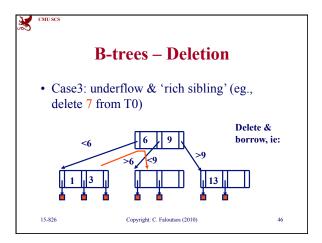
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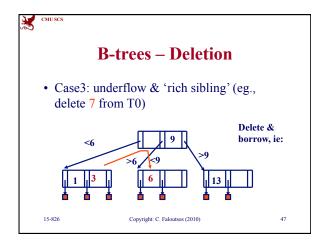


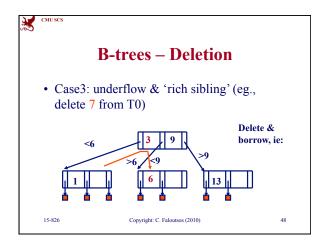


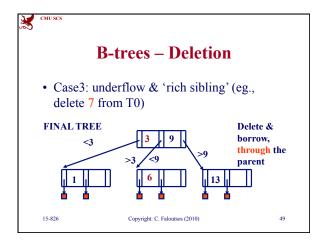


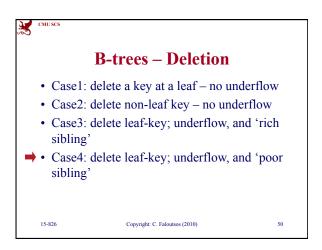


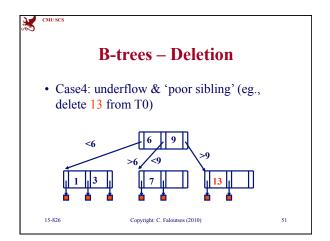


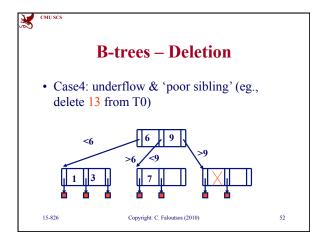


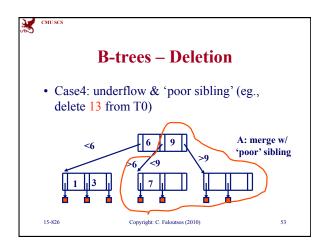


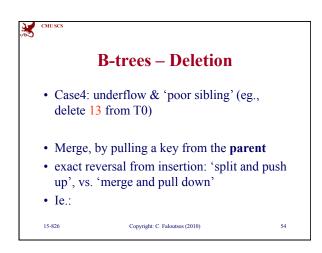


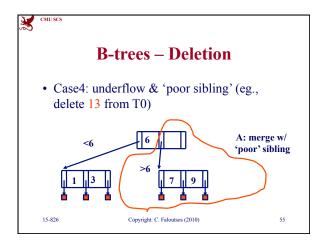


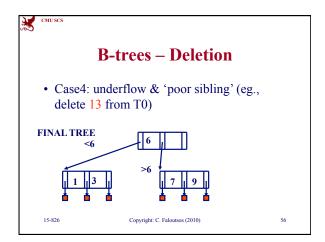


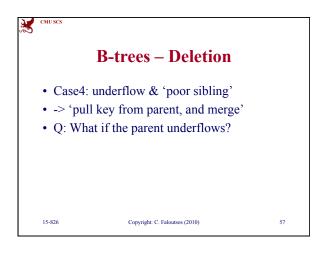


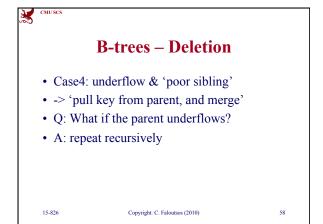


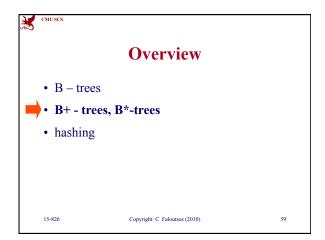


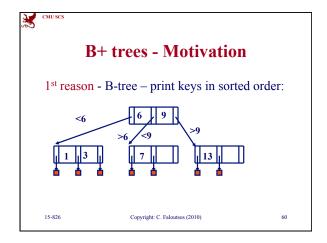


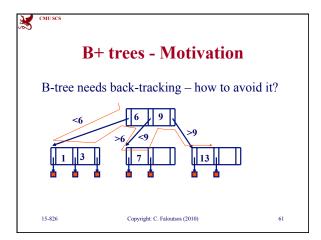


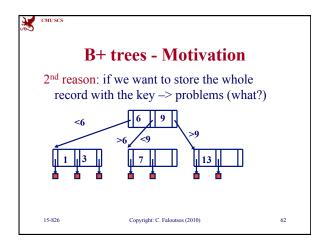


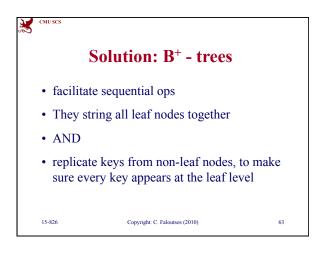


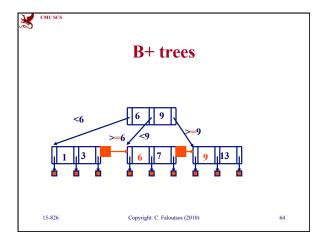


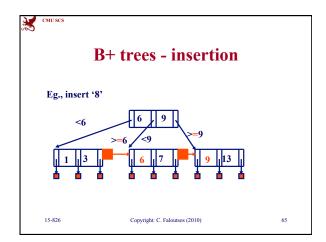


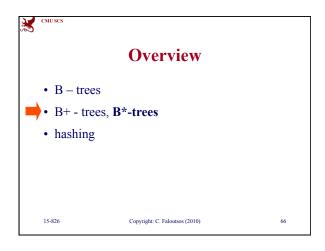


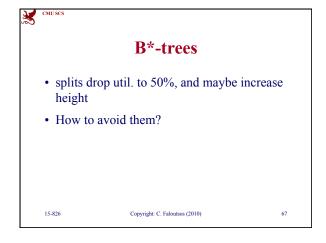


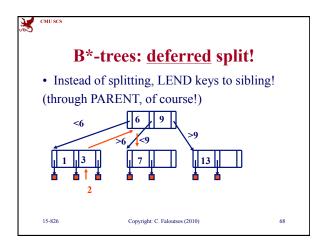


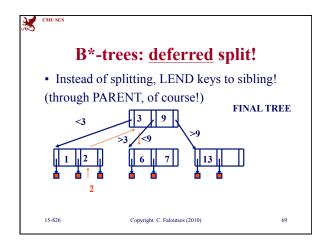














B*-trees: deferred split!

- Notice: shorter, more packed, faster tree
- It's a rare case, where space utilization and speed improve together
- BUT: What if the sibling has no room for our 'lending'?

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B*-trees: deferred split!

- BUT: What if the sibling has no room for our 'lending'?
- A: 2-to-3 split: get the keys from the sibling, pool them with ours (and a key from the parent), and split in 3.
- Details: too messy (and even worse for deletion)

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Conclusions

- Main ideas: recursive; block-aware; on overflow -> split; **defer** splits
- All B-tree variants have excellent, O(logN) worst-case performance for ins/del/search
- B+ tree is the prevailing indexing method
- More details: [Knuth vol 3.] or [Ramakrishnan & Gehrke, 3rd ed, ch. 10]

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