

Robust Blind Multiuser Detection Against Signature Waveform Mismatch Based on Second-Order Cone Programming

Shuguang Cui, Mikalai Kisialiou, Zhi-Quan Luo, *Senior Member, IEEE*, and Zhi Ding, *Fellow, IEEE*

Abstract—Blind signal detection in multiuser code division multiple access (CDMA) system is particularly attractive when only the desired user signature is known to a given receiver. A problem common to several existing blind multiuser CDMA detectors is that the detection performance is very sensitive to the signature waveform mismatch (SWM) which may be caused by channel distortion. In this paper, we consider the design of a blind multiuser CDMA detector that is robust to the SWM. We present a convex formulation for this problem by using the second-order cone (SOC) programming. The resulting SOC problem can be solved efficiently using the recently developed interior point methods. Computer simulations indicate that the performance of our new robust blind multiuser detector is superior to those of many existing methods.

Index Terms—Blind multiuser detection, robust multiuser detection, second-order cone (SOC) programming.

I. INTRODUCTION

A COMMONLY encountered problem in code division multiple access (CDMA) systems is the so-called near-far effect whereby weaker users are dominated by stronger users (interferers). It is well known that in such circumstances, the traditional matched filter single-user detection is not effective, and multiuser detection should be used [1], [8], [9]. While in a standard multiuser detector, all user signature and timing information must be known [1] to the receiver; a recent work [2] presented a simple blind near-far resistant “multiuser” detector that requires only the desired users’ waveform. Some further work along this line have been reported in [3], [4], [6], and [7].

A problem common to several existing blind multiuser CDMA detectors is that their performance tend to be negatively affected by the signature waveform mismatch (SWM) caused by channel distortion. Since channel distortion exists in most environments where CDMA is deployed (e.g., cellular mobile telephony), it is essential for the blind multiuser receivers to mitigate the SWM effect when we design a practical CDMA

detector with near-far resistance [2], [10]. One possible approach to deal with the SWM problem is to allow the use of training sequences during transmission such that the channel distortion can be periodically estimated by the receiver. The identified channel response (distortion) can be used to design compensating measures against SWM. However, in a mobile communication environment where channel distortion varies quickly, training-based approaches may consume too much channel capacity. An alternative means of mitigating SWM is to design a blind multiuser detector that has strong robustness to SWM. In [2] (see also [5]), a particular mechanism was presented for the design of robust blind multiuser CDMA detectors that call for the minimization of the detector’s output energy. Moreover, two gradient descent algorithms (the stochastic gradient (SG) algorithm and the least squares (LS) algorithm) were proposed in [2] for achieving the minimum output energy (MOE) under the constraint that the so-called “surplus energy” created by SWM is bounded. However, constraining the “surplus energy” is an indirect and heuristic way to achieve receiver robustness. A more natural (and perhaps also more desirable) formulation is to directly maximize the worst case system performance given a specific bound of SWM. Such is the approach taken in this paper. Another drawback of the two iterative algorithms proposed in [2] is that they require some data-dependent parameters that are not easy to select, and a poor choice could lead to unacceptable performance. The constrained MOE (CMOE) method [6] first estimates the channel blindly and then minimizes the channel output energy subject to certain constraints aimed at protecting the desired signal that has propagated through the estimated channel. However, the channel identification phase of the CMOE method requires a large number of samples and a high signal-to-noise ratio (SNR). Moreover, it requires special techniques to resolve an intrinsic unitary ambiguity matrix.

In this correspondence, we present a new formulation for the design of robust blind multiuser CDMA detectors. Our formulation is direct in the sense that it allows explicit control of the amount of required robustness in the detector. Moreover, our optimization formulation is convex since it is based on the second-order cone (SOC) programming. As such, this new robust blind multiuser detector can be obtained using the highly efficient interior point methods recently developed in the optimization community. Computer simulations indicate that the performance of our new robust blind multiuser detector, when combined with a blind signal separation method (e.g., the JADE algorithm [13]), is superior to those that exist in the literature for both nondispersive and dispersive propagation environment, while the number of required samples is significantly smaller.

Manuscript received December 6, 2002; revised September 30, 2003; accepted May 4, 2004. The editor coordinating the review of this paper and approving it for publication is A. Yener. The work of S. Cui, M. Kisialiou, and Z.-Q. Luo was supported by the Natural Sciences and Engineering Research Council of Canada under Grant OPG0090391, and by the Canada Research Chair Program. The work of Z.-Q. Luo was also supported in part by the National Science Foundation under Grant CCR-0196364, Grant ECS-0121469, and Grant DMS-0312416.

S. Cui is with the Department of Electrical Engineering, Stanford University, Stanford, CA 94305-9505 USA.

M. Kisialiou and Z.-Q. Luo are with the Department of Electrical and Computer Engineering, University of Minnesota, Minneapolis, MN 55455 USA.

Z. Ding is with the Department of Electrical and Computer Engineering, University of California at Davis, Davis, CA 95616 USA.

Digital Object Identifier 10.1109/TWC.2005.850330

II. PROBLEM DESCRIPTION

Consider an antipodal K -user synchronous direct sequence CDMA channel corrupted by some additive and white Gaussian noise $n(t)$. Our notation follows that of [2], where

- σ standard deviation of channel $n(t)$;
- $s_k(t)$ normalized signature waveform for the k th user with $\|s_k(t)\| = 1$;
- $\{b_k[z]\}$ transmitted binary phase-shift keying (BPSK) data bits;
- T bit duration at the transmission rate of $1/T$.

Given the above notations, the received signal can be written as

$$y(t) = \sum_{k=1}^K A_k b_k s_k(t) + n(t), \quad t \in [0, T]. \quad (1)$$

When we sample the received signal waveform $y(t)$ at the chip rate $1/\Delta$, where $\Delta > 0$ is the chip interval, we obtain the following discrete version of (1):

$$\mathbf{y} = \sum_{k=1}^K A_k b_k \mathbf{s}_k + \mathbf{n} \quad (2)$$

where

$$\mathbf{y} = \begin{bmatrix} y(\Delta) \\ y(2\Delta) \\ \vdots \\ y(N\Delta) \end{bmatrix} \quad \mathbf{s}_k = \begin{bmatrix} s_k(\Delta) \\ s_k(2\Delta) \\ \vdots \\ s_k(N\Delta) \end{bmatrix} \quad \mathbf{n} = \begin{bmatrix} n(\Delta) \\ n(2\Delta) \\ \vdots \\ n(N\Delta) \end{bmatrix}$$

with N being the code spreading factor. Note that $T = N\Delta$ as a result.

Without loss of generality, suppose that user 1 is our desired user whose signature waveform is denoted as \mathbf{s}_1 . Our goal in receiver design is to select a vector \mathbf{c}_1 , which, upon correlating with the received vector \mathbf{y} and passing through a hard limiter, will recover the data bits $\{b_1[i]\}$ sent by user 1. The MOE-based multiuser detector introduced in [2] can be described as follows:

$$\begin{aligned} &\text{minimize} \quad E |\langle \mathbf{y}, \mathbf{c}_1 \rangle|^2 = \mathbf{c}_1^T \mathbf{R} \mathbf{c}_1 \\ &\text{subject to} \quad \mathbf{c}_1^T \mathbf{s}_1 = 1 \end{aligned} \quad (3)$$

where \mathbf{c}_1 is the vector to be determined, and $\mathbf{R} = E(\mathbf{y}\mathbf{y}^T) \in \Re^{N \times N}$. In practice, we only have a finite number of snapshots of the received data. Thus, we need to replace \mathbf{R} in (3) with the sample covariance matrix

$$\hat{\mathbf{R}} = \frac{1}{N_b} \sum_{n=1}^{N_b} \mathbf{y}[n] (\mathbf{y}[n])^T$$

where N_b is the number of transmitted data bits and $\mathbf{y}[n]$ is the n th received data vector. This leads to the following implementable version of (3):

$$\begin{aligned} &\text{minimize} \quad \mathbf{c}_1^T \hat{\mathbf{R}} \mathbf{c}_1 \\ &\text{subject to} \quad \mathbf{c}_1^T \mathbf{s}_1 = 1. \end{aligned} \quad (4)$$

It is well known that the MOE solution to (4) is highly sensitive to SWM and often leads to poor bit error rate (BER) performance. To overcome this sensitivity to SWM, Honig *et al.* [2] introduced the following energy-constrained version of MOE detector:

$$\begin{aligned} &\text{minimize} \quad \mathbf{c}_1^T \hat{\mathbf{R}} \mathbf{c}_1, \\ &\text{subject to} \quad \mathbf{c}_1^T \mathbf{s}_1 = 1 \quad \|\mathbf{c}_1 - \mathbf{s}_1\|^2 = \chi \end{aligned} \quad (5)$$

where χ is called the surplus energy and is chosen by the user *a priori* so that $\chi_I < \chi < \chi_S$, with χ_I and χ_S being the user-selected lower and upper bounds on the surplus energy. Also, an SG algorithm was proposed [2] to solve (5), but rigorous convergence analysis was neither given nor known. In some sense, (5) attempts to generate a robust solution to (4), which is insensitive to SWM in \mathbf{s}_1 . This robustness is achieved indirectly by constraining the surplus energy. The main weakness of (5) is its lack of convexity.

III. SOC ALGORITHM DEVELOPMENT

We now describe a more direct (and arguably a more natural) way to construct a robust solution for the MOE formulation (4) under SWM. It turns out that both the objective function and constraints in this new formulation are convex so that a globally optimal solution can be found efficiently.

We model the actual received signature waveform as $\bar{\mathbf{s}}_k = A_k(\mathbf{s}_k + \mathbf{e}_k)$, where \mathbf{e}_k is the mismatch error vector and A_k is the channel gain. Notice that A_k can be easily estimated by matching the channel output power with $\|\mathbf{s}_k\|^2$. In this way, we obtain the following normalized received signature waveform:

$$\hat{\mathbf{s}}_k = \mathbf{s}_k + \mathbf{e}_k. \quad (6)$$

Clearly, $\|\mathbf{e}_k\|$ is a measure of the magnitude of signal waveform mismatch. The distortion can be due to asynchronism or multipath fading. For example, in the case of timing asynchronism, we can use Taylor approximation to bound $s(t + \tau) - s(t)$, where τ is the timing offset. Hence, the SWM error is easily bounded by $\|\mathbf{e}\| = \|\hat{\mathbf{s}} - \mathbf{s}\| \leq BN\tau$, where B is the upper bound for the derivative of the continuous signature waveform $s(t)$, and N is the spreading factor. In a multipath environment with an M -tap channel response \mathbf{h} , the actual received signature waveform is $\hat{\mathbf{s}}_k = \mathbf{s}_k \otimes \mathbf{h}$. Hence, we can obtain the following bound on the mismatch error vector:

$$\begin{aligned} \|\mathbf{e}\| &= \|\hat{\mathbf{s}}_k - \mathbf{s}_k\| \leq \|\mathbf{s}_k \otimes \mathbf{h} - \mathbf{s}_k\| \\ &\leq \|\mathbf{s}_k \otimes (\mathbf{h} - \mathbf{h}_{\text{ideal}})\| \\ &\leq \sqrt{M} \|\mathbf{h} - \mathbf{h}_{\text{ideal}}\| \end{aligned} \quad (7)$$

where $\mathbf{h}_{\text{ideal}}$ denotes the ideal channel response (i.e., delta function). If the channel has a main line of sight component and small multipath components, then $\|\mathbf{h} - \mathbf{h}_{\text{ideal}}\|$ will be small.

We assume the distortion error \mathbf{e}_1 in the desired signal waveform can be bounded by some constant $\delta > 0$, that is, $\|\mathbf{e}_1\| \leq \delta$. The size of δ can be estimated using, for example,

(7). The actual received signal waveform \hat{s}_1 can be described as a vector in the set

$$S_1(\delta) = \{\hat{s}_1 | \hat{s}_1 = \mathbf{s}_1 + \mathbf{e}_1, \|\mathbf{e}_1\| \leq \delta\}.$$

Since \hat{s}_1 can be any vector in $S_1(\delta)$, we must ensure that the detector gain for all signals in $S_1(\delta)$ should be greater than 1, that is, $\mathbf{c}_1^T \hat{s}_1 \geq 1$ for all vectors $\hat{s}_1 \in S_1(\delta)$. Such a constraint ensures that we can extract the data bits from user 1 regardless of how its signature waveform is distorted, as long as the distortion is bounded by δ . Now suppose that this gain constraint is enforced, then our goal remains to find a vector \mathbf{c}_1 that minimizes $\mathbf{c}_1^T \hat{\mathbf{R}} \mathbf{c}_1$. Consequently, a robust version of (4) can be described as follows:

$$\begin{aligned} & \text{minimize} && \mathbf{c}_1^T \hat{\mathbf{R}} \mathbf{c}_1 \\ & \text{subject to} && \mathbf{c}_1^T \hat{s}_1 \geq 1, \quad \text{for all } \hat{s}_1 \in S_1(\delta) \end{aligned} \quad (8)$$

where δ is an upper bound on the norm of the signal mismatch error vector.

For each choice of $\hat{s}_1 \in S_1(\delta)$, the condition $\mathbf{c}_1^T \hat{s}_1 \geq 1$ represents a linear constraint on \mathbf{c}_1 . Since there are an infinite number of \hat{s}_1 in $S_1(\delta)$, the constraints in (8) are semi-infinite and linear. To facilitate the computation of optimal \mathbf{c}_1 , we will convert these semi-infinite linear constraints into a so-called SOC constraint. This is achieved by considering the worst case performance as follows. Note that the optimal solution of the minimization problem

$$\min_{\hat{s}_1 \in S_1(\delta)} \mathbf{c}_1^T \hat{s}_1 \text{ or equivalently } \min_{\|\mathbf{e}_1\| \leq \delta} \mathbf{c}_1^T (\mathbf{s}_1 + \mathbf{e}_1)$$

is given by

$$\mathbf{e}_1 = -\frac{\delta \mathbf{c}_1}{\|\mathbf{c}_1\|}.$$

This can be easily verified by Cauchy–Schwartz inequality. Therefore, the constraint

$$\mathbf{c}_1^T \hat{s}_1 \geq 1, \quad \text{for all } \hat{s}_1 \in S_1(\delta)$$

can be equivalently described by

$$\mathbf{c}_1^T \left(\mathbf{s}_1 - \frac{\delta \mathbf{c}_1}{\|\mathbf{c}_1\|} \right) \geq 1 \text{ or } \mathbf{c}_1^T \mathbf{s}_1 - \delta \|\mathbf{c}_1\| \geq 1. \quad (9)$$

Substituting (9) into (8), we obtain a new problem formulation

$$\begin{aligned} & \text{minimize} && \mathbf{c}_1^T \hat{\mathbf{R}} \mathbf{c}_1 \\ & \text{subject to} && \mathbf{c}_1^T \mathbf{s}_1 - \delta \|\mathbf{c}_1\| \geq 1. \end{aligned} \quad (10)$$

Notice that the constraint in (10) is of the form

$$\|\mathbf{P} \mathbf{c}_1\| \leq \mathbf{p}^T \mathbf{c}_1 + q$$

for some given $\mathbf{P} \in \Re^{N \times N}$, $\mathbf{p} \in \Re^N$, and $q \in \Re$, which is called a SOC constraint.

Next we convert the quadratic objective function of (10) into a linear one. To do so, we first notice that $\mathbf{c}_1^T \hat{\mathbf{R}} \mathbf{c}_1 = \|\mathbf{L} \mathbf{c}_1\|^2$, where $\mathbf{L}^T \mathbf{L} = \hat{\mathbf{R}}$ is the Cholesky factorization. Obviously, min-

imizing the quadratic norm $\|\mathbf{L} \mathbf{c}_1\|^2$ is equivalent to minimizing $\|\mathbf{L} \mathbf{c}_1\|$. Introducing a new variable t and a new constraint $\|\mathbf{L} \mathbf{c}_1\| \leq t$, we can convert (10) into the following form:

$$\begin{aligned} & \text{minimize} && t \\ & \text{subject to} && \|\mathbf{L} \mathbf{c}_1\| \leq t \quad \|\delta \mathbf{c}_1\| \leq \mathbf{s}_1^T \mathbf{c}_1 - 1. \end{aligned} \quad (11)$$

The above formulation (11) is now in the standard form of a SOC programming [11] problem. This is because the objective function is linear and the two constraints are both SOC constraints (which are convex). Such optimization problem can be efficiently solved using the primal-dual potential reduction method SeDuMi [14]. The total computational complexity for solving (11) is $O(N^{3.5} \log 1/\epsilon)$. This, plus the complexity of accumulating the sample correlation matrix $\hat{\mathbf{R}}$ and performing its Cholesky factorization, gives the SOC approach an overall complexity of $O(N^{3.5} \log 1/\epsilon + N_b N^2)$, where N_b is the total number of transmitted data bits. The accuracy parameter ϵ can be either fixed (say, $\epsilon = 10^{-4}$) or chosen to vary inversely proportional to the SNR.

IV. SIMULATIONS

We now compare the simulation performance of our new SOC method with those of the existing blind linear CDMA receivers, which include the classical matched filtering (MF) method, the standard (nonrobust) MOE detector, the two versions of robust MOE methods proposed in [2] (one based on LS approach and the other based on SG approach), as well as the CMOE method [6]. Although time synchronism was assumed throughout the algorithm development, we first test the performance of our algorithm on asynchronous CDMA systems. Then we consider multipath propagation CDMA systems.

A. SWM Timing Asynchronism Model

Timing asynchronism is modeled through the presence of SWM as in (6), where $\mathbf{e}_k \sim \mathcal{N}(0, \sigma^2)$. We consider CDMA systems using Gold codes of length $N = 31$ with the number of users $K = 7$ and $K = 30$. For the system with $K = 7$ users the interference-to-signal ratio (ISR) is set to be

$$\text{ISR} = 20 \log \left(\frac{A_k}{A_1} \right) = 20 \text{ dB}, \quad k = 2, \dots, K$$

where A_k denotes the received signal amplitude of the k th user. For the other system with $K = 30$, ISR is taken to be

$$\text{ISR} = 20 \log \left(\frac{A_k}{A_1} \right) = 10 \text{ dB}, \quad k = 2, \dots, K.$$

Both cases represent a severe near–far effect.

In our simulations, we test the systems with long sequences of transmitted bits ($N_b = 100$ and $N_b = 400$) to ensure adequate iterative convergence of both LS and SG methods, which we shall compare with our SOC method. It is also needed to ensure that the sample covariance matrix $\hat{\mathbf{R}}$ is a close approximation of the true covariance matrix \mathbf{R} . At the ℓ th run, a random distortion with a norm no more than δ is added to every

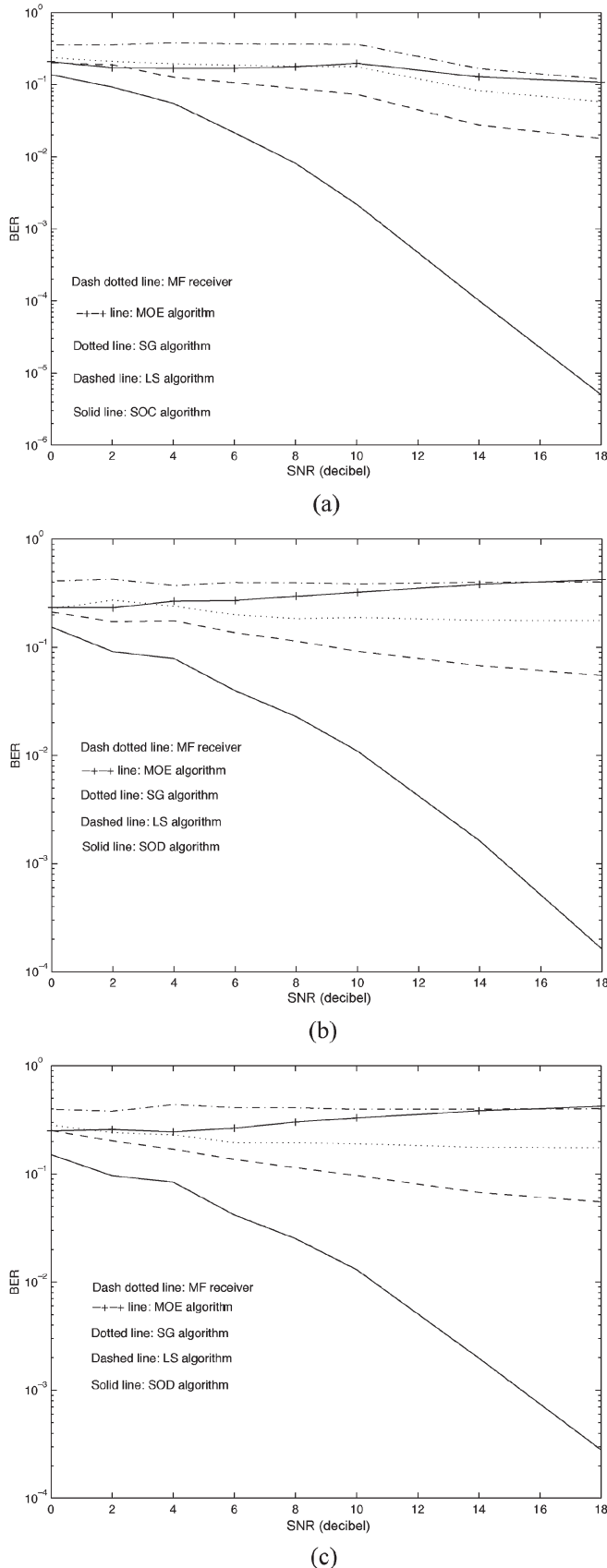


Fig. 1. BER versus SNR, comparison of SOC, LS, SG, MOE, and MF detectors. (a) $\delta = 0.4$ and $\hat{\delta} = 0.4$. (b) $\delta = 0.4$ and $\hat{\delta} = 0.6$. (c) $\delta = 0.4$ and $\hat{\delta} = 0.2$.

signature waveform \mathbf{s}_k to result in a mismatched waveform $\hat{\mathbf{s}}_k^\ell$. In addition, new additive Gaussian noise vectors \mathbf{n}^ℓ as well as a new data sequence $\{b_k^\ell\}$ are generated.

To solve (11), we have used a Matlab-based tool called SeDuMi [14], which is an efficient implementation of a primal-dual interior point method for solving SOC problems. For the LS and the SG methods, we have experimented with various different values of χ [the “surplus energy” in (5)] and have chosen the one that gives the best averaged BER performance, even though such a luxury is not practically affordable.

The results for $K = 7$ users are shown in Fig. 1. We test this system with mismatch $\delta = 0.4$. Note that δ is the upper bound on the SWM realization at each random run. We experimented with different δ values and results seem to be the same qualitatively. Fig. 1 shows that the SOC method has the best BER performance, followed by LS, SG, MOE, and MF. Fig. 1(a) assumes that the value of δ is known to the detector and we use this value ($\hat{\delta} = \delta$) in the SOC formulation (11). Fig. 1(b) and (c) shows the performance of the SOC method when δ is overestimated and underestimated, respectively. It can be seen that the SOC detector is robust to errors in estimating the SWM bound. In all of above reported simulation results, we have chosen the surplus energy χ optimally (by trial and error) and have plotted only the best results. It comes as no surprise that the MF detector has a poor BER performance since it does not deal with the presence of strong cochannel interferences. Notice that the BER for the MOE detector worsens when the SNR increases. This is the case for a nonrobust detector like the MOE method because a part of the signal power will be contributing towards the interference when SWM is present, leading to larger interference power and worse BER performance as the signal power increases.

Fig. 2 shows the results for heavily loaded system with $K = 30$ users and severe interference with ISR set to be 10 dB. Fig. 2(a) and (b) shows the comparison of SOC formulation, LS and SG for data blocks of 100 and 400 bits, respectively. At each run, a mismatch of norm $\delta = 0.4$ is added to signature waveforms of all users, and δ is assumed to be known to the detector. Inaccuracy of estimating the mismatch does not lead to the significant deterioration of the performance of the SOC method, thus, in practice, an approximate estimate of δ will be enough. The simulations suggest that the robust SOC formulation is superior to both LS and SG methods.

B. Multipath Propagation

We now test the performance of our algorithm in a multipath propagation scenario. In our simulation, the dispersive channel is modeled as a finite-impulse response filter with a tap-spacing equal to the chip rate [12]. The spreading codes are again chosen to be Gold sequences of length $N = 31$. The input signal is a BPSK independent identically distributed sequence for every user. Each user's chip sequence is transmitted through a randomly generated multipath fading channel of length $q + 1 = 3$ chip periods. The user of interest is assumed to be the weak user: The channel gains are scaled so that each interfering user is 20 dB stronger than the user of interest. This corresponds to a severe near-far situation.

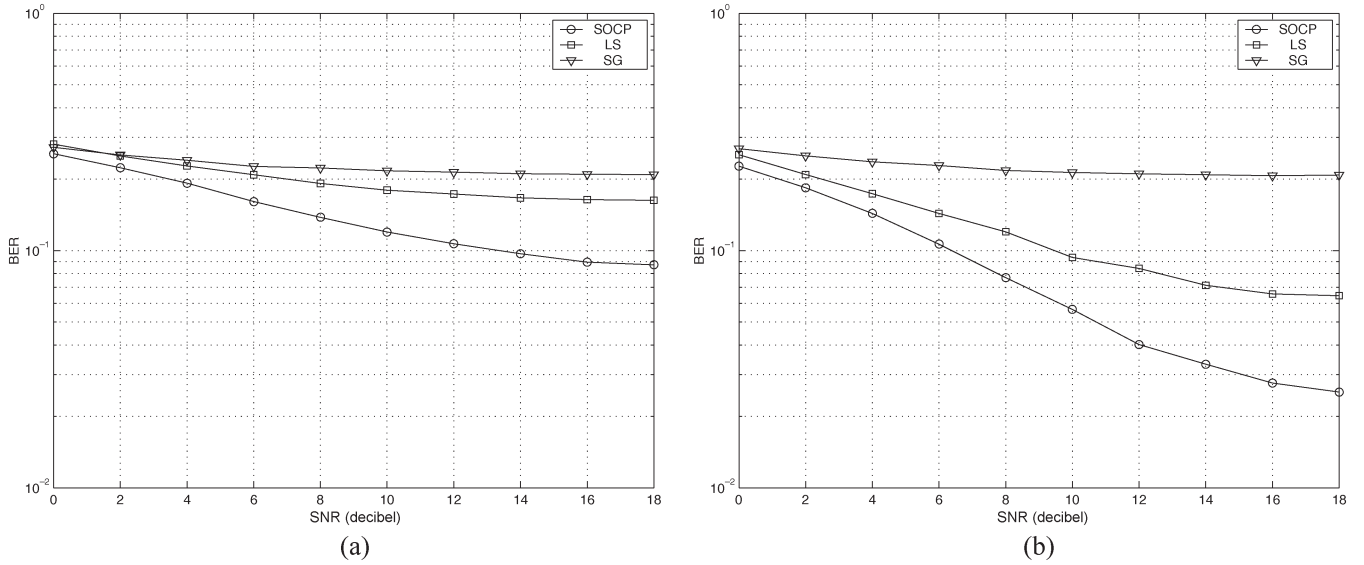


Fig. 2. BER versus SNR, 30 users, ISR = 10 dB, mismatch $\delta = 0.4$. (a) Data block 100 bits. (b) Data block 400 bits.

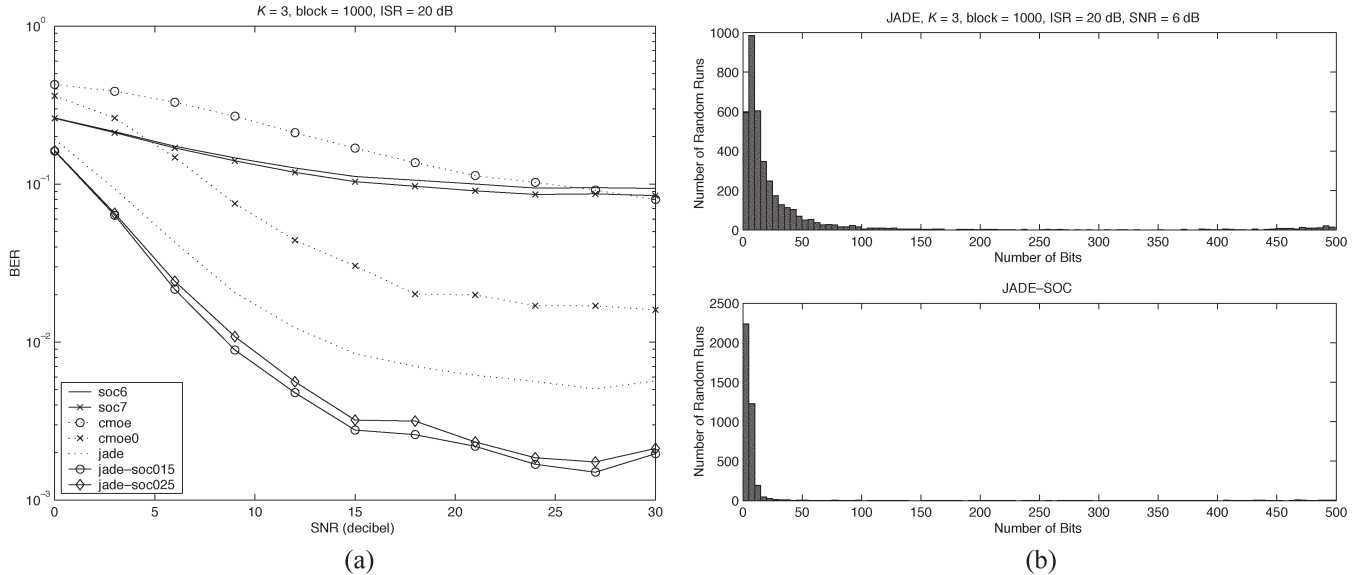


Fig. 3. Comparison of SOC, CMOE, JADE, and JADE-SOC. (a) Probability of error versus SNR. (b) Histogram.

Comparison of CMOE, SOC, and JADE Methods: Under the above model, we compared the CMOE and SOC on a CDMA system with $K = 3$ users. The other multiuser detectors considered in the previous section showed a poor performance under the given multipath propagation model.

Notice that a unitary ambiguity matrix exists in the blind identification phase of the CMOE algorithm. Such ambiguity is generic to the multiuser blind identification approaches based on second-order statistics and cannot be resolved unless additional information is available. In our simulation, we have manually resolved this ambiguity using a (unrealistic) training sequence prior to data transmission. Even with this ambiguity removed, the CMOE algorithm still cannot recover the desired (weak) user, regardless of the block size. The BER results, averaged over 4000 Monte Carlo runs, are shown in Fig. 3, with a curve “cmoe.” At each run, new data sequences of length 5000 bits (compared to 1000 bits for the other algorithms), new

additive white Gaussian noise vectors, as well as new channel realizations, are generated. We have experimented with longer data sequences (10 000–20 000 bits), but the results appear the same qualitatively. We also tested the CMOE algorithm on a CDMA system in which all users had the same power (ISR = 0 dB), and those results are shown with a curve “cmoe0.” Our simulation results suggest that the performance of the CMOE is seriously affected by the presence of noise and other users in the system. It should be also recognized that in scenarios when the channel length is unknown and has to be estimated, the performance of the CMOE would further degrade.

We have also compared our SOC method to the JADE [13] algorithm. The curves “SOC6” and “SOC7” represent our method when $\hat{\delta}$ parameter is set to be $\hat{\delta} = 0.6$ and $\hat{\delta} = 0.7$, respectively. The curve “jade” represents the JADE algorithm. For the SOC algorithm, we have used the desired user’s Gold code sequence as the nominal signature waveform \hat{s}_1 in (8). We can see in

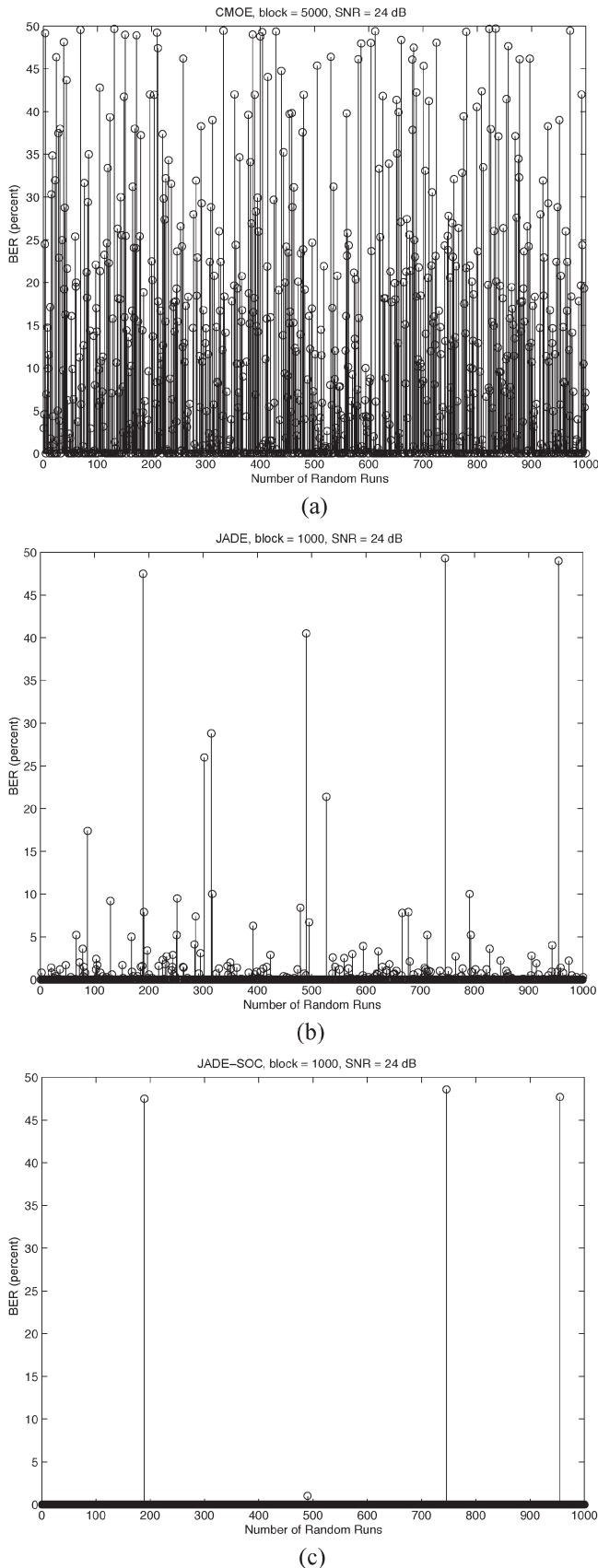


Fig. 4. Probability of error for different random runs. (a) CMOE. (b) JADE. (c) JADE-SOC.

Fig. 3(a) that this choice of nominal signature waveform is not appropriate, i.e., the actual received signature waveforms do not lie in the $\hat{\delta}$ vicinity of the chosen nominal signature waveforms. In other words, the norm-bounded channel distortion model is appropriate for communication systems with a strong line of sight and small multipath components, as derived in (7). For systems with severe presence of multipath components, we propose the algorithm discussed in Section IV-C.

C. JADE-SOC Methods

It is possible to combine JADE and SOC methods to achieve a better performance than what is possible by either method individually. Indeed, when operating alone, the JADE method may not identify the channel accurately due to the combined effect of noise, multiuser interference, and short sample size, while the SOC method may suffer from a poor choice of nominal signature waveform. However, when operating in tandem (JADE followed by SOC), the robustness of the SOC method can be used to mitigate the estimation error found in the estimates of the JADE method.

We have tested this combined approach: We first use the JADE algorithm to estimate the received signature waveform of the desired user, and then use it as the nominal signature waveform \hat{s}_1 in our formulation (8) of the SOC method. This combined approach (named JADE-SOC algorithm) outperforms the JADE, as shown by the curves “jade-soc015” and “jade-soc025” (corresponding to $\hat{\delta} = 0.15$ and $\hat{\delta} = 0.25$, respectively) in Fig. 3. This suggests that the robust SOC blind multiuser detector is able to correct the estimation errors caused by the JADE algorithm.

We can see in Fig. 3(b) that in most of the random runs, the received blocks in JADE-SOC algorithm had less than 25 corrupted bits per block. In particular, nearly 2500 blocks were successfully (error free) decoded. This is not true for the JADE algorithm. The given histogram [Fig. 3(b)] compares the performance of JADE-SOC to the JADE when SNR is set to 6 dB. Similar results have been obtained for other SNR values. If we set SNR to 24 dB, we can see in Fig. 4 that the JADE-SOC algorithm is able to successfully decode even those blocks for which the JADE algorithm has a BER of up to 40%. This clearly demonstrates the added value of our new robust blind multiuser detector. In contrast, the CMOE algorithm has a poor performance [see Fig. 4(a)].

We point out that the SOC method can be used in conjunction with any channel identification method (not just the JADE method), blind or nonblind. The extra robustness of the SOC method can be expected to partially mitigate the errors found in the channel estimates, thus leading to improved BER performance.

Finally, we remark that, in our simulations, solving each SOC problem (11) with the MATLAB tool SeDuMi [14] takes less than a second on a 600-MHz Pentium III PC.

V. CONCLUSION

In this correspondence, we have proposed a new robust blind multiuser detector for synchronous CDMA in the presence of

SWM. Our method is based on a robust formulation of the MOE detector using the SOC programming technique. The SOC formulation (11) is convex and can be efficiently solved by the recently developed interior point methods. Computer simulations indicate that the new SOC detector has a much better performance when compared to the existing multiuser detectors (robust or otherwise). Simulation results also show that the SOC detector can be used effectively in the dispersive propagation environment, provided that a reasonable estimate of the received signature waveform for the desired user is available.

ACKNOWLEDGMENT

The authors are grateful to B. Maričić for generating several simulations curves in Section IV.

REFERENCES

- [1] R. Lupas and S. Verdú, "Linear multiuser detector for synchronous code-division multiple-access channels," *IEEE Trans. Inf. Theory*, vol. IT-35, no. 1, pp. 123–136, Jan. 1989.
- [2] M. L. Honig, U. Madhow, and S. Verdú, "Blind adaptive multiuser detection," *IEEE Trans. Inf. Theory*, vol. IT-41, no. 4, pp. 944–960, Jul. 1995.
- [3] U. Madhow, "Adaptive signal processing for direct-sequence spread-spectrum CDMA," in *Proc. Int. Conf. Acoustics, Speech, and Signal Processing*, Atlanta, GA, 1996, pp. 1065–1068.
- [4] H. V. Poor, "Adaptive suppression of narrowband digital interferers from spread spectrum signals," in *Proc. Int. Conf. Acoustics, Speech, and Signal Processing*, Atlanta, GA, 1996, pp. 1061–1064.
- [5] K. Fukawa and H. Suzuki, "Orthogonalizing matched filter (OMF) detection for DS-CDMA mobile radio system," in *Proc. 1994 Global Telecommunications Conference (Globecom)*, San Francisco, CA, Nov. 28–Dec. 1 1995, pp. 385–389.
- [6] M. K. Tsatsanis and Z. Xu, "Performance analysis of minimum variance CDMA receivers," *IEEE Trans. Signal Process.*, vol. 46, no. 11, pp. 3014–3022, Nov. 1998.
- [7] U. Madhow, "Blind adaptive interference suppression for direct-sequence CDMA," *Proc. IEEE*, vol. 86, no. 10, pp. 2049–2069, Oct. 1998.
- [8] J. B. Schodorf and D. B. Schodorf, "A constrained optimization approach to multiuser detection," *IEEE Trans. Signal Process.*, vol. 45, no. 1, pp. 258–262, Jan. 1997.
- [9] D. Gesbert and A. Paulraj, "Blind multi-user linear detection of CDMA signals in frequency selective channels," in *Proc. 1998 IEEE Int. Conf. Communications*, Atlanta, GA, vol. 3, pp. 1335–1339.
- [10] X. Wang and H. V. Poor, "Robust multiuser detection in non-Gaussian channels," *IEEE Trans. Signal Process.*, vol. 47, no. 2, pp. 289–305, Feb. 1999.
- [11] Y. Nesterov and A. Nemirovsky, "Interior-point polynomial methods in convex programming," in *Studies in Applied Mathematics*, vol. 13. Philadelphia, PA: SIAM, 1994.
- [12] M. Honig and M. K. Tsatsanis, "Adaptive techniques for multiuser CDMA receivers," *IEEE Signal Process. Mag.*, vol. 49, no. 2, pp. 49–61, May 2000.
- [13] J.-F. Cardoso and A. Souloumiac, "Blind beamforming for non-Gaussian signals," *Proc. Inst. Elect. Eng.*, pt. F, vol. 140, no. 6, pp. 362–370, Dec. 1993.
- [14] J. F. Sturm, "Using Sedumi 1.02, a Matlab toolbox for optimization over symmetric cones," *Optim. Methods Softw.*, vol. 11–12, no. 1–4, pp. 625–653, Aug. 1999 [Online]. Available: <http://fewcal.kub.nl/sturm/software/sedumi.html> for updates.