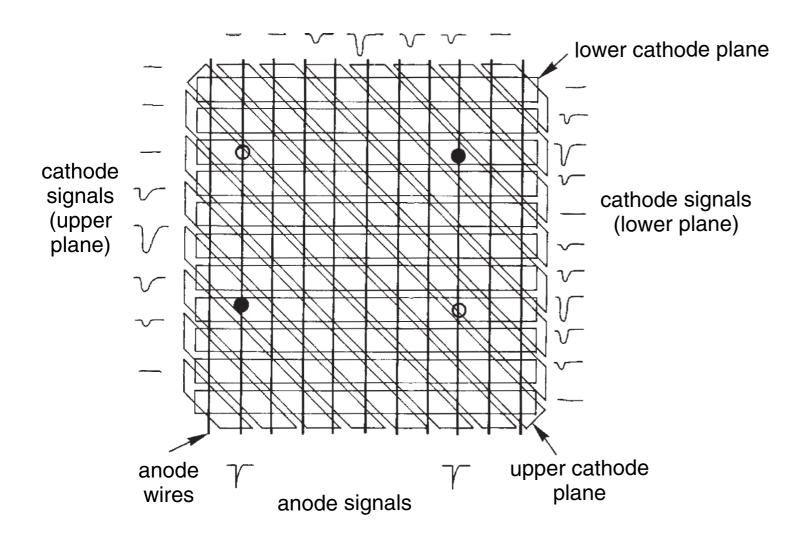
Multi-Wire Proportional Chamber (MWPC)

MWPC ...

substantial functionality improvement due to cathode strips/pads ...



Cathode readout yields:

2-dim. information true 2d: use pads ...

high spatial resolution due to center of gravity reconstruction

resolving ambiguities using second strip pattern or pads

Can wires be avoided?

Micro-strip Gas Chambers (MSGC)

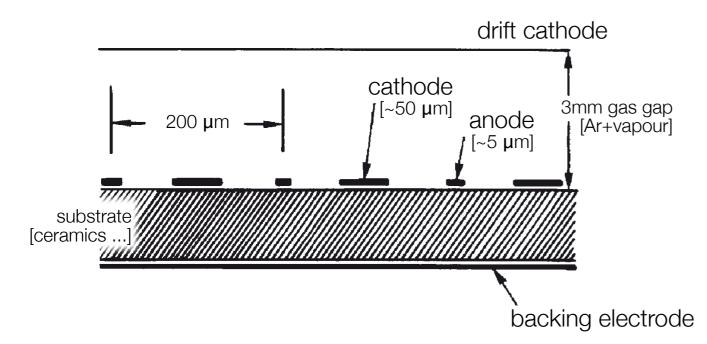
Can one avoid wires?

Anode realized via microstructures on dielectrics ...

Simple construction (today) Enhanced stability & flexibility Improved rate capabilities

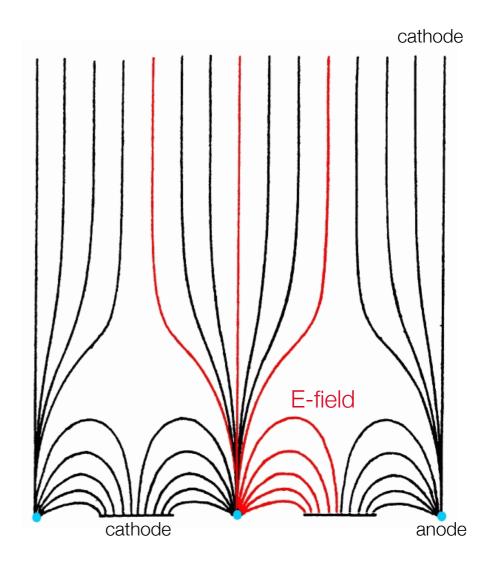
First MSGCs developed in 1990ies ...

Problems: charging of isolation structure [> time-dependent gain; sparks, anode destruction]



Schematics of MSGC field lines

high field directly above anode ions drift only 100 µm; yields low dead time ...



Micro-strip Gas Chambers (MSGC)

MSGCs prone to aging problems ... Solution: intermediate grid ...

e.g.: Micromegas
GEM detectors [Sauli, 1997]

Micromegas:

Fine cathode mesh collects ions still fast; no wires ...

GEM (Gas Electron Multiplier):

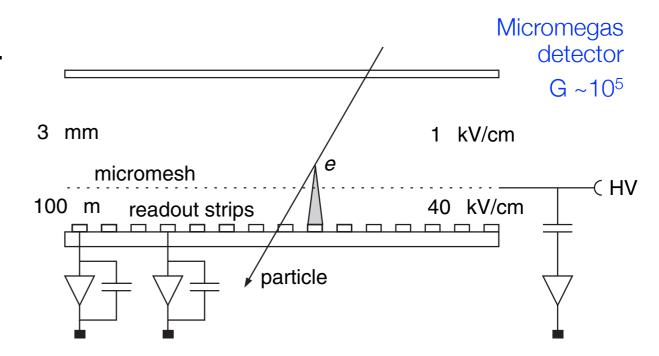
Thin insulating kapton foil coated with metal film ...

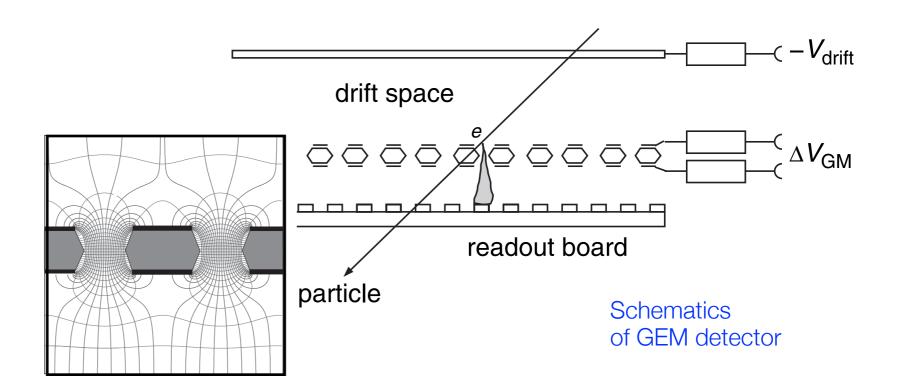
Contains chemically produced holes [100-200 µm]

Electrons are guided by high electric drift field of GEMs ...

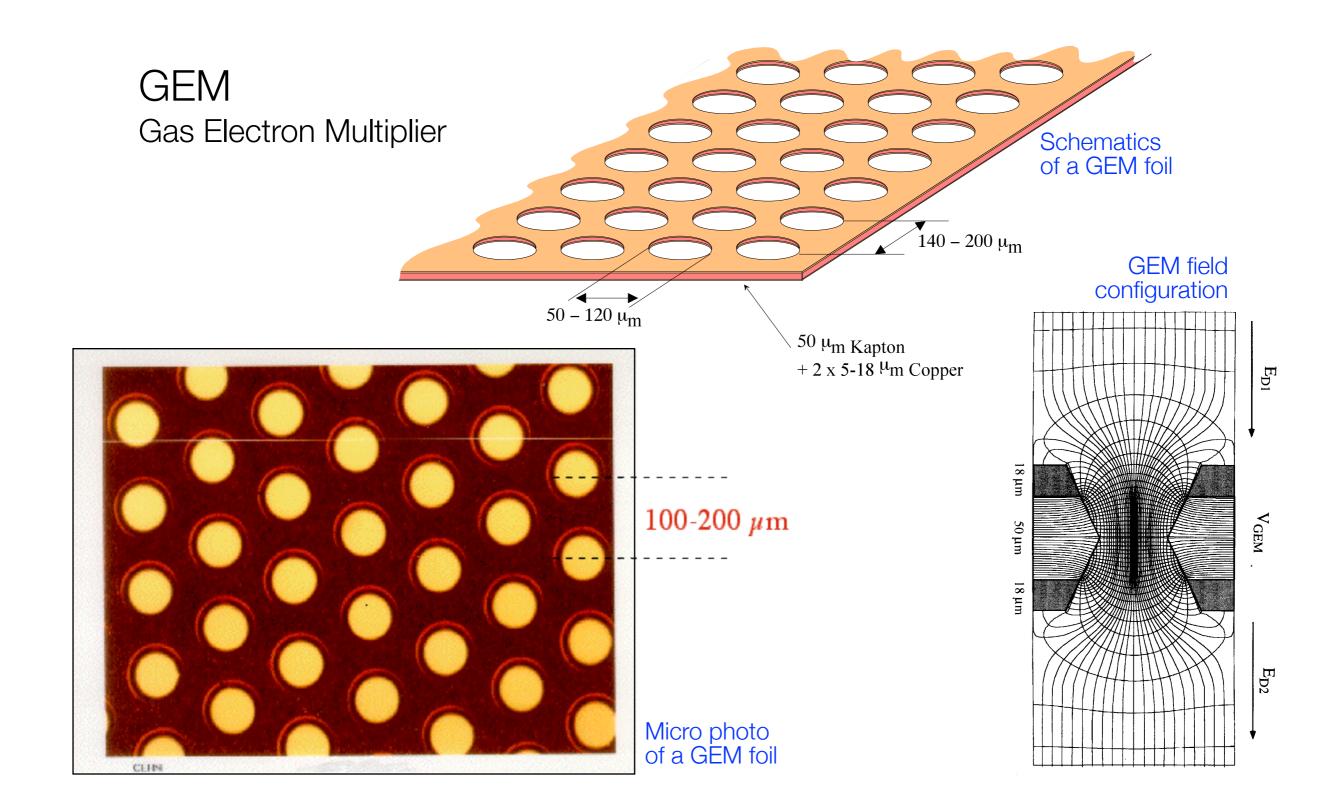
Avalanche production ...

Electrons drift to anode GEM collects ions





Micro-strip Gas Chambers (MSGC)



Ionization Chambers - Signal Shape

Pulse mode operation

derive signal for single ionizing particle $[R = \infty]$

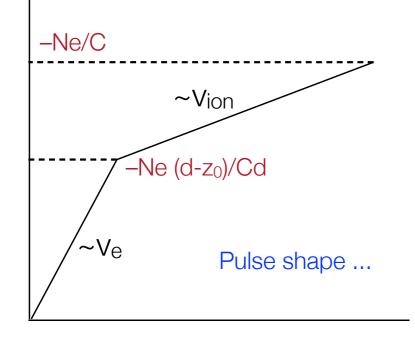
$$\begin{split} W &= \frac{1}{2} C U^2 = \frac{1}{2} C U_0^2 - N \int_{z_0}^{z_f} q E_z dz \\ &= \frac{1}{2} C U_0^2 - N_+ q_+ \frac{U_0}{d} (z_+ - z_0) + N_- q_- \frac{U_0}{d} (z_- - z_0) \end{split}$$

$$U = U_0 + \Delta U$$
 $U^2 = U_0^2 + 2\Delta U U_0 + \Delta U^2$

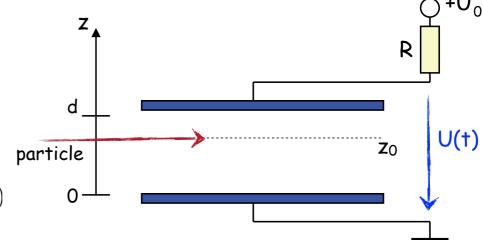
$$\Delta U = -\frac{N_{+}q_{+}}{Cd}(d-z_{0}) + \frac{N_{-}q_{-}}{Cd}(0-z_{0}) = \Delta U_{-} + \Delta U_{+}$$

$$\frac{N_{-}q_{-}}{Cd}(0-z_{0}) = \frac{N_{-}q_{-}}{Cd}(0-z_{0}) = \frac{N_{-}q_{0}}{Cd}(0-z_{0}) = \frac{N_{-}q_{-}}{Cd}(0-z_{0}) = \frac{N_{-}q_{-}}{Cd$$

 $= -\frac{N}{Cd} [e(d - z_0) - e(0 - z_0)] = -\frac{Ne}{C}$



 $-\Delta \cup$



Schematic view of an ionization chamber

Final signal independent of ionization position and of detector dimension ... [see also Geiger counter]

Time evolution of pulse height:

$$z(t) = v_D \cdot t$$

$$\Delta U = -\frac{Ne}{Cd} \left(v_D^{\rm e} + v_D^{\rm ion} \right) t \qquad \text{with:}$$

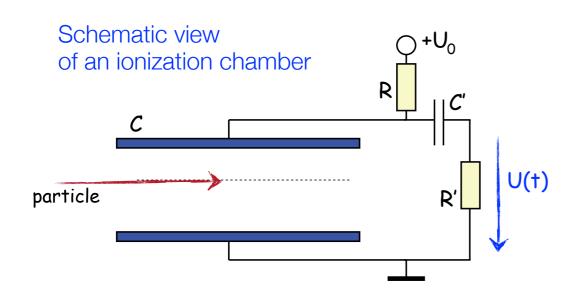
$$v_D^{\rm e} \approx 1000 \cdot v_D^{\rm ion}$$

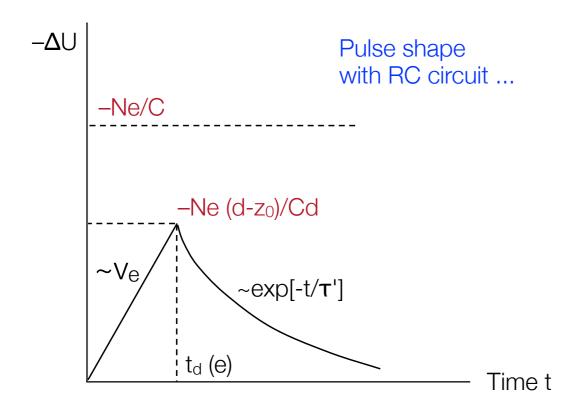
Typical:

$$v_{d,e} = 4 \text{ cm/} \mu \text{s}$$

 $v_{d,ion} = 4 \text{ cm/ms}$

Ionization Chambers - Signal Shape





Pulse mode operation [Use RC circuit; R finite]

Response time of chamber: $\tau = RC$

Must be sufficiently large with respect to t_{signal}

Example: 2 x 2 x 10 cm³ chamber

Electron drift time: $t_{max} = d/v_{d,e} = 2cm/4cm/\mu s = 500 \text{ ns}$

Ion drift time: $t^+_{max} = d/v_{d,ion} = 500 \mu s$

Suppress ion signal by C'R' high pass filter with time constant $\tau'=R'C'$

Chose: $t^-_{max} < \tau' < t^+_{max}$

Ex.:
$$\tau' = 1 \mu s$$

 $C = 1 pF, R = 10 M\Omega$
 $C' = 1 pF, C_{tot} = CC'/(C+C') = 0.5 pF$
 $R' = \tau/C = 1 \mu s/0.5 pF = 2 M\Omega$

Features:

linear rise; exponential fall dead time $T_{dead} \approx \tau$ ' position dependent pulse height position dependent resolution

Ionization Chambers – Frisch Grid

Removal of position dependent signal ...

[O. Frisch, 1944]

Principle:

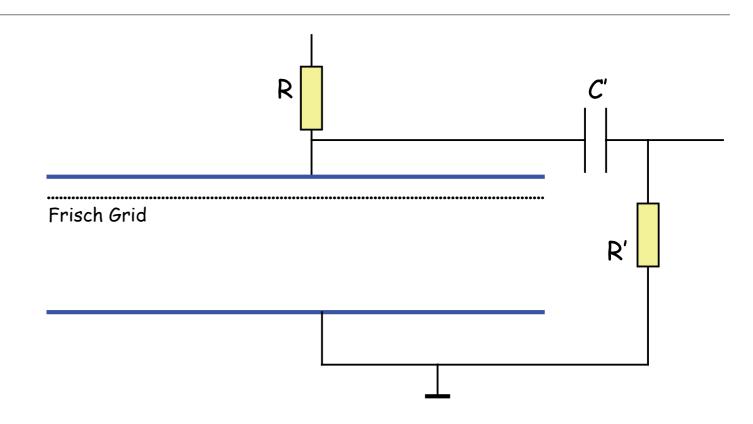
Introduce wire plane at intermediate potential ...

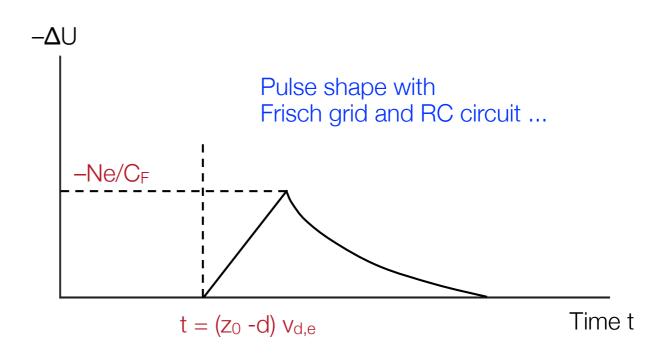
Shielding of induced charges Wire plane transparent to electrons

Signal on anode only generated by electrons that have passed the Frisch grid

All electrons appear at the same distance thus: no position dependence ...

Difficulty: Small signals ... Need sensitive, low-noise pre-amplifiers ...





Ionization Chambers - Music II

Parameters:

gas P10 (Ar/Methan 90/10)

pressure 1 atm

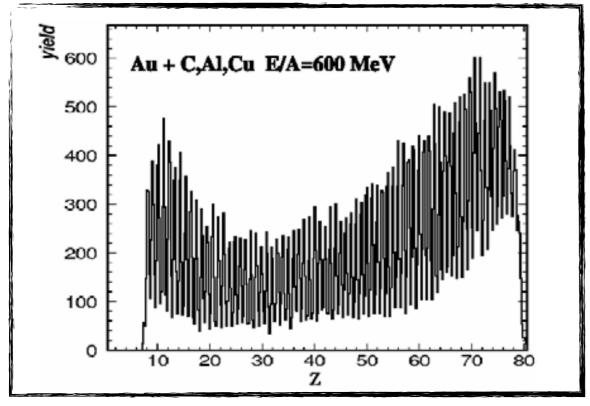
active area 102 x 60 cm²

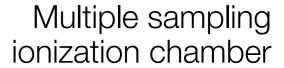
depth 51 cm electric field 150 V/cm

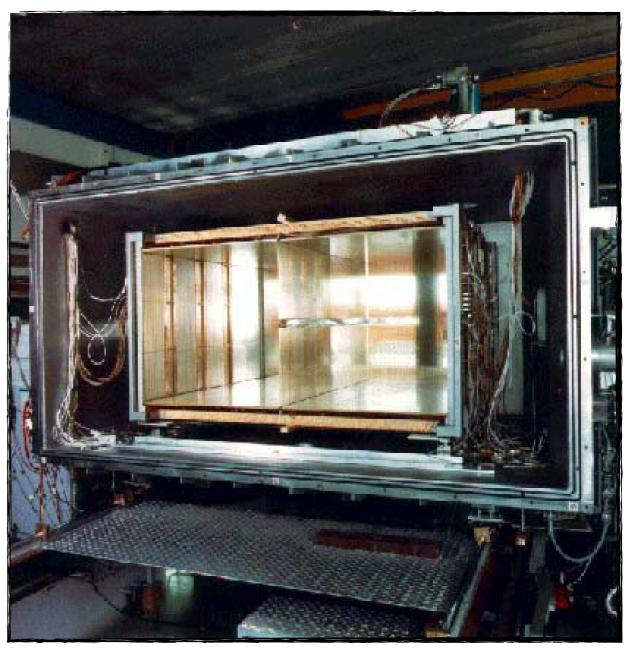
potential 9 kV

ionization 70 Z² pairs/cm drift velocity 5 cm/µsec

Fragment charge spectrum







Ionization Chambers - Na 48

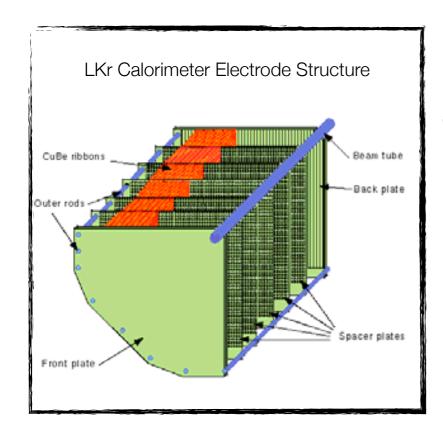
Liquid Krypton Ionization Chamber

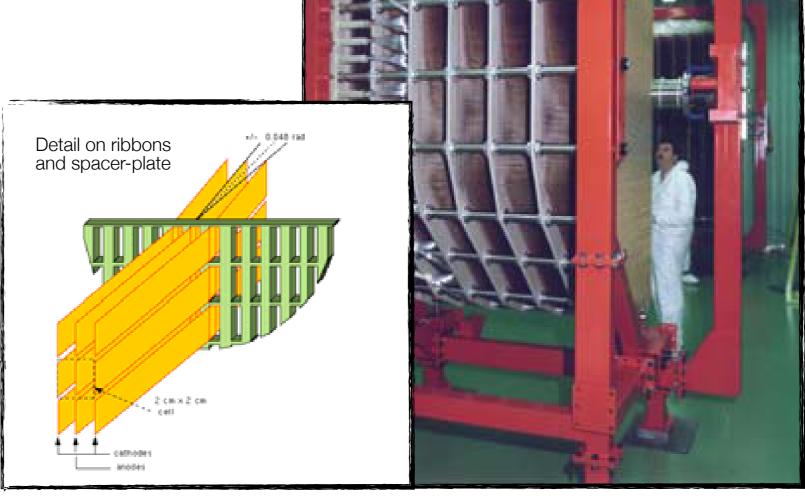
Homogeneous LKr; gain = 1

184 cells formed by thin electrodes; cell size: 2x2 cm²

Each cell formed by two drift gaps sharing readout electrode

Electrodes: CuBe ribbons





Drift Chambers - Principle

Measure drift time t_D [need to know t₀; fast scintillator, beam timing]

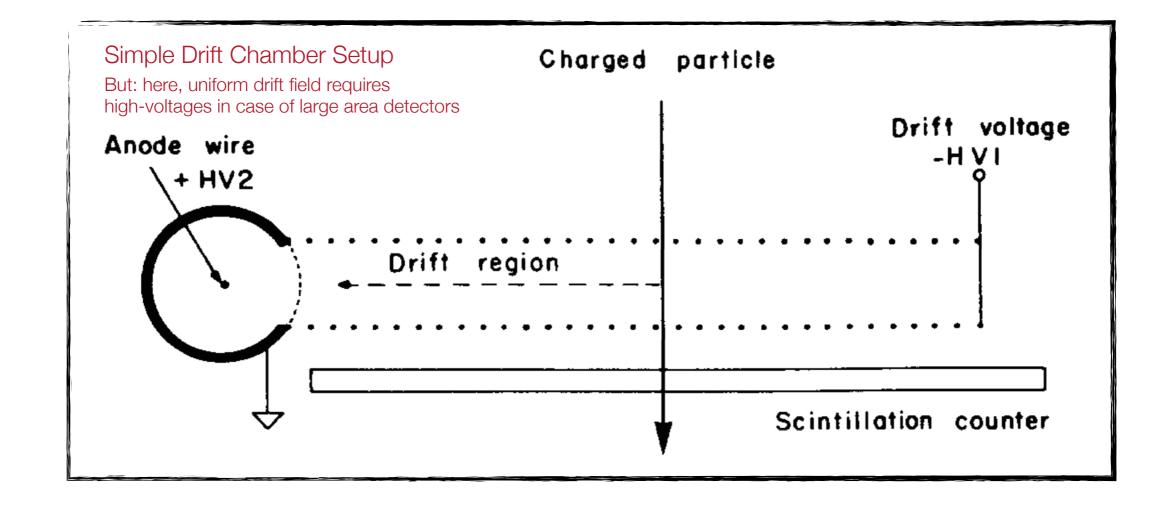
Determine location of original ionization:

$$x = x_0 \pm v_D \cdot t_D$$
$$y = y_0 \pm v_D \cdot t_D$$

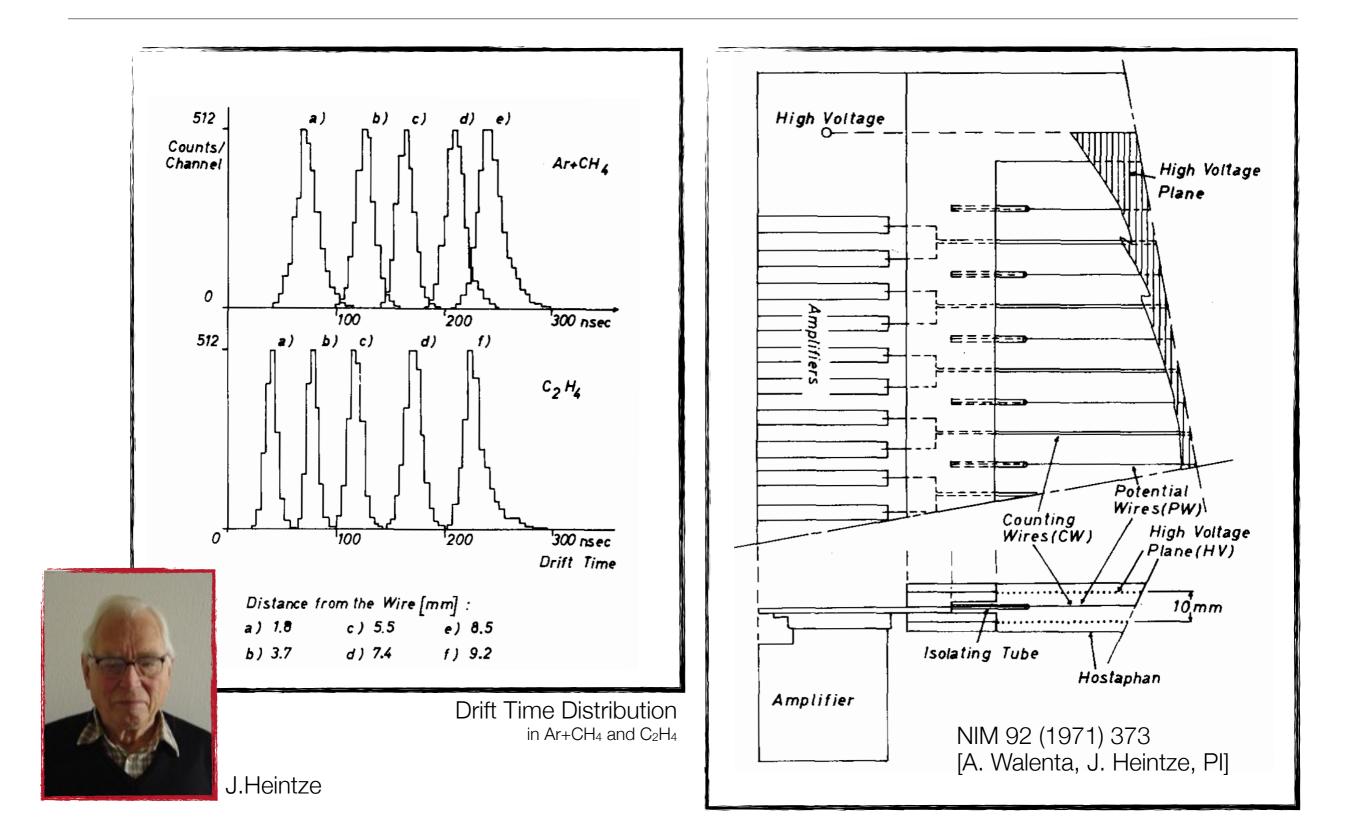
If drift velocity changes along path: $x = \int_0^{t_D} v_D \, dt$

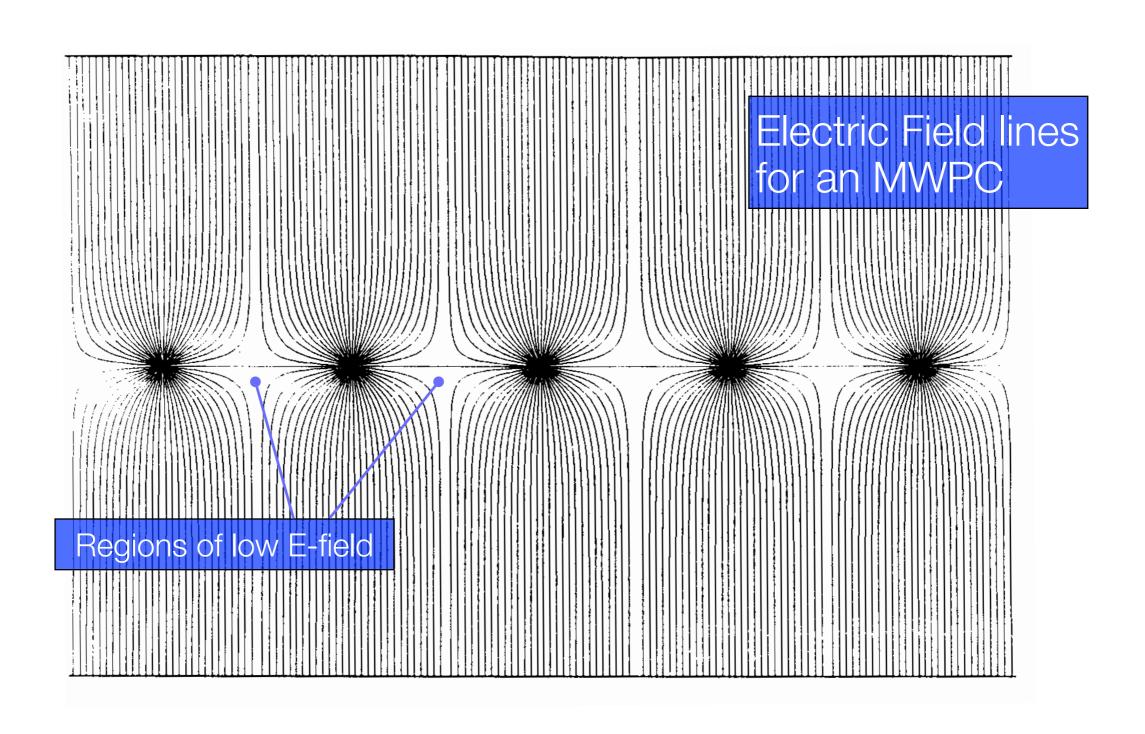
In any case:

Need well-defined drift field ...



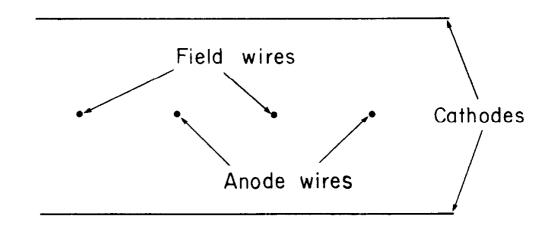
Drift Chambers – The First One





Modified MWPC ...

Introduce field wires to avoid low field regions, i.e. long drift-times



Field wires are at negative potential ...

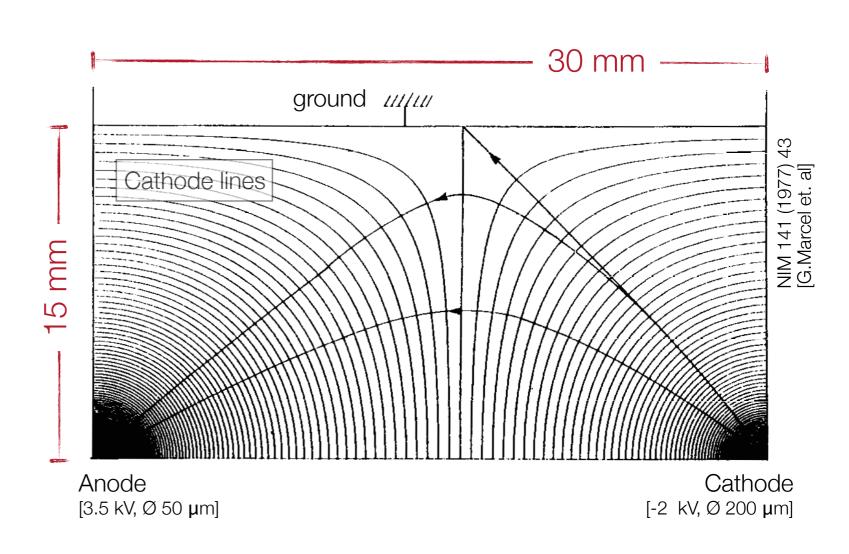
Anode wires are at positive potential ...

Cathode planes are at zero potential ...

But:

Uniform drift field requires: Gap length/wire spacing ≈ 1

i.e. for typical convenient wire spacing one needs thick chambers ...



Principle of an adjustable field multi-wire drift chamber

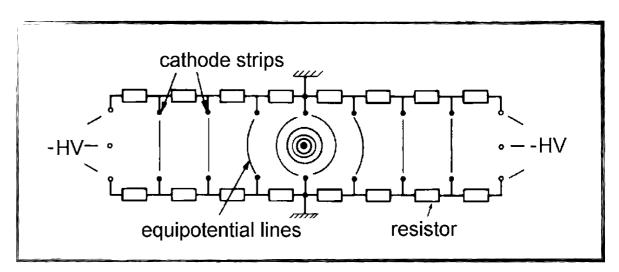
Introduction of voltage divider via cathode wire planes ...

Features:

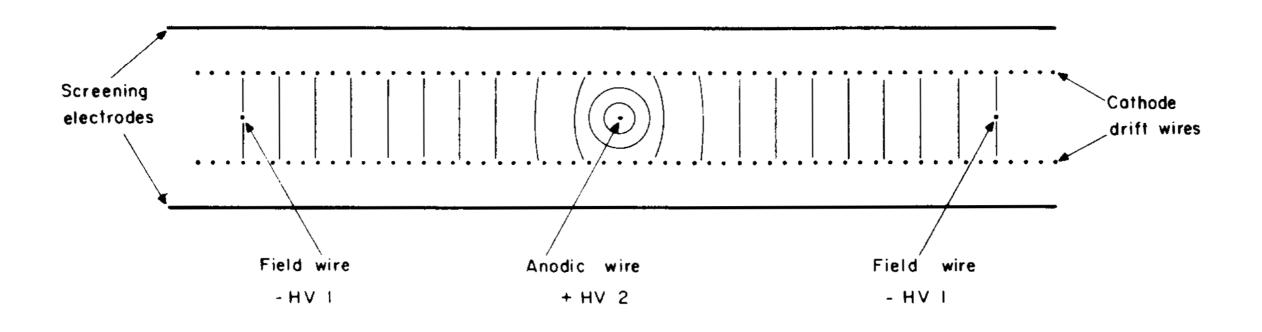
very few (or only one) anode wires

space point resolution limited by mechanical accuracy [for large chambers: $\sigma \approx 200 \ \mu m$]

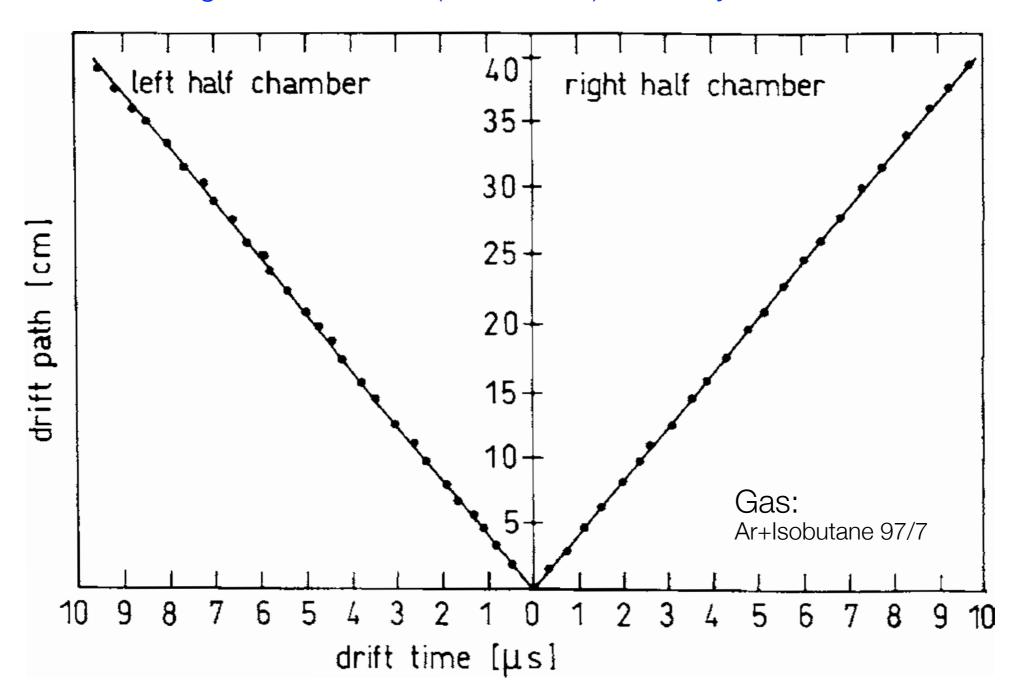
But: hit density needs to be low.



Schematics of voltage divider chain



Drift time space relation for a large drift chamber (80x80 cm²) with only one anode wire

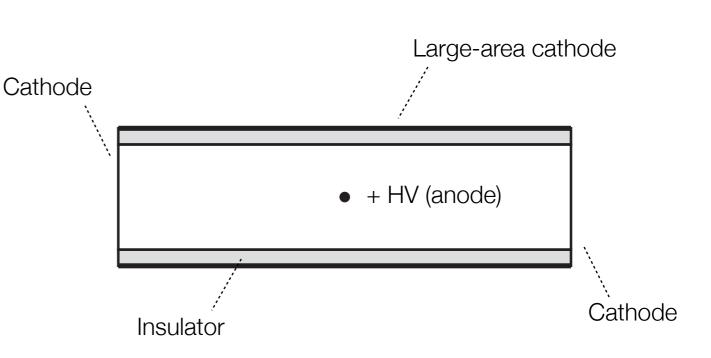


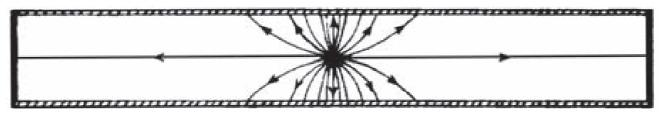
Alternative:

Field formation by charging (insulated) chamber walls with ions ...

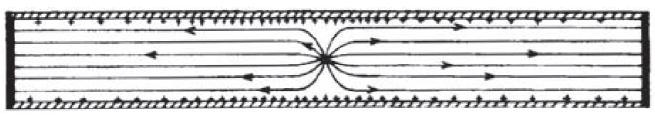
Electrodeless drift chamber [Allison et al., 1982]

Requires some charging time ...

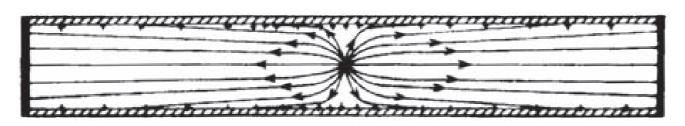




Before charging up: field line end at cathode ...

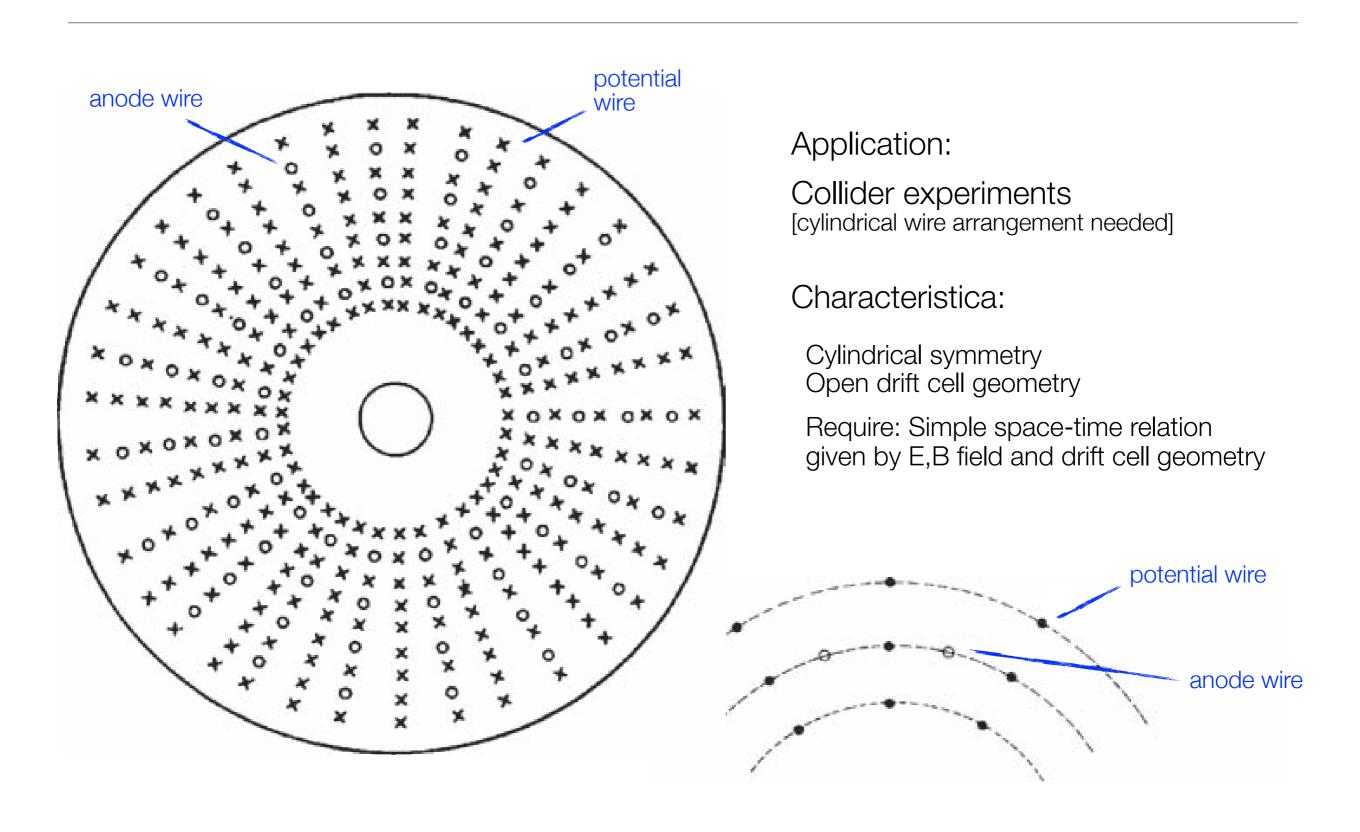


After charging time: no field line end at cathode ...

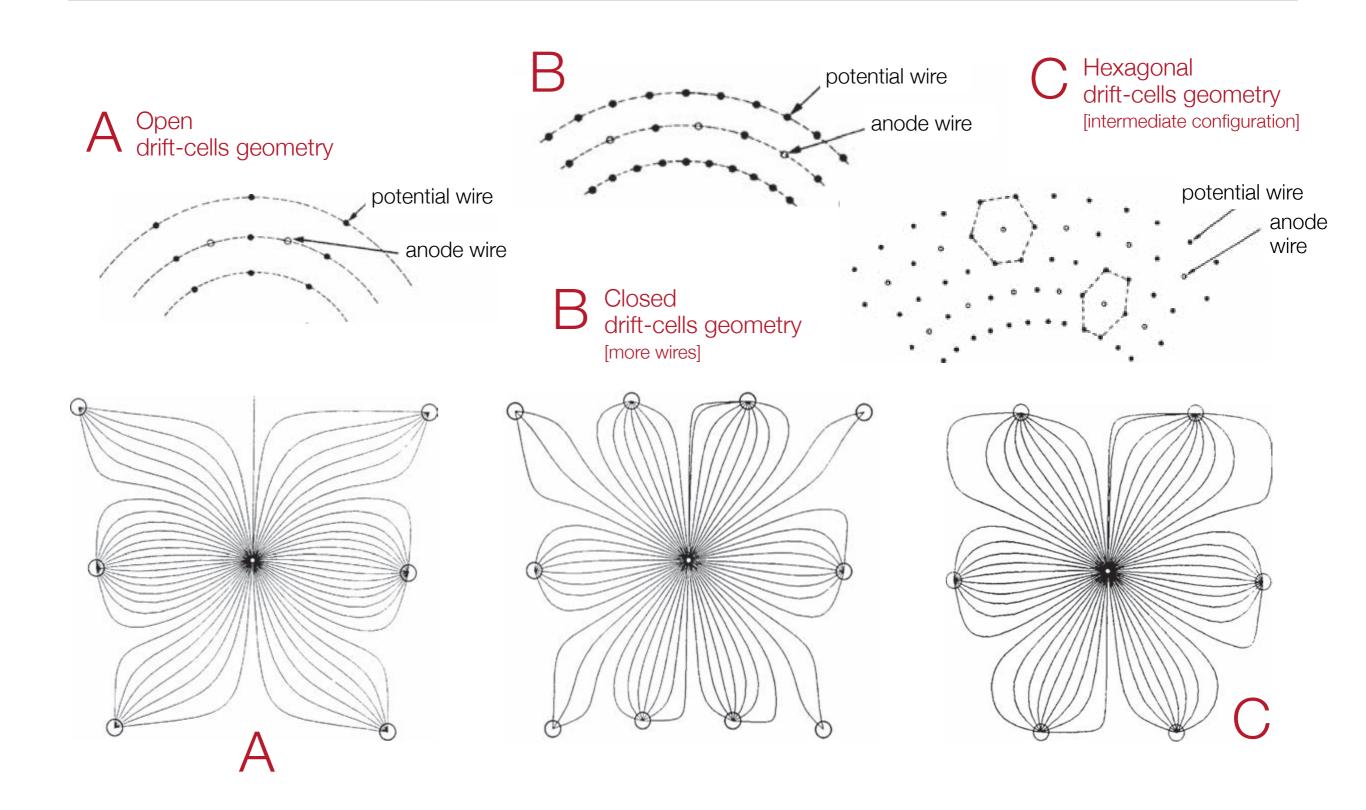


To avoid overcharging: Finite resistance of insulator [i.e. some field lines end at cathode]

Cylindrical Drift Chambers



Cylindrical Drift Chambers

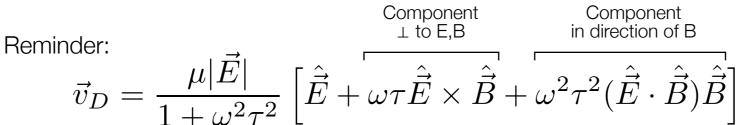


Drift Chambers - Lorentz Angle

Require B field for momentum measurement ...

In general drift field E ⊥ to B field ...

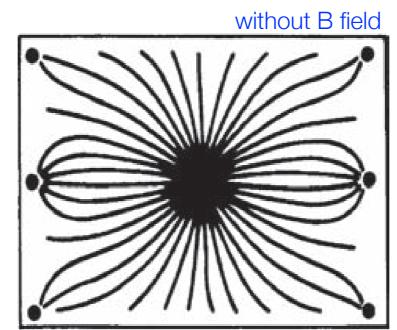
→ Lorentz angle:
$$\alpha_L = \langle (\overrightarrow{V_D}, \overrightarrow{E}) \dots \rangle$$

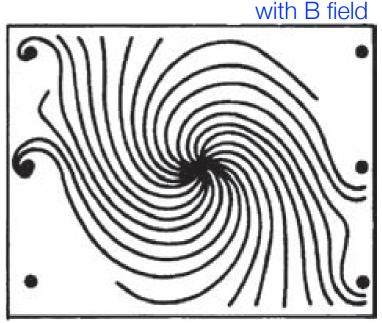


Using:

$$v_{D,x} = \frac{\mu E}{1 + \omega^2 \tau^2}$$
$$v_{D,y} = \frac{\mu E}{1 + \omega^2 \tau^2} \cdot \omega \tau$$

$$\Rightarrow \tan \alpha_L = \omega \tau \\ = v_D \frac{B}{E}$$
 [with $\omega = \frac{eB}{m}$ and $\tau = \frac{mv_D}{eE}$]





Lorentz angle

 $\overrightarrow{\mathsf{V}}_\mathsf{D}$

Drift Chamber - Spatial Resolution

Resolution determined by accuracy of drift time measurement ...

Influenced by:

Diffusion [$\sigma_{\text{Diff.}} \sim \sqrt{x}$]

see above: $\sigma^2 \sim 2Dt = 2Dx/v_D \sim x \dots$

δ-electrons [σ_{δ} = const.]

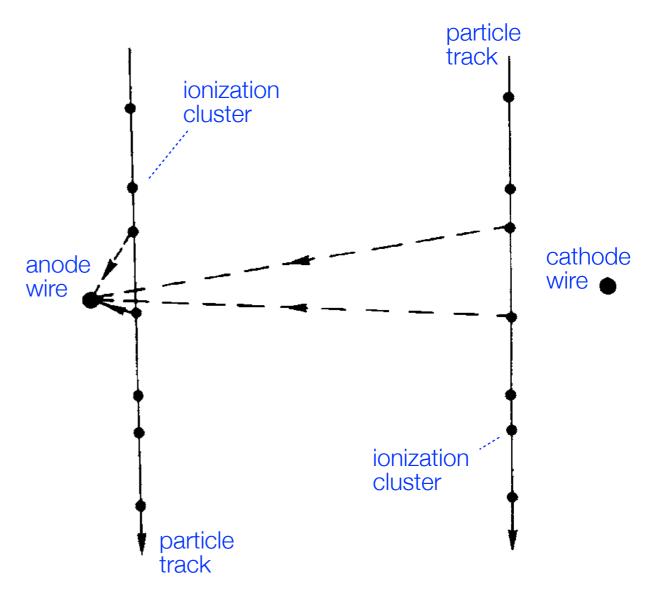
independent of drift length; yields constant term in spatial resolution ...

Electronics [$\sigma_{\text{electronics}} = \text{const.}$]

contribution also independent of drift length ...

Primary ionization statistics $[\sigma_{prim} = 1/x]$

Spatial fluctuations of charge-carrier production result in large drift-path differences for particle trajectories close to the anode ... [minor influence for tracks far away from anode]



Drift Chamber - Spatial Resolution

Primary ionization statistics:

Step 1: Consider a track passing through an anode wire ...

Probability of no ionization within distance d:

$$P_0(d) = e^{-2Nd}$$

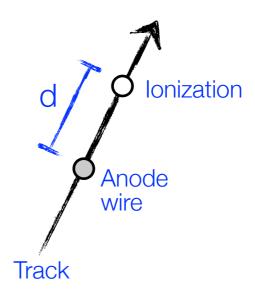
N: number of ionizations per unit length

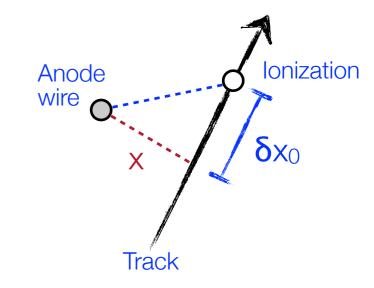
Normalization

Average minimum distance of closest ionization cluster:

$$\delta x_0 = \langle d_{\min} \rangle = \int_0^{\infty} x e^{-2Nx} \, 2N \, dx = \frac{1}{2N}$$

$$\sigma_{\langle d_{\min} \rangle}^2 = \int_0^{\infty} (x - \frac{1}{2N})^2 e^{-2Nx} \, 2N \, dx = \frac{1}{4N^2}$$





Step 2: Track at distance x ...

$$\delta x = \sqrt{x^2 + (\delta x_0)^2} - x = x \left(\sqrt{1 + \left(\frac{\delta x_0}{x}\right)^2} - 1 \right) \approx \frac{x}{2} \left(\frac{\delta x_0}{x}\right)^2 \propto \frac{1}{x}$$

Drift Chamber - Spatial Resolution

$$\sigma_x^2 = \left(\frac{1}{64N^2}\right) \cdot \frac{1}{x^2} + \frac{2D}{v_d} \cdot x + \sigma_{\text{const}}^2$$

$$\frac{1^{\text{st ionization statistics}}}{1^{\text{st ionization statistics}}} \cdot \frac{1}{v_d} \cdot x + \sigma_{\text{const}}^2$$

Possible improvements:

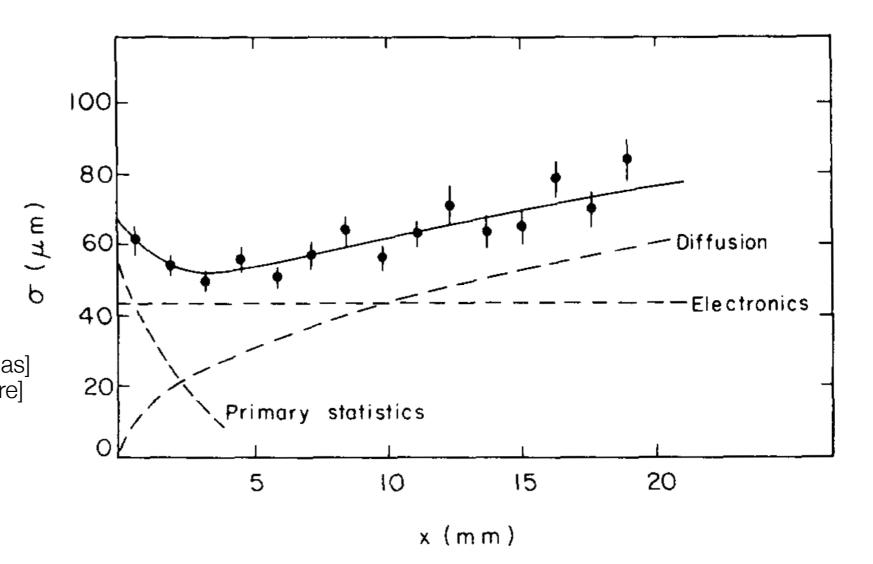
Increase N by increasing pressure ...

Decrease D by increasing pressure ...

$$D \sim \frac{\lambda_0^2}{\tau} \sim \frac{1/n^2}{1/n} \sim \frac{1}{n}$$

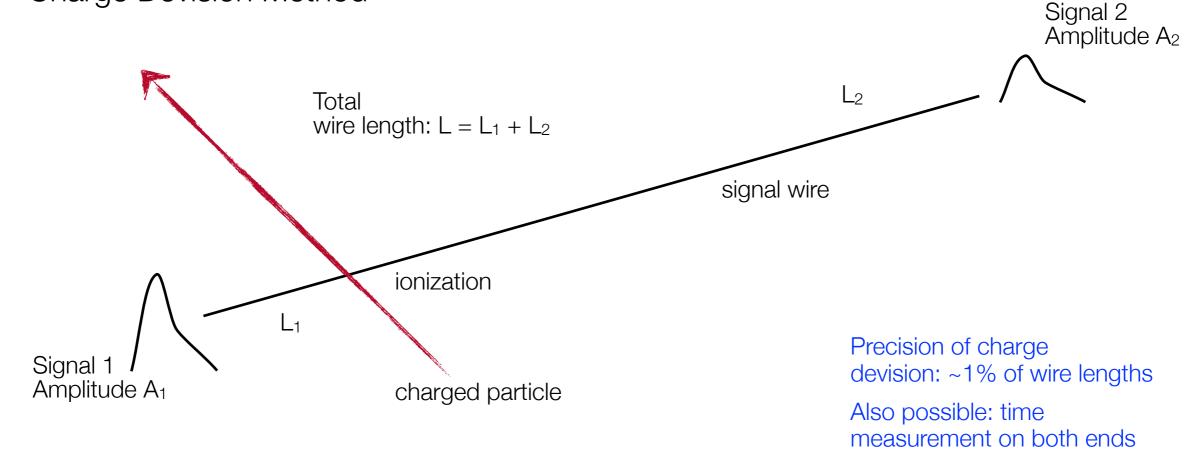
[n: particle density in gas] [increases with pressure]

i.e.: increase pressure ... [up to 4 atm possible]



Drift Chamber – Determination of z

Principle of Charge Devision Method



Determination of L₁, L₂:

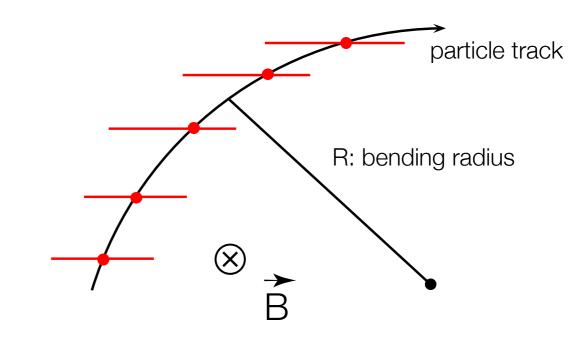
$$L_2 = \frac{A_1}{A_1 + A_2} \cdot L$$
 $L_1 = \frac{A_2}{A_1 + A_2} \cdot L$

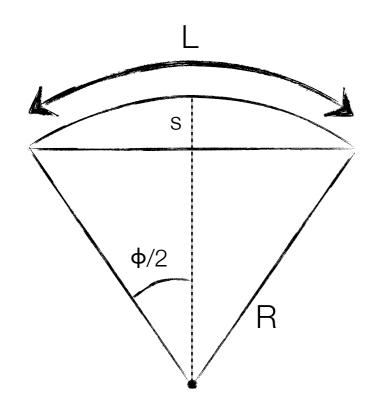
Momentum determination

in a cylindrical drift chamber ...

$$\frac{mv^2}{R} = evB \quad \rightarrow \quad p = eB \cdot R$$

$$p\left[\frac{\text{GeV}}{c}\right] = 0.3B \,[\text{m}] \cdot R \,[\text{T}]$$





For Sagitta s:

$$s = R - R\cos\frac{\phi}{2} \approx R\frac{\phi^2}{8} \qquad \text{with } \phi = \frac{L}{R}$$

$$s = R\frac{L^2}{8R^2} = \frac{L^2}{8R} \quad \text{and} \quad R = \frac{L^2}{8s}$$

$$\Rightarrow \quad \frac{\Delta p}{p} = \frac{\Delta R}{R} = \frac{L^2}{8Rs} \cdot \frac{\Delta s}{s}$$

Momentum measurement

uncertainty:

$$\frac{\sigma_p}{p} = \frac{L^2}{8Rs} \cdot \frac{\sigma_s}{s} = \frac{L^2}{8R} \cdot \frac{\sigma_s}{L^4/64R^2} = \frac{\sigma_s}{L^2} \cdot 8R = \frac{\sigma_s}{L^2} \cdot \frac{8p}{eB} \sim p \cdot \frac{\sigma_s}{BL^2}$$

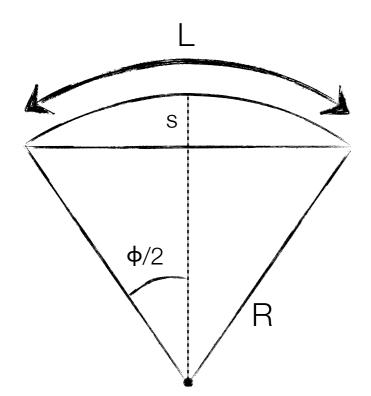
Uncertainty σ_s depends on number and spacing of track point measurements; for equal spacing and large N:

$$\sigma_s = \frac{\sigma_{r\phi}}{8} \sqrt{\frac{720}{N+5}} \quad \text{see: Glückstern, NIM 24 (1963) 381 or}$$

Blum & Rolandi, Particle Detection ...

Good momentum resolution:

- large path length L
- large magnetic field B
- good Sagitta measurement



Multiple scattering contribution:

Reminder:

$$\sigma_{\phi} = \frac{13.6 \text{MeV}}{\beta cp} z \sqrt{x/X_0} \left[1 + 0.038 \ln(x/X_0) \right]$$

$$\sigma_{\phi} \approx \frac{14~{\rm MeV}/c}{p} \sqrt{\frac{L}{X_0}} \quad {\rm and} \quad \frac{\sigma_p}{p} = \frac{\sigma_R}{R} = \frac{\sigma_{\phi}}{\phi}$$
 as $R =$

Multiple scattering contribution:

[cont'd]

$$\frac{\sigma_p}{p} = \frac{\sigma_\phi}{\phi} = \frac{14 \text{ MeV}/c}{p} \sqrt{\frac{L}{X_0}} \cdot \frac{R}{L} = \frac{14 \text{ MeV}/c}{p} \sqrt{\frac{1}{LX_0}} \cdot \frac{p}{eB} \sim \frac{1}{\sqrt{LX_0}B}$$

 σ_p/p [%]

Generally pt measured:

$$\left(\frac{\sigma_{p_t}}{p_t}\right)^2 = \text{const} \cdot \left(\frac{p_t}{BL^2}\right)^2 + \text{const} \cdot \left(\frac{1}{B\sqrt{LX_0}}\right)^2$$

For momentum p:

$$\left(\frac{\sigma_p}{p}\right)^2 = \left(\frac{\sigma_{p_t}}{p_t}\right)^2 + \left(\frac{\sigma_{\theta}}{\sin \theta}\right)^2$$

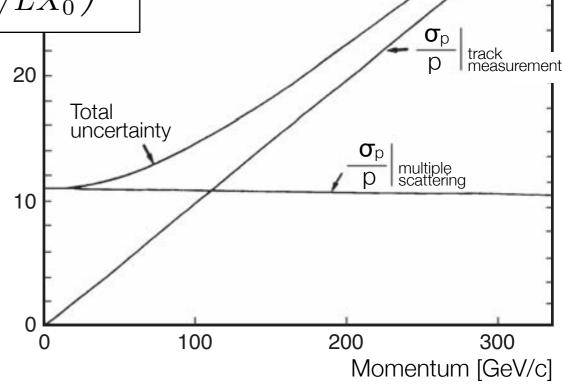
$$\text{using } p = \frac{p_t}{\tan \theta}$$

Examples:

Argus: $\sigma_{pt}/p_t = 0.009^2 + (0.009 p_t)^2$

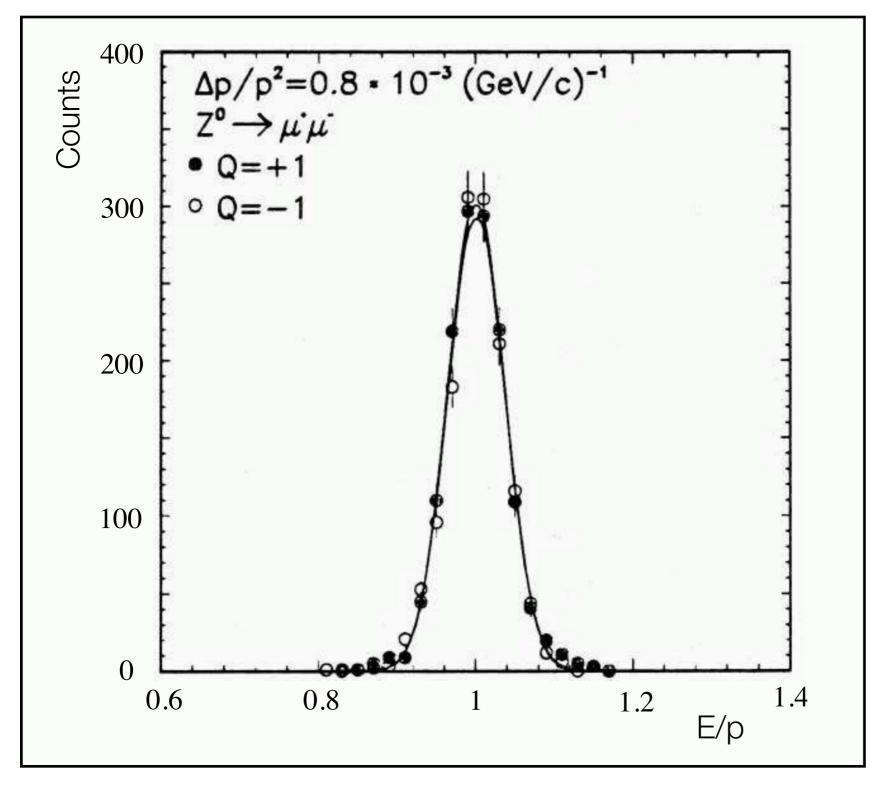
ATLAS: $\sigma_{pt}/p_t = 0.001^2 + (0.0005 p_t)^2$

[ATLAS nominal; TDR]



momentum

independent

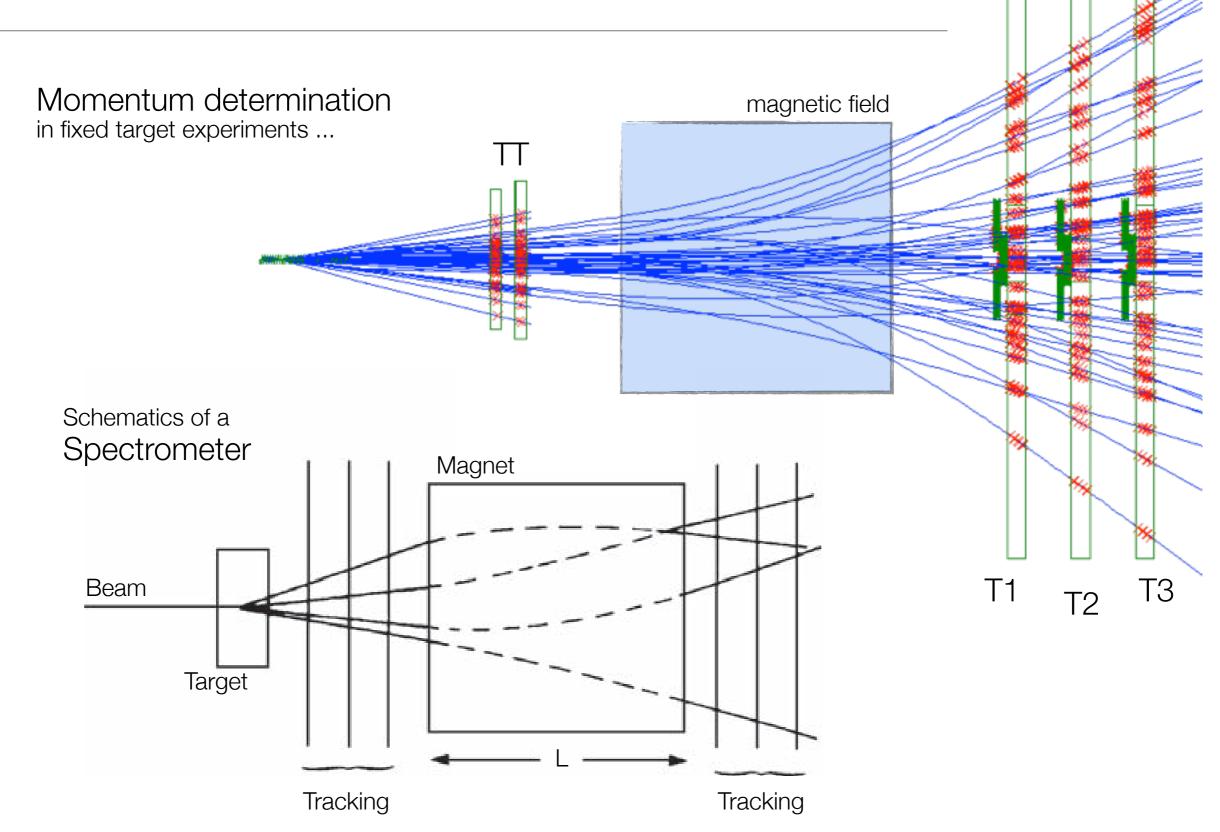


Momentum resolution for muons in $Z \rightarrow \mu\mu$

s ~ 1/R ~ 1/p measured! → 1/p is Gaussian

LHCb Tracking

Magnetic Spectrometer Resolution

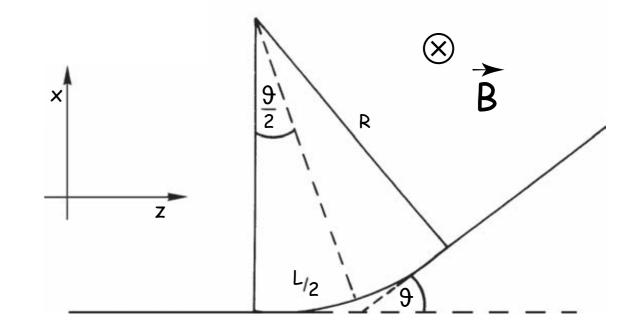


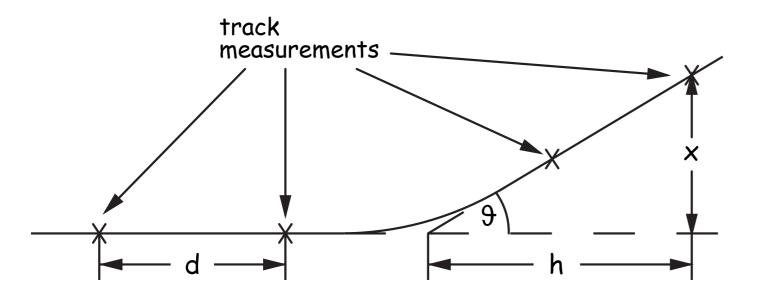
Momentum determination

in fixed target experiments ...

$$p = eRB \qquad \vartheta = L/R$$
$$= L/p \cdot eB$$
$$p = eB \cdot L/\vartheta$$

Momentum resolution:





Determination of σ_p/p :

$$\vartheta = \frac{x}{h} \qquad \sigma_{\vartheta} = \frac{\sigma_{x}}{h}$$
$$\frac{\sigma_{p}}{p} = \frac{\sigma_{\vartheta}}{\vartheta} = \frac{\sigma_{x}}{h} \cdot \frac{p}{eBL}$$

Long lever arm improves momentum resolution ...

Drift Chambers – Ambiguities

Particle track

Difficulty:

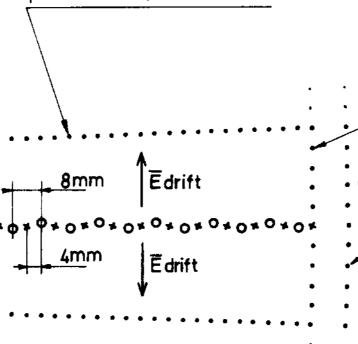
Time measurement cannot distinguish whether particle has passed right or left from a wire ...

"Left-Right Ambiguity"

Solution: "Staggered wires"

Use multiple (two) layers displaced relative to each other ...

r -702 mm



(cathode) drift field wires at

potential -V(r) = -ar - b

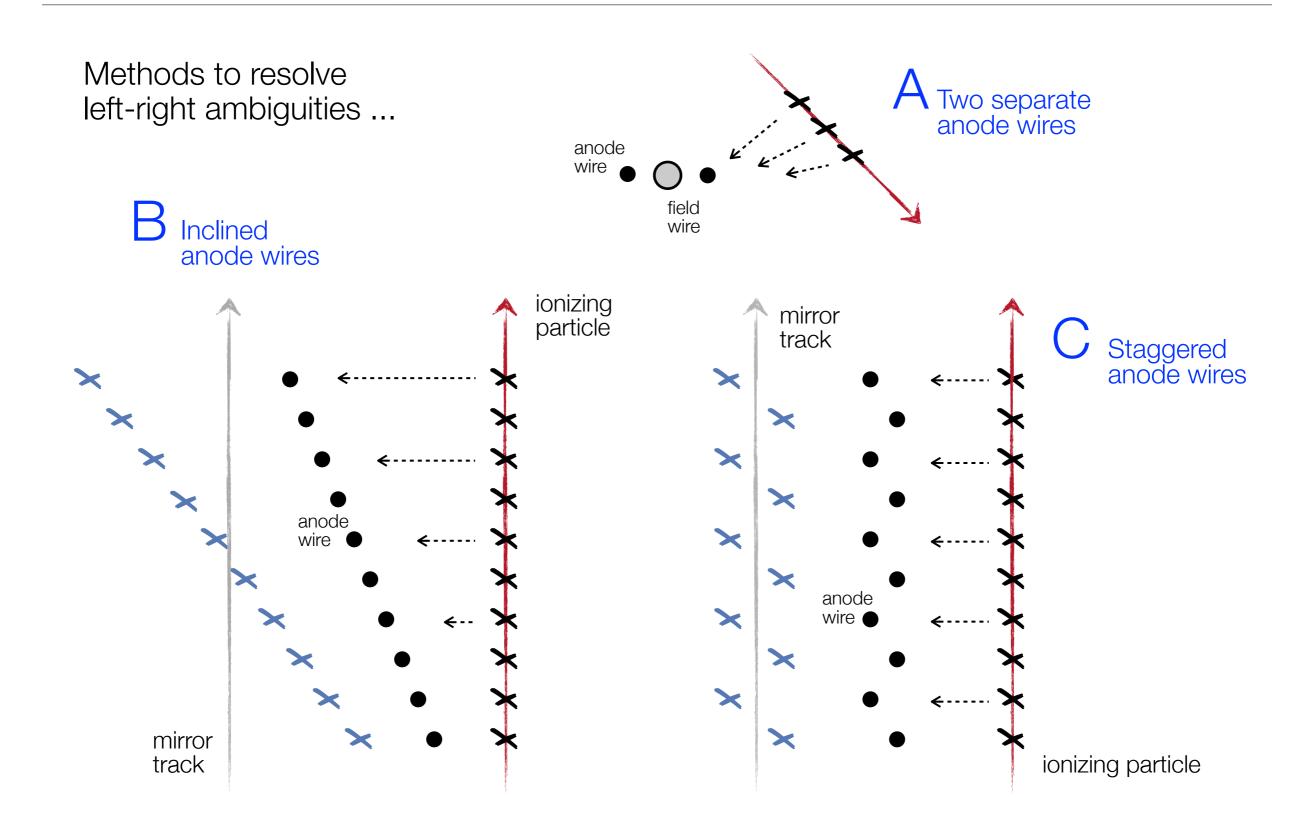
Staggered wires

field shaping wires
at potential -Vn

Staggering in a cylindrical drift chamber [see later]

grounded guard

Drift Chambers – Ambiguities



Aging in Wire Chambers

Avalanche formation can be considered as micro plasma discharge.

Consequences:

Formation of radicals i.e. molecule fragments Polymerization yields long chains of molecules Polymers may be attached to the electrodes Reduction of gas amplification

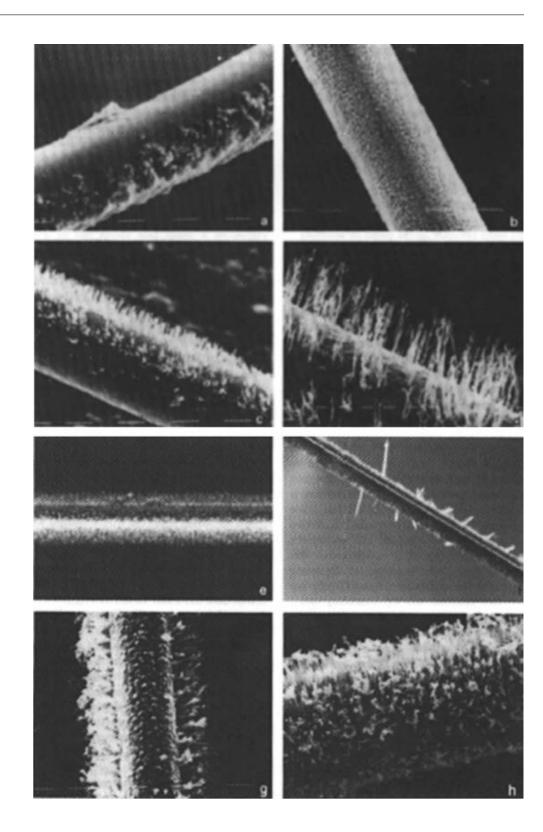
Important:

Avoid unnecessary contamination ...

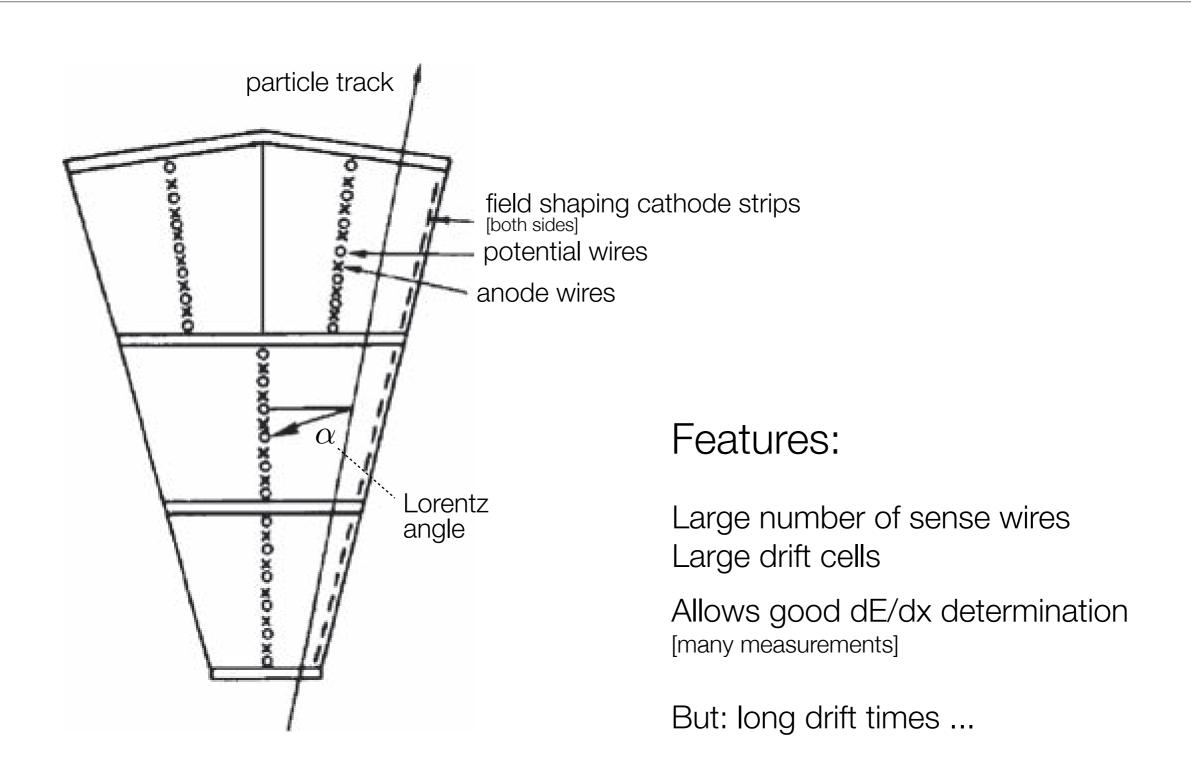
Harmful are ...

Halogens or halogen compounds Silicon compounds Carbonates, halocarbons Polymers Oil, fat ...

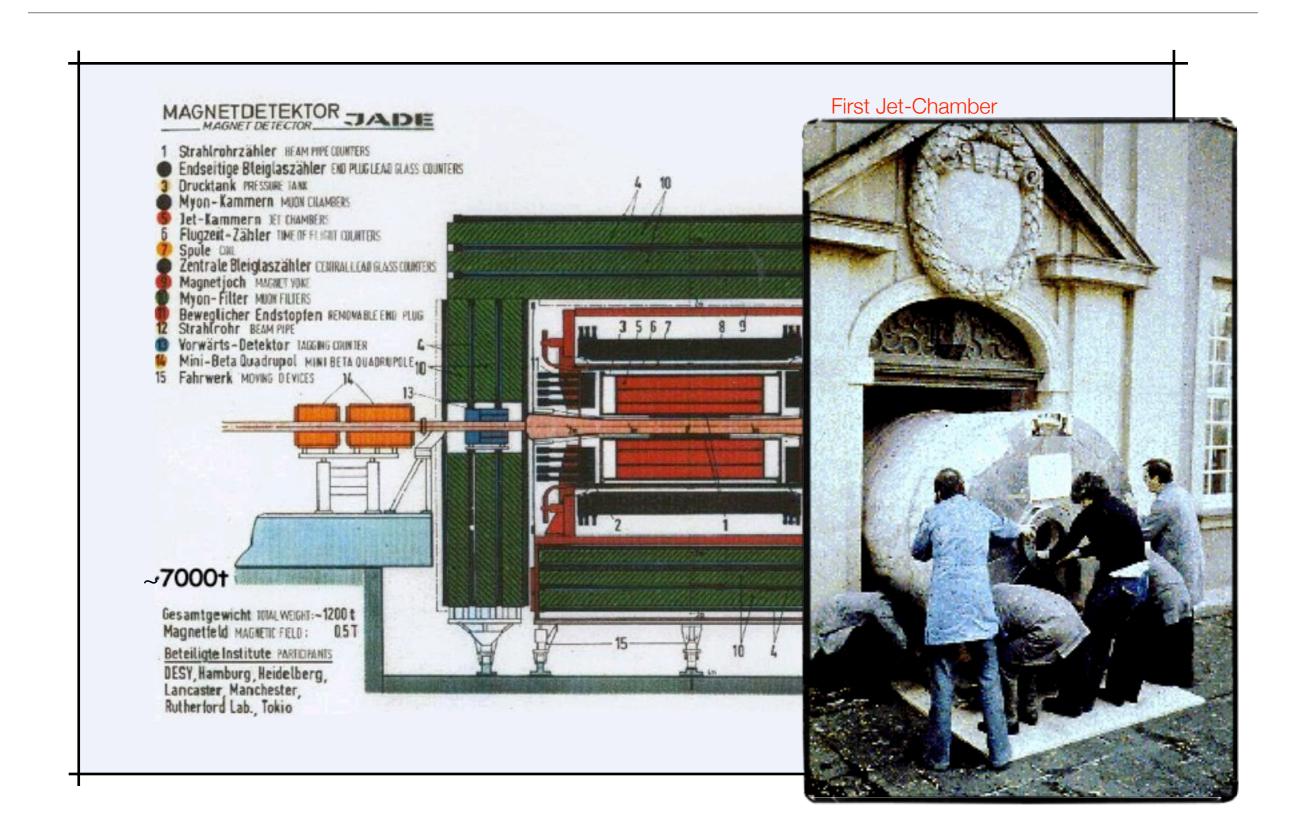
. . . .



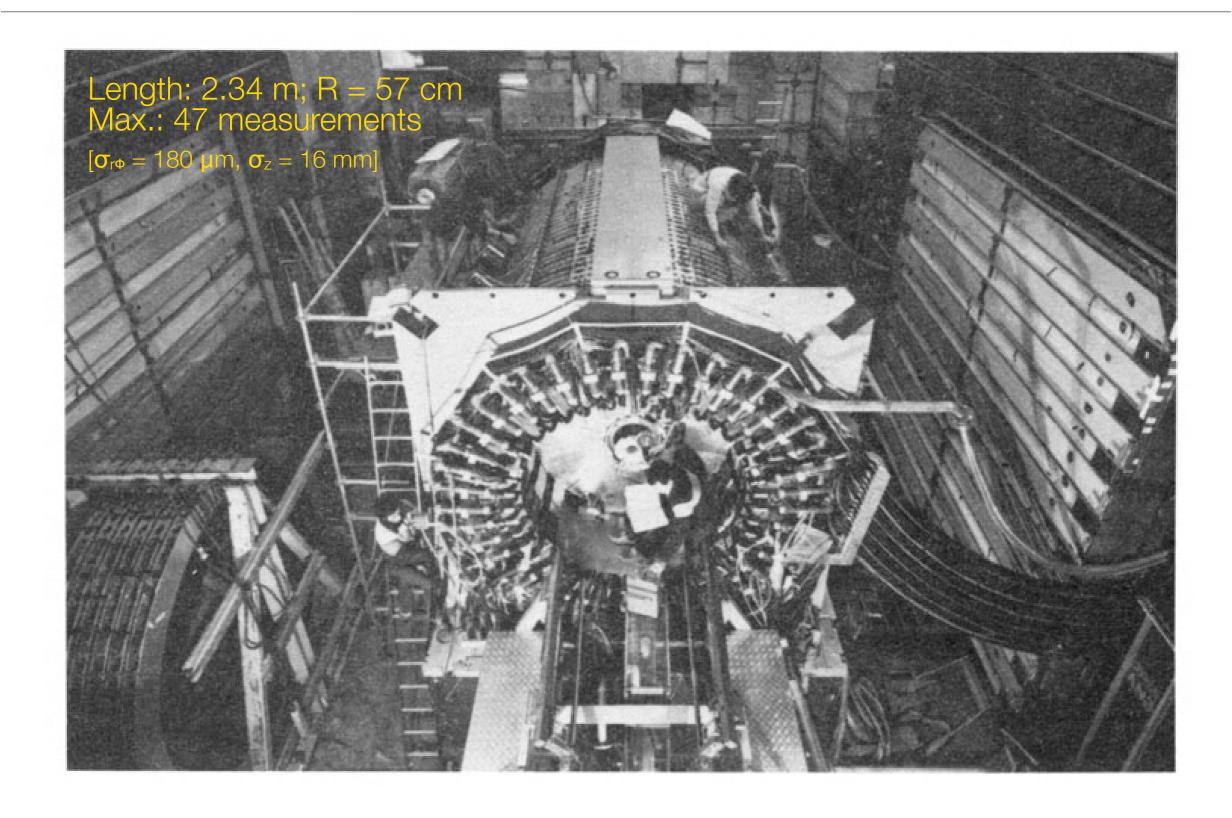
Jet Drift Chambers



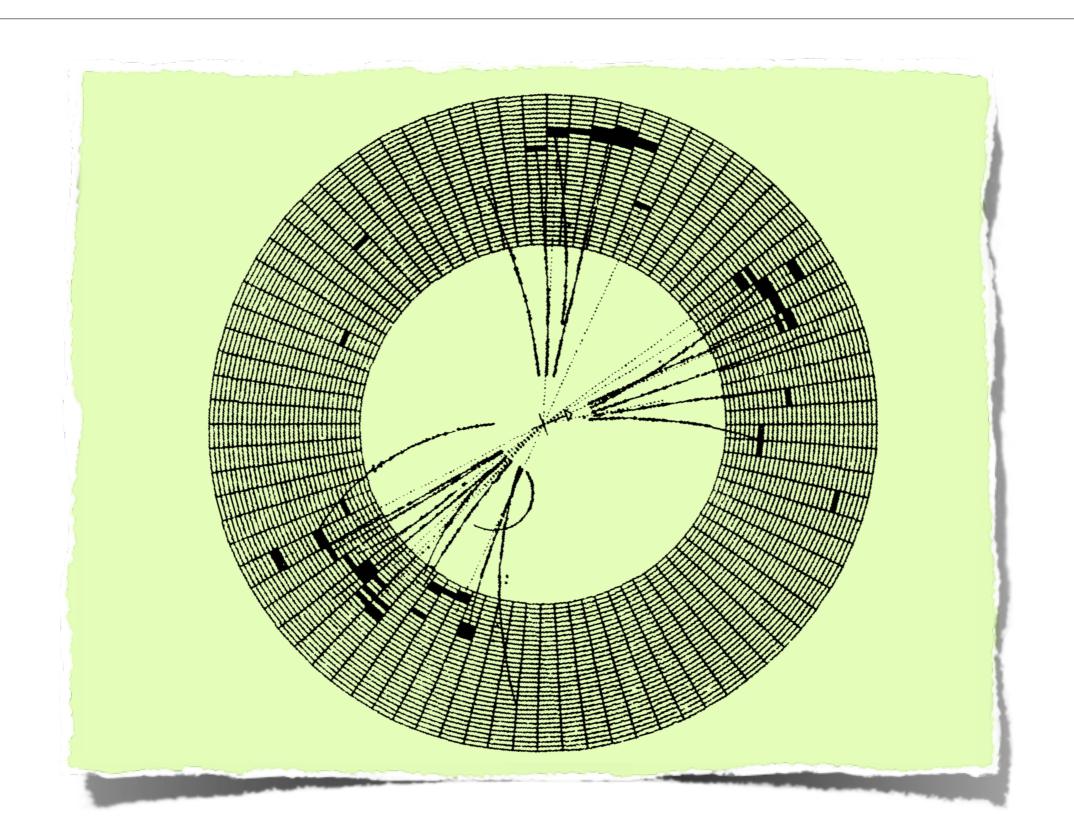
Jet Drift Chambers – JADE



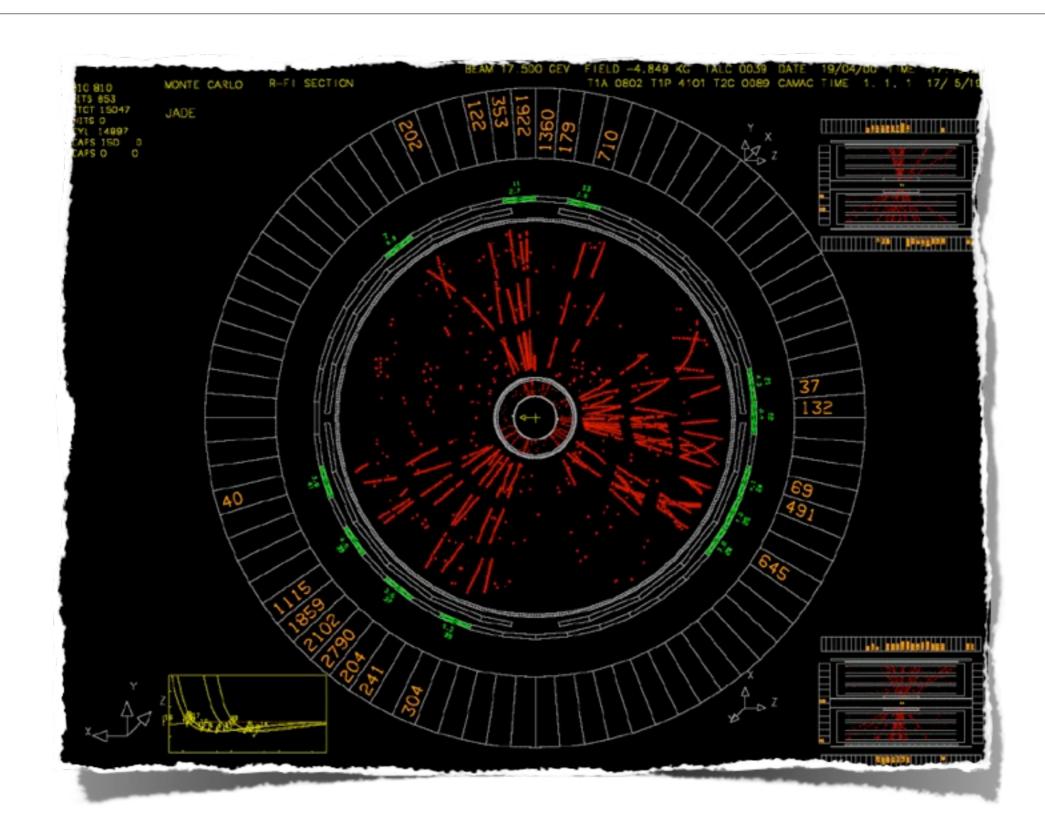
Jet Drift Chambers – JADE



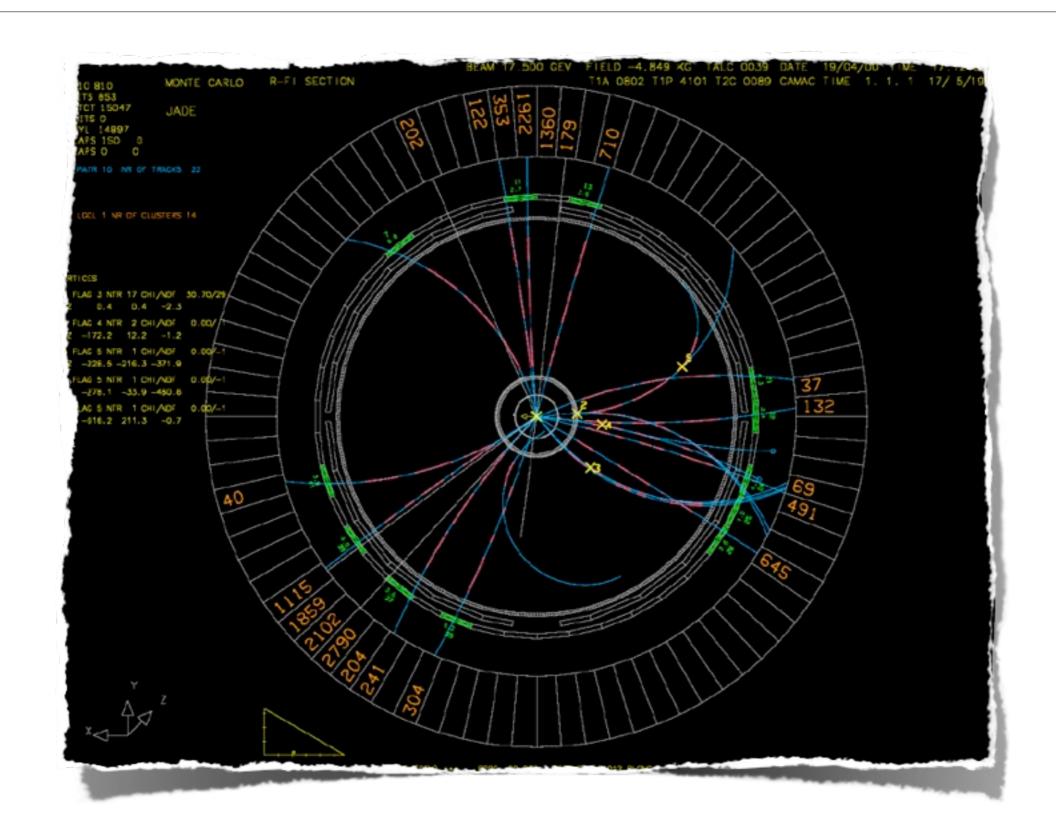
Jet Drift Chambers – JADE



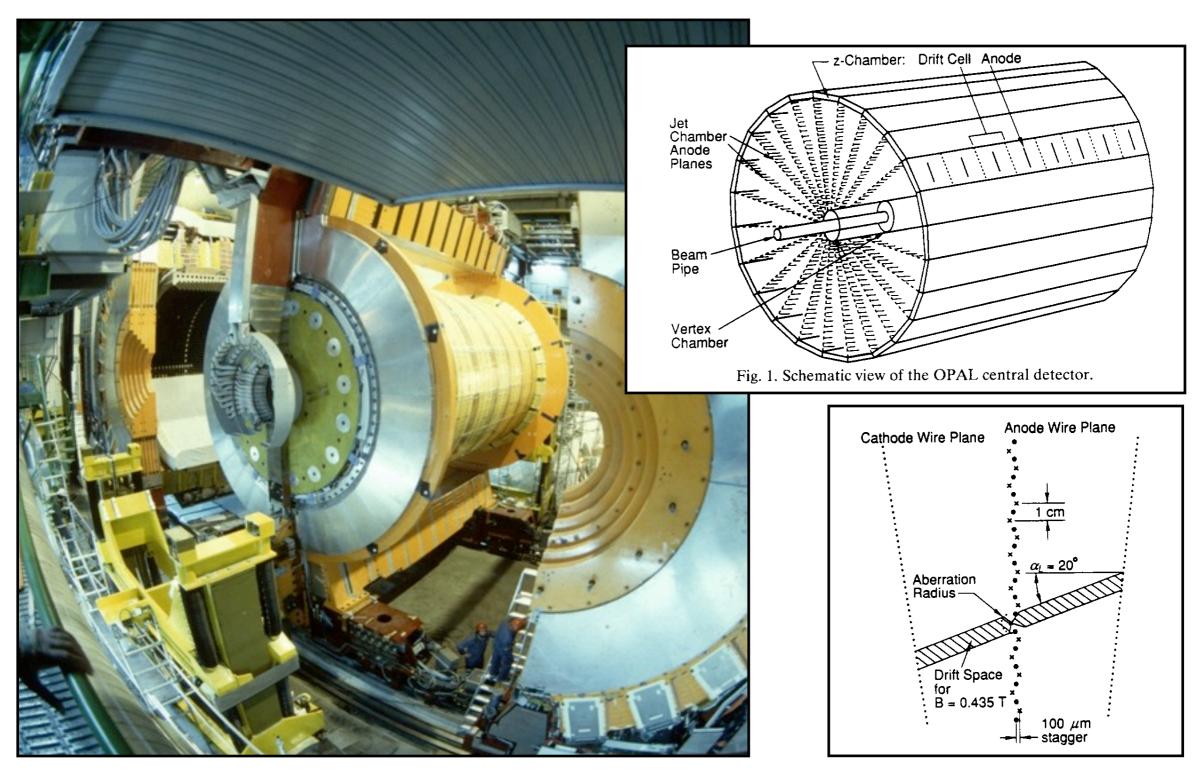
Jet Drift Chambers – JADE



Jet Drift Chambers – JADE



Jet Drift Chambers - OPAL



Opal Jet Chamber

Jet Drift Chambers – OPAL



Jet Drift Chambers – OPAL



Electronic 'bubble chamber' Full 3D reconstruction ...

xy: from wires and pads of MWPC ...

z: from drift time measurement

Momentum measurement ... space point measurement plus B field ...

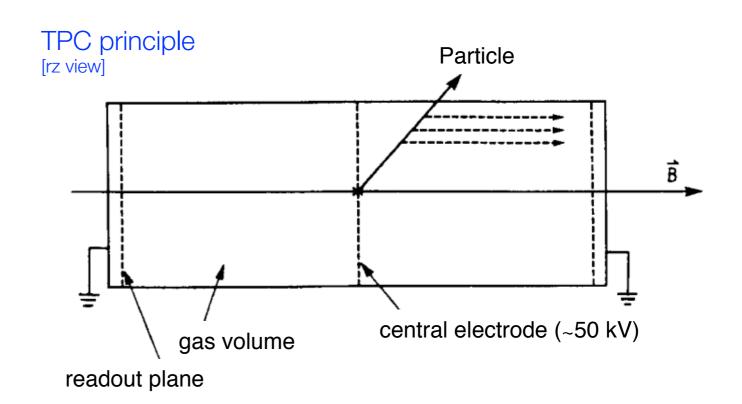
Energy measurement ... via dF/dx ...

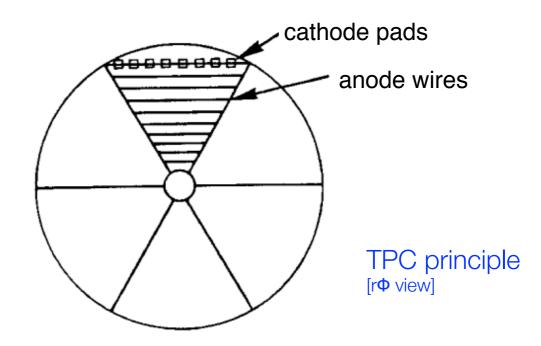
TPC setup:

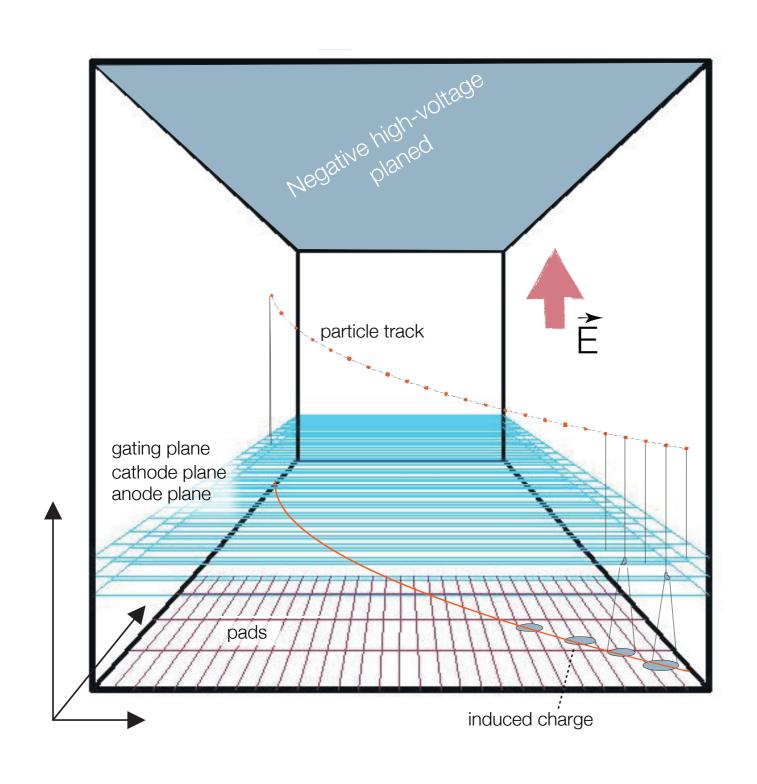
(mostly) cylindrical detector central HV cathode MWPCs at end-caps of cylinder B || to E → Lorentz angle = 0

Charge transport:

Electrons drift to end-caps
Drift distance several meters
Continuous sampling of induced charges in MWPC







Advantages:

Complete track within one detector yields good momentum resolution

Relative few, short wires (MWPC only)

Good particle ID via dE/dx

Drift parallel to B suppresses transverse diffusion by factors 10 to 100

Challenges:

Long drift time; limited rate capability [attachment, diffusion ...]

Large volume [precision]

Large voltages [discharges]

Large data volume ...

Extreme load at high luminosity; gating grid opened for triggered events only ...

Typical resolution:

z: mm; x: 150 - 300 µm; y: mm

dE/dx: 5 - 10%

Difficulty: space charge effects due to slow moving ions

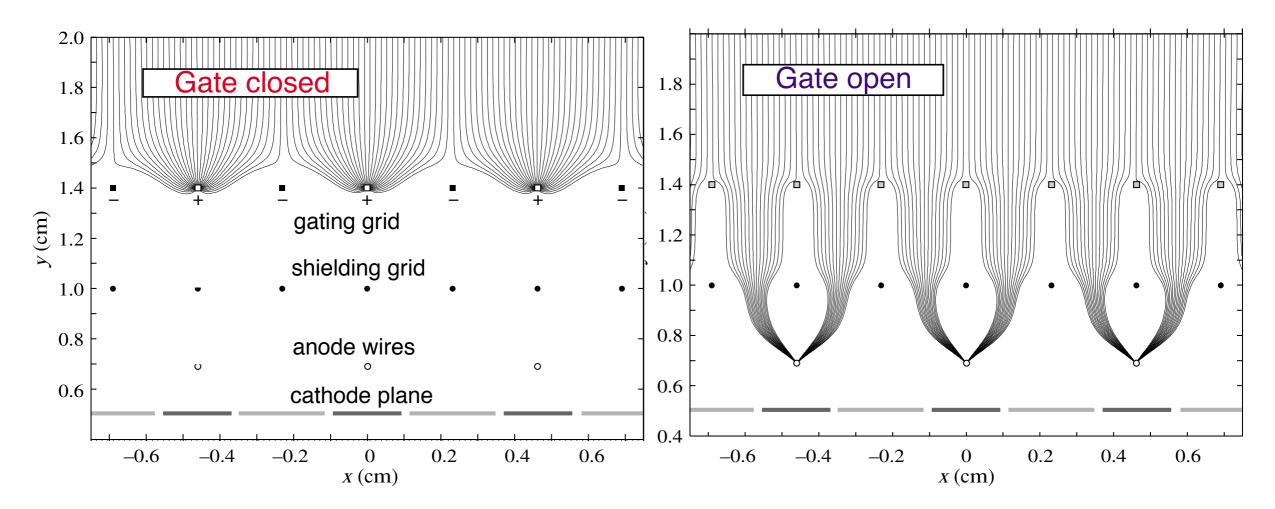
change effective E-field in drift region

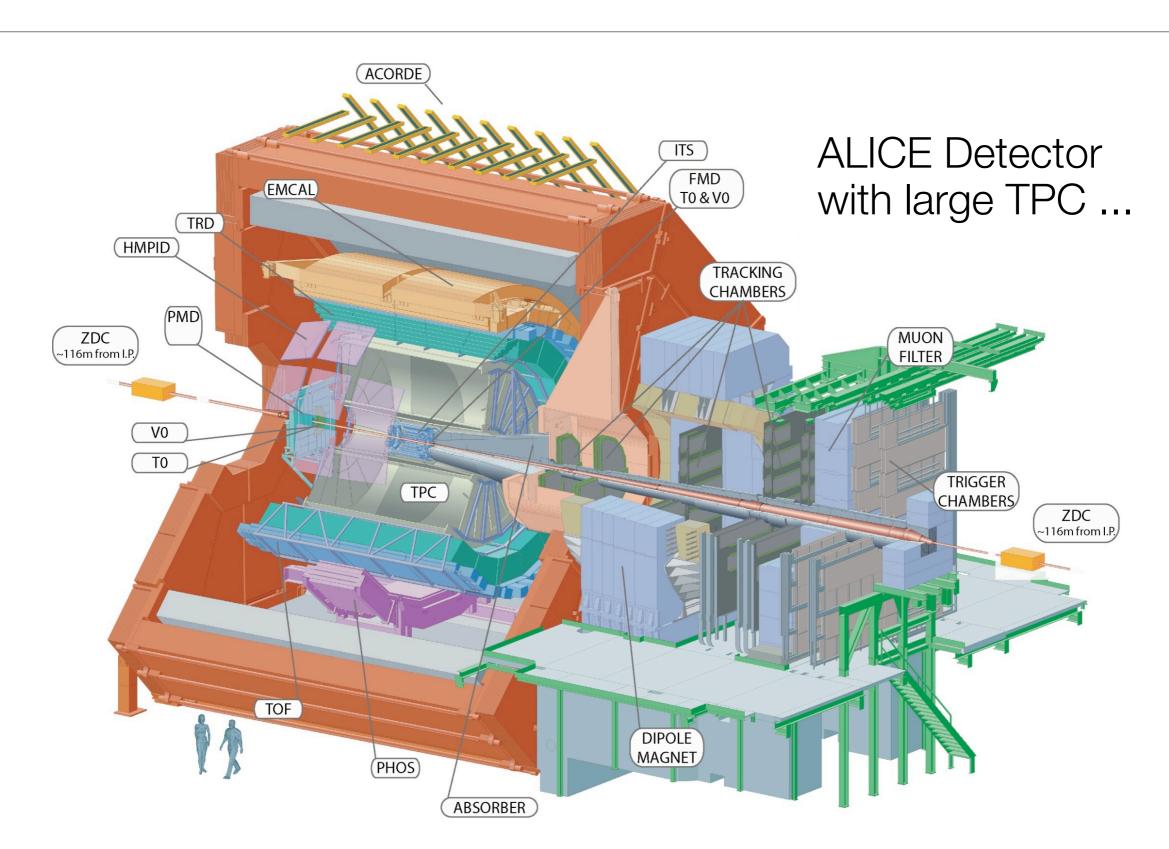
Important: most ions come from amplification region

Solution: Invention of gating grid; ions drift towards grid ...

[Also: shielding grid to avoid sense wire disturbance when switching]

Requires external trigger to switch gating grid ...





ALICE TPC:

Length: 5 meter Radius: 2.5 meter Gas volume: 88 m³

Total drift time: 92 μ s High voltage: 100 kV

End-cap detectors: 32 m² Readout pads: 557568

159 samples radially 1000 samples in time

Gas: Ne/CO₂/N₂ (90-10-5) Low diffusion (cold gas)

Gain: $> 10^4$

Diffusion: $\sigma_t = 250 \ \mu m$ Resolution: $\sigma \approx 0.2 \ mm$

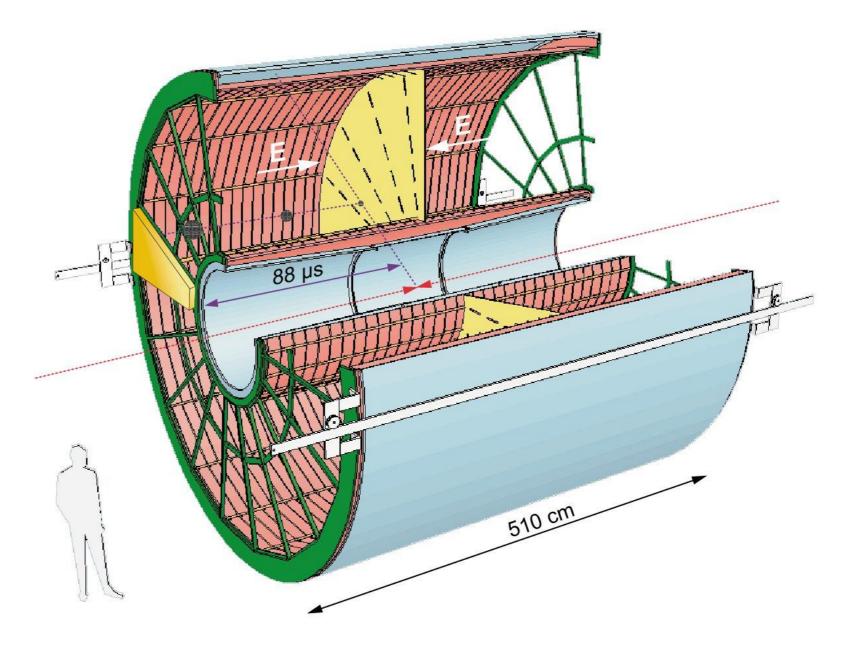
Magnetic field: 0.5 T

Pad size: 5x7.5 mm² (inner)

6x15 mm² (outer)

Temperature control: 0.1 K

[also resistors ...]



Material: Cylinder build from composite material of airline industry (X₀= ~ 3%)

