# Testing General Relativity at Cosmological Scales: Effects of Spatial Curvature <br> Jason Dossett <br> Advisor:Mustapha Ishak 

## Motivations for Testing GR?

- Cosmic acceleration
- Dark Energy
- Modification to gravity at cosmological scales.
- Extend tests to other gravity theories.
- Are gravity models proposed for quantizing gravity or unifying the four forces correct?



## Methods of Distinguishing between GR and Modifications to Gravity

- Looking for inconsistencies between expansion history and growth of structure
- The growth rate of large scale structure is coupled to the expansion history via Einstein's equations. These two effects must be consistent.
- "Trigger parameters", $\gamma$. The logarithmic growth rate $f=d \ln \delta / d \ln a$ can be approximated by:

$$
f=\Omega_{m}^{\gamma}
$$

For different gravity models $\gamma$ has a unique value.

- Gravitational Slip and Modifications to the Growth Eqns.


## Growth Equations

Perturbed FLRW Metric.

$$
\begin{aligned}
& d s^{2}=a(\tau)^{2}\left[-(1+2 \psi) d \tau^{2}+(1-2 \phi) \gamma_{i j} d x^{i} d x^{j}\right] \\
& \text { where } \\
& \gamma_{i j}=\delta_{i j}\left[1+\frac{K}{4}\left(x^{2}+y^{2}+z^{2}\right)\right]^{-2} \text { and } \quad K=-\Omega_{k} \mathcal{H}_{0}^{2}
\end{aligned}
$$

Modified Growth Equations

$$
\begin{gathered}
\left(k^{2}-3 K\right) \phi=-4 \pi G a^{2} \sum_{i} \rho_{i} \Delta_{i} Q \\
k^{2}(\psi-R \phi)=-12 \pi G a^{2} \sum_{i} \rho_{i}\left(1+w_{i}\right) \sigma_{i} Q \\
k^{2}(\psi+\phi)=\frac{-8 \pi G a^{2}}{1-3 K / k^{2}} \sum_{i} \rho_{i} \Delta_{i} \mathcal{D}-12 \pi G a^{2} \sum_{i} \rho_{i}\left(1+w_{i}\right) \sigma_{i} Q . \\
\mathcal{D}=Q(1+R) / 2 \\
\quad \text { where } \\
\Delta_{i}=\delta_{i}+3 \mathcal{H} \frac{q_{i}}{k}
\end{gathered}
$$

## Evolving the Modified Gravity Parameters: Binning Methods

Both Traditional binning and Hybrid Method evolve in redshift as

$$
\begin{aligned}
& X(k, z)=\frac{1+X_{z_{1}}(k)}{2}+\frac{X_{z_{2}}(k)-X_{z_{1}}(k)}{2} \tanh \frac{z-z_{d i v}}{z_{t w}}+\frac{1-X_{z_{2}}(k)}{2} \tanh \frac{z-z_{T G R}}{z_{t w}}, \\
& \underbrace{\substack{X_{z_{1}}(\mathrm{k}) \\
x_{22}(\mathbf{k})}}_{z_{\text {div }}^{\prime}} \underbrace{2}_{z_{\text {TGR }}} \\
& \text { Scale Dependence }
\end{aligned}
$$

Traditional Binning Method


Hybrid Method

$$
X_{z_{1}}(k)=X_{1} e^{-k / k_{c}}+X_{2}\left(1-e^{-k / k_{c}}\right)
$$

$$
X_{z_{2}}(k)=X_{3} e^{-k / k_{c}}+X_{4}\left(1-e^{-k / k_{c}}\right),
$$




## Evolving the Modified Gravity Parameters: Binning Methods

Both Traditional binning and Hybrid Method evolve in redshift as


## Evolving the Modified Gravity Parameters: Functional evolution

In this evolution method we assume scale independent evolution. The parameters evolve in terms of the scale factor as:

$$
X(a)=\left(X_{0}-1\right) a^{s}+1
$$

As a function of redshift with $\mathrm{s}=3$


## CORRELATIONS WITH CURVATURE PARAMETER $\Omega_{k}$

- What can we predict analytically?
- We would expect the MG parameters to be positively correlated with $\Omega_{k}$

$$
k^{2}(\psi+\phi)=\frac{-8 \pi G a^{2}}{1-3 K / k^{2}} \sum_{i} \rho_{i} \Delta_{i} \mathcal{D}-12 \pi G a^{2} \sum_{i} \rho_{i}\left(1+w_{i}\right) \sigma_{i} Q . \quad K=-\Omega_{k} \mathcal{H}_{0}^{2}
$$

- Use current data to explore correlations.
- WMAP 7 year temperature and polarization spectra
- Union 2 Supernovae Data
- BAO from Two-Degree Field, SDSS-DR7, and WiggleZ
- Matter Power Spectrum (MPK) from SDSS-DR7
- ISW-galaxy cross-correlations (SDSS-LRG, 2MASS, NVSS)
- Refined HST COSMOS 3D weak lensing tomography.


## Correlations with curvature PARAMETER $\Omega_{k}$ CONT'D

Traditional Binning









- Can assuming a flat universe when the universe is actually curved affect MG parameter constraints?
- Generate simulated higher precision data to see.


## Effect of curvature on MG PARAMETER CONSTRAINTS



## Effect of curvature on MG PARAMETER CONSTRAINTS CONT'D



$\Omega_{k}=0.05$

$\Omega_{k}=-0.1$

## Effect of curvature on MG PARAMETER CONSTRAINTS CONT'D

| Traditional Binning Evolution | Hybrid Evolution | Functional Form Evolution |
| :---: | :---: | :---: |
|  |  |  |
|  |  |  |

## Conclusions

- Curvature is positively correlated with the MG parameters Q and D.
- Ignoring curvature can cause an apparent deviation from GR.
- Negatively curved models deviate more significantly than do positively curved models.
- Must include $\Omega_{\mathrm{k}}$ in parameter analysis along with MG and other cosmological parameters when using future data.


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## ISITGR

- ISiTGR is publicly available at:
http://www.utdallas.edu/~jdossett/isitgr
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