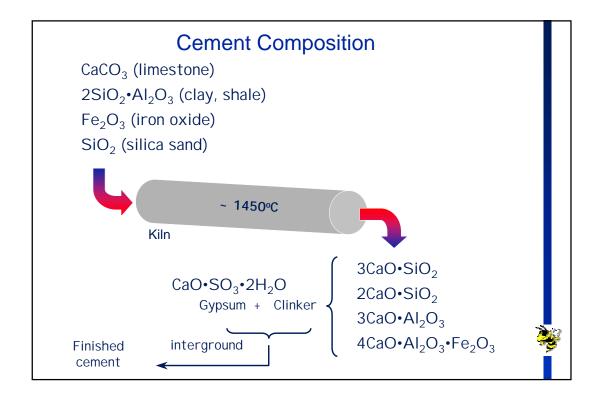
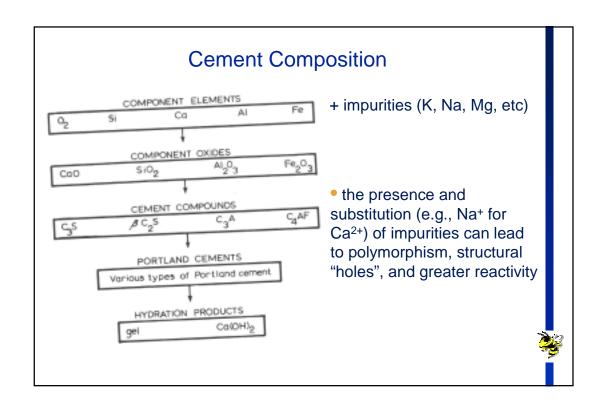
# Portland Cement Hydration

#### Dr. Kimberly Kurtis

School of Civil Engineering Georgia Institute of Technology Atlanta, Georgia







### **Cement Hydration**

Hydration - chemical combination of cement and water

#### Two primary mechanisms:

<u>Through solution</u> - involves dissolution of anhydrous compounds to their ionic constituents, formation of hydrates in solution, and eventual precipitation due to their low solubility

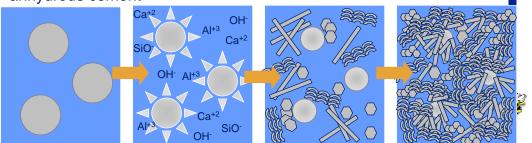
<u>Topochemical</u> - or solid-state hydration - reactions take place directly at the surface of the anhydrous cement compounds without going into solution

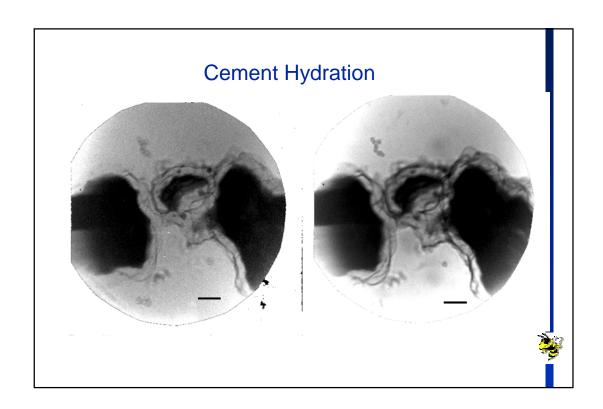


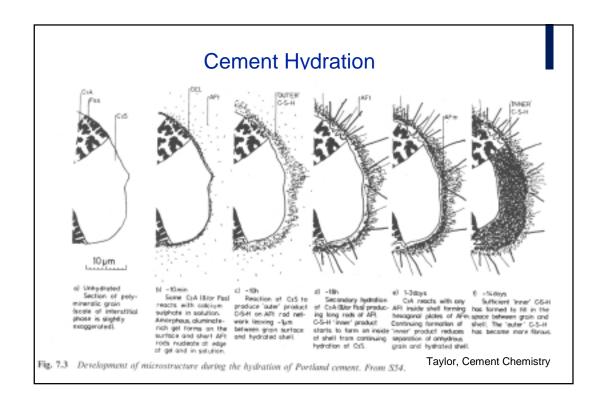


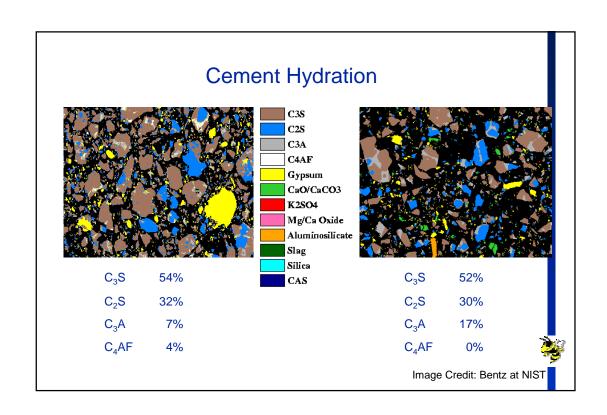
When water is added to cement, what happens?

- Dissolution of cement grains
- Growing ionic concentration in "water" (now a solution)
- Formation of compounds in solution
- After reaching a saturation concentration, compounds precipitate out as solids ("hydration products")
- In later stages, products form on or very near the surface of the anhydrous cement









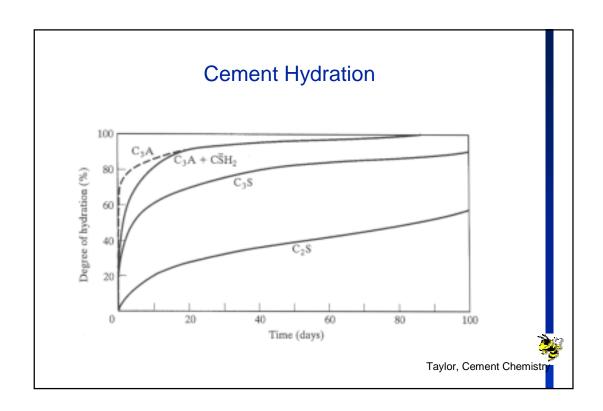
# **Cement Hydration**

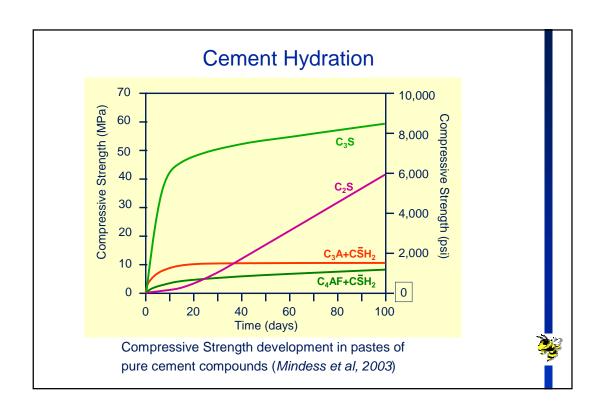
Because the hydration rates of the 4 key phases vary considerably, properties like

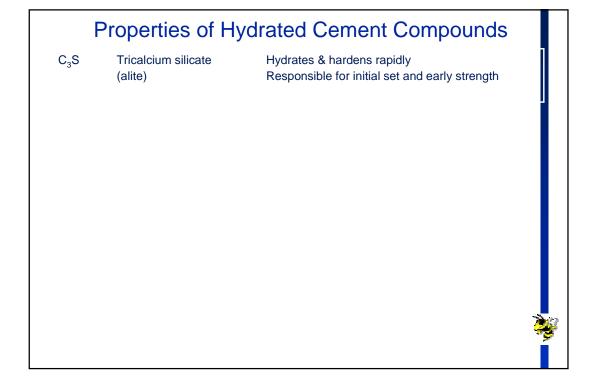
- time to stiffening
- setting time
- hardening rate

will vary with cement composition.









# **Properties of Hydrated Cement Compounds**

C<sub>3</sub>S Tricalcium silicate Hydrates & hardens rapidly

(alite) Responsible for initial set and early strength

C<sub>2</sub>S Dicalcium silicate Hydrates & hardens slowly

(belite) Contributes to later age strength (beyond 7 days)



# **Properties of Hydrated Cement Compounds**

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(belite) Contributes to later age strength (beyond 7 days)

C<sub>3</sub>A Tricalcium aluminate Liberates a large amount of heat during first few

days

Contributes slightly to early strength development Cements with low %-ages are more resistant to

sulfates



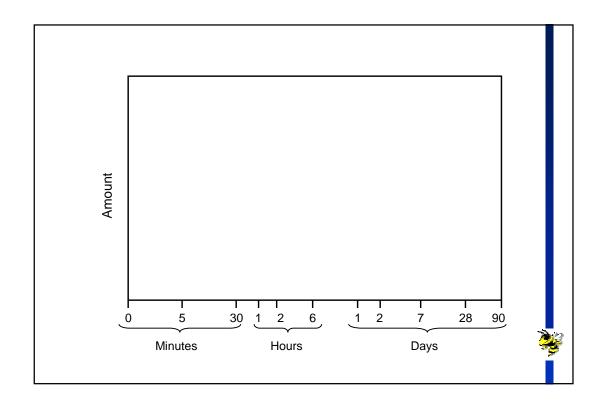
# Properties of Hydrated Cement Compounds

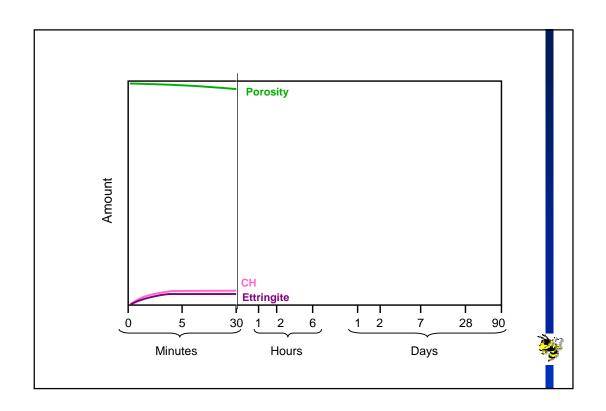
| C <sub>4</sub> AF | Tetracalcium<br>aluminoferrite<br>(ferrite) | Reduces clinkering temperature<br>Hydrates rapidly but contributes little to strength<br>Colour of hydrated cement (gray) due to ferrite<br>hydrates             |
|-------------------|---|--|
| C <sub>3</sub> A  | Tricalcium aluminate                        | Liberates a large amount of heat during first few days Contributes slightly to early strength development Cements with low %-ages are more resistant to sulfates |
| C <sub>2</sub> S  | Dicalcium silicate (belite)                 | Hydrates & hardens slowly<br>Contributes to later age strength (beyond 7 days)   |
| C <sub>3</sub> S  | Tricalcium silicate (alite)                 | Hydrates & hardens rapidly Responsible for initial set and early strength  |

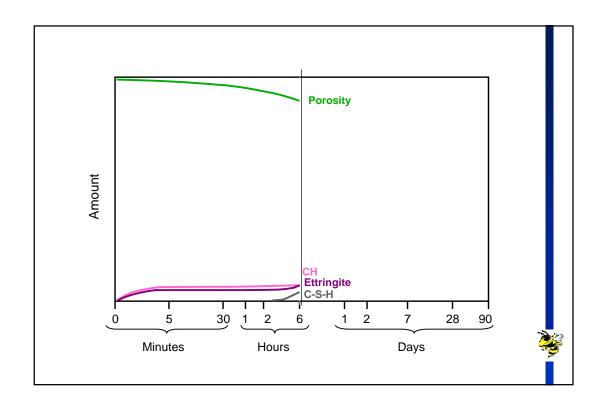


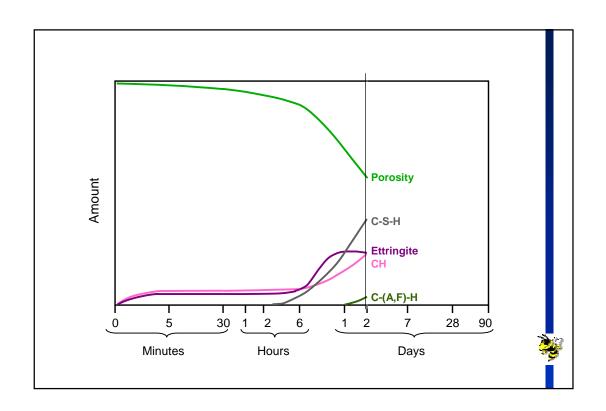
| BLE 3.4 CHARACTER                                       |                  | n of the Cement       | Contribution to Cement<br>Heat       |                       |
|---|------------------|-----------------------|--------------------------------------|-----------------------|
|   | Reaction<br>Rate | of Heat<br>Liberated  | Strength                             | Liberation            |
| C <sub>2</sub> S<br>C <sub>2</sub> S                    | Moderate<br>Slow | Moderate<br>Low       | High<br>Low initially,<br>high later | High<br>Low           |
| $C_3A + C\overline{S}H_2$<br>$C_4AF + C\overline{S}H_2$ | Fast<br>Moderate | Very high<br>Moderate | Low<br>Low                           | Very high<br>Moderate |

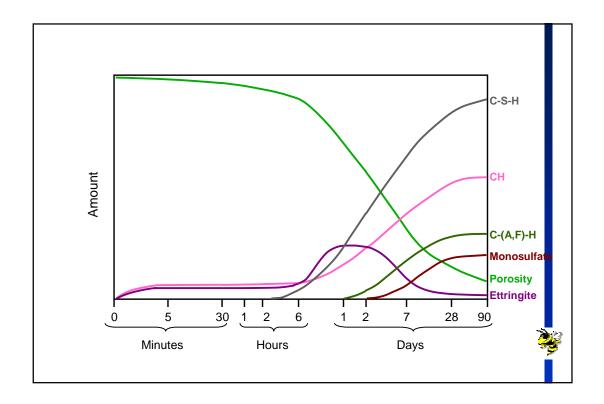












# **Cement Hydration**

- •Is the chemical combination of cement and water to form hydration products
- Takes time
- •May not proceed to 100% completion

Formation of hydration products over time leads to:

- Stiffening (loss of workability)
- Setting (solidification)
- Hardening (strength gain)

Let's look at the hydration reactions in more detail...



## Hydration of the Calcium Silicates

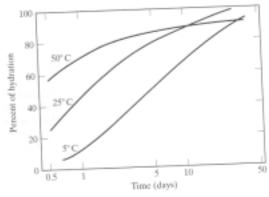
$$2C_3S + 7H \rightarrow C_3S_2H_8 + 3CH$$
  $\Delta H=-500J/g$   $2C_2S + 7H \rightarrow C_3S_2H_8 + CH$   $\Delta H=-250J/g$ 

- •Both produce C-S-H and CH as reaction products
- •C<sub>2</sub>S produces less CH (important for durability in sulfate rich environments)
- •More heat is evolved during C<sub>3</sub>S hydration
- •C<sub>3</sub>S hydration is more rapid, contributing to early age strength (2-3h to 14 days)
- •C<sub>2</sub>S hydration occurs more slowly to contributing to strength after ~7-14 days.



### Hydration of the Calcium Silicates

Like most chemical reactions, the rate of cement hydration is influenced by temperature.





#### C-S-H

- Calcium silicate hydrate
- •C/S varies between 1.1-2; ~1.5 is typical
- •H is even more variable
- Structure ranges from poorly crystalline to amorphous - highly variable and poorly understood
- •Occupies 50-60% of the solid volume of the hydrated cement paste (hcp)
- •Huge surface area (100-700 m<sup>2</sup>/g)
- Strength due to covalent/ionic bonding (~65%) and Van der Waals bonding (~35%) within the complex structure
- Primary strength-giving phase in portland cement concrete

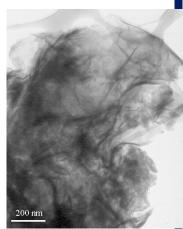
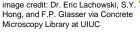


image credit: Dr. Eric Lachowski, S.Y. Hong, and F.P. Glasser via Concrete



# C-S-H The structure of C-S-H is poorly understood.



wet

dry

16 hr. C<sub>3</sub>S paste

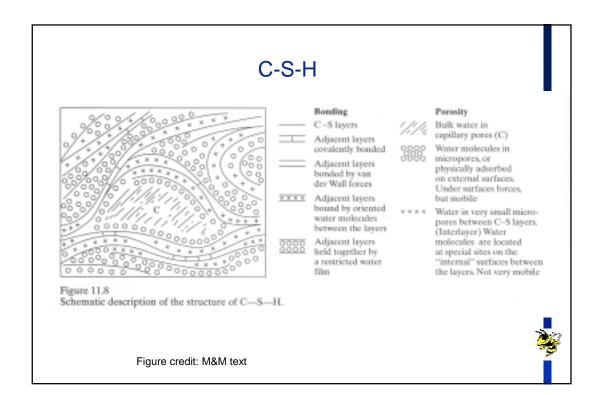
Variations in surface area, depending on technique used

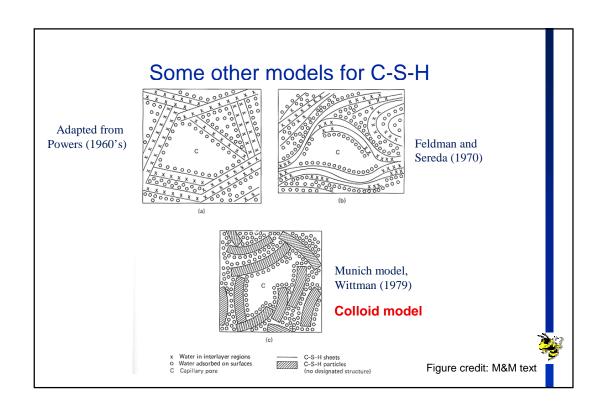
$$S_{H2O} = 200 \text{ m}^2/\text{g}$$

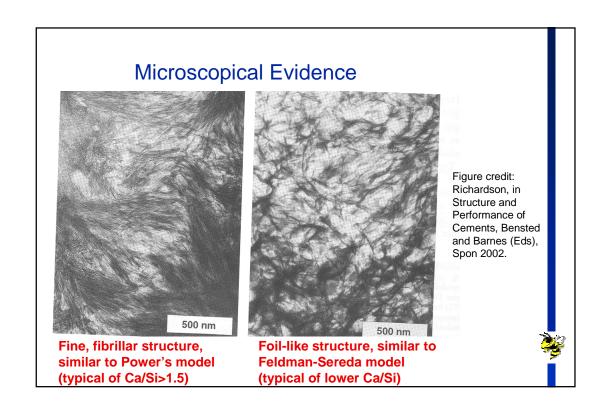
$$S_{N2} = 5-50 \text{ m}^2/\text{g}$$

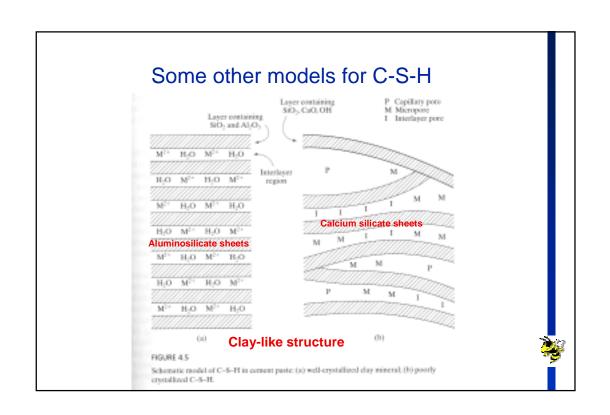
 $S_{neutrons} = 50 \text{ m}^2/\text{g}$ 

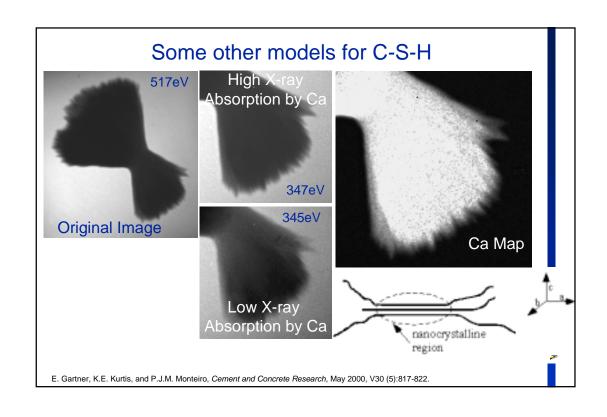


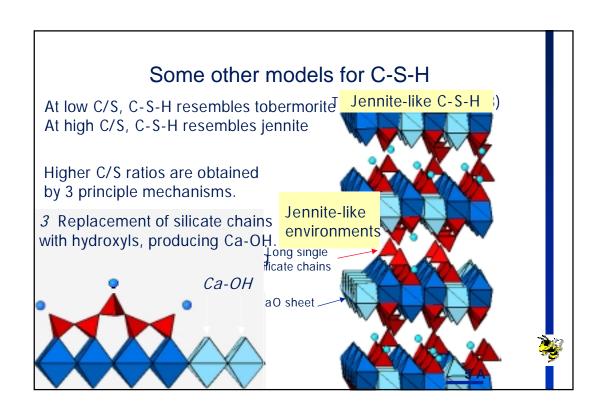












# Summary of Models for C-S-H

 Table 6: Summary of models for the structure of C-S-H.

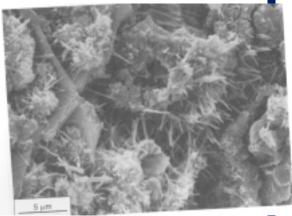
| Name of Model  | Primary Experimental<br>Basis   | Type of Model                      | Selected Characteristics of Model   |
|----------------|---|------------------------------------|---|
| Powers         | Water sorption<br>Volume of pores                                     | Colloid                            | All products are gel<br>Particle radius, 5 nm<br>Gel pore volume, 28%                 |
| Taylor         | X-ray<br>TGA  | Imperfect<br>Tobomerite<br>Jennite | Atomic structure of C-S-H   |
| Brunauer       | Water Sorption  | 2-3 layers                         | Structure changes upon drying   |
| Feldman-Sereda | Nitrogen sorption<br>Length vs. RH<br>Modulus vs. RH<br>Weight vs. RH | Layers                             | Crumpled and folded layers with<br>interlayer water reversibly<br>removed upon drying |
| Wittmann       | Modulus vs. RH  | Colloid                            | Structure not defined   |
| Jennings       | Density vs. RH<br>Composition vs. RH<br>Surface area                  | Colloid                            | Fractal: density and surface area depend on length scale                              |



#### Inner vs. Outer Product C-S-H

# Outer product (early) C-S-H/groundmass

- forms during early hydration
- C-S-H forms away from the cement particle surface, filling water-filled space
- higher porosity
- contains high levels of impurities
- $\bullet$  probably admixed with nanoscale  $\mathrm{C_4A\check{S}H_{12}}$

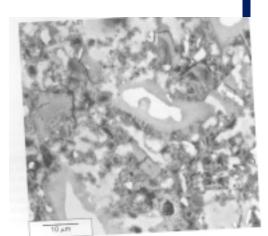




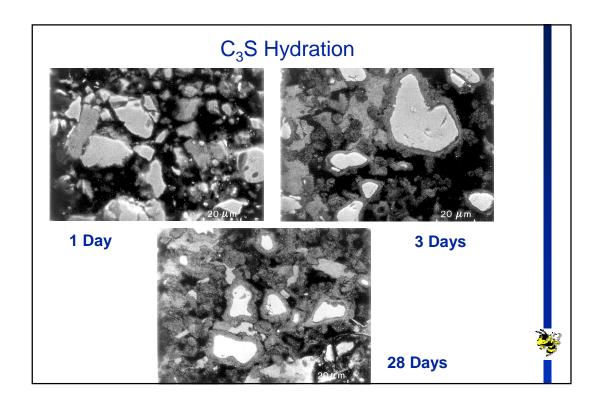
#### Inner vs. Outer Product C-S-H

# <u>Inner product (late) C-S-H/phenograins</u>

- forms during later hydration, when the process is diffusion controlled
- C-S-H grows inwards and outwards from the C-S-H "barrier"
- C-S-H formed takes shape of cement grains
- lower porosity, more dense
- fewer impurities
- more resistant to physical change on drying
- more abundant as hydration  $\uparrow$  or as w/c  $\downarrow$

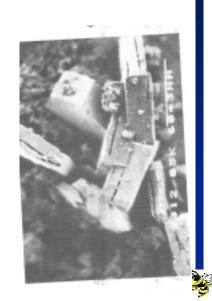






#### CH

- Calcium hydroxide or Ca(OH)<sub>2</sub>
- Definite stoichiometry
- Variable morphology from large, hexagonal prisms to thin, elongated crystals
- •Size of the crystals depends on the amount of space available
- •Occupies 20-25% of the solid volume in the hcp
- •Much lower surface area than C-S-H
- Does not contribute much to strength
- •Keeps the pore solution alkaline (pH 12.4-13.5)



### Hydration of the Calcium Aluminates

- •Reaction of C<sub>3</sub>A with water occurs *very* quickly and liberates much heat "Flash Set"
- •Gypsum (CŠH<sub>2</sub>) is added to the cement to control the hydration of C<sub>3</sub>A

 $C_3A + 3C\dot{S}H_2 + 26H \rightarrow C_6A\dot{S}_3H_{32}$   $\Delta H$ =-1350J/g

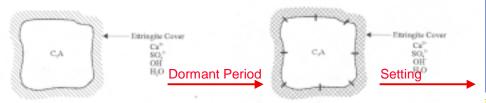
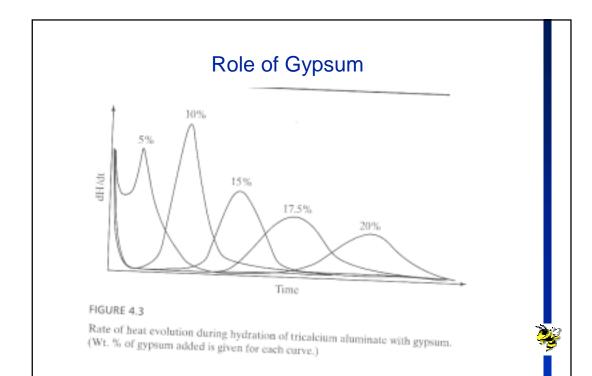
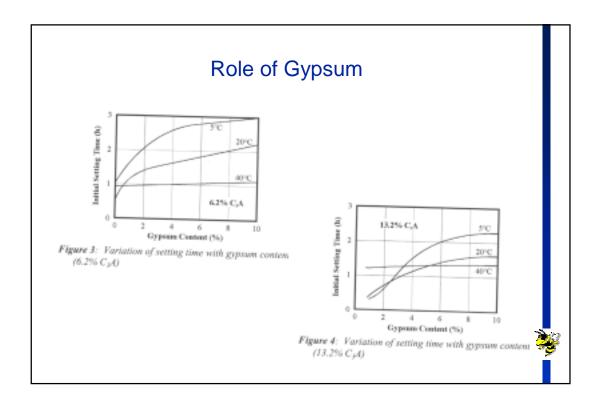


Figure 1: First stage - formation of a thin cover of estringise on the C<sub>2</sub>A surface

Figure 2: Second stage - a further amount of ettringite is formed on the C<sub>3</sub>A surface





## Hydration of the Calcium Aluminates

When more  $C_3A$  remains,  $C_6A\mathring{S}_3H_{32} + 2C_3A + 4H \rightarrow 3C_4A\mathring{S}H_{12}$ 

•Reaction of  $C_4AF$  occurs more slowly  $C_4AF + 2CH + 14H \rightarrow C_4(A,F) H_{13} + (A,F)H_3$ 



### Hydration of the Calcium Aluminates

- •Reaction of  $C_4AF$  (ferrite) phase are slower and evolve less heat than  $C_3A$
- · Also heavily retarded by gypsum

$$C_4AF + 3C\dot{S}H_2 + 21H \rightarrow C_6(A,F)\dot{S}_3H_{32} + (F,A)H_3$$

$$C_4AF + C_6(A,F) \mathring{S}_3H_{32} \rightarrow 3C_4(A,F)\mathring{S}H_{12} + (F,A)H_3$$

•Products of C<sub>4</sub>AF are more resistant to sulfate attack than those of C<sub>3</sub>A hydration



# Hydration of the Calcium Aluminates

# $C_6 A \mathring{S}_3 H_{32}$ (Ettringite, $A_{ft}$ )

- Needle-like morphology
- · Needles interlock, take up much water
- · contributes to stiffening of mixture
- · some early strength

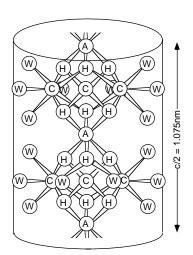






# Hydration of the Calcium Aluminates

Ettringite crystal structure as part of a single column projection where A=AI, C=Ca, H=O of an OH group, W=O of an H<sub>2</sub>O molecule. Hydrogen atoms have been omitted, as are the H<sub>2</sub>O molecules attached to the calcium atoms lying in the central vertical line of the figure. (based on Taylor, 1997)

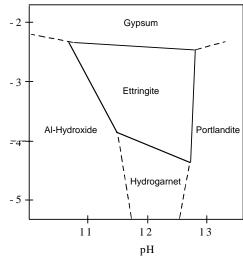




# Hydration of the Calcium Aluminates

Ettringite stability in alkaline environments as a function of pH and sulfate ion concentration. (adapted from Hampson and Bailey, 1982)

Log [SO<sub>4</sub>-2]

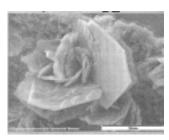




# Hydration of the Calcium Aluminates

# $C_4 A \mathring{S} H_{12}$ (monosulfate, $A_{fm}$ )

- hexagonal plate morphology arranged in "rosettes" during early hydration
- become more "platey" with continued hydration
- · can contain impurities
- vulnerable to sulfate attack





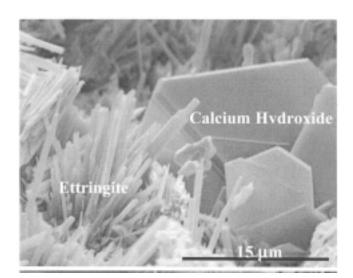


# Calcium Aluminates and Calcium Sulfoaluminates

- •Includes ettringite, monosulfate hydration, calcium aluminate hydrates, and ferric-aluminum hydroxide gels
- Comprise 15-20% of solid volume of hcp
- •Do not contribute much to strength
- •Formation of ettringite, in particular, does influence setting time
- •High heat of hydration for C<sub>3</sub>A can be favorable or unfavorable, depending upon application

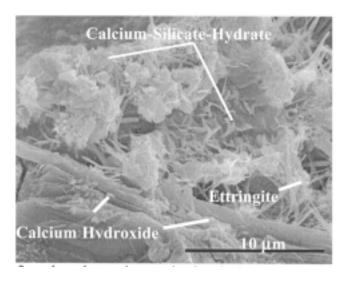


### Hydrated Cement Paste (hcp)





# Hydrated Cement Paste (hcp)



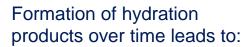


# Hydrated Cement Paste (hcp)

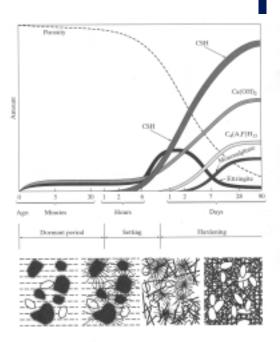
TABLE 4.4 Summary of Properties of the Hydration Products of Portland Cement Compounds

| Compound                | Specific<br>Gravity  | Crystallinity | Morphology<br>in Pastes                           | Typical Crystal<br>Dimensions<br>in Pastes | Resolved<br>by* |
|-------------------------|----------------------|---------------|---|--|-----------------|
| C-S-H                   | 2.3-2.6 <sup>b</sup> | Very poor     | Spines;<br>Unresolved<br>morphology               | 1 × 0.1 μm<br>(Less than 0.01<br>μm thick) | SEM, TEM        |
| CH                      | 2.24                 | Very good     | Nonporous<br>striated<br>material                 | 0.01-0.1 mm                                | OM, SEM         |
| Ettringite              | ~1.75                | Good          | Long slender<br>prismatic<br>needles              | 10 × 0.5 μm                                | OM, SEM         |
| Monosulfo-<br>aluminate | 1.95                 | Fair-good     | Thin hexagonal<br>plates; irregular<br>"rosettes" | $1 \times 1 \times 0.1 \mu\text{m}$        | SEM             |

<sup>&</sup>quot;OM, optical microscopy; SEM, scanning electron microscopy; TEM, transmission electron microscopy."



- Stiffening (loss of workability
- Setting (solidification)
- Hardening (strength gain)



# **Cement Hydration**

TABLE 11.4 Influence of Cement Compounds on Concrete Properties

| Property                          | Compound                             | Remarks  |
|-----------------------------------|--------------------------------------|--|
| Setting behavior                  | C <sub>2</sub> S                     | Controls normal setting  |
| Temperature rise during hydration | C₃S<br>C₃A<br>C₃S                    | Can cause premature stiffening   |
| Strength development              | C <sub>3</sub> A<br>C <sub>3</sub> S | Responsible for early strength   |
| Creep and shrinkage               | C2S<br>C2S, C2S                      | Contributes to long-term strength<br>Major contributions                           |
| Durability                        | C₃A, Ć₄AF<br>C₃S<br>C₃A              | Minor effects<br>Leaching of Ca(OH) <sub>2</sub> , sulfate attac<br>Sulfate attack |



## **Heat of Hydration**

- Cement hydration is exothermic
- Concrete is an insulator

#### Heat of hydration can be:

- detrimental (thermal gradients --> cracking)
- helpful (heat provides activation energy when concreting in cold weather; higher early strength)

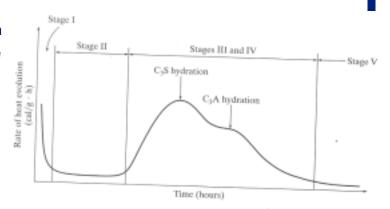


#### **Heat of Hydration**

Heat evolution can be used to map the progress of hydration:

- (1) Initial dissolution of solids (increasing ionic concentration)
- (2) Induction period
- (3) Acceleration
- (4) Deceleration
- (5) Steady state

Figure 11.4
Rate of heat evolution during the hydration of portland coment (after S. Mindess and J. F. Young, Concrete, Prentice Hall, 1981, Fig. 4.4, p. 85).



#### Cement Hydration: Avrami Model\*

 Popular model for describing hydration during the acceleration periods (Stages 2&3)

 $-\ln(1-\alpha)=[k(t-t_o)]^{m}$ 

or when  $\alpha$  is small,  $\alpha$ =

Where  $\alpha$  is degree of hydration

t is time of hydration, where to corresponds to the length of induction period

*k* is a rate constant for a nucleation-controlled process

m = [(p/s)+q], where p= 1 for 1D growth (needles/fibers)  $m \sim 1-3$  for  $C_3S$  2 for 2D (sheets/plates)

2 for 2D (sheets/plates)
3 for 3D isotropic growth (sphere)

s=1 for interface or phase-boundary-controlled growth

=2 for diffusion-controlled growth

and q=0 for no nucleation (nucleation saturation)

1 for continuous nucleation at a constant rate

\* Avrami, M. J. Phys. Chem., 7, 1103 (1938), 8, 212 (1940).

### Cement Hydration: Avrami Model

- *k*, then, is a combined rate constant, accounting for rate of nucleation, rate of product growth, and other factors not accounted for (e.g., changing diffusion coefficients)
- Can calculate the rate constant *k* from calorimetry data and the Avrami equation:
- $-\ln(1-\alpha)=[k(t-t_o)]^{m}$
- when modeling as a function of time rather than degree of hydration:

 $d\alpha/dt = Amk^{m} (t-t_{o})^{m-1} exp\{-[k(t-t_{o})]^{m}\}$ 

Where A is a preexponential factor.

Thomas and Jennings, *Chem. Mat.*, 11:1907-14, 1999.

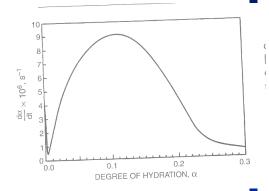


Figure credit: Gartner et al, in Structure and Performance of Cements, Bensted and Barnes (Eds), Spon 2002.



#### Cement Hydration: Avrami Model

•Can also determine the activation energy (E<sub>a</sub>) for the reaction, which can be used to assess the temperature-dependence of the reaction:

$$k(T)=A \exp(-E_a/RT)$$

Where T is absolute temperature (K), R is gas constant,

Table 5. Avrami Fit Parameters as Reported by FitzGerald et al.<sup>9</sup> for the Hydration Rate of C<sub>3</sub>S/H<sub>2</sub>O Pastes As Measured by QENS

|        | rate parameter |                    |                       |      |                       |
|--------|----------------|--------------------|-----------------------|------|-----------------------|
| T (°C) | $t_{max}^{2}$  | t <sub>0</sub> (h) | (h-10)                | m    | $k (h^{-1})^{\delta}$ |
| 20     | 10.2           | 3.5                | $7.4 \times 10^{-3}$  | 2.15 | 0.1021                |
| 30     | 5.7            | 1.5                | $1.74 \times 10^{-2}$ | 2.27 | 0.1678                |
| 40     | 3.2            | 0.5                | $3.3 \times 10^{-2}$  | 2.59 | 0.2679                |

<sup>a</sup> Estimated from Figure 3 of ref 9.  $b k = (\text{rate parameter})^{160}$ .

Thomas and Jennings, *Chem. Mat.*, 11:1907-14, 1999.



# Cement Hydration: Jander Equation\*

• In the deceleration period, the Jander equation for diffusion controlled processes has been used to model the reaction of cement during this period:

$$[1-(1-\alpha)^{1/3}]^2 = k_D$$

Where  $k_D$  is the rate constant for diffusion controlled processes.



<sup>\*</sup> Jelenic, Adv. Cem. Tech. Gosh (Ed), p.397, Pergamon, 1987. Bezjak and Jelenic, Cem. Conc. Res., 10:553, 1980.

## Cement Hydration: Simple Kinetic Models

Can estimate α based upon the available water-filled porosity (Φ<sub>w</sub>):

$$\frac{\partial \alpha}{\partial t} = k_1 \phi_W(t)$$

where  $k_1$  is analogous to a first-order rate constant and depends on the specific cement composition, particle size distribution, curing temperature, etc.

- This approach, based upon first order "physical" kinetics and described by Bentz\*, assumes hydration rate is simply proportional to the volume fraction of this water-filled porosity
- Other models\*\* relate the kinetics of hydration to the changing radius of an idealized cement particle or particle distribution

\*D. P. Bentz, "Influence of Water-to-Cement Ratio on Hydration Kinetics: Simple Models Based on Spatial Considerations" at http://ciks.cbt.nist.gov/~garbocz/hydration\_rates/index.html
\*\*J.M. Pommersheim, J.R. Clifton, Mathematical modeling of tricalcium silicate hydration. Cem Concr Res 9 (1979) 765-770.



- T. Knudsen, The dispersion model for hydration of portland cement 1. General concepts, Cem Concr Res 14 (1984) 622-630.
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## Cement Hydration: Simple Kinetic Models

Substituting 
$$\frac{\partial \alpha}{\partial t} = k_1 \phi_W(t)$$

into Powers equation for water-filled porosity

$$\phi_{W}(t) = \frac{\rho_{cem}(w/c) - (f_{exp} + \rho_{cem}CS)\alpha}{1 + \rho_{cem}(w/c)}$$

the result can be integrated and solved with the boundary condition that  $\alpha(0)=0$  to yield:

$$\alpha(t) = Min\{1, \frac{\rho_{cem}(w/c)}{(f_{exp} + \rho_{cem}CS)}[1 - \exp(\frac{-(f_{exp} + \rho_{cem}CS)k_1t}{1 + \rho_{cem}(w/c)})]\}$$

$$CS \text{ is the chemical shrinkage per gram}$$

 $f_{\rm exp}$  is the volumetric expansion coefficient for the "solid" cement

CS is the chemical shrinkage per gram

(the minimum function assures that  $\alpha$ <1)

 Although derived from a different perspective, the above is similar in form to kinetics equations often derived considering nucleation and growth kinetics for cement hydration (so-called Avrami behavior)



# **Heat of Hydration**

For the usual portland cement:

- ~ 1/2 total heat is evolved in 1-3 days
- 3/4 at 7 days
- 83-91% at 180 days



# **Heat of Hydration**

The RATE of heat evolution is related to

- cement composition
- cement fineness
- cement content
- casting temperature

The total heat evolved is related to

- cement composition
- degree of hydration
- cement content



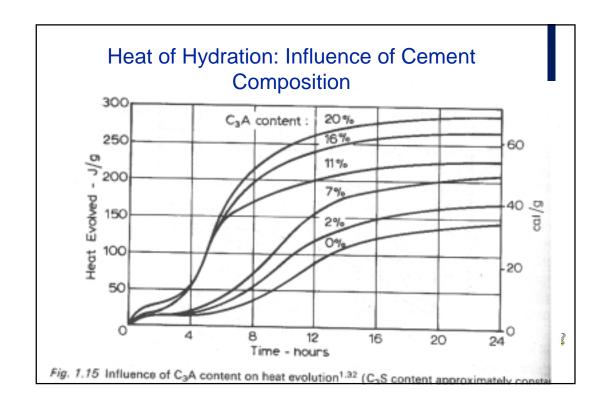
# Heat of Hydration

TABLE 4.3 Heats of Hydration of the Cement Compounds

|   | $\Delta H$ (I/g) for Complete Hydration <sup>e</sup> |                     |                                    |                                   |  |  |
|---|--|---------------------|------------------------------------|-----------------------------------|--|--|
| Reaction                                | Pure Cor<br>Calculated                               | mpounds<br>Measured | Clinker <sup>b,d</sup><br>Measured | Cement <sup>c,d</sup><br>Measured |  |  |
|   |  |                     |                                    |                                   |  |  |
| $C_3S \rightarrow CSH + CH$             | ~380   | 520                 | 570                                | 490                               |  |  |
| $C_2S \rightarrow C-S-H + CH$           | -170   | 260                 | 260                                | 225                               |  |  |
| $C_3A \rightarrow C_4AH_{13} + C_3AH_8$ | ~1160  | -                   | _                                  | -                                 |  |  |
| $\rightarrow C_3AH_4$                   | 900  | 880                 | 840                                | -                                 |  |  |
| → ettringite                            | 1670   | 1670                | -                                  | -                                 |  |  |
| → monosulfoaluminate                    | 1150   | 1140                | -                                  | 1170                              |  |  |
| $C_3AF \rightarrow C_1(A,F)H_6$         | 420  | 420                 | 335                                | -                                 |  |  |
| → monosulfouluminate                    | -  | - 1,11              | _                                  | 380                               |  |  |
| → ettringite                            | 730  | -                   | _                                  | -                                 |  |  |

<sup>&</sup>quot;These values should be negative since they refer to exothermic reactions, but they are customarily written without the negative sign.

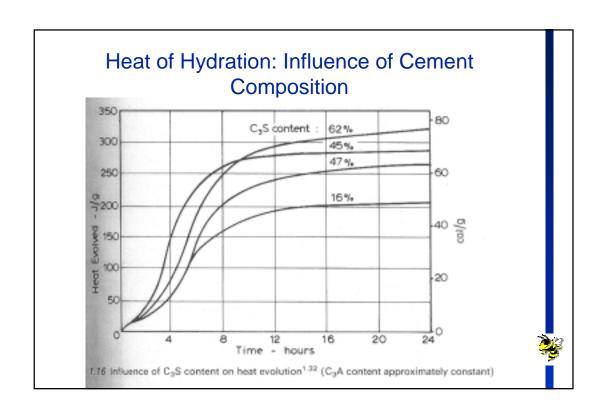


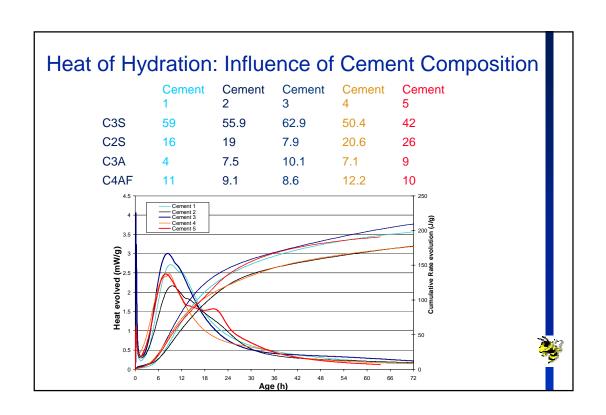


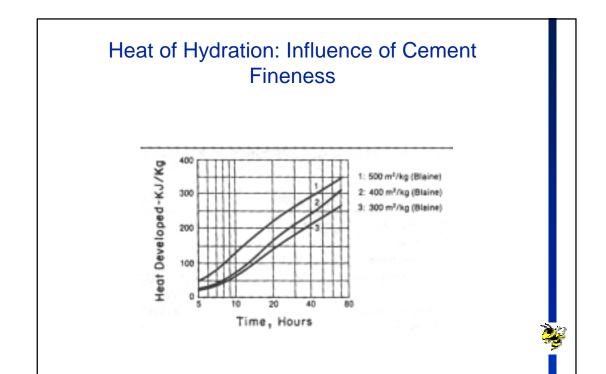
Done-year-old pastes of ground clinker (no added gypsum).

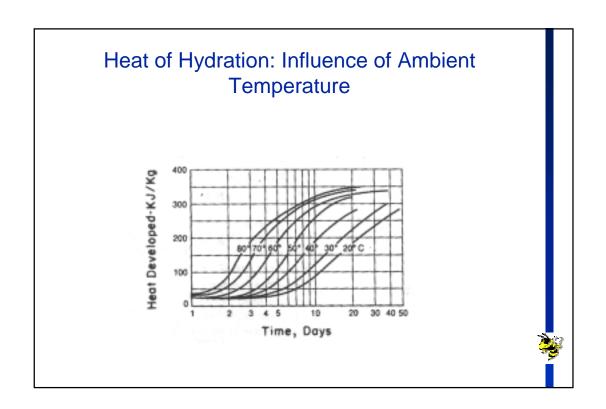
<sup>&#</sup>x27;One-year-old pastes assumed to be completely hydrated.

<sup>&</sup>quot;Individual contributions determined by multiple linear regression analysis.









#### **Estimating Heat of Hydration**

Verbeck and Foster estimated that the overall heat of hydration of a cement is near the sum of the heats of hydration of the individual components.

$$H = aA + bB + cC + dD$$

A,B,C,D are % by wt of C3S, C2S, C3A, C4AF

a,b,c,d are coefficients representing the contribution of 1% of the corresponding compound to the heat of hydration

$$H_{3days}$$
= 240(C3S) + 50(C2S) + 880(C3A) + 290(C4AF) J/g  $H_{1yr}$ = 490(C3S) + 225(C2S) + 1160(C3A) + 375(C4AF) J/g

