

# Link-based and Content-based Evidential Information in a Belief Network Model

*I. Silva, B. Ribeiro-Neto, P. Calado, E. Moura, N. Ziviani*  
Best Student Paper in SIGIR '2000

Ruey-Lung, Hsiao  
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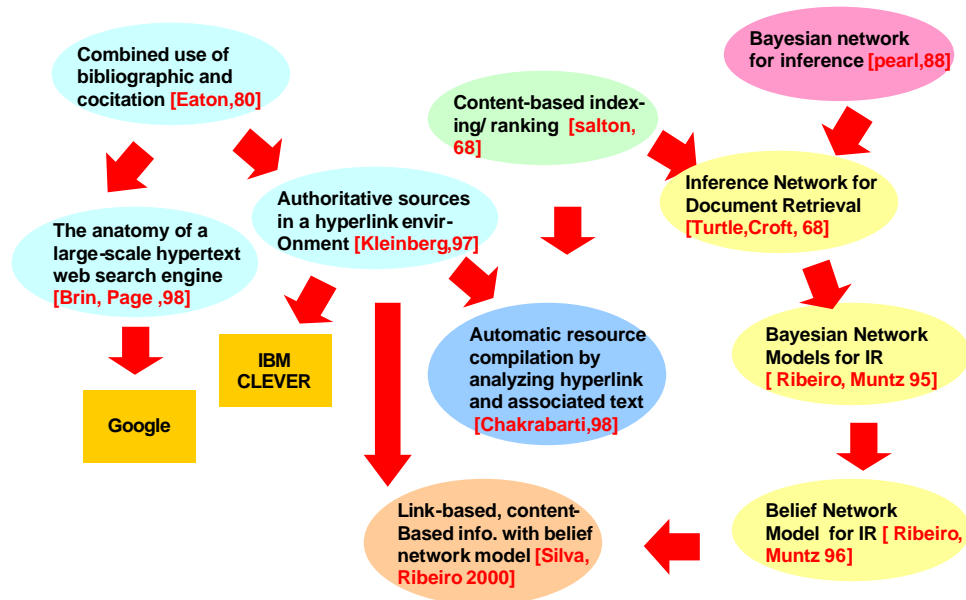
## Introduction

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- **Strategies to determine the ranking of documents in Web Search Engine**
  - Content-Based
  - Link-based
  - Combination of Content-based and Link-based
- **Inference Network / Belief Network Model**
  - Can be used as a general framework for classical IR
  - Allows combining features of distinct models into the same representation scheme

In this paper, the authors propose a retrieval model, which provides a framework for combining information extracted from the content of the documents with information derived from cross-references among the documents, based on belief network model.

## History



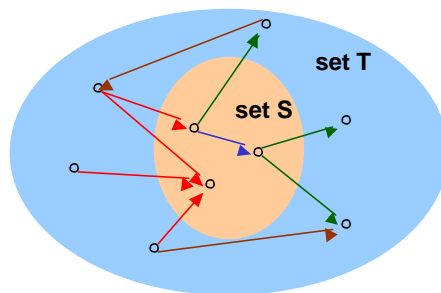
## Related Work (1/4)

- Link-based information
  - Kleinberg(HITS) algorithm [kleinberg '97] [12]
    - hub/authority value for local set
  - PageRank algorithm [Brin,Page '98] [4]
- Bayesian Network Model for Information Retrieval
  - Judea Pearl purpose bayesian network to represent and infer in intelligent system. [13]
  - Turtle, Croft first use bayesian network to model information retrieval problem [19]
  - B. Ribeiro and Muntz generalize bayesian network model to be belief network model. [14,15]
- Combination of link-based/content-based information
  - Automatic resource compilation by analyzing hyperlink structure and associated text , [Chakrabarti 98] [5]
  - Improved algorithm for topic distillation in a hyperlinked environment [Bharat] [2]

## Related Work (2/4)

### – HITS algorithm

- Start with a root set  $S$ 
  - $S_s$  is relatively small (typically up to 200 pages)
  - $S_s$  is rich in relevant pages
  - $S_s$  contains most (or many) of the strongest authorities.
- Recursively compute the degree of authority and hub for each element.



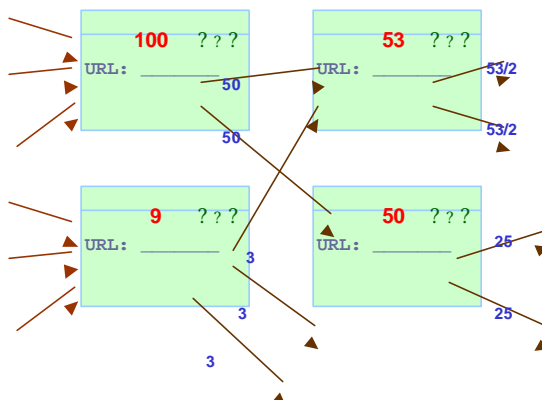
$$a(p) = \sum_{q: p \rightarrow q} h(q)$$

$$h(p) = \sum_{p' : p' \rightarrow p} a(p')$$

## Related Work (3/4)

### – PageRank algorithm

- Propagation of ranking through links



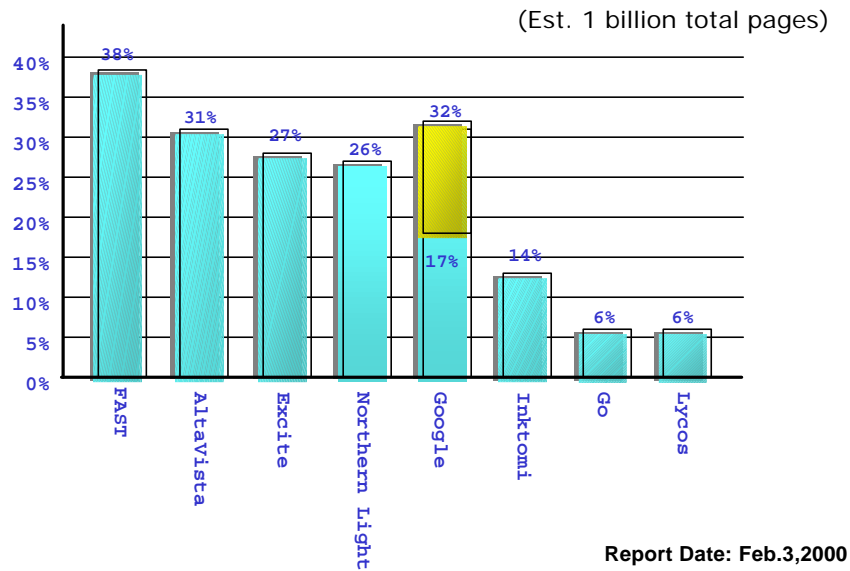
$B_u$  : back link

$F_u$  : forward link

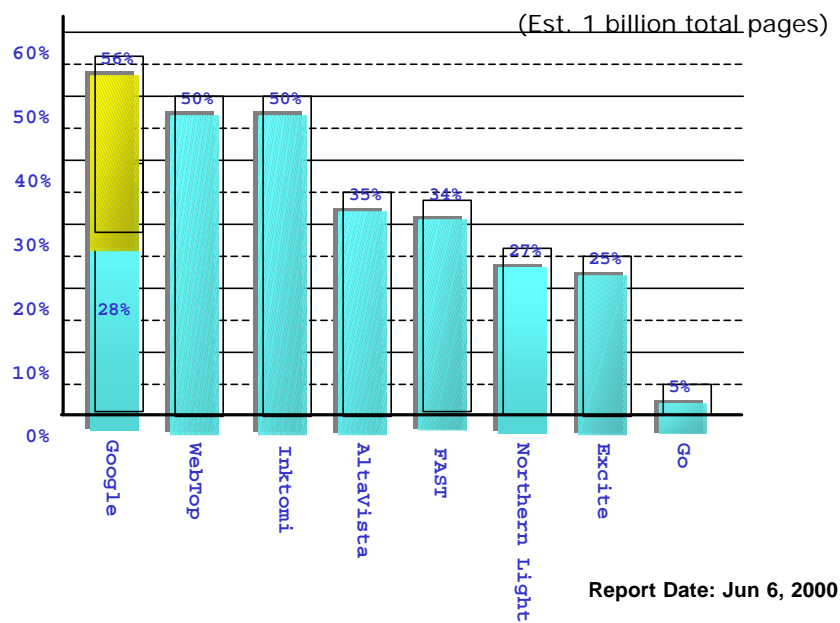
$N_u = |F_u|$

$$R'(u) = c \sum_{v: B_u} \frac{R(v)}{N_v} + cE(u)$$

## Coverage of the Web (1/2)



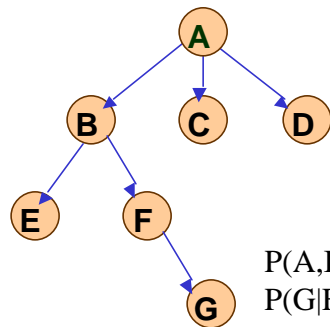
## Coverage of the Web (2/2)



## Related Work (4/4)

- Belief Network Model

- Based on Bayesian Network
- Subsumes the classical models in IR
- More general than the inference network model



$$X = X_1, \dots, X_n$$

$$P(X) = \prod_{i=1}^n P(X_i | \text{Parents}(X_i))$$

$$P(A, B, C, D, E, F, G) =$$

$$P(G|F)P(F|B)P(E|B)P(B|A)P(C|A)P(D|A)P(A)$$

## Belief Network Model - Ranking

Degree of coverage of the space U by c

$$P(c) = \sum_u P(c|u) \times P(u)$$

$$P(u) = \binom{t}{2}^t$$

Ranking

$$P(d_i|q) = \sum_u P(d_i|u) \times P(q|u) \times P(u)$$

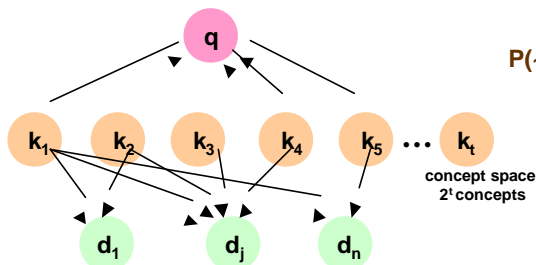
Vector Space Model

$$P(q|u) = \begin{cases} 1 & \text{if } k_i, g_i(q) = g_i(u) \\ 0 & \text{otherwise} \end{cases}$$

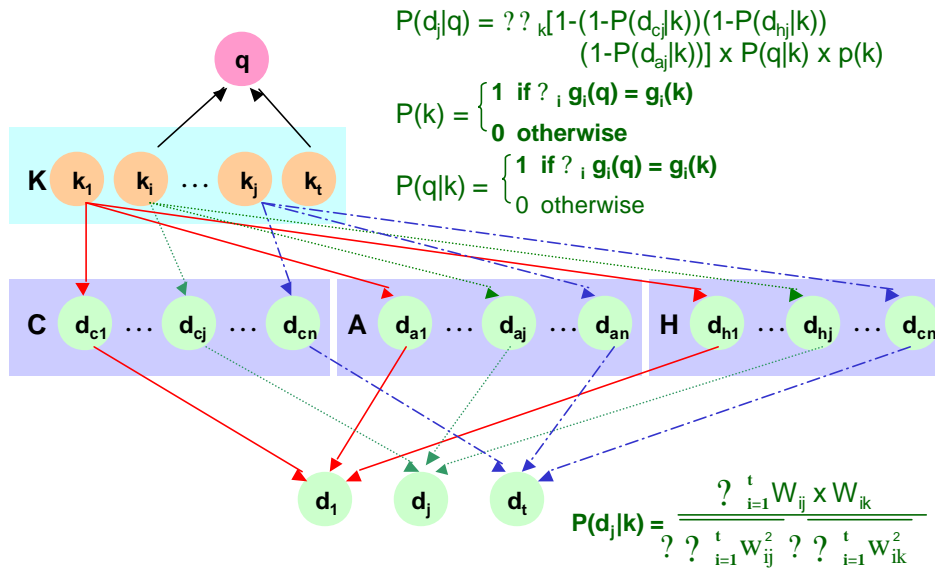
$$P(\sim q|u) = 1 - p(q|u)$$

$$P(d|u) = \frac{\sum_{i=1}^t w_{ij} \times w_{ik}}{\sum_{i=1}^t w_{ij}^2 \times \sum_{i=1}^t w_{ik}^2}$$

$$P(\sim d|u) = 1 - p(d|u)$$



## Modeling Content/Link-Based Evidence



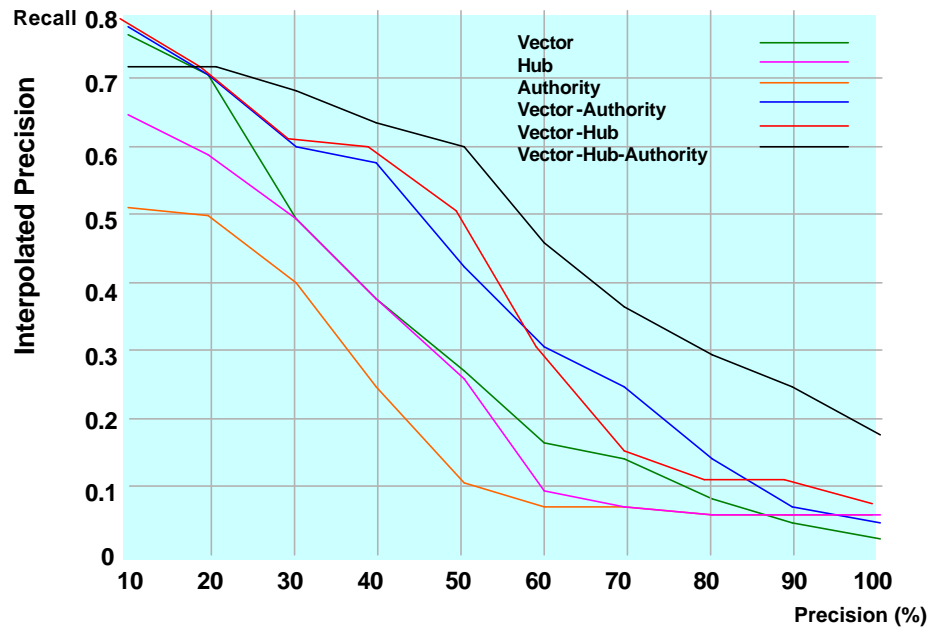
## Evaluation

- **Reference collection**

- 3,027,540 pages of the Brazilian Web. (collected by CoBWeb, indexed by inverted lists)
- 20 queries are selected from hot queries of TodoBR search engine logs.
- For each of the 20 queries, use top 10 documents to compose query pool (so each query contains at most 60 distinct pages).
  - Average number of pages per query pool is 38.15
  - Average number of relevant pages per query pool is 17.05

Number of pages	Number of keywords	Average # of word / page	# of queries	Average # of word / query	Ave. # of page / query pool	Ave. # of relevant page / query pool
3,027,540	3,456,910	512	20	1.6	38.15	17.05

## Recall ? Average precision for 20 Web queries



## Conclusion

- Belief network model provides powerful mechanisms to model the information retrieval problem, specially when distinct sources of evidence are available.
- Hub and authority values performs better in combination than in isolation.

Average Precision and Gains							
Recall	Vector	Vector-authority	Gain	Vector-authority	Gain	Vector-hub authority	Gain
10%	0.765	0.780	+1%	0.776	+1%	0.722	-5%
20%	0.700	0.700	+0%	0.690	-1%	0.726	+3%
30%	0.502	0.604	+20%	0.605	+20%	0.685	+36%
40%	0.366	0.574	+56%	0.591	+61%	0.640	+74%
50%	0.275	0.447	+62%	0.503	+82%	0.604	+119%
60%	0.166	0.312	+87%	0.295	+77%	0.439	+164%
70%	0.154	0.250	+62%	0.144	-6%	0.368	+138%
80%	0.080	0.144	+79%	0.098	+22%	0.297	+271%
90%	0.035	0.062	+77%	0.096	+174%	0.247	+605%
100%	0.020	0.040	+100%	0.037	+84%	0.162	+710%
Average	0.306	0.391	+27%	0.384	+25%	0.489	+59%

## Reference

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	Title	Author	From
Model	13. Probabilistic Reasoning in Intelligent Systems	Judea Pearl	Book 1988
	14. Bayseian network model for ir	B. Ribeiro , I. Silva	Soft Computing
	15. A belief network model for ir	B. Ribeiro , R. Muntz.	SIGIR '96
	19. Evaluation of an inference network-based retrieval model	H. Turtle , W. Croft	ACM trns. IS '91
	21. A probabilistic inference model for information retrieval.	S. Wong and Y. Yao	Info. System '91
Link	04. The anatomy of a large-scale hypertext web search engine	S. Brin , L. Page	WWW '98
	12. Authoritative sources in a hyperlinked environment.	J. M. Kleinberg	ACM-SIAM '98
Content	01. Modern Information Retrieval	R. Baesz-Yates, B. Ribeiro	Book '99
	16. Introduction to Modern Information Retrieval	G. Salton , M. McGill	Book 1983
	17. Automatic Information Organization and Retrieval	G. Salton	Book 1968
Hybrid	02. Improved algorithms for topic distillation in a hyperlink environment	K. Bharat , M. R. Henzinger	SIGIR '98
	05. Automatic resource compilation by analyzing hyperlink structure and associated text	G. Salton	Book 1998