

Horizontal reflection of a low-frequency sound signal from a moving nonlinear internal wave front

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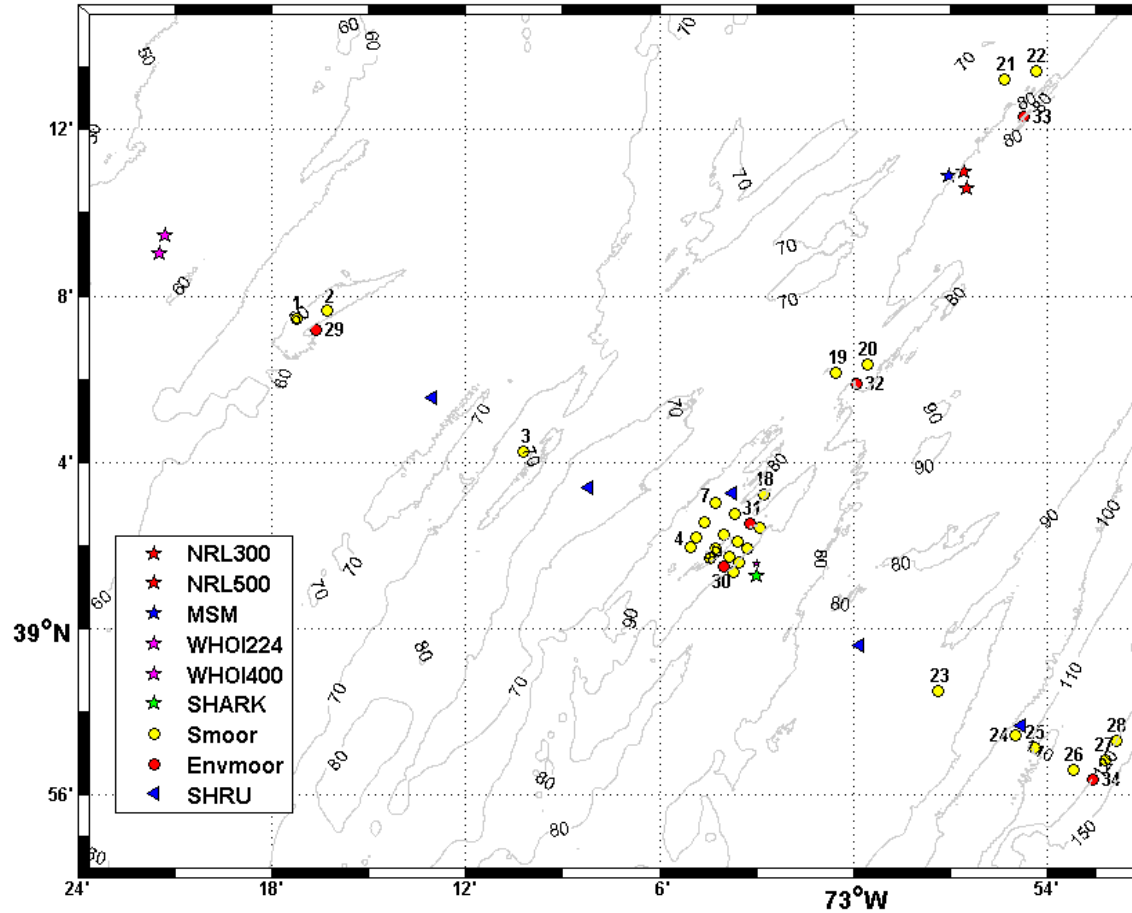
159 ASA meeting in Baltimore

April 22, 2010

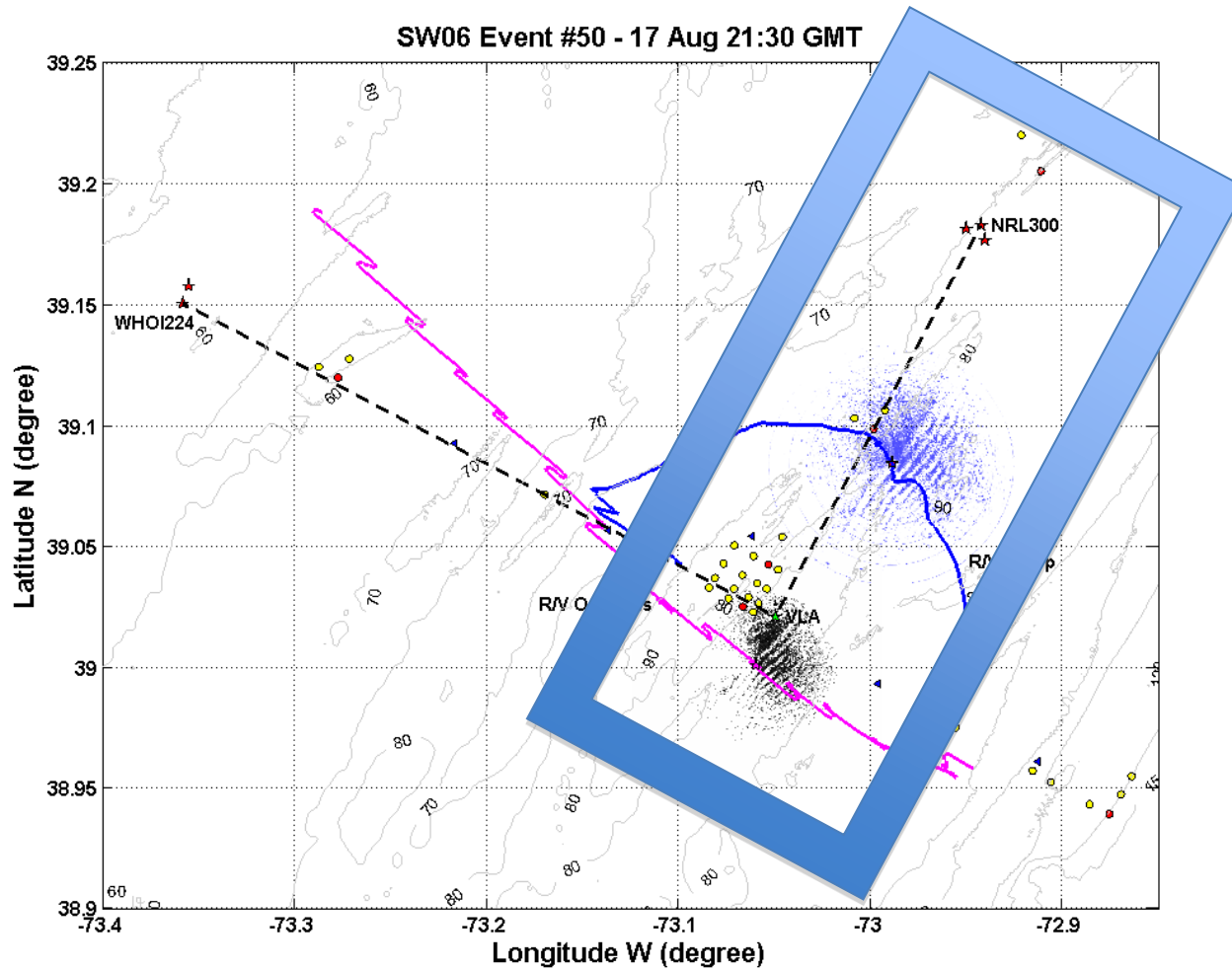
Outline

- Observation
- Modal picture
- Theory
- Discussion
- Summary

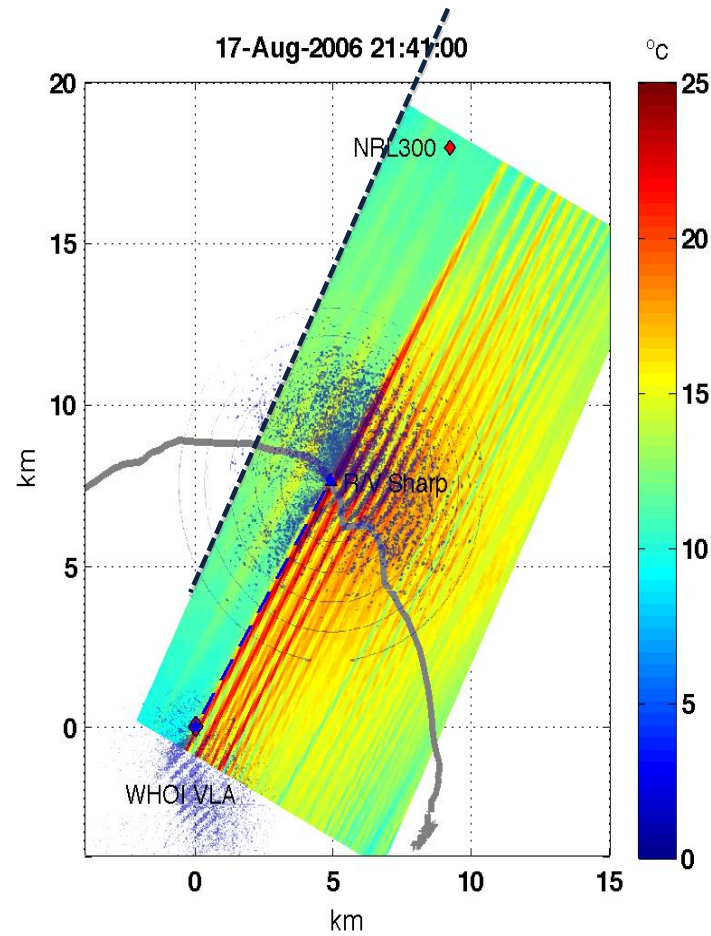
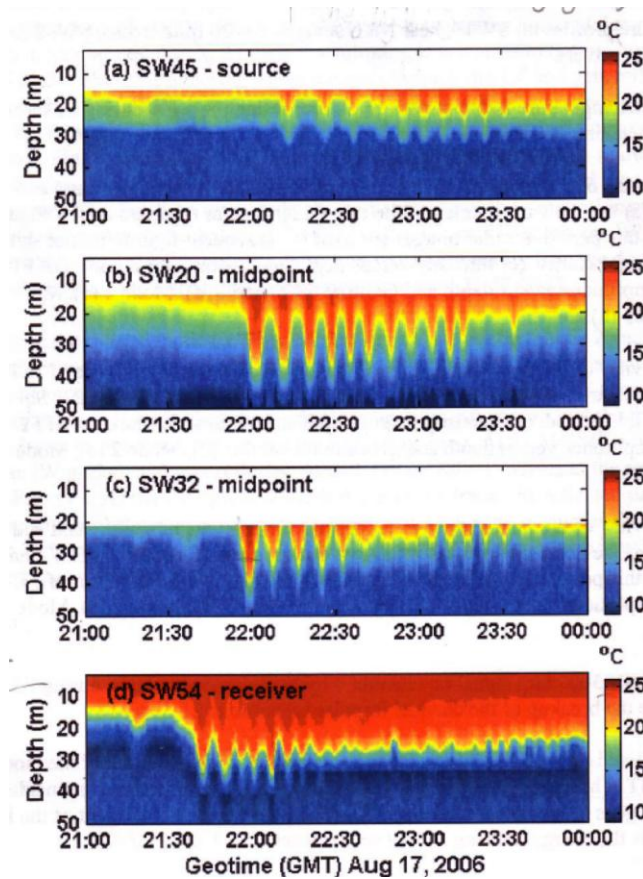
SW06 experiment, fixed source-receiver, IW Event 50



Source-receiver configuration

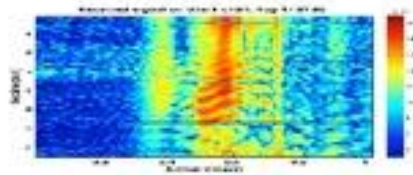


Environment re-construction

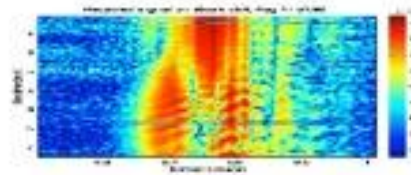


Hydrophones in depth

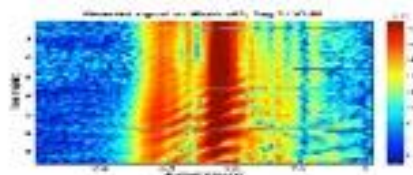
13.5 m



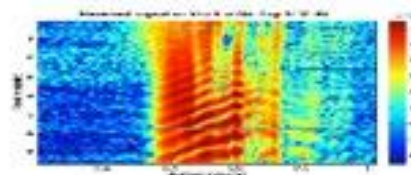
42.25 m



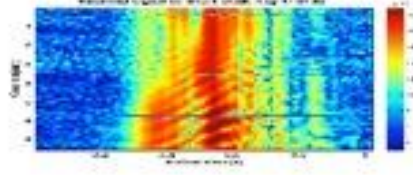
24.75 m



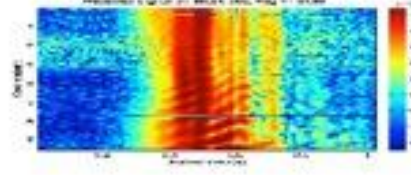
54.75 m



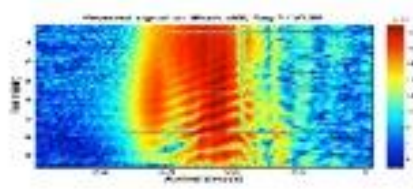
28.5 m



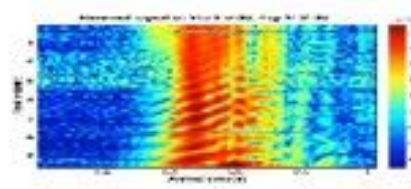
62.25 m



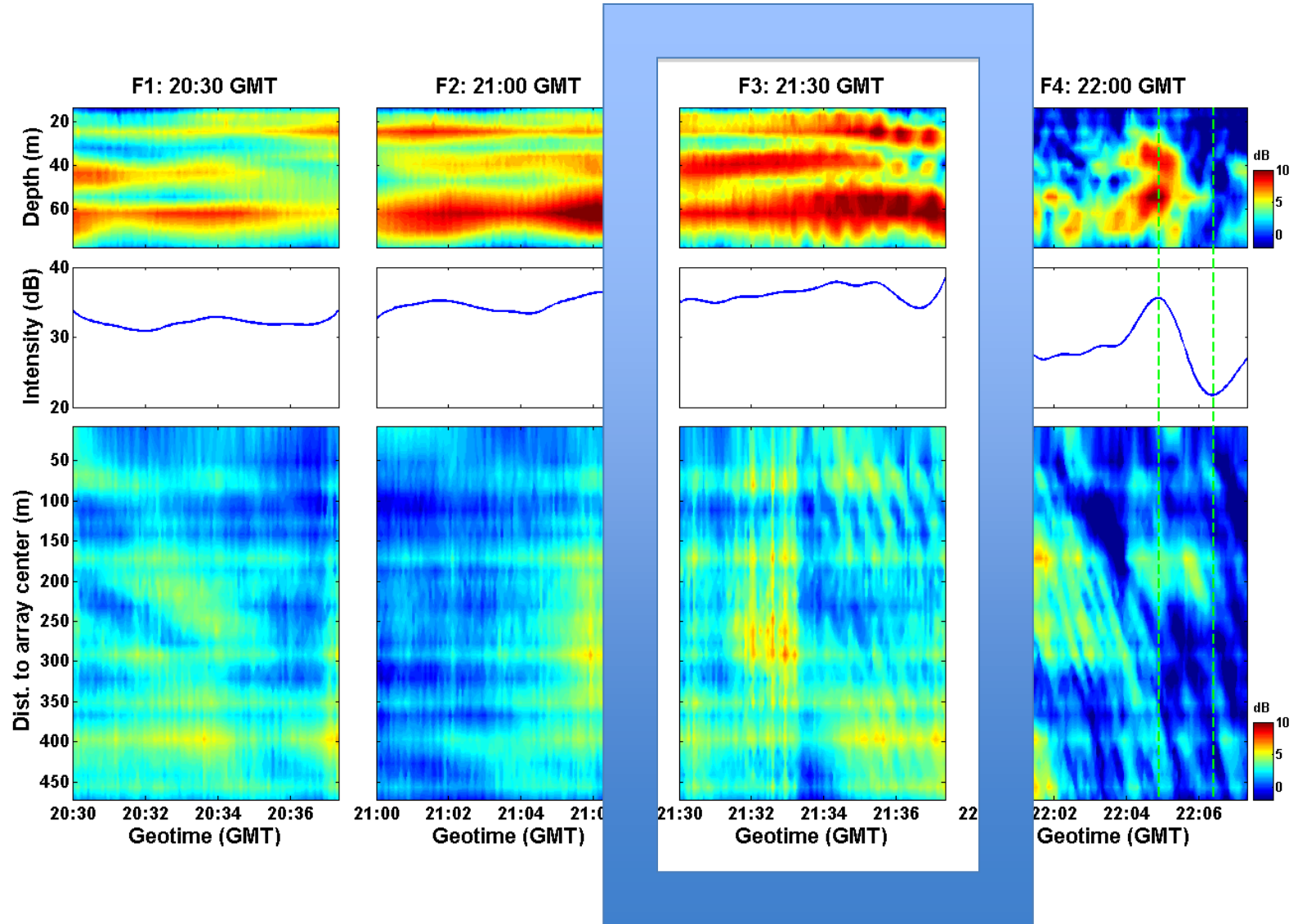
39.75 m



69.75 m



VLA & HLA for 4 Transmissions 7 mins each

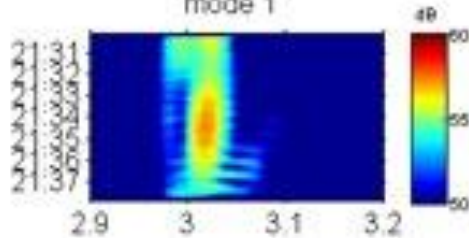


Mode filtering

Transmission starting from 17/Aug 21:30

NRL300

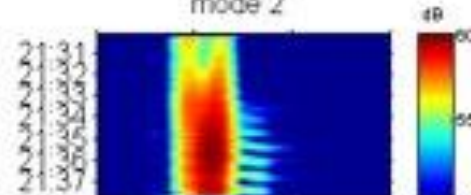
mode 1



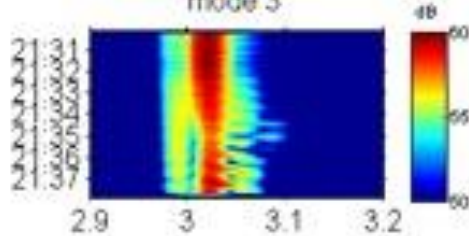
Transmission starting from 17/Aug 21:30

NRL300

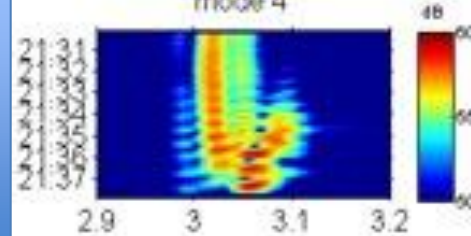
mode 2



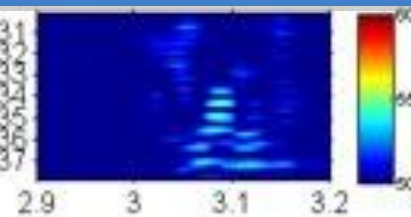
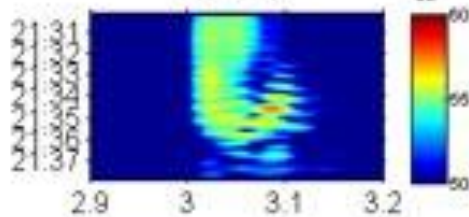
mode 3



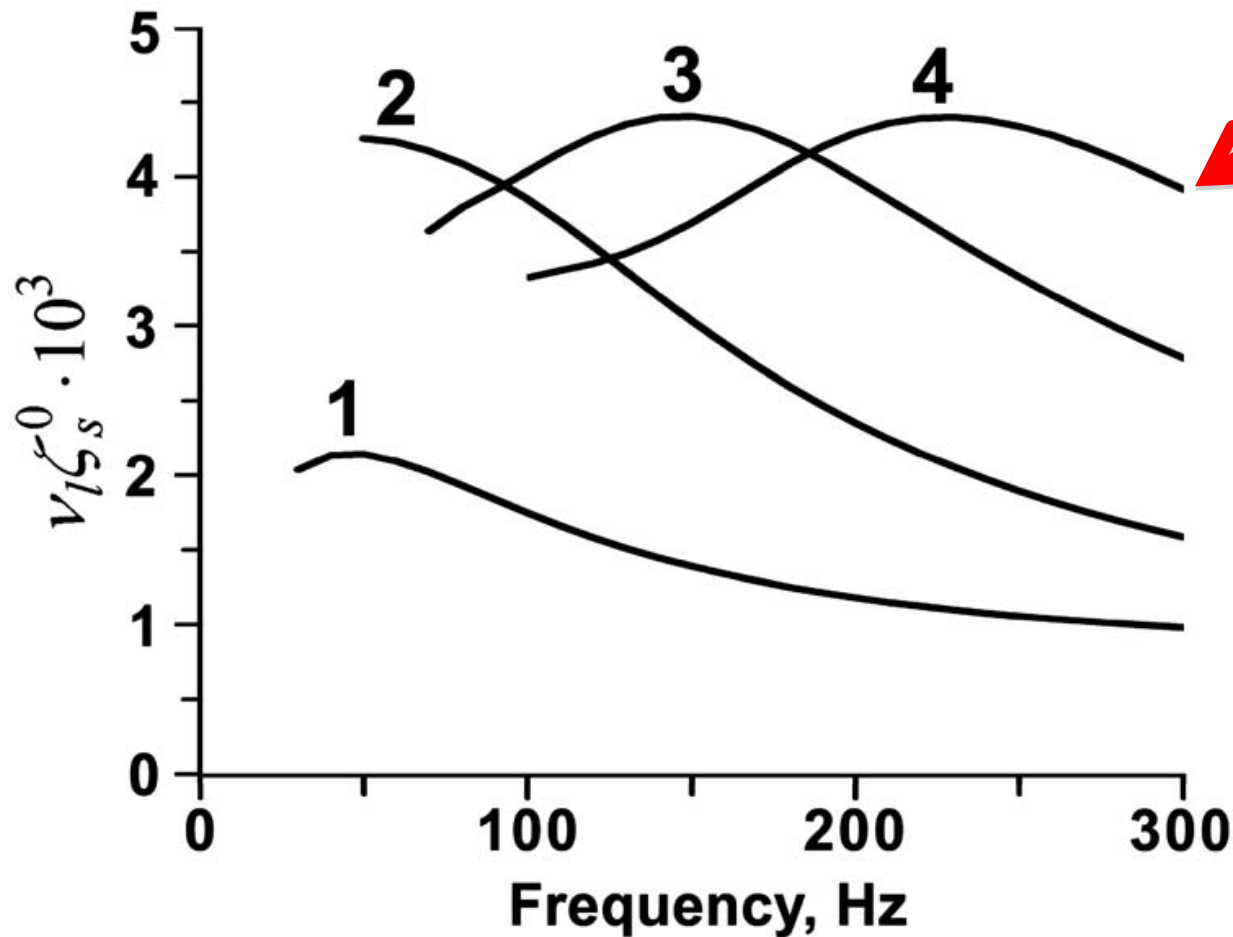
mode 4



mode 5

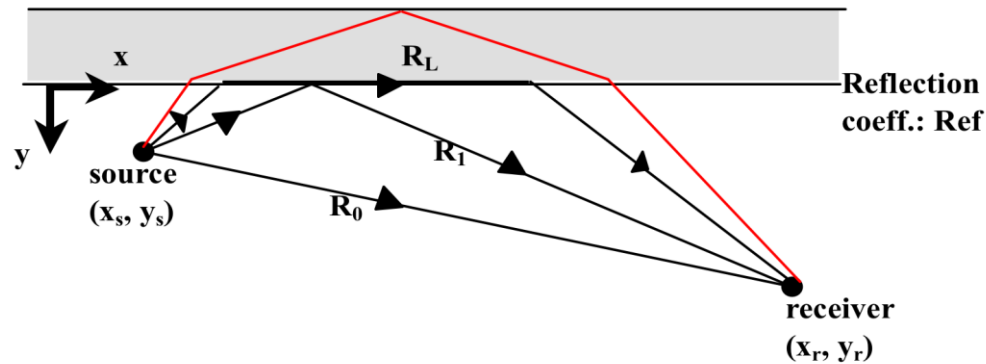


Frequency dependent index of refraction

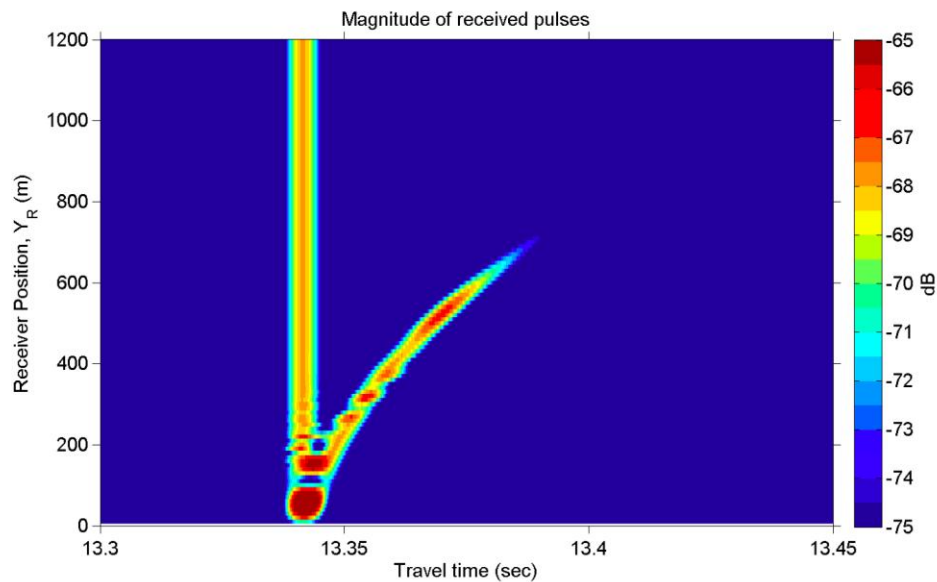


Badiey, Katsnelson, Lynch, Preselkov "Frequency dependence and intensity fluctuations due to shallow water internal waves" JASA 122(2), 2007

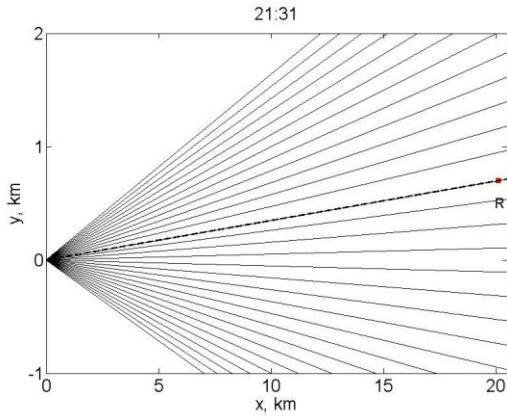
Simple theory



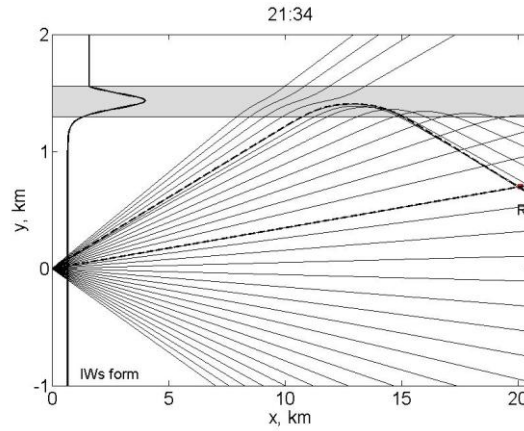
$$p = \frac{1}{2\pi} \int_{-\infty}^{\infty} \frac{i}{2k_y} \left(e^{ik_y|y-y_s|} + \text{Ref} \cdot e^{ik_y(y+y_s)} \right) e^{ik_x} dk_x$$



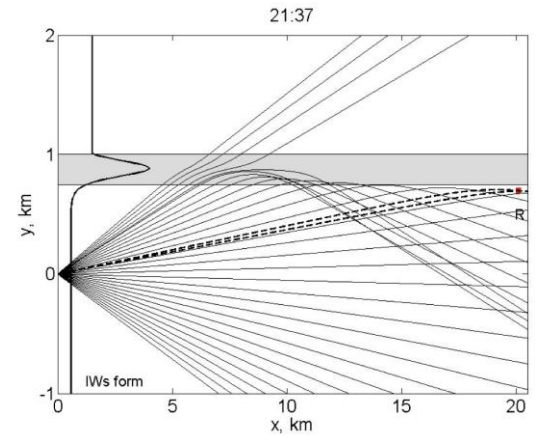
(a) No Internal Wave



(b) Internal Wave+ refraction



(c) After Internal Wave



$$\frac{d^2 \psi_l(\mathbf{r}, z, T)}{dz^2} + \left\{ \frac{\omega^2}{[c_0(z) + \delta c(\mathbf{r}, z, T)]^2} - \xi_l^2(\mathbf{r}, T) \right\} \psi_l(\mathbf{r}, z, T) = 0$$

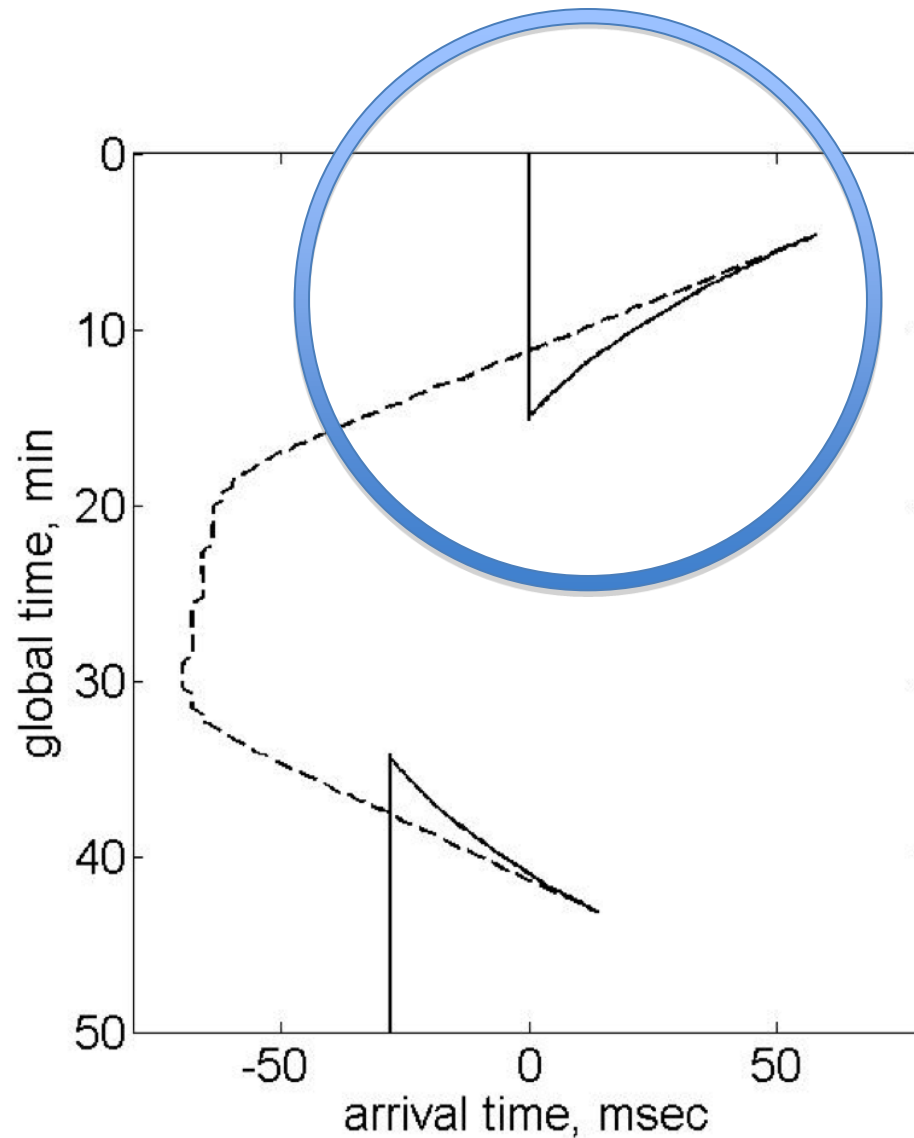
$$P(\mathbf{r}, z, t) = 2 \int_0^\infty S(\omega) \sum_l P_l(\mathbf{r}, \mathbf{r}_s) \psi_l(\mathbf{r}, z) e^{-i\omega t} d\omega$$

$$\mu_l = -v_l \zeta_s(\mathbf{r}, T)$$

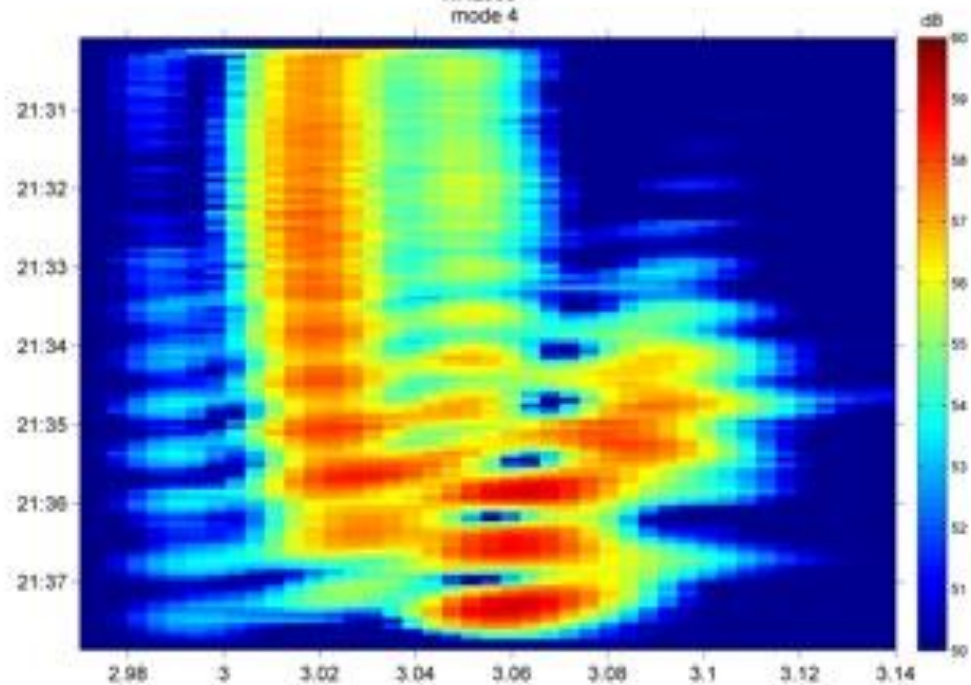
Where

$$v_l = \frac{2Qk^2}{(q_l^0)^2} \int_0^H [\psi_l^0(z)]^2 N^2(z) \Phi(z) dz$$

Ray coupling & shadow zone



Transmission starting from 17/Aug 21:30
NRL300
mode 4



Summary & conclusions

- Unique observation of reflection/refraction of signal in horizontal plane from an approaching internal wave in the water column
- Mechanism of horizontal refraction is confirmed (Modal and frequency dependence)
- Observation confirmed with our previous data collected in the same area in SWARM95