



Higgs self-coupling in the MSSM and NMSSM after the LHC Run 1



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ABSTRACT

Measuring the Higgs self-coupling is one of the crucial physics goals at the LHC Run-2 and other future colliders. In this work, we attempt to figure out the size of SUSY effects on the trilinear self-coupling of the 125 GeV Higgs boson in the MSSM and NMSSM after the LHC Run-1. Taking account of current experimental constraints, such as the Higgs data, flavor constraints, electroweak precision observables and dark matter detections, we obtain the observations: (1) In the MSSM, the ratio $\lambda_{3h}^{\text{MSSM}}/\lambda_{3h}^{\text{SM}}$ has been tightly constrained by the LHC data, which can be only slightly smaller than 1 and minimally reach 97%; (2) In the NMSSM with $\lambda < 0.7$, a sizable reduction of $\lambda_{3h_2}^{\text{NMSSM}}/\lambda_{3h_2}^{\text{SM}}$ can occur and minimally reach 10% when the lightest CP-even Higgs boson mass m_{h_1} is close to the SM-like Higgs boson m_{h_2} due to the large mixing angle between the singlet and doublet Higgs bosons; (3) In the NMSSM with $\lambda > 0.7$, a large enhancement or reduction $-1.1 < \lambda_{3h_1}^{\text{NMSSM}}/\lambda_{3h_1}^{\text{SM}} < 2$ can occur, which is accompanied by a sizable change of $h_1\tau^+\tau^-$ coupling. The future colliders, such as the HL-LHC and ILC, will have the capacity to test these large deviations in the NMSSM.

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1. Introduction

With the discovery of the Higgs boson at the LHC [1,2], much effort has been devoted to study its properties. So far, the measurements of its couplings and quantum numbers are compatible with the standard model (SM) predictions at $1-2\sigma$ level. However, to ultimately understand its nature, we need to fully reconstruct the Higgs potential at the LHC and future e^+e^- colliders [3,4]. The parameters in the Higgs potential determine the relations among the Higgs masses and self-couplings. Measuring these relations is therefore crucial for our understanding of the Higgs nature.

In the SM the tree-level Higgs potential is given by

$$V^{(0,\text{SM})} = -\mu^2(\phi^\dagger\phi) + \lambda(\phi^\dagger\phi)^2, \quad \phi = \frac{1}{\sqrt{2}}(0, v+h)^T \quad (1)$$

which yields the following trilinear and quartic self-couplings

$$\lambda_{hhh}^{(0,\text{SM})} = \frac{3m_h^2}{v}, \quad \lambda_{hhhh}^{(0,\text{SM})} = \frac{3m_h^2}{v^2}. \quad (2)$$

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Here $v = (\sqrt{2}G_F)^{-1/2} \simeq 246$ GeV is the vacuum expectation value of the Higgs field and $m_h \simeq 125$ GeV is the Higgs boson mass. Within the SM, the trilinear Higgs coupling receives the dominant correction from the top quark loop, $\delta\lambda_{hhh}^{\text{SM}} \simeq m_t^4/(\pi^2 v^2 m_h^2)$ [5], which reduces its tree-level value by about 10%. Hence, the determination of the Higgs trilinear coupling λ_{hhh} and quartic coupling λ_{hhhh} can directly test the relation in Eq. (2) which is obtained from the minimization of the Higgs potential. At the LHC, the only way to measure the Higgs trilinear coupling is through the Higgs pair production, which is dominated by the gluon fusion mechanism and has a small cross section [6]. However, in many new physics models, such as the minimal supersymmetric model (MSSM) and the next-to-minimal supersymmetric model (NMSSM), the Higgs pair production rate can be significantly altered by new particles and Higgs couplings [7]. Among various decay channels of the Higgs pair, the $4b$ final state has the largest fraction [8], but the rare process $hh \rightarrow b\bar{b}\gamma\gamma$ is expected to have the most promising sensitivity due to the low backgrounds at the LHC [9]. The recent applications of jet substructure and other techniques to Higgs pair production have been found to improve the sensitivity to the trilinear Higgs couplings in $\tau^+\tau^-$ and W^+W^- final states [10]. On the other hand, the measurement of the Higgs quartic coupling is more challenging due to a much smaller cross section of triple Higgs production at the LHC.

The supersymmetric (SUSY) corrections to the Higgs self-coupling have two kinds of sources: one is the mixing between the Higgs bosons, and the other is radiative quantum effects. For the first kind, the authors in [11] studied the Higgs self-coupling in some simplified SUSY models, while in [12] the Higgs self-couplings in the MSSM and NMSSM (with a decoupled singlet boson) were investigated. Also, in [13] the authors studied the properties of the Higgs bosons in the NMSSM with $\lambda > 0.7$ (called λ -SUSY) and found a sizable enhancement in the Higgs self-coupling. For the second kind of SUSY corrections, the loop corrections to the Higgs self-couplings have been studied using the effective potential [14–22] or Feynman diagrammatic approach [23–25] in the MSSM and NMSSM. Recently, the leading two-loop SUSY-QCD corrections from the top/stop sector in the MSSM have been performed [26]. Since all these previous studies are limited to some simplified or special cases and the relevant experimental constraints are not fully considered, in this work we give a comprehensive study for the SM-like Higgs self-coupling in the MSSM and NMSSM with both $\lambda < 0.7$ and $\lambda > 0.7$ by considering all the relevant experimental constraints after the LHC Run-1.

The existing experimental data, both from low energy precision measurements and high energy direct searches, may have imposed important constraints on the Higgs self-coupling in SUSY models. For example, in the MSSM, the SM-like Higgs self-coupling is sensitive to the pseudo-scalar mass m_A and $\tan\beta$, which could have been tightly constrained by the LHC direct search of a light non-SM Higgs boson [27–29] as well as from precision B -physics [30]. Furthermore, the measured mass of the SM-like Higgs boson requires rather heavy stops and/or large Higgs-stop trilinear couplings, and the direct searches for the stop pair production have also pushed stop masses above hundreds of GeV in the natural SUSY [31]. Since the Higgs self-couplings are sensitive to stop masses and Higgs-stop trilinear couplings, all these constraints should be taken into account.

The structure of this paper is organized as follows. In Section 2, we will briefly describe the Higgs sectors of MSSM and NMSSM. In Section 3, we perform a scan over the parameter space of each model and present the numerical results for the trilinear self-coupling of the SM-like Higgs. Finally, we draw our conclusions in Section 4.

2. Higgs trilinear self-couplings in MSSM and NMSSM

2.1. Higgs trilinear self-couplings in the MSSM

In the MSSM there are two doublets of complex scalar fields with opposite hypercharges:

$$H_u = \begin{pmatrix} H_u^+ \\ H_u^0 \end{pmatrix}, \quad H_d = \begin{pmatrix} H_d^0 \\ H_d^- \end{pmatrix}. \quad (3)$$

The scalar Higgs potential consists of the D -terms and F -terms of the superpotential as well as the soft SUSY-breaking mass terms. Among them, the D -terms determine the quartic Higgs interactions. The full tree-level Higgs potential is given by

$$V^{(0,MSSM)} = m_1^2 |H_u|^2 + m_2^2 |H_d|^2 - B_\mu \epsilon_{\alpha\beta} (H_u^\alpha H_d^\beta + h.c.) + \frac{g^2 + g'^2}{8} (|H_u|^2 - |H_d|^2)^2 + \frac{g^2}{2} |H_u^\dagger H_d|^2, \quad (4)$$

where $\epsilon_{\alpha\beta}$ is the antisymmetric tensor and $m_{1,2}^2 = m_{H_{u,d}}^2 + \mu^2$ with $m_{H_{u,d}}$ and μ denoting the soft SUSY-breaking masses and the higgsino mass, respectively. The parameters $m_{1,2}$ can be eliminated by the minimization condition of the Higgs potential, while the

parameter B_μ is traded for the pseudoscalar mass M_A . The quartic Higgs couplings are fixed in terms of the $SU(2) \times U(1)$ gauge couplings g and g' in the MSSM.

After the electroweak symmetry breaking, the neutral components of the two Higgs fields $H_{u,d}^0$ develop vacuum expectation values (vevs) $v_{u,d}$ and can be decomposed into scalar and pseudoscalar components as

$$\begin{aligned} \text{Re } H_d^0 &= (v_d + H c_\alpha - h s_\alpha)/\sqrt{2}, \\ \text{Im } H_d^0 &= (G^0 c_\beta - A s_\beta)/\sqrt{2}, \end{aligned} \quad (5)$$

$$\begin{aligned} \text{Re } H_u^0 &= (v_u + H s_\alpha + h c_\alpha)/\sqrt{2}, \\ \text{Im } H_u^0 &= (G^0 s_\beta + A c_\beta)/\sqrt{2} \end{aligned} \quad (6)$$

where h, H and A are the neutral physical Higgs bosons and G^0 is the would-be Goldstone boson. The vevs are defined as $v_u = v s_\beta$ and $v_d = v c_\beta$ with $v \approx 246$ GeV (here and in the following we use the notation $c_x \equiv \cos x$, $s_x \equiv \sin x$).

Taking the third derivatives of $V^{(0,MSSM)}$ with respect to the physical Higgs fields yields the trilinear Higgs couplings. In the physical mass eigenstates, the neutral CP-even Higgs trilinear couplings at leading order are given by

$$\begin{aligned} \lambda_{hhh}^{(0,MSSM)} &= \frac{3M_Z^2}{v} c_{2\alpha} s_{\alpha+\beta}, \\ \lambda_{Hhh}^{(0,MSSM)} &= \frac{M_Z^2}{v} [2s_{2\alpha} s_{\alpha+\beta} - c_{2\alpha} c_{\alpha+\beta}], \end{aligned} \quad (7)$$

$$\begin{aligned} \lambda_{HHH}^{(0,MSSM)} &= \frac{3M_Z^2}{v} c_{2\alpha} c_{\alpha+\beta}, \\ \lambda_{HHh}^{(0,MSSM)} &= -\frac{M_Z^2}{v} [2s_{2\alpha} c_{\alpha+\beta} + c_{2\alpha} s_{\alpha+\beta}]. \end{aligned} \quad (8)$$

In the MSSM, either the lighter scalar h or the heavier scalar H can be the SM-like Higgs boson. The latter interpretation occurs for low values of M_A (between 100 and 120 GeV) with moderate values of $\tan\beta$ (about 10). In this case, H has approximately SM-like properties, while the other four Higgs bosons of the MSSM would be rather light and have a mass of order 100 GeV or even below. A dedicated scan for this region of parameter space has been performed in [32] and it was found that this scenario can be excluded by recasting the LHC search for $H/A \rightarrow \tau^+ \tau^-$ [27]. In addition, the latest ATLAS limits from H^\pm searches have also excluded such a possibility [29]. Thus, in this work, we will only study the case that h is the SM-like Higgs boson in the MSSM. According to Appelquist–Carazzone decoupling theorem, the MSSM must go back to the SM in the decoupling limit. In the tree-level Higgs sector, we can make this limit by setting $m_A \rightarrow \infty$, which gives $\alpha \rightarrow \beta - \frac{\pi}{2}$. Applying this relation to the first identity in Eq. (7) yields

$$\lambda_{hhh}^{(0,MSSM)} \simeq \frac{3M_Z^2}{v} c_{2\beta}^2 \simeq \frac{3m_{h,(0,MSSM)}^2}{v}, \quad (9)$$

where $m_{h,(0,MSSM)} \simeq M_Z c_{2\beta}$ is the lighter CP-even Higgs mass at tree-level. This demonstrates that the lighter Higgs boson h in the MSSM almost behaves like the SM Higgs boson in the decoupling limit (even when the loop corrections are included) [23,24].

2.2. Higgs trilinear self-couplings in the NMSSM

After the discovery of a 125 GeV Higgs boson, the NMSSM [33] seems to be more favored than the MSSM because it can naturally give such a Higgs boson without very heavy top-squarks [34]. More importantly, this model can solve the μ -problem: after the singlet field develops a vev $\langle S \rangle = v_s/\sqrt{2}$, an effective μ -term

($\mu_{\text{eff}} = \lambda v_s / \sqrt{2}$) is dynamically generated. Due to the contribution of the singlet scalar field S , the full tree-level Higgs potential can be written as

$$\begin{aligned} V^{(0, \text{NMSSM})} = & (|\lambda S|^2 + m_{H_u}^2) H_u^\dagger H_u \\ & + (|\lambda S|^2 + m_{H_d}^2) H_d^\dagger H_d + m_S^2 |S|^2 \\ & + \frac{1}{8} (g_2^2 + g_1^2) (H_u^\dagger H_u - H_d^\dagger H_d)^2 + \frac{1}{2} g_2^2 |H_u^\dagger H_d|^2 \\ & + |\epsilon^{\alpha\beta} \lambda H_u^\alpha H_d^\beta + \kappa S^2|^2 \\ & + [\epsilon^{\alpha\beta} \lambda A_\lambda H_u^\alpha H_d^\beta S + \frac{1}{3} \kappa A_\kappa S^3 + h.c.], \end{aligned} \quad (10)$$

where κ and λ are dimensionless parameters, and A_λ and A_κ are the corresponding trilinear soft breaking parameters. To clearly show the properties of the Higgs sector, we can expand the neutral scalar fields around the vevs as [33]

$$\begin{aligned} \text{Re } H_d^0 &= (v_d - H \sin \beta + h \cos \beta) / \sqrt{2}, \\ \text{Im } H_d^0 &= (P \sin \beta + G^0 \cos \beta) / \sqrt{2}, \\ \text{Re } H_u^0 &= (v_u + H \cos \beta + h \sin \beta) / \sqrt{2}, \\ \text{Im } H_u^0 &= (P \cos \beta - G^0 \sin \beta) / \sqrt{2}, \\ \text{Re } S &= (v_s + s) / \sqrt{2}, \\ \text{Im } S &= P_S / \sqrt{2}. \end{aligned} \quad (11)$$

Substituting Eq. (11) into Eq. (10), we obtain the mass matrix squared M_S^2 for the neutral CP-even Higgs bosons and the trilinear Higgs self-interactions as

$$V_{\text{CP-even}}^{(0, \text{NMSSM})} = \frac{1}{2} (H, h, s) M_S^2 \begin{pmatrix} H \\ h \\ s \end{pmatrix} + \lambda_{h_\alpha h_\beta h_\gamma} h_\alpha h_\beta h_\gamma, \quad (12)$$

with $h_{\alpha, \beta, \gamma} = H, h, s$. The tree-level M_{Sij}^2 are given by [35]

$$M_{S11}^2 = M_A^2 + (M_Z^2 - \frac{1}{2} \lambda^2 v^2) \sin^2 2\beta, \quad (13)$$

$$M_{S12}^2 = -\frac{1}{2} (M_Z^2 - \frac{1}{2} \lambda^2 v^2) \sin 4\beta, \quad (14)$$

$$M_{S13}^2 = -\sqrt{2} \lambda v \mu x \cot 2\beta, \quad (15)$$

$$M_{S22}^2 = M_Z^2 \cos^2 2\beta + \frac{1}{2} \lambda^2 v^2 \sin^2 2\beta, \quad (16)$$

$$M_{S23}^2 = \sqrt{2} \lambda v \mu (1 - x), \quad (17)$$

$$M_{S33}^2 = 4 \frac{\kappa^2}{\lambda^2} \mu^2 + \frac{\kappa}{\lambda} A_\kappa \mu + \frac{\lambda^2 v^2}{2} x - \frac{\kappa \lambda}{2} v^2 \sin 2\beta, \quad (18)$$

with

$$M_A^2 = \frac{\lambda v_s}{\sin 2\beta} \left(\sqrt{2} A_\lambda + \kappa v_s \right), \quad x = \frac{1}{2\mu} (A_\lambda + 2 \frac{\kappa}{\lambda} \mu). \quad (19)$$

Here, it should be mentioned that the mass parameter M_A in the NMSSM becomes the mass of the heavy pseudoscalar Higgs boson only in the MSSM limit ($\lambda, \kappa \rightarrow 0$ with the ratio κ/λ fixed). In the NMSSM, M_A can be traded by the soft parameter A_λ .

The CP-even Higgs mass eigenstates h_i ($i = 1, 2, 3$) can be obtained by diagonalizing M_S^2 with a rotation matrix \mathcal{O}

$$h_i = \mathcal{O}_{i\alpha} h_\alpha, \quad (h_\alpha = H, h, s), \quad \text{diag}(m_{h_1}^2, m_{h_2}^2, m_{h_3}^2) = \mathcal{O} M_S^2 \mathcal{O}^T \quad (20)$$

with $\mathcal{O}_{i\alpha}$ being the elements of the rotation matrix satisfying the sum rules

$$\mathcal{O}_{1\alpha}^2 + \mathcal{O}_{2\alpha}^2 + \mathcal{O}_{3\alpha}^2 = 1. \quad (21)$$

The mass eigenstates h_i are aligned by the masses $m_{h_1} \leq m_{h_2} \leq m_{h_3}$. The singlet or non-SM doublet components in a physical Higgs boson h_i is determined by the rotation matrix elements $\mathcal{O}_{i(H,s)}$. With Eq. (20), the corresponding tree-level trilinear Higgs couplings in the mass eigenstates h_i are given by

$$\lambda_{h_i h_j h_k}^{(0, \text{NMSSM})} = \mathcal{O}_{i\alpha} \mathcal{O}_{j\beta} \mathcal{O}_{k\gamma} \lambda_{h_\alpha h_\beta h_\gamma}. \quad (22)$$

In the NMSSM, we take h_1 or h_2 as the SM-like Higgs boson when $|\mathcal{O}_{(1,2)h}|^2 \geq 0.5$. In general, due to the introduction of the singlet s and its couplings to the MSSM Higgs sector, the mass of the SM-like Higgs boson M_{S22}^2 can be lifted by the extra large λ -term at tree level, as shown in Eq. (16). The value of λ at the weak scale is upper bounded by 0.7 in order for the NMSSM to remain perturbative up to the GUT scale [33,35]. Whereas, the case of $\lambda > 0.7$ (dubbed as λ -SUSY model) is still of interest because it can suppress the sensitivity of the Higgs mass with respect to changes of the soft SUSY-breaking masses and keep the fine tuning at a moderate level even for stop masses up to 1 TeV. So, in our study, we consider both $\lambda < 0.7$ and $\lambda > 0.7$ cases:

- For $\lambda < 0.7$, in addition to the tree-level λ contribution, the mixture of the singlet s with the MSSM Higgs h and H , as shown in Eq. (13), in particular with h , could further modify the SM-like Higgs mass. If H is decoupled, when $M_{S22}^2 > M_{S33}^2$, the mass eigenvalues for the SM-like Higgs boson m_{h_2} is pushed up by the positive mixing effect after the diagonalization of the $h-s$ mass matrix. However, when $M_{S22}^2 < M_{S33}^2$, the mass eigenvalues for the SM-like Higgs boson m_{h_1} is pulled down by the negative mixing effect. Without the negative mixing effect, the maximal tree-level SM-like Higgs mass m_{h_1} can only reach to about 110 GeV [36,37], which needs a sizable loop correction from the stop sector to obtain a 125 GeV Higgs boson like in the MSSM. In this sense, h_2 being the observed SM-like Higgs boson may be more natural than h_1 in the NMSSM. So, we choose the next-to-lightest CP-even Higgs boson h_2 as the SM-like Higgs boson in the following discussions for the NMSSM with $\lambda < 0.7$. Note that the lightest Higgs boson h_1 in this case is predominantly singlet-like and its mass can be as light as about 20 GeV in our scanned samples. Consequently, the SM-like Higgs boson h_2 can decay into a pair of light scalars h_1 and hence the $\gamma\gamma$ and ZZ^* signal rates are suppressed. In order to be consistent with the LHC Higgs data, the branching ratio of $h_2 \rightarrow h_1 h_1$ was found to be less than about 30% [38] and may be tested through $h_1 h_1 \rightarrow b\bar{b} \mu^+ \mu^-$ production channel at the 14 TeV LHC [39]. However, due to our interests in the large mixing region, we only display the results with $m_{h_1} > m_{h_2}/2$ in the following analysis. We will also decouple the heaviest CP-even Higgs boson h_3 by requiring $m_{h_3} > 1$ TeV and focus on the singlet-doublet system. On the other hand, as mentioned above, if h_1 is the SM-like Higgs boson, the value of λ tends to be large in order to maximize the tree-level Higgs mass (so in our study for λ -SUSY with $\lambda > 0.7$, we will choose h_1 as the SM-like Higgs boson). This feature may lead to a sizable change in Higgs self-coupling when doublet-singlet mixing effect is large. We checked this possibility and found that the ratio $\lambda_{3h_1}^{\text{NMSSM}} / \lambda_{3h}^{\text{SM}}$ can vary from 0.29 to 1.17 for our samples with $\lambda < 0.7$.
- For $\lambda > 0.7$, we choose the lightest CP even Higgs boson h_1 as the SM-like Higgs boson. The reason is that for $\lambda > 0.7$ the tree-level Higgs mass will be significantly lifted. If h_2 is assumed as the SM-like Higgs boson, the large λ -term in M_{S22}^2 and the positive doublet-singlet mixing effect can readily

make the SM-like Higgs mass m_{h_2} exceed 125 GeV. Thus, such a choice is strongly disfavored by the LHC observed Higgs mass [37] and will not be further studied in our work. If h_1 is the SM-like Higgs boson, as pointed before, the cancellation between the tree-level λ -term and the negative doublet–singlet mixing effect can easily yield a 125 GeV SM-like Higgs boson. However, λ cannot be too large, because the large trilinear and quartic couplings of singlet scalar field s will largely contribute to the scattering amplitude $ss \rightarrow ss$. In the high energy limit, the unitarity condition requires $|\lambda| \leq 3$ and $|\kappa| \leq 3$. Furthermore, if combined with the dark matter relic abundance constraint, the above-mentioned unitarity bound can set a generic upper bound 20 TeV for the heavy Higgs masses [40]. The requirement of perturbativity up to the cut-off scale Λ , i.e., $\lambda(\Lambda) \lesssim 2\pi$ and $\kappa(\Lambda) \lesssim 2\pi$, will set upper bounds on λ and κ at weak scale. In this study, we assume the new unknown strong dynamics, for restoring the unitarity of scattering processes, appears at some scale Λ above 10 TeV, and require $\lambda^2 + \kappa^2 \lesssim 4.2$ [35,41].

Before closing this section, we note that since both Higgs boson masses and Higgs self-interactions arise from the Higgs potential, one has to adopt the same method to calculate them up to the same order for comparing the self-couplings in SUSY and SM. Although the most accurate evaluation of Higgs mass is up to three-loop level in the MSSM [42], there is no corresponding result for the Higgs self-couplings. Hence, in our study, we derive the Higgs mass and self-couplings by following the effective potential approaches in the MSSM [14] and NMSSM [21], where the explicit dominant one- and two-loop corrections to the effective potential are presented. Then we coded those expressions in our numerical calculation. On the other hand, since the tree-level mixing effects in the Higgs sector are usually dominant over the loop corrections in the NMSSM, we will focus on the doublet–singlet mixing effects for the NMSSM results.

3. Numerical calculations and results

3.1. Scan over the parameter space

In our numerical calculations, we take the input parameters of the SM as [43]

$$\begin{aligned} m_t &= 173.5 \text{ GeV}, \quad m_W = 80.385 \text{ GeV}, \quad m_Z = 91.1876 \text{ GeV}, \\ m_b^{\overline{\text{MS}}}(m_b^{\overline{\text{MS}}}) &= 4.18 \text{ GeV}, \quad \alpha_s(M_Z) = 0.1184, \\ \alpha(m_Z)^{-1} &= 128.962 \end{aligned} \quad (23)$$

We use NMSSMTools-4.4.1 [44] to perform a random scan over the parameter space. Note that for any given value of μ_{eff} , the phenomenology of the NMSSM is identical to the MSSM in the limit $\lambda, \kappa \rightarrow 0$ with the ratio κ/λ fixed (A_κ should be negative and satisfy $|A_\kappa| < 4\kappa\mu/\lambda$ to guarantee the squared mass of the singlet scalar to be positive) [33]. In our scan for the MSSM, we take $\lambda = \kappa = 10^{-7}$ and $A_\kappa = -10$ GeV. The validity of such a method has been justified by the authors of the NMSSMTools [44] and our previous calculations [34]. We also numerically checked our MSSM results of m_h by using the codes FeynHiggs [45], SOFTSUSY [46] and SuSpect [47], and found the results to agree with that given by the NMSSMTools within about 1% level when $m_h \sim 125$ GeV. So it is feasible to use the package NMSSMTools in the MSSM limit to study the phenomenology of the MSSM. For simplicity, we decouple the sleptons, gauginos and the first two generations of squarks by fixing the corresponding soft mass parameters at 2 TeV. We also set $M_{Q3} = M_{D3} = M_{U3}$ and $A_t = A_b$ for the third generation

of squarks. The lower limit of $\tan\beta$ in the MSSM is taken as 5, which is inspired by the recent LHC Higgs results [32]. The parameter ranges in our scan are chosen as the following:

(a) For the MSSM,

$$\begin{aligned} 5 \leq \tan\beta \leq 60, \quad 0.2 \text{ TeV} \leq M_A \leq 1 \text{ TeV}, \quad |\mu| \leq 1 \text{ TeV}, \\ 0.1 \text{ TeV} \leq M_{Q3} \leq 2.5 \text{ TeV}, \quad |A_t| \leq 3M_{Q3}. \end{aligned} \quad (24)$$

(b) For the NMSSM with $\lambda < 0.7$,

$$\begin{aligned} 0 \leq \lambda \leq 0.7, \quad |\kappa| \leq 0.7, \quad 0.2 \text{ TeV} \leq A_\lambda \leq 1 \text{ TeV}, \\ |A_\kappa| \leq 1 \text{ TeV}, \quad 1 \leq \tan\beta \leq 20, \quad 0.1 \text{ TeV} \leq \mu \leq 1 \text{ TeV}, \\ 0.1 \text{ TeV} \leq M_{Q3} \leq 1 \text{ TeV}, \quad |A_t| \leq 3M_{Q3}. \end{aligned} \quad (25)$$

(c) For the NMSSM with $\lambda > 0.7$,

$$\begin{aligned} 0.7 < \lambda \leq 2, \quad 0 < \kappa \leq 2, \quad 0.2 \text{ TeV} \leq A_\lambda \leq 1 \text{ TeV}, \\ |A_\kappa| \leq 1 \text{ TeV}, \quad 1 \leq \tan\beta \leq 20, \quad 0.1 \text{ TeV} \leq \mu \leq 1 \text{ TeV}, \\ 0.1 \text{ TeV} \leq M_{Q3} \leq 1 \text{ TeV}, \quad |A_t| \leq 3M_{Q3}. \end{aligned} \quad (26)$$

In our scan, we consider the following constraints:

- (1) We require the SM-like Higgs mass in the range of 123–127 GeV and consider the exclusion limits (at the 95% confidence level) from LEP, Tevatron and LHC in Higgs searches with HiggsBounds-4.2.0 [48]. We also perform the Higgs data fit by calculating χ^2 of the Higgs couplings with the public package HiggsSignals-1.3.0 [49] and require our samples to be consistent with Higgs data at 2σ level. We choose the SLHA input choice of HiggsBounds/HiggsSignals, where the effective Higgs couplings are only used to calculate the Higgs production cross section ratios. The Higgs decay branching ratios are taken directly from the corresponding decay blocks in the SLHA file generated by the NMSSMTools.
- (2) We require one-loop SUSY predictions for B -physics observables to satisfy the 2σ bounds as encoded in NMSSMTools, which include $B \rightarrow X_s \gamma$, $B_s \rightarrow \mu^+ \mu^-$, $B_d \rightarrow X_s \mu^+ \mu^-$ and $B^+ \rightarrow \tau^+ \nu$. Theoretical uncertainties in B -physics observables are taken into account as implemented in NMSSMTools.
- (3) We require the one-loop SUSY predictions for the precision electroweak observables such as ρ_l , $\sin^2 \theta_{\text{eff}}^l$, m_W and R_b [50] to be within the 2σ ranges of the experimental values.
- (4) We require the thermal relic density of the lightest neutralino (as the dark matter candidate) is below the 2σ upper bound of the Planck value [51] and the spin-independent neutralino–proton scattering cross section satisfy the direct detection bound from LUX at 90% confidence level [52].
- (5) We also consider the theoretical constraints from the stability of the Higgs potential as encoded in the NMSSMTools.

3.2. Results for the MSSM

Precision measurements of the Higgs boson properties (its mass and couplings to other particles) at the LHC provide relevant constraints on possible weak-scale extensions of the SM. In the usual context of the MSSM, these constraints suggest that all the additional non-SM-like Higgs bosons should be heavy. In Fig. 1, we show that in the decoupling limit of the MSSM, the region with $m_A < 330$ GeV has been excluded by various constraints. Similar result has been recently pointed out in [53]. The lower part of Fig. 1 shows that the value of $\tan\beta$ cannot be too small due to the requirement of 125–127 GeV Higgs mass in our scan. For

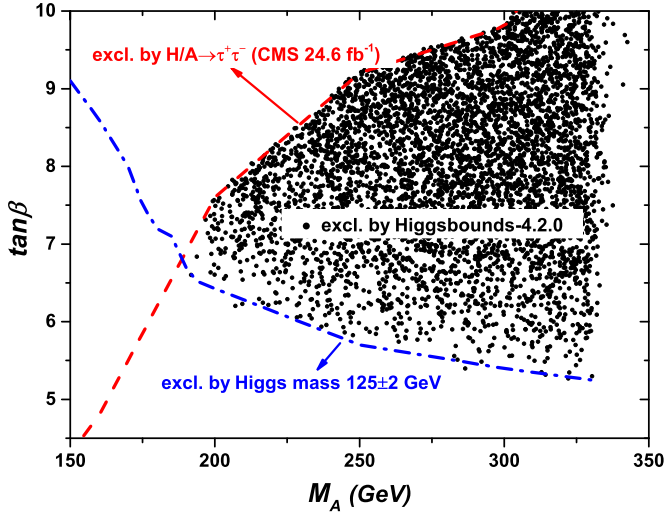


Fig. 1. Excluded region in the $\tan\beta$ versus M_A plane of the MSSM.

a small $\tan\beta$, heavy stops ($\gtrsim 10$ TeV) or a large mixing parameter A_t is needed to produce a large positive correction to the Higgs mass, which, however, will easily lead to vacuum instability and large uncertainty in the numerical calculation. So, we focus on $m_{\tilde{t}_1} < 2.5$ TeV region in our calculations. The additional constraints on the MSSM parameters imposed by the Higgs data are obtained by using the HiggsBounds-4.2.0 package. The key algorithm of HiggsBounds can be described in two steps. Firstly, the HiggsBounds uses the expected experimental limits from LEP, Tevatron and LHC to determine which decay channel has the highest statistical sensitivity. Secondly, for this particular channel, the theory prediction is compared to the observed experimental limits to conclude whether this sample is allowed or excluded at 95% CL. With the HiggsBounds, we find that most of samples (black bullets) with $180 \lesssim M_A \lesssim 330$ GeV and $5 \lesssim \tan\beta \lesssim 10$ have been excluded. Particularly, the latest CMS result of searching for $H/A \rightarrow \tau^+\tau^-$ has excluded most parameter space with a low M_A and low to moderate values of $\tan\beta$, as shown in the upper left corner of Fig. 1. We have checked that the current low energy constraints from $B_s \rightarrow \mu^+\mu^-$ and $B_s \rightarrow X_s\gamma$ are weaker than $H/A \rightarrow \tau^+\tau^-$ for our interested region (low to moderate values of $\tan\beta$). We note that the supersymmetric loop corrections generally lead to a contribution of the order of a few percent of the SM value. Hence, the suppressions in Higgs signal strengths $\mu_{\gamma\gamma}$ and μ_{VV^*} are mostly governed by the increase of the width of the lightest CP-even Higgs decay into bottom quarks and tau leptons at low values of m_A .

Fig. 1 suggests that all the additional non-SM-like Higgs bosons should be heavy, with masses larger than about 330 GeV. This is the commonly discussed decoupling limit of the MSSM. However, as discussed in [54], it is also possible to have the MSSM parameter conditions for “alignment independent of decoupling”, where the lightest CP-even Higgs boson has SM-like tree-level couplings to fermions and gauge bosons, independently of the non-standard Higgs boson masses. In the alignment region, $\sin(\alpha - \beta) \sim 1$ and the bounds on the heavy Higgs bosons that arise from the measurements of $h \rightarrow VV$ may be relaxed. Such alignment conditions are associated with very SM-like $h\tilde{t}\tilde{t}^*$ coupling and tend to be restricted to values of $\tan\beta$ of order 10 or larger within the MSSM [54–56]. As will be shown below, for such a large value of $\tan\beta$, the supersymmetric contributions to the SM-like Higgs self-coupling are found to be small (at a percent level). Hence, even in the alignment condition, we cannot expect a large deviation of the Higgs self-coupling with the SM value.

In Fig. 2 we project the samples surviving all the experimental constraints on the planes of m_A and $m_{\tilde{t}_1}$ versus $\tan\beta$. The ratio $\lambda_{3h}^{\text{MSSM}}/\lambda_{3h}^{\text{SM}}$ is always smaller than 1 because of the negative MSSM corrections to Higgs self-coupling [23]. From the left panel it can be seen that in most part of the allowed parameter space (the blue triangles), the values of $\lambda_{3h}^{\text{MSSM}}/\lambda_{3h}^{\text{SM}}$ (we use $3h$ to denote hhh) are larger than 0.99. When both $\tan\beta$ and m_A become small, $\lambda_{3h}^{\text{MSSM}}/\lambda_{3h}^{\text{SM}}$ gets smaller, which can minimally reach about 0.97 for our samples. The reasons for $\lambda_{3h}^{\text{MSSM}}$ being so close to λ_{3h}^{SM} are the following: (1) The dominant MSSM contributions to $\lambda_{3h}^{\text{MSSM}}/\lambda_{3h}^{\text{SM}}$ are from the stop loops, while the Higgs coupling with the stops is proportional to $1/\sin\beta$. So it leads to an overall enhancement factor $1/\sin^3\beta$ in the corrections when $\tan\beta$ is small. However, such a region is obviously not favored by the measured Higgs mass, which needs a large $\tan\beta$ to enhance the Higgs mass; (2) A light m_A causes a large mixing between two CP-even Higgs bosons and can sizably change the Higgs couplings with the SM fermions. But as mentioned before, m_A should be heavier than about 330 GeV to satisfy the experimental constraints in our scan. For the right panel it should be mentioned that since the small values of $\lambda_{3h}^{\text{MSSM}}/\lambda_{3h}^{\text{SM}}$ occur in the small $\tan\beta$ region, heavy stops are usually needed to enhance the Higgs mass through loop corrections.

In Fig. 3, we show the MSSM Higgs couplings in comparison with the SM predictions. The ILC (1 TeV, 1 ab^{-1}) sensitivities to the alteration of the couplings [57] are also plotted, where the regions between the bars give too small alterations to be detectable at ILC. The HL-LHC (14 TeV , 3 ab^{-1}) sensitivities are much worse than ILC and are not shown here. From Fig. 3, we have the following observations: (1) In the MSSM, the Higgs gauge couplings and top-Higgs couplings are respectively changed by the factors $\sin(\beta - \alpha)$ and $\cos\alpha/\sin\beta$, but the ratios $C_{hVV}^{\text{MSSM}}/C_{hVV}^{\text{SM}}$ and $C_{h\tilde{t}\tilde{t}^*}^{\text{MSSM}}/C_{h\tilde{t}\tilde{t}^*}^{\text{SM}}$ for our survived samples are very close to unity due to $m_A \gg m_Z$. So, even if these couplings can be measured at percent level at ILC, it cannot constrain the MSSM parameter space with a small $\lambda_{3h}^{\text{MSSM}}/\lambda_{3h}^{\text{SM}}$; (2) The ratio $C_{hgg}^{\text{MSSM}}/C_{hgg}^{\text{SM}}$ is always smaller than one for our samples because a large mixing between the stops or heavy stops needed by the Higgs mass interferes destructively with the top loop and C_{hgg}^{MSSM} is suppressed, while $C_{h\gamma\gamma}^{\text{MSSM}}/C_{h\gamma\gamma}^{\text{SM}}$ can be greater than one due to the constructive contribution with the W loop. Although both couplings only slightly deviate from the SM predictions, the high precision measurements on $C_{gg,\gamma\gamma}$ at the ILC will be able to exclude some part of the parameter space with $\lambda_{3h}^{\text{MSSM}}/\lambda_{3h}^{\text{SM}} > 0.977$.

3.3. Results for the NMSSM ($\lambda < 0.7$)

In Fig. 4, we project the NMSSM ($\lambda < 0.7$) samples allowed by the constraints (1)–(5) on the planes of λ versus κ and κ versus the singlet component $|\mathcal{O}_{2S}|$ in the SM-like Higgs boson h_2 . Here we take $2m_{h_1} > m_{h_2}$ so that h_2 will not decay into a pair of h_1 . We can see that when λ and κ approach to zero, $\tan\beta$ has to be large in order to enhance the Higgs mass. While in small $\tan\beta \lesssim 10$ region, the values of λ for most samples are larger (in magnitude) than κ . Since the singlet component $|\mathcal{O}_{2S}|$ in the SM-like Higgs boson h_2 can potentially affect the Higgs self-coupling in Eq. (22), we also show the dependence of $|\mathcal{O}_{2S}|$. Since the singlet component $|\mathcal{O}_{2S}|$ in the SM-like Higgs boson h_2 can potentially affect the Higgs self-coupling in Eq. (22), we also show the dependence of $|\mathcal{O}_{2S}|$ on λ and κ for the NMSSM (with $\lambda < 0.7$) samples which survive all the experimental constraints. It can be seen that $|\mathcal{O}_{2S}|$ decreases if both λ and κ go to zero. However, if $\lambda \gg |\kappa| \sim 0$, which usually happens for small $\tan\beta \lesssim 10$, $|\mathcal{O}_{2S}|$ can be sizeable and lead to a large deviation from the SM prediction in triple Higgs boson cou-

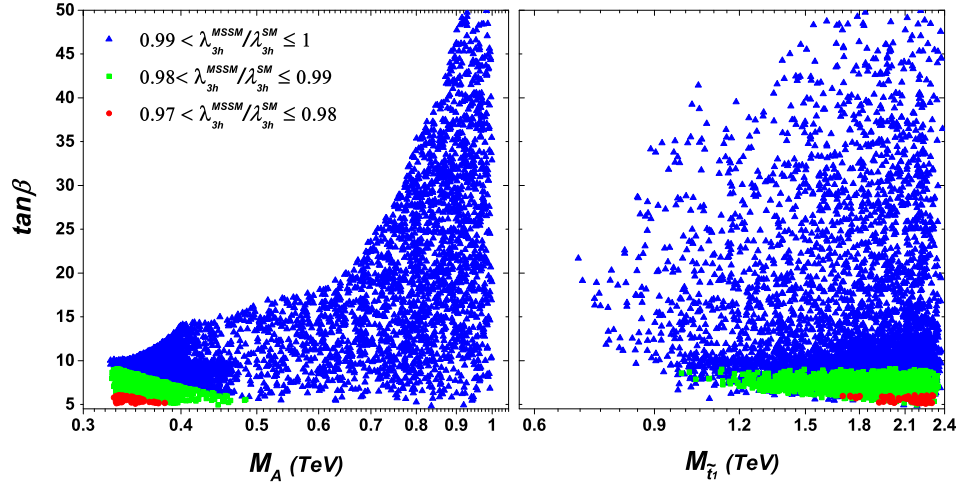


Fig. 2. Scatter plots of the samples surviving all the experimental constraints, projected on the planes of $\tan\beta$ versus m_A and $m_{\tilde{t}_1}$. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

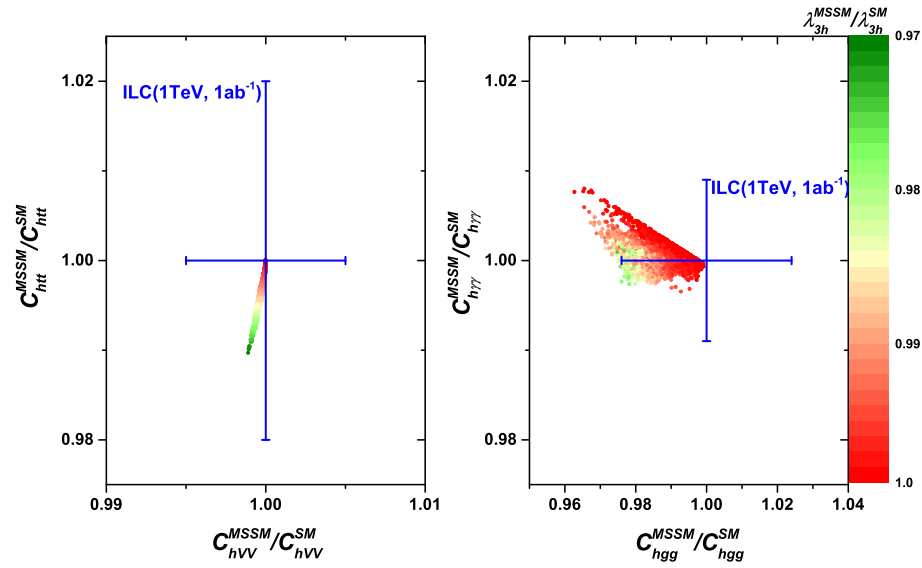


Fig. 3. Same as Fig. 2, but showing the Higgs couplings. The ILC (1 TeV, 1 ab⁻¹) sensitivities to the alteration of the couplings [57] are also plotted (the regions between the bars give too small alterations to be detectable at ILC).

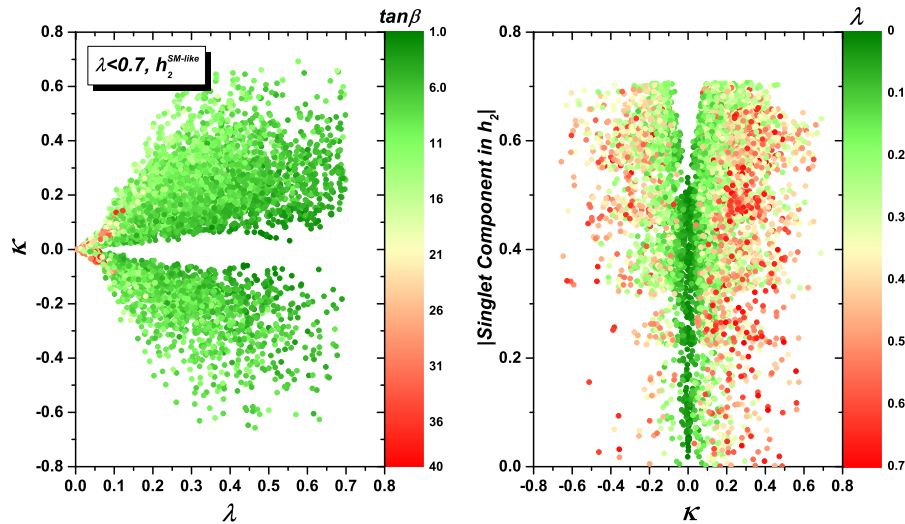


Fig. 4. The NMSSM ($\lambda < 0.7$) samples surviving all the experimental constraints, projected on the planes of λ versus κ and the singlet component $|O_{25}|$ in the SM-like Higgs boson h_2 .

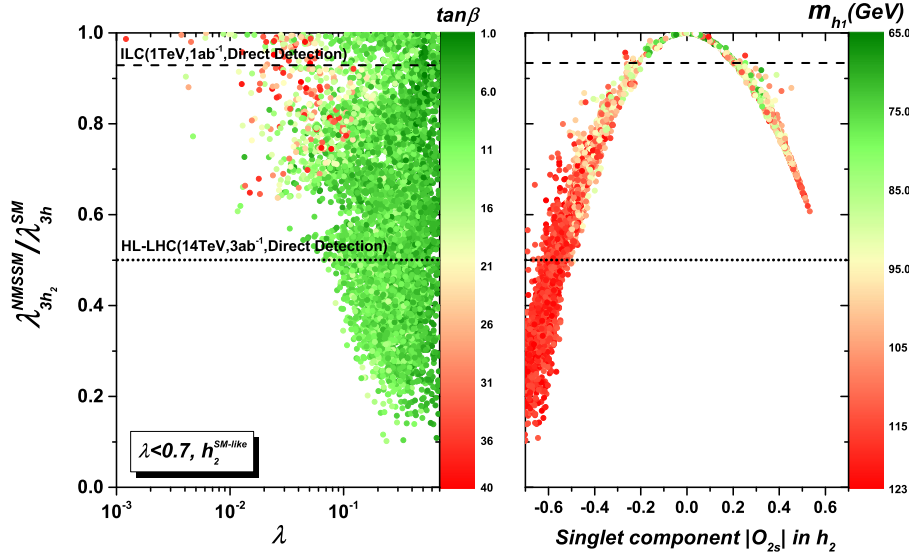


Fig. 5. Same as Fig. 4, but showing the dependence of $\lambda_{3h_2}^{NMSSM}/\lambda_{3h}^{SM}$ versus λ and the singlet component $|O_{2s}|$ in h_2 , where $m_{h_2} < 2m_{h_1}$. The ILC (1 TeV, 1 ab^{-1}) and HL-LHC (14 TeV, 3 ab^{-1}) sensitivities are also plotted (the region below each horizontal line is detectable).

pling. For example, for $\lambda = 0.017$ and $\kappa = -0.0038$, $O_{2s} \sim 0.215$ and $\lambda_{3h_2}^{NMSSM}/\lambda_{3h}^{SM} \sim 0.7$. The reason is that in the singlet-doublet system, after decoupling h_3 by requiring $M_{h_3} > 1$ TeV, $|O_{2s}|$ is proportional to $\sin\theta$, where the mixing angle θ that determines the mixture of the singlet and the SM-like Higgs states can be approximately expressed as $\tan 2\theta \sim 2M_{23}^2/(M_{22}^2 - M_{33}^2)$ [35,37]. Here, M_{ij}^2 are the CP-even Higgs mass matrix elements listed in Eqs. (13)–(18). In case that λ is not too small, a large θ can happen when $M_{22}^2 - M_{33}^2 \sim M_{23}^2$. This leads to a large singlet component in the SM-like Higgs state and hence a sizeable modification of the Higgs trilinear couplings.

In Fig. 5, we display the dependence of $\lambda_{3h_2}^{NMSSM}/\lambda_{3h}^{SM}$ versus λ and $\tan\beta$ for the NMSSM ($\lambda < 0.7$). As mentioned above, due to the Higgs mass constraint, most of the allowed model samples tend to have large values of λ . Furthermore, the ratio $\lambda_{3h_2}^{NMSSM}/\lambda_{3h}^{SM}$ is not sensitive to the value of $\tan\beta$. We also show the dependence of $\lambda_{3h_2}^{NMSSM}/\lambda_{3h}^{SM}$ versus the singlet component $|O_{2s}|$ in the SM-like Higgs boson h_2 and the lightest CP-even Higgs mass m_{h_1} for the NMSSM ($\lambda < 0.7$). Besides, we plot the expected ILC (1 TeV, 1 ab^{-1}) and HL-LHC (14 TeV, 3 ab^{-1}) sensitivities to Higgs self-coupling from the direct measurements [57]. We can see that $\lambda_{3h_2}^{NMSSM}/\lambda_{3h}^{SM}$ becomes small with the increase of the singlet component $|O_{2s}|$ and can minimally reach 0.1 in the allowed parameter space. Meanwhile, such a large mixing can make the mass of the lightest singlet-dominant CP-even Higgs boson h_1 close to the 125 GeV SM-like Higgs boson h_2 .

In Table 1, we present the properties of two CP-even Higgs bosons h_1 and h_2 for such a benchmark point at 14 TeV LHC. We can see that the cross sections of the single h_1 production are close to those of SM-like h_2 because of the large doublet and singlet mixing components in both h_1 and h_2 . However, the branching ratio $h_1 \rightarrow VV$ ($V = Z, W\gamma, g$) is greatly suppressed by the increase of the partial width of $h_1 \rightarrow b\bar{b}$. Thus, the observed production rate of $gg \rightarrow h_1 \rightarrow VV$ is much smaller than that of SM-like h_2 . We also checked and found that although the cross section of $gg \rightarrow h_1 \rightarrow \tau^+\tau^-$ can reach 2.06 pb, it is still smaller than the upper bound given by the current LHC searches for $H/A \rightarrow \tau^+\tau^-$ [28]. Besides, it should be mentioned that the sizable modification of the self-coupling of the SM-like Higgs boson h_2 always accompanies with the great changes in other Higgs couplings, which can be seen in Fig. 6. So, given the limited sensitivity of measuring the

Higgs boson self-couplings, we anticipate that the precision measurement of Higgs couplings to gauge bosons and fermions could test this scenario at the LHC and future colliders prior to the direct detection of triple or quartic Higgs couplings.

In Fig. 6, we show the Higgs couplings in the NMSSM ($\lambda < 0.7$) surviving all the experimental constraints. For comparison, we also show the discovery potential of the expected ILC (1 TeV, 1 ab^{-1}) and HL-LHC (14 TeV, 3 ab^{-1}) [57]. From this figure, we obtain the following observations: (1) Due to the singlet admixture in the SM-like Higgs boson, both Higgs gauge couplings and top-Higgs coupling can be maximally reduced by about 30% in the allowed region, which is much larger than in the MSSM. So, the expected measurements of the Higgs gauge couplings at the HL-LHC and ILC can exclude the parameter space with $\lambda_{3h_2}^{NMSSM}/\lambda_{3h}^{SM} < 0.82$ and $\lambda_{3h_2}^{NMSSM}/\lambda_{3h}^{SM} < 0.93$, respectively; (2) With the increase of the singlet component in the Higgs couplings, both $C_{h\gamma\gamma}^{NMSSM}/C_{h\gamma\gamma}^{SM}$ and $C_{h\gamma\gamma}^{NMSSM}/C_{h\gamma\gamma}^{SM}$ are significantly reduced. On the other hand, due to the additional tree-level contribution ($\sim \lambda v \sin 2\beta$) and the positive mixing effect, we find that a stop with mass less than 200 GeV is still allowed by the SM-like Higgs mass constraint in the NMSSM (similar results have been obtained in previous NMSSM works [58]). Consequently, the ratio $C_{hgg}^{NMSSM}/C_{hgg}^{SM}$ becomes larger than one, due to the constructive contribution from the light stop in loop. We also note that even when $\lambda_{3h_2}^{NMSSM}$ approaches to λ_{3h}^{SM} , $C_{h_2\gamma\gamma}^{NMSSM}/C_{h_2\gamma\gamma}^{SM}$ can still be enhanced by about 8%.

3.4. Results for the NMSSM ($\lambda > 0.7$)

In Fig. 7, we display the dependence of $\lambda_{3h_1}^{NMSSM}/\lambda_{3h}^{SM}$ versus $\tan\beta$ and m_{h_2} for the NMSSM ($\lambda > 0.7$). Similar to Fig. 4, the larger λ is, the smaller $\tan\beta$ becomes to satisfy the requirement of the Higgs mass. The ratio $\lambda_{3h_1}^{NMSSM}/\lambda_{3h}^{SM}$ can vary from -1.1 to 1.9 in our scan. For example, the ratio $\lambda_{3h_1}^{NMSSM}/\lambda_{3h}^{SM}$ is equal to 1.89 when $\lambda = 1.51$ and $\kappa = 0.67$, and is -1.04 for $\lambda = 1.57$ and $\kappa = 1.16$. Since we require $m_{h_3} > 1$ TeV, for our samples with $m_{h_3} \gg m_{h_{1,2}}$, $\lambda_{3h_1}^{NMSSM}/\lambda_{3h}^{SM}$ is approximately proportional to λ^2 and becomes large with the increase of λ . In our scan ranges, such a feature could either enhance or suppress the Higgs self-coupling with respect to the SM prediction, and yield potentially large effects in Higgs

Table 1

A benchmark point for the NMSSM with $\lambda < 0.7$ (h_2 is the SM-like Higgs boson). The cross sections (pb) are calculated for LHC-14 TeV.

λ	κ	$\tan \beta$	μ (GeV)	A_λ (GeV)	A_κ (GeV)	$\lambda_{3h_2}^{\text{NMSSM}} / \lambda_{3h_2}^{\text{SM}}$
0.16	0.31	17.9	105.3	1461.9	−716.2	0.798
m_{h_1} (GeV)	$\sigma_{gg h_1}$	$\sigma_{VV h_1}$	σ_{Wh_1}	σ_{Zh_1}	$\sigma_{t\bar{t} h_1}$	$\sigma_{b\bar{b} h_1}$
119.56	25.41	2.14	0.85	0.49	0.33	0.54
$Br_{h_1 \rightarrow \gamma\gamma}$	$Br_{h_1 \rightarrow gg}$	$Br_{h_1 \rightarrow ZZ^*}$	$Br_{h_1 \rightarrow WW^*}$	$Br_{h_1 \rightarrow c\bar{c}}$	$Br_{h_1 \rightarrow b\bar{b}}$	$Br_{h_1 \rightarrow \tau^+ \tau^-}$
0.135%	3.60%	0.717%	7.88%	2.12%	77.3%	8.10%
m_{h_2} (GeV)	$\sigma_{gg h_2}$	$\sigma_{VV h_2}$	σ_{Wh_2}	σ_{Zh_2}	$\sigma_{t\bar{t} h_2}$	$\sigma_{b\bar{b} h_2}$
127.30	24.81	2.05	0.71	0.41	0.29	0.14
$Br_{h_2 \rightarrow \gamma\gamma}$	$Br_{h_2 \rightarrow gg}$	$Br_{h_2 \rightarrow ZZ^*}$	$Br_{h_2 \rightarrow WW^*}$	$Br_{h_2 \rightarrow c\bar{c}}$	$Br_{h_2 \rightarrow b\bar{b}}$	$Br_{h_2 \rightarrow \tau^+ \tau^-}$
0.381%	8.11%	3.92%	34.0%	4.14%	44.6%	4.55%

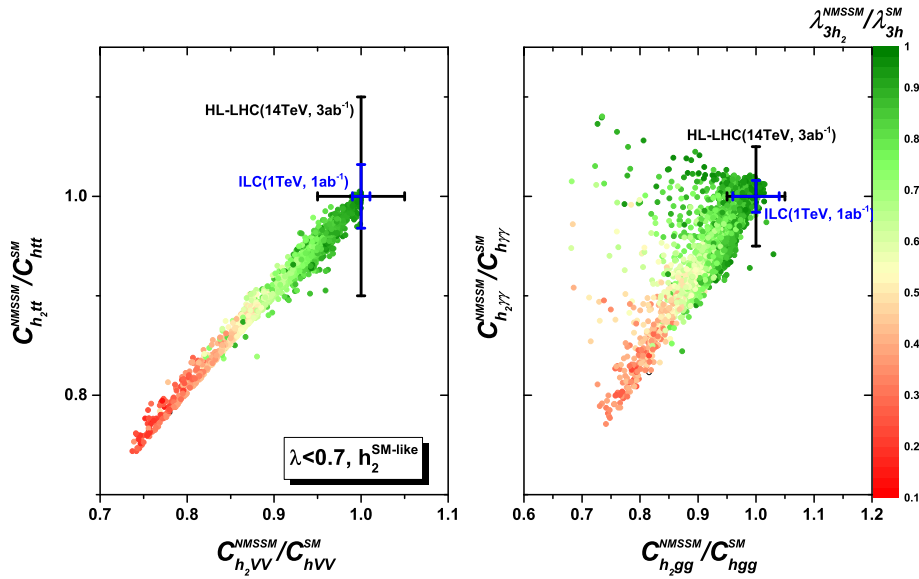


Fig. 6. Same as Fig. 3 but for the NMSSM ($\lambda < 0.7$).

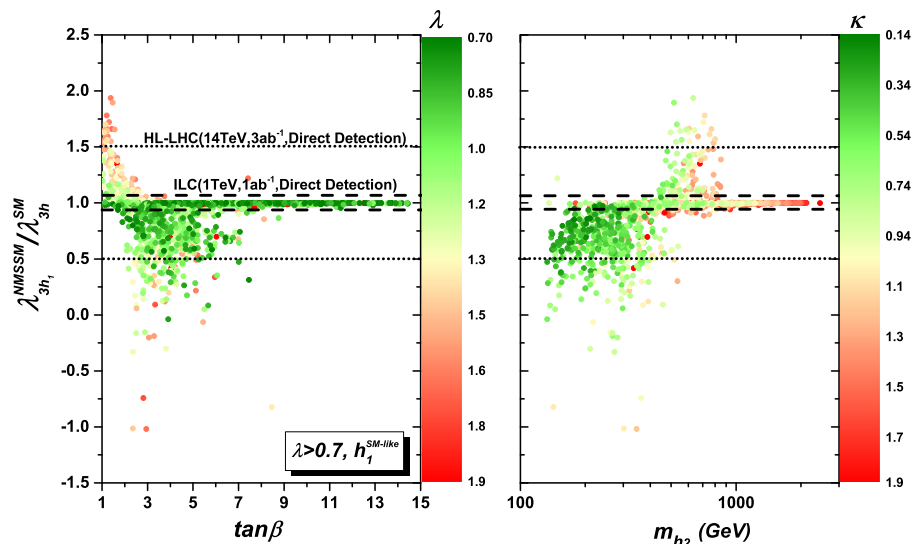


Fig. 7. The NMSSM ($\lambda > 0.7$) samples surviving all the experimental constraints, showing the dependence of $\lambda_{3h_1}^{\text{NMSSM}} / \lambda_{3h_1}^{\text{SM}}$ versus $\tan \beta$ and m_{h_2} . The ILC (1 TeV, 1 ab^{-1}) and HL-LHC (14 TeV, 3 ab^{-1}) sensitivities are also plotted.

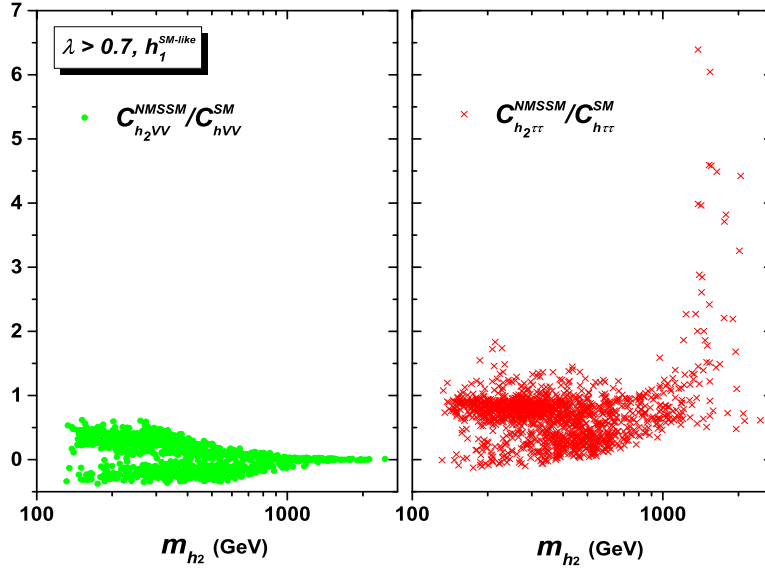


Fig. 8. The NMSSM ($\lambda > 0.7$) samples surviving all the experimental constraints, showing the dependence of the Higgs couplings versus m_{h_2} .

Table 2

A benchmark point for the NMSSM with $\lambda > 0.7$ (h_1 is the SM-like Higgs boson). The cross sections (pb) are calculated for LHC-14 TeV.

λ	κ	$\tan \beta$	μ (GeV)	A_λ (GeV)	A_κ (GeV)	$\lambda_{3h_2}^{\text{NMSSM}} / \lambda_{3h_2}^{\text{SM}}$
1.54	0.75	3.06	474.00	1035.41	−644.30	−0.203
m_{h_1} (GeV)	$\sigma_{gg h_1}$	$\sigma_{VV h_1}$	σ_{Wh_1}	σ_{Zh_1}	$\sigma_{\tau\tau h_1}$	$\sigma_{b\bar{b} h_1}$
126.9	42.86	3.42	1.17	0.70	0.52	0.29
$Br_{h_1 \rightarrow \gamma\gamma}$	$Br_{h_1 \rightarrow gg}$	$Br_{h_1 \rightarrow ZZ^*}$	$Br_{h_1 \rightarrow WW^*}$	$Br_{h_1 \rightarrow c\bar{c}}$	$Br_{h_1 \rightarrow b\bar{b}}$	$Br_{h_1 \rightarrow \tau^+\tau^-}$
0.427%	9.87%	4.18%	36.5%	4.98%	39.7%	4.03%
m_{h_2} (GeV)	$\sigma_{gg h_2}$	$\sigma_{VV h_2}$	σ_{Wh_2}	σ_{Zh_2}	$\sigma_{\tau\tau h_2}$	$\sigma_{b\bar{b} h_2}$
282.0	6.33	0.90	0.06	0.03	0.03	0.04
$Br_{h_2 \rightarrow \gamma\gamma}$	$Br_{h_2 \rightarrow gg}$	$Br_{h_2 \rightarrow ZZ^*}$	$Br_{h_2 \rightarrow WW^*}$	$Br_{h_2 \rightarrow b\bar{b}}$	$Br_{h_2 \rightarrow \tau^+\tau^-}$	$Br_{h_2 \rightarrow h_1 h_1}$
0.000663%	0.0173%	14.1%	32.1%	0.0996%	0.012%	53.6%

pair production cross sections [13,59]. However, in general, the two masses m_{h_2} and m_{h_3} are virtually independent and the mixing patterns are complicated. It is worth mentioning that the value of $\lambda_{3h_1}^{\text{NMSSM}} / \lambda_{3h_1}^{\text{SM}} \leq 1$ strongly relies on the mass of the next-to-lightest CP-even Higgs boson h_2 . To be specific, when κ becomes small (large), m_{h_2} is inclined to be light (heavy). If m_{h_2} is lighter (heavier) than about 400 GeV, $\lambda_{3h_1}^{\text{NMSSM}} / \lambda_{3h_1}^{\text{SM}}$ is smaller (larger) than unity for most samples. The properties of h_2 will be discussed in the following. We should mention that the large λ and κ that produce the large deviation of $\lambda_{3h_1}^{\text{NMSSM}} / \lambda_{3h_1}^{\text{SM}}$ jeopardize the perturbativity up to GUT scale. Thus, the new unknown strong dynamics will appear at some cut-off scale Λ . On the other hand, the constructions of high scale theory by adding vector-like matter can allow for a larger λ value and relax the cutoff scale to high values [60], which is however beyond the scope of our study.

In Fig. 8, we plot the couplings of h_2 with gauge bosons and τ leptons, normalized to the SM values. We can see that the gauge coupling $h_2 VV$ is always suppressed due to the presence of singlet (s) and non-SM doublet (H) components in h_2 . If h_2 is singlet-like, the $h_2 \tau^+ \tau^-$ coupling is suppressed as well, while if h_2 is non-SM doublet-like, $h_2 \tau^+ \tau^-$ coupling can be enhanced by $\tan \beta$. The detailed mixing patterns of s and H in h_2 and its couplings have been thoroughly investigated in [59]. We checked that the cross section $gg \rightarrow h_2 \rightarrow \tau^+ \tau^-$ for our samples is at least one order lower than the current direct search bound on the non-SM Higgs bosons [27, 28]. The main reason is that for a heavy Higgs boson h_2 , the new

decay channels, such as $h_2 \rightarrow h_1 h_1$ [61], can be opened and the branching ratio of $h_2 \rightarrow \tau^+ \tau^-$ will be highly suppressed.

In Table 2, we present the properties of two CP-even Higgs bosons h_1 and h_2 for a benchmark point at 8 TeV LHC. We can see that all the SM branching ratios of h_2 are reduced due to the opened decay mode $h_2 \rightarrow h_1 h_1$, which can reach 53.6% for $m_{h_2} = 282.0$ GeV. Such a Higgs-to-Higgs decay will lead to a resonant SM-like di-Higgs bosons production $pp \rightarrow h_2 \rightarrow h_1 h_1$ at the LHC. A resonance feature in the $h_1 h_1$ invariant mass can be served as a smoking gun to search for the heavy Higgs boson h_2 . With one SM-like Higgs boson h_1 decaying to two photons and the other decaying to b -quarks, the resonant signal may be observable above the di-Higgs continuum background for $m_{h_2} < 1$ TeV at the HL-LHC [62].

Next, we present in Fig. 9 the couplings of the SM-like h_1 to weak gauge bosons and tau pair for the NMSSM ($\lambda > 0.7$). To show their correlation with the Higgs self-coupling, we use the red color to highlight the points that satisfy $|\lambda_{3h_1}^{\text{NMSSM}} / \lambda_{3h_1}^{\text{SM}} - 1| > 0.3$. It can be seen that the large Higgs self-couplings corrections correspond to the sizable shifts in Higgs couplings with gauge bosons and tau pair. Since the tree-level mass of the SM-like Higgs boson h_1 could easily exceed 125 GeV, h_1 is likely to have non-negligible singlet and/or non-SM doublet components, which makes its couplings deviate from the SM predictions. From this figure, it can be seen that $C_{h_1 VV}^{\text{NMSSM}} / C_{h_1 VV}^{\text{SM}}$ is always less than unity since any singlet and/or non-SM doublet components in h_1 will make the Higgs couplings to weak gauge bosons smaller than the SM pre-

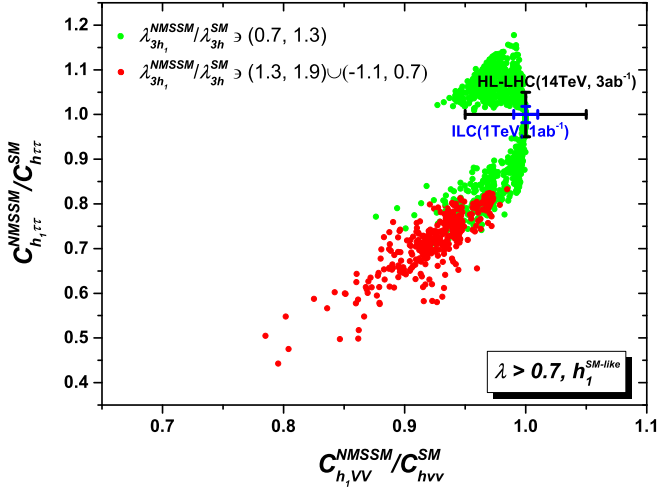


Fig. 9. Same as Fig. 8, but showing the couplings of h_1 . The HL-LHC (14 TeV, 3 ab^{-1}) and ILC (1 TeV, 1 ab^{-1}) sensitivities [57] are also plotted.

dictions. However, as mentioned above, if the next-to-dominant component in h_1 is the non-SM doublet, the Higgs coupling with the down-type fermions may be enhanced and larger than the SM predictions, such as the $h_1\tau^+\tau^-$ coupling. Therefore, the future measurements of $C_{h_1\tau^+\tau^-}$ and C_{h_1VV} couplings can give strong constraints on the parameters space of the NMSSM with $\lambda > 0.7$ and set limits on the Higgs self-coupling $C_{3h_1}^{NMSSM}$.

From the above discussions, we can see that the large deviation of the Higgs self-coupling λ_{3h_1} for the NMSSM ($\lambda > 0.7$) is always accompanied by other collider signatures, such as a shift in the Higgs couplings and the production on resonance of the non-SM doublet h_2 . At the LHC, the resonant production of h_2 may be observed through the channels $gg \rightarrow h_2 \rightarrow \tau^+\tau^-$, h_1h_1 . However, the sensitivities of these channels strongly depend on the mass of h_2 and on its singlet and non-SM doublet components. If h_2 is dominantly singlet, both direct searches will not be powerful in probing our scenario at the LHC since all the h_2 couplings to SM particles are greatly reduced. Thus, the precision measurement of the observed 125 GeV Higgs boson couplings will play a unique role in probing this scenario at future colliders. If h_2 is dominantly doublet (non-SM), and if $m_{h_1} < m_{h_2} < 2m_{h_1}$, the process $gg \rightarrow h_2 \rightarrow \tau^+\tau^-$ is still greatly suppressed due to the reduction of the coupling $h_2t\bar{t}$ despite the fact that the coupling $h_2\tau^+\tau^-$ can be maximally enhanced by a factor of 2. On the other hand for $2m_{h_1} < m_{h_2}$, the decay $h_2 \rightarrow h_1h_1$ is open and contributes to the cross section of $pp \rightarrow h_1h_1$. Therefore, besides the Higgs coupling measurements, a resonance feature in the h_1h_1 invariant mass or an excess in the inclusive h_1h_1 production can be used to probe this model at the future LHC.

4. Conclusion

We examined the currently allowed values of trilinear self-couplings of the SM-like 125 GeV Higgs boson (h) in the MSSM and NMSSM after the LHC Run-1. Considering all the relevant experimental constraints, such as the Higgs data, the flavor constraints, the electroweak precision observables as well as the dark matter detections, we performed a scan over the parameter space of each model and obtained the following observations:

- In the MSSM, the Higgs self-coupling is suppressed relative to the SM value. Such a suppression was found to be rather weak and the ratio $\lambda_{hhh}^{MSSM}/\lambda_{hhh}^{SM}$ is above 0.97 due to the tightly constrained parameter space, cf. Figs. 1 and 2;

- In the NMSSM with $\lambda < 0.7$, we consider the case that the SM-like Higgs boson mass m_{h_2} is less than twice of m_{h_1} , so that h_2 will not decay into a pair of h_1 . We found that the Higgs self-coupling was found to be likely suppressed and the ratio $\lambda_{hhh}^{NMSSM}/\lambda_{hhh}^{SM}$ can be as low as 0.1 due to the large mixing between singlet and doublet Higgs bosons, cf. Fig. 5. In that case, the coupling of the SM-like Higgs boson (h_2) to W and Z bosons and top quark pairs are all suppressed as compared to the SM prediction. On the other hand, its couplings to loop-induced processes, such as photon pairs or gluon pairs, can be enhanced, cf. Fig. 6. Given the limited sensitivity of measuring the Higgs boson self-couplings, we anticipate that the precision measurement of Higgs couplings to gauge bosons and fermions could test this scenario at the LHC and future colliders prior to the direct detection of triple or quartic Higgs couplings;
- In the NMSSM with $\lambda > 0.7$ (also called λ -SUSY), the Higgs self-coupling can be greatly suppressed or enhanced relative to the SM value (the ratio $\lambda_{hhh}^{NMSSM}/\lambda_{hhh}^{SM}$ can vary from -1.1 to 1.9), cf. Fig. 7, when h_1 is taken as the SM-like Higgs boson. Its coupling to W and Z bosons are always suppressed as compared to the SM predictions. On the contrary, its couplings to tau pairs can be either enhanced or suppressed relative to the SM value, cf. Fig. 9. When $m_{h_2} > 2m_{h_1}$, it is possible to observe a new resonance production in the di-Higgs boson channel at the LHC. While the couplings of h_2 to W and Z bosons are always suppressed, its coupling to tau pair can deviate largely from the SM value, depending on the mass of h_2 , cf. Fig. 8.

Since the NMSSM can give rather different values (compared with the SM) for the trilinear self-couplings of the SM-like Higgs boson, the future collider experiments like the high luminosity LHC or ILC can probe NMSSM through measuring the Higgs self-couplings.

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