Lecture 6

Register Allocation

- I. Introduction
- II. Abstraction and the Problem

III. Algorithm

Reading: Chapter 8.8.4 Before next class: Chapter 10.1 - 10.2

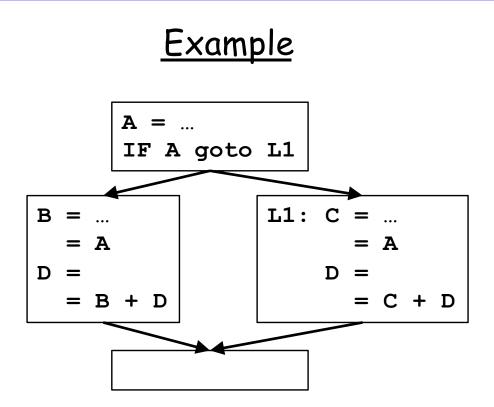
I. Motivation

• Problem

- Allocation of variables (pseudo-registers) to hardware registers in a procedure
- Perhaps the most important optimization
 - Directly reduces running time
 - (memory access \rightarrow register access)
 - Useful for other optimizations
 - e.g. cse assumes old values are kept in registers.

<u>Goal</u>

- Find an assignment for all pseudo-registers, if possible.
- If there are not enough registers in the machine, choose registers to spill to memory



II. An Abstraction for Allocation & Assignment

- Intuitively
 - Two pseudo-registers interfere if at some point in the program they cannot both occupy the same register.
- Interference graph: an undirected graph, where
 - nodes = pseudo-registers
 - there is an edge between two nodes if their corresponding pseudo-registers interfere
- What is not represented
 - Extent of the interference between uses of different variables
 - Where in the program is the interference

<u>Register Allocation and Coloring</u>

- A graph is **n-colorable** if:
 - every node in the graph can be colored with one of the n colors such that two adjacent nodes do not have the same color.
- Assigning n register (without spilling) = Coloring with n colors
 - assign a node to a register (color) such that no two adjacent nodes are assigned same registers(colors)
- Is spilling necessary? = Is the graph n-colorable?
- To determine if a graph is n-colorable is NP-complete, for n>2
 - Too expensive
 - Heuristics

III. Algorithm

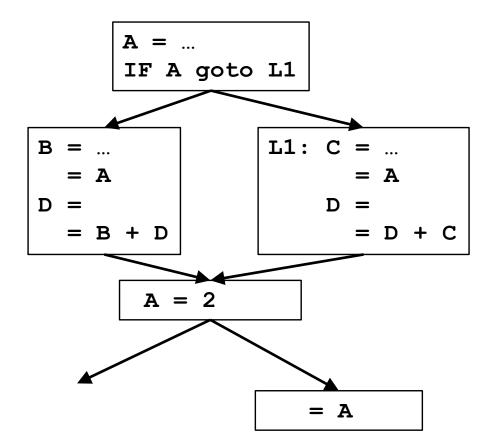
Step 1. Build an interference graph

- a. refining notion of a node
- b. finding the edges

Step 2. Coloring

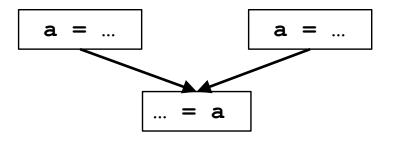
- use heuristics to try to find an n-coloring
 - Success:
 - colorable and we have an assignment
 - Failure:
 - graph not colorable, or
 - graph is colorable, but it is too expensive to color

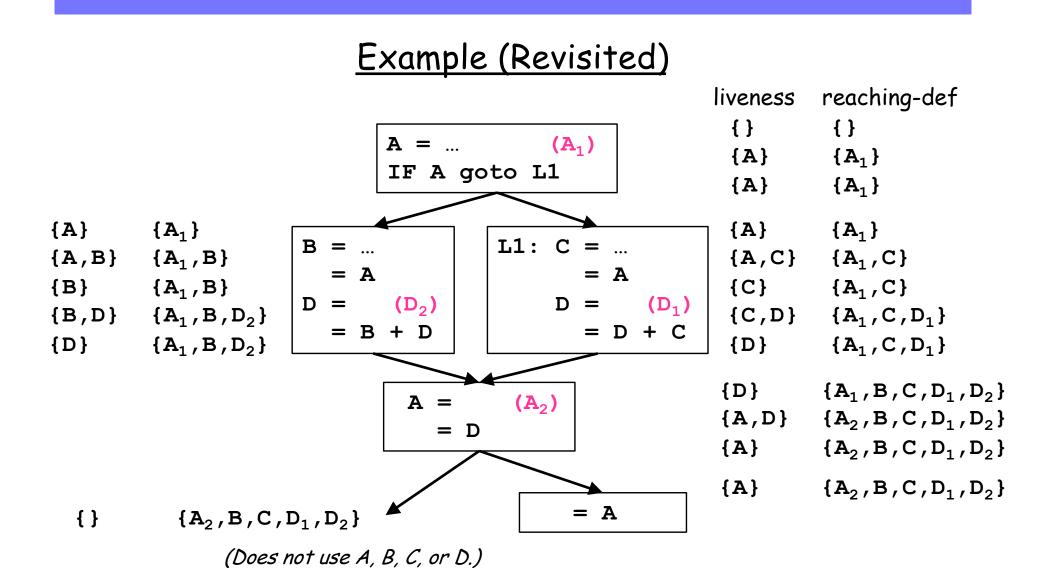
<u>Step 1a. Nodes in an Interference Graph</u>



Live Ranges and Merged Live Ranges

- Motivation: to create an interference graph that is easier to color
 - Eliminate interference in a variable's "dead" zones.
 - Increase flexibility in allocation:
 - can allocate same variable to different registers
- A live range consists of a definition and all the points in a program (e.g. end of an instruction) in which that definition is live.
 - How to compute a live range?
- Two overlapping live ranges for the same variable must be merged





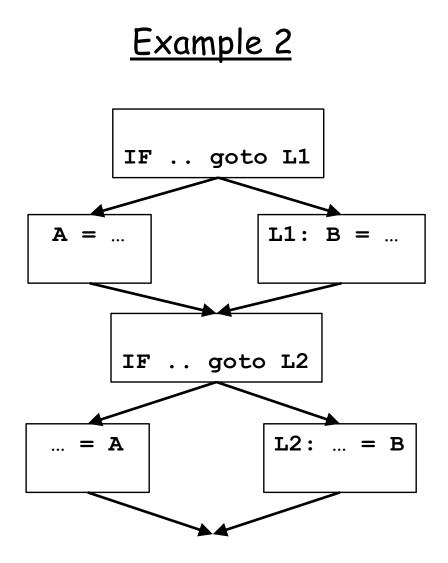
<u>Merging Live Ranges</u>

- Merging definitions into equivalence classes
 - Start by putting each definition in a different equivalence class
 - For each point in a program:
 - if (i) variable is live, and (ii) there are multiple reaching definitions for the variable, then:
 - merge the equivalence classes of all such definitions into one equivalence class
- From now on, refer to merged live ranges simply as live ranges

<u>Step 1b. Edges of Interference Graph</u>

- Intuitively:
 - Two live ranges (necessarily of different variables) may interfere if they overlap at some point in the program.
 - Algorithm:
 - At each point in the program:
 - enter an edge for every pair of live ranges at that point.

- An optimized definition & algorithm for edges:
 - Algorithm:
 - check for interference only at the starts of each merged live range
 - Faster
 - Better quality



Step 2. Coloring

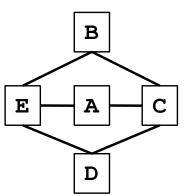
- Reminder: coloring for n > 2 is NP-complete
- Observations:
 - a node with degree < n \Rightarrow
 - can always color it successfully, given its neighbors' colors
 - a node with degree = $n \Rightarrow$

– a node with degree > n \Rightarrow

<u>Coloring Algorithm</u>

<u>Algorithm</u>:

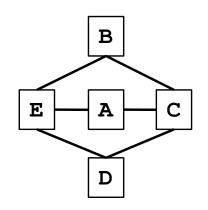
- Iterate until stuck or done
 - Pick any node with degree < n
 - Remove the node and its edges from the graph
- If done (no nodes left)
 - reverse process and add colors
- Example (n = 3):



- Note: degree of a node may drop in iteration
- Avoids making arbitrary decisions that make coloring fail

What Does Coloring Accomplish?

- Done:
 - colorable, also obtained an assignment
- Stuck:
 - colorable or not?



What if Coloring Fails?

• Use heuristics to improve its chance of success and to spill code

Build interference graph

Iterative until there are no nodes left If there exists a node v with less than n neighbor place v on stack to register allocate else v = node chosen by heuristics (least frequently executed, has many neighbors) place v on stack to register allocate (mark as spilled) remove v and its edges from graph

While stack is not empty Remove v from stack Reinsert v and its edges into the graph Assign v a color that differs from all its neighbors (guaranteed to be possible for nodes not marked as spilled)

Summary

- Problems:
 - Given n registers in a machine, is spilling avoided?
 - Find an assignment for all pseudo-registers, whenever possible.
- Solution:
 - Abstraction: an interference graph
 - nodes: live ranges
 - edges: presence of live range at time of definition
 - Register Allocation and Assignment problems
 - equivalent to n-colorability of interference graph
 - → NP-complete
 - Heuristics to find an assignment for n colors
 - successful: colorable, and finds assignment
 - not successful: colorability unknown & no assignment