# Package 'pls'

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R topics documented:
biplot.mvr

2 biplot.mvr

																							58
3	arn		٠	•	 •	•	•		 	٠		 •	٠	•	 ٠		 •	•	 •	•	 •	•	 56
	widekernel <sub>]</sub>																						
	ar.jack .																						
	alidationp																						
	vdpc.fit .																						
	ummary.m																						
	tdize																						
	impls.fit .																						
S	electNcom	ıp							 														
S	cores								 														
S	coreplot.								 														
ľ	oredplot .								 														 37
-	redict.mvr																						
-	ols.options																						
I	olot.mvr .								 														 32
(	scorespls.	fit							 														 31
(	oliveoil .								 														 30
1	nvrVal								 														 28
1	nvrCv								 														 25
I	nvr								 														 21
1	nsc								 														 20
	nayonnaise																						
ŀ	ernelpls.fi	t.							 														 18
٦	ack.test .																						
	gasoline .																						
	evsegments																						
	crossval .																						
(	eppls.fit .																						8

biplot.mvr

Biplots of PLSR and PCR Models.

**58** 

# Description

Biplot method for mvr objects.

# Usage

```
## S3 method for class 'mvr'
biplot(x, comps = 1:2, which = c("x", "y", "scores", "loadings"),
           var.axes = FALSE, xlabs, ylabs, main, ...)
```

biplot.mvr 3

# **Arguments**

x	an mvr object.
comps	integer vector of length two. The components to plot.
which	character. Which matrices to plot. One of "x" (X scores and loadings), "y" (Y scores and loadings), "scores" (X and Y scores) and "loadings" (X and Y loadings).
var.axes	logical. If TRUE, the second set of points have arrows representing them.
xlabs	either a character vector of labels for the first set of points, or FALSE for no labels. If missing, the row names of the first matrix is used as labels.
ylabs	either a character vector of labels for the second set of points, or FALSE for no labels. If missing, the row names of the second matrix is used as labels.
main	character. Title of plot. If missing, a title is constructed by biplot.mvr.
	Further arguments passed on to biplot.default.

# **Details**

biplot.mvr can also be called through the mvr plot method by specifying plottype = "biplot".

# Author(s)

Ron Wehrens and Bjørn-Helge Mevik

#### See Also

```
mvr, plot.mvr, biplot.default
```

# **Examples**

```
data(oliveoil)
mod <- plsr(sensory ~ chemical, data = oliveoil)
## Not run:
## These are equivalent
biplot(mod)
plot(mod, plottype = "biplot")

## The four combinations of x and y points:
par(mfrow = c(2,2))
biplot(mod, which = "x") # Default
biplot(mod, which = "y")
biplot(mod, which = "scores")
biplot(mod, which = "loadings")

## End(Not run)</pre>
```

4 coef.mvr

coef.mvr

Extract Information From a Fitted PLSR or PCR Model

## **Description**

Functions to extract information from mvr objects: Regression coefficients, fitted values, residuals, the model frame, the model matrix, names of the variables and components, and the X variance explained by the components.

## Usage

```
## S3 method for class 'mvr'
coef(object, ncomp = object$ncomp, comps, intercept = FALSE, ...)
## S3 method for class 'mvr'
fitted(object, ...)
## S3 method for class 'mvr'
residuals(object, ...)
## S3 method for class 'mvr'
model.matrix(object, ...)
## S3 method for class 'mvr'
model.frame(formula, ...)
prednames(object, intercept = FALSE)
respnames(object)
compnames(object, comps, explvar = FALSE, ...)
explvar(object)
```

# **Arguments**

```
object, formula an mvr object. The fitted model.  
ncomp, comps vector of positive integers. The components to include in the coefficients or to extract the names of. See below.  
intercept logical. Whether coefficients for the intercept should be included. Ignored if comps is specified. Defaults to FALSE.  
explvar logical. Whether the explained X variance should be appended to the component names.  
other arguments sent to underlying functions. Currently only used for model.frame.mvr and model.matrix.mvr.
```

# **Details**

These functions are mostly used inside other functions. (Functions coef.mvr, fitted.mvr and residuals.mvr are usually called through their generic functions coef, fitted and residuals, respectively.)

coef.mvr 5

coef.mvr is used to extract the regression coefficients of a model, i.e. the B in y = XB (for the Q in y = TQ where T is the scores, see Yloadings). An array of dimension c(nxvar, nyvar, length(ncomp)) or c(nxvar, nyvar, length(comps)) is returned.

If comps is missing (or is NULL), coef()[, ncomp[i]] are the coefficients for models with ncomp[i] components, for  $i=1,\ldots,length(ncomp)$ . Also, if intercept = TRUE, the first dimension is nxvar+1, with the intercept coefficients as the first row.

If comps is given, however, coef()[,,comps[i]] are the coefficients for a model with only the component comps[i], i.e. the contribution of the component comps[i] on the regression coefficients.

fitted.mvr and residuals.mvr return the fitted values and residuals, respectively. If the model was fitted with na.action = na.exclude (or after setting the default na.action to "na.exclude" with options), the fitted values (or residuals) corresponding to excluded observations are returned as NA; otherwise, they are omitted.

model.frame.mvr returns the model frame; i.e. a data frame with all variables neccessary to generate the model matrix. See model.frame for details.

model.matrix.mvr returns the (possibly coded) matrix used as X in the fitting. See model.matrix for details.

prednames, responses and components, respectively. With intercept = TRUE in prednames, the name of the intercept variable (i.e. "(Intercept)") is returned as well. components can also extract component names from score and loading matrices. If explvar = TRUE in components, the explained variance for each component (if available) is appended to the component names. For optimal formatting of the explained variances when not all components are to be used, one should specify the desired components with the argument comps.

explvar extracts the amount of X variance (in per cent) explained by each component in the model. It can also handle score and loading matrices returned by scores and loadings.

## Value

coef.mvr returns an array of regression coefficients.

fitted.mvr returns an array with fitted values.

residuals.mvr returns an array with residuals.

model.frame.mvr returns a data frame.

model.matrix.mvr returns the X matrix.

prednames, respnames and compnames return a character vector with the corresponding names.

explvar returns a numeric vector with the explained variances, or NULL if not available.

# Author(s)

Ron Wehrens and Bjørn-Helge Mevik

#### See Also

```
mvr, coef, fitted, residuals, model.frame, model.matrix, na.omit
```

6 coefplot

## **Examples**

coefplot

Plot Regression Coefficients of PLSR and PCR models

# **Description**

Function to plot the regression coefficients of an mvr object.

# Usage

```
coefplot(object, ncomp = object$ncomp, comps, intercept = FALSE,
    separate = FALSE, se.whiskers = FALSE, nCols, nRows, labels,
    type = "l", lty, lwd = NULL, pch, cex = NULL, col, legendpos,
    xlab = "variable", ylab = "regression coefficient", main,
    pretty.xlabels = TRUE, xlim, ylim,
    ask = nRows * nCols < nPlots && dev.interactive(), ...)</pre>
```

# **Arguments**

object	an mvr object. The fitted model.
ncomp, comps	vector of positive integers. The components to plot. See coef.mvr for details.
separate	logical. If TRUE, coefficients for different model sizes are blotted in separate plots.
se.whiskers	logical. If TRUE, whiskers at plus/minus 1 estimated standard error are added to the plot. This is only available if the model was cross-validated with jackknife = TRUE. Also, in the current implementation, intercept must be FALSE, and separate must be TRUE if length(ncomp) > 1.
intercept	logical. Whether coefficients for the intercept should be plotted. Ignored if comps is specified. Defaults to FALSE. See coef.mvr for details.
nCols, nRows	integer. The number of coloumns and rows the plots will be laid out in. If not specified, coefplot tries to be intelligent.
labels	optional. Alternative $x$ axis labels. See Details.
type	character. What type of plot to make. Defaults to "1" (lines). Alternative types include "p" (points) and "b" (both). See plot for a complete list of types.

coefplot 7

lty	vector of line types (recycled as neccessary). Line types can be specified as integers or character strings (see par for the details).
lwd	vector of positive numbers (recycled as neccessary), giving the width of the lines.
pch	plot character. A character string or a vector of single characters or integers (recycled as neccessary). See points for all alternatives.
cex	numeric vector of character expansion sizes (recycled as neccessary) for the plotted symbols.
col	character or integer vector of colors for plotted lines and symbols (recycled as neccessary). See par for the details.
legendpos	Legend position. Optional. Ignored if separate is TRUE. If present, a legend is drawn at the given position. The position can be specified symbolically (e.g., legendpos = "topright"). This requires $R >= 2.1.0$ . Alternatively, the position can be specified explicitly (legendpos = $t(c(x,y))$ ) or interactively (legendpos = $locator()$ ). This only works well for plots of single-response models.
xlab,ylab	titles for $x$ and $y$ axes. Typically character strings, but can be expressions (e.g., expression(R^2) or lists. See title for details.
main	optional main title for the plot. See Details.
pretty.xlabels	logical. If TRUE, coefplot tries to plot the $\boldsymbol{x}$ labels more nicely. See Details.
xlim,ylim	optional vector of length two, with the $x$ or $y$ limits of the plot.
ask	logical. Whether to ask the user before each page of a plot.
• • •	Further arguments sent to the underlying plot functions.

# Details

coefplot handles multiple responses by making one plot for each response. If separate is TRUE, separate plots are made for each combination of model size and response. The plots are laid out in a rectangular fashion.

If legendpos is given, a legend is drawn at the given position (unless separate is TRUE).

The argument labels can be a vector of labels or one of "names" and "numbers". The labels are used as x axis labels. If labels is "names" or "numbers", the variable names are used as labels, the difference being that with "numbers", the variable names are converted to numbers, if possible. Variable names of the forms "number" or "number text" (where the space is optional), are handled.

The argument main can be used to specify the main title of the plot. It is handled in a non-standard way. If there is only on (sub) plot, main will be used as the main title of the plot. If there is *more* than one (sub) plot, however, the presence of main will produce a corresponding 'global' title on the page. Any graphical parameters, e.g., cex.main, supplied to coefplot will only affect the 'ordinary' plot titles, not the 'global' one. Its appearance can be changed by setting the parameters with par, which will affect *both* titles. (To have different settings for the two titles, one can override the par settings with arguments to coefplot.)

The argument pretty.xlabels is only used when labels is specified. If TRUE (default), the code tries to use a 'pretty' selection of labels. If labels is "numbers", it also uses the numerical values

8 cppls.fit

of the labels for horisontal spacing. If one has excluded parts of the spectral region, one might therefore want to use pretty.xlabels = FALSE.

When separate is TRUE, the arguments lty, col, and pch default to their par() setting. Otherwise, the default for all of them is 1:nLines, where nLines is the number of model sizes specified, i.e., the length of ncomp or comps.

The function can also be called through the mvr plot method by specifying plottype = "coefficients".

#### Note

legend has many options. If you want greater control over the appearance of the legend, omit the legendpos argument and call legend manually.

The handling of labels and pretty.xlabels is experimental.

## Author(s)

Ron Wehrens and Bjørn-Helge Mevik

#### See Also

```
mvr, plot.mvr, coef.mvr, plot, legend
```

## **Examples**

```
data(yarn)
mod.nir <- plsr(density ~ NIR, ncomp = 8, data = yarn)
## Not run:
coefplot(mod.nir, ncomp = 1:6)
plot(mod.nir, plottype = "coefficients", ncomp = 1:6) # Equivalent to the previous
## Plot with legend:
coefplot(mod.nir, ncom = 1:6, legendpos = "bottomright")

## End(Not run)

data(oliveoil)
mod.sens <- plsr(sensory ~ chemical, ncomp = 4, data = oliveoil)
## Not run: coefplot(mod.sens, ncomp = 2:4, separate = TRUE)</pre>
```

cppls.fit

CPPLS (Indahl et al.)

# Description

Fits a PLS model using the CPPLS algorithm.

## Usage

9 cppls.fit

## **Arguments**

Χ a matrix of observations. NAs and Infs are not allowed. Υ a vector or matrix of responses. NAs and Infs are not allowed. ncomp the number of components to be used in the modelling. Y.add a vector or matrix of additional responses containing relevant information about the observations. center logical, determines if the X and Y matrices are mean centered or not. Default is to perform mean centering. logical. If TRUE the calculations are stripped as much as possible for speed; this stripped is meant for use with cross-validation or simulations when only the coefficients are needed. Defaults to FALSE. lower a vector of lower limits for power optimisation. Defaults to 0.5. upper a vector of upper limits for power optimisation. Defaults to 0.5. logical. If TRUE an experimental alternative power algorithm is used. (Optional) trunc.pow

a vector of individual weights for the observations. (Optional) weights

other arguments. Currently ignored. . . .

#### **Details**

This function should not be called directly, but through the generic functions cppls or mvr with the argument method="cppls". Canonical Powered PLS (CPPLS) is a generalisation of PLS incorporating discrete and continuous responses (also simultaneously), additional responses, individual weighting of observations and power methodology for sharpening focus on groups of variables. Depending on the input to cppls it can produce the following special cases:

- PLS: uni-response continuous Y
- PPLS: uni-response continuous Y, (lower | | upper) != 0.5
- PLS-DA (using correlation maximisation B/W): dummy-coded descrete response Y
- PPLS-DA: dummy-coded descrete response Y, (lower | | upper) != 0.5
- CPLS: multi-response Y (continuous, discrete or combination)
- CPPLS: multi-response Y (continuous, discrete or combination), (lower | | upper) != 0.5

The name "canonical" comes from canonical correlation analysis which is used when calculating vectors of loading weights, while "powered" refers to a reparameterisation of the vectors of loading weights which can be optimised over a given interval.

#### Value

A list containing the following components is returned:

coefficients an array of regression coefficients for 1, ..., ncomp components. The dimen-

sions of coefficients are c(nvar, npred, ncomp) with nvar the number of X

variables and npred the number of variables to be predicted in Y.

a matrix of scores. scores

10 cppls.fit

loadings a matrix of loadings.

loading.weights

a matrix of loading weights.

Yscores a matrix of Y-scores.
Yloadings a matrix of Y-loadings.

projection the projection matrix used to convert X to scores.

Xmeans a vector of means of the X variables.

Ymeans a vector of means of the Y variables.

fitted.values an array of fitted values. The dimensions of fitted.values are c(nobj,npred,ncomp)

with nobj the number samples and npred the number of Y variables.

residuals an array of regression residuals. It has the same dimensions as fitted.values.

Xvar a vector with the amount of X-variance explained by each component.

Xtotvar total variance in X.

gammas gamma-values obtained in power optimisation.

canonical.correlations

Canonical correlation values from the calculations of loading weights.

A matrix containing vectors of weights a from canonical correlation (cor(Za, Yb)).

smallNorms vector of indices of explanatory variables of length close to or equal to 0.

If stripped is TRUE, only the components coefficients, Xmeans, Ymeans and gammas are returned.

# Author(s)

Kristian Hovde Liland

#### References

Indahl, U. (2005) A twist to partial least squares regression. Journal of Chemometrics, 19, 32-44.

Liland, K.H and Indahl, U.G (2009) Powered partial least squares discriminant analysis, *Journal of Chemometrics*, **23**, 7–18.

Indahl, U.G., Liland, K.H. and Næs, T. (2009) Canonical partial least squares - a unified PLS approach to classification and regression problems. *Journal of Chemometrics*, **23**, 495–504.

#### See Also

```
mvr plsr pcr widekernelpls.fit simpls.fit oscorespls.fit
```

# **Examples**

crossval 11

```
# Predict CPLS scores for test data
may.cpls <- cppls(dummy ~ NIR, 10, data = mayonnaise, subset = train)</pre>
may.test <- predict(may.cpls, newdata = mayonnaise[!mayonnaise$train,], type = "score")</pre>
# Predict CPLS scores for test data (experimental used design as additional Y information)
may.cpls.yadd <- cppls(dummy ~ NIR, 10, data = mayonnaise, subset = train, Y.add=design)
may.test.yadd <- predict(may.cpls.yadd, newdata = mayonnaise[!mayonnaise$train,], type = "score")</pre>
# Classification by linear discriminant analysis (LDA)
library(MASS)
error <- matrix(ncol = 10, nrow = 2)
dimnames(error) <- list(Model = c('CPLS', 'CPLS (Y.add)'), ncomp = 1:10)</pre>
for (i in 1:10) {
    fitdata1 <- data.frame(oil.type = mayonnaise$oil.type[mayonnaise$train],</pre>
                            NIR.score = I(may.cpls$scores[,1:i,drop=FALSE]))
    testdata1 <- data.frame(oil.type = mayonnaise$oil.type[!mayonnaise$train],</pre>
                             NIR.score = I(may.test[,1:i,drop=FALSE]))
    error[1,i] <-
        (42 - sum(predict(lda(oil.type ~ NIR.score, data = fitdata1),
                  newdata = testdata1)$class == testdata1$oil.type)) / 42
    fitdata2 <- data.frame(oil.type = mayonnaise$oil.type[mayonnaise$train],</pre>
                            NIR.score = I(may.cpls.yadd$scores[,1:i,drop=FALSE]))
    testdata2 <- data.frame(oil.type = mayonnaise$oil.type[!mayonnaise$train],</pre>
                             NIR.score = I(may.test.yadd[,1:i,drop=FALSE]))
    error[2,i] <-
        (42 - sum(predict(lda(oil.type ~ NIR.score, data = fitdata2),
                  newdata = testdata2)$class == testdata2$oil.type)) / 42
round(error,2)
```

crossval

Cross-validation of PLSR and PCR models

## **Description**

A "stand alone" cross-validation function for mvr objects.

#### **Usage**

## **Arguments**

object an mvr object; the regression to cross-validate.

segments the number of segments to use, or a list with segments (see below).

segment.type the type of segments to use. Ignored if segments is a list.

12 crossval

length.seg Positive integer. The length of the segments to use. If specified, it overrides

segments unless segments is a list.

jackknife logical. Whether jackknifing of regression coefficients should be performed.

trace if TRUE, tracing is turned on. If numeric, it denotes a time limit (in seconds).

If the estimated total time of the cross-validation exceeds this limit, tracing is

turned on.

... additional arguments, sent to the underlying fit function.

#### **Details**

This function performs cross-validation on a model fit by mvr. It can handle models such as  $plsr(y \sim msc(X),...)$  or other models where the predictor variables need to be recalculated for each segment. When recalculation is not needed, the result of crossval(mvr(...)) is identical to crossval(mvr(...)) but slower.

Note that to use crossval, the data *must* be specified with a data argument when fitting object.

If segments is a list, the arguments segment.type and length.seg are ignored. The elements of the list should be integer vectors specifying the indices of the segments. See cvsegments for details.

Otherwise, segments of type segment.type are generated. How many segments to generate is selected by specifying the number of segments in segments, or giving the segment length in length.seg. If both are specified, segments is ignored.

If jackknife is TRUE, jackknifed regression coefficients are returned, which can be used for for variance estimation (var. jack) or hypothesis testing (jack.test).

When tracing is turned on, the segment number is printed for each segment.

By default, the cross-validation will be performed serially. However, it can be done in parallel using functionality in the parallel package by setting the option parallel in pls.options. See pls.options for the different ways to specify the parallelism. See also Examples below.

# Value

The supplied object is returned, with an additional component validation, which is a list with components

method eugals "CV" for cross-validation.

pred an array with the cross-validated predictions.

coefficients (only if jackknife is TRUE) an array with the jackknifed regression coefficients.

The dimensions correspond to the predictors, responses, number of components,

and segments, respectively.

PRESS0 a vector of PRESS values (one for each response variable) for a model with zero

components, i.e., only the intercept.

PRESS a matrix of PRESS values for models with 1, ..., ncomp components. Each row

corresponds to one response variable.

adj a matrix of adjustment values for calculating bias corrected MSEP. MSEP uses

this.

segments the list of segments used in the cross-validation.

crossval 13

ncomp the number of components.

gammas if method cppls is used, gamma values for the powers of each CV segment are

returned.

#### Note

The PRESS0 is always cross-validated using leave-one-out cross-validation. This usually makes little difference in practice, but should be fixed for correctness.

The current implementation of the jackknife stores all jackknife-replicates of the regression coefficients, which can be very costly for large matrices. This might change in a future version.

## Author(s)

Ron Wehrens and Bjørn-Helge Mevik

#### References

Mevik, B.-H., Cederkvist, H. R. (2004) Mean Squared Error of Prediction (MSEP) Estimates for Principal Component Regression (PCR) and Partial Least Squares Regression (PLSR). *Journal of Chemometrics*, **18**(9), 422–429.

#### See Also

```
mvr mvrCv cvsegments MSEP var.jack jack.test
```

# **Examples**

```
data(yarn)
yarn.pcr <- pcr(density ~ msc(NIR), 6, data = yarn)</pre>
yarn.cv <- crossval(yarn.pcr, segments = 10)</pre>
## Not run: plot(MSEP(yarn.cv))
## Not run:
## Parallelised cross-validation, using transient cluster:
pls.options(parallel = 4) # use mclapply (not available on Windows)
pls.options(parallel = quote(parallel::makeCluster(4, type = "PSOCK"))) # parLapply
## A new cluster is created and stopped for each cross-validation:
yarn.cv <- crossval(yarn.pcr)</pre>
yarn.loocv <- crossval(yarn.pcr, length.seg = 1)</pre>
## Parallelised cross-validation, using persistent cluster:
library(parallel)
## This creates the cluster:
pls.options(parallel = makeCluster(4, type = "FORK")) # not available on Windows
pls.options(parallel = makeCluster(4, type = "PSOCK"))
## The cluster can be used several times:
yarn.cv <- crossval(yarn.pcr)</pre>
yarn.loocv <- crossval(yarn.pcr, length.seg = 1)</pre>
## The cluster should be stopped manually afterwards:
stopCluster(pls.options()$parallel)
```

14 cvsegments

```
## Parallelised cross-validation, using persistent MPI cluster:
## This requires the packages snow and Rmpi to be installed
library(parallel)
## This creates the cluster:
pls.options(parallel = makeCluster(4, type = "MPI"))
## The cluster can be used several times:
yarn.cv <- crossval(yarn.pcr)
yarn.loocv <- crossval(yarn.pcr, length.seg = 1)
## The cluster should be stopped manually afterwards:
stopCluster(pls.options()$parallel)
## It is good practice to call mpi.exit() or mpi.quit() afterwards:
mpi.exit()
## End(Not run)</pre>
```

cvsegments

Generate segments for cross-validation

# Description

The function generates a list of segments for cross-validation. It can generate random, consecutive and interleaved segments, and supports keeping replicates in the same segment.

#### **Usage**

# **Arguments**

N Integer. The number of rows in the data set.k Integer. The number of segments to return.

length.seg Integer. The length of the segments. If given, it overrides k.

nrep Integer. The number of (consecutive) rows that are replicates of the same object.

Replicates will always be kept in the same segment.

type One of "random", "consecutive" and "interleaved". The type of segments

to generate. Default is "random".

#### **Details**

If length, seg is specified, it is used to calculate the number of segments to generate. Otherwise k must be specified. If  $k*length.seg \neq N$ , the k\*length.seg - N last segments will contain only length.seg - 1 indices.

If type is "random", the indices are allocated to segments in random order. If it is "consecutive", the first segment will contain the first length.seg indices, and so on. If type is "interleaved", the first segment will contain the indices  $1, length.seg + 1, 2 * length.seg + 1, \ldots, (k-1) * length.seg + 1, and so on.$ 

gasoline 15

If nrep >, it is assumed that each nrep consecutive rows are replicates (repeated measurements) of the same object, and care is taken that replicates are never put in different segments.

Warning: If k does not divide N, a specified length.seg does not divide N, or nrep does not divide length.seg, the number of segments and/or the segment length will be adjusted as needed. Warnings are printed for some of these cases, and one should always inspect the resulting segments to make sure they are as expected.

#### Value

A list of vectors. Each vector contains the indices for one segment. The attribute "incomplete" contains the number of incomplete segments, and the attribute "type" contains the type of segments.

## Author(s)

Bjørn-Helge Mevik and Ron Wehrens

## **Examples**

```
## Segments for 10-fold randomised cross-validation:
cvsegments(100, 10)
## Segments with four objects, taken consecutive:
cvsegments(60, length.seg = 4, type = "cons")
## Incomplete segments
segs <- cvsegments(50, length.seg = 3)</pre>
attr(segs, "incomplete")
## Leave-one-out cross-validation:
cvsegments(100, 100)
## Leave-one-out with variable/unknown data set size n:
n <- 50
cvsegments(n, length.seg = 1)
## Data set with replicates
cvsegments(100, 25, nrep = 2)
## Note that rows 1 and 2 are in the same segment, rows 3 and 4 in the
## same segment, and so on.
```

gasoline

Octane numbers and NIR spectra of gasoline

#### **Description**

A data set with NIR spectra and octane numbers of 60 gasoline samples. The NIR spectra were measured using diffuse reflectance as log(1/R) from 900 nm to 1700 nm in 2 nm intervals, giving 401 wavelengths. Many thanks to John H. Kalivas.

16 jack.test

#### Usage

```
gasoline
```

#### **Format**

A data frame with 60 observations on the following 2 variables.

```
octane a numeric vector. The octane number.
```

NIR a matrix with 401 columns. The NIR spectrum.

## **Source**

Kalivas, John H. (1997) Two Data Sets of Near Infrared Spectra *Chemometrics and Intelligent Laboratory Systems*, **37**, 255–259.

jack.test

Jackknife approximate t tests of regression coefficients

# Description

Performes approximate t tests of regression coefficients based on jackknife variance estimates.

## Usage

```
jack.test(object, ncomp = object$ncomp, use.mean = TRUE)
## S3 method for class 'jacktest'
print(x, P.values = TRUE, ...)
```

# **Arguments**

object an mvr object. A cross-validated model fitted with jackknife = TRUE.

ncomp the number of components to use for estimating the variances

use.mean logical. If TRUE (default), the mean coefficients are used when estimating the (co)variances; otherwise the coefficients from a model fitted to the entire data set. See var.jack for details.

x an jacktest object, the result of jack.test.

P.values logical. Whether to print p values (default).

Further arguments sent to the underlying print function printCoefmat.

## **Details**

jack test uses the variance estimates from var. jack to perform t tests of the regression coefficients. The resulting object has a print method, print.jacktest, which uses printCoefmat for the actual printing.

jack.test 17

#### Value

jack.test returns an object of class "jacktest", with components

coefficients The estimated regression coefficients

sd The square root of the jackknife variance estimates

tvalues The t statistics

df The 'degrees of freedom' used for calculating p values

pvalues The calculated p values

print.jacktest returns the "jacktest" object (invisibly).

## Warning

The jackknife variance estimates are known to be biased (see var.jack). Also, the distribution of the regression coefficient estimates and the jackknife variance estimates are unknown (at least in PLSR/PCR). Consequently, the distribution (and in particular, the degrees of freedom) of the resulting t statistics is unknown. The present code simply assumes a t distribution with t0 degrees of freedom, where t1 is the number of cross-validation segments.

Therefore, the resulting p values should not be used uncritically, and should perhaps be regarded as mere indicator of (non-)significance.

Finally, also keep in mind that as the number of predictor variables increase, the problem of multiple tests increases correspondingly.

#### Author(s)

Bjørn-Helge Mevik

# References

Martens H. and Martens M. (2000) Modified Jack-knife Estimation of Parameter Uncertainty in Bilinear Modelling by Partial Least Squares Regression (PLSR). *Food Quality and Preference*, **11**, 5–16.

#### See Also

```
var.jack, mvrCv
```

# **Examples**

```
data(oliveoil)
mod <- pcr(sensory ~ chemical, data = oliveoil, validation = "LOO", jackknife = TRUE)
jack.test(mod, ncomp = 2)</pre>
```

18 kernelpls.fit

# **Description**

Fits a PLSR model with the kernel algorithm.

# Usage

```
kernelpls.fit(X, Y, ncomp, center = TRUE, stripped = FALSE, ...)
```

## **Arguments**

X a matrix of observations. NAs and Infs are not allowed.Y a vector or matrix of responses. NAs and Infs are not allowed.

ncomp the number of components to be used in the modelling.

center logical, determines if the X and Y matrices are mean centered or not. Default

is to perform mean centering.

stripped logical. If TRUE the calculations are stripped as much as possible for speed; this

is meant for use with cross-validation or simulations when only the coefficients

are needed. Defaults to FALSE.

... other arguments. Currently ignored.

## **Details**

This function should not be called directly, but through the generic functions plsr or mvr with the argument method="kernelpls" (default). Kernel PLS is particularly efficient when the number of objects is (much) larger than the number of variables. The results are equal to the NIPALS algorithm. Several different forms of kernel PLS have been described in literature, e.g. by De Jong and Ter Braak, and two algorithms by Dayal and MacGregor. This function implements the fastest of the latter, not calculating the crossproduct matrix of X. In the Dyal & MacGregor paper, this is "algorithm 1".

# Value

A list containing the following components is returned:

coefficients an array of regression coefficients for 1, ..., ncomp components. The dimen-

sions of coefficients are c(nvar, npred, ncomp) with nvar the number of X

variables and npred the number of variables to be predicted in Y.

scores a matrix of scores.

loadings a matrix of loadings.

loading.weights

a matrix of loading weights.

Yscores a matrix of Y-scores.

mayonnaise 19

Yloadings a matrix of Y-loadings.

projection the projection matrix used to convert X to scores.

Xmeans a vector of means of the X variables.

Ymeans a vector of means of the Y variables.

fitted.values an array of fitted values. The dimensions of fitted.values are c(nobj, npred, ncomp)

with nobj the number samples and npred the number of Y variables.

residuals an array of regression residuals. It has the same dimensions as fitted.values.

Xvar a vector with the amount of X-variance explained by each component.

Xtotvar Total variance in X.

If stripped is TRUE, only the components coefficients, Xmeans and Ymeans are returned.

## Author(s)

Ron Wehrens and Bjørn-Helge Mevik

#### References

de Jong, S. and ter Braak, C. J. F. (1994) Comments on the PLS kernel algorithm. *Journal of Chemometrics*, **8**, 169–174.

Dayal, B. S. and MacGregor, J. F. (1997) Improved PLS algorithms. *Journal of Chemometrics*, **11**, 73–85.

## See Also

mvr plsr cppls pcr widekernelpls.fit simpls.fit oscorespls.fit

mayonnaise	NIR measurements and oil types of mayonnaise

## **Description**

Raw NIR measurements (351 wavelengths, 1100-2500 nm in steps of 4 nm) taken on 54 samples of mayonnaise based on six different oil types (soybean, sunflower, canola, olive, corn, and grapeseed). The resulting 54 samples were measured in triplicates, resulting in 54 x 3 = 162 different spectra (120/42 training/test).

#### Usage

data(mayonnaise)

20 msc

## **Format**

A data frame with 162 observations on the following 4 variables.

```
NIR a matrix with 351 columns
oil.type a numeric vector
design a matrix with 5 columns
train a logical vector
```

#### **Source**

Indahl U, Sahni NS, Kirkhus B, Næs T. Multivariate strategies for classification based on NIR-spectra-with application to mayonnaise. Chemometr. Intell. Lab. Sys. 1999; 49: 19-31.

msc

Multiplicative Scatter Correction

## **Description**

Performs multiplicative scatter/signal correction on a data matrix.

## Usage

```
msc(X, reference = NULL)
## S3 method for class 'msc'
predict(object, newdata, ...)
## S3 method for class 'msc'
makepredictcall(var, call)
```

## **Arguments**

X, newdata numeric matrices. The data to scatter correct.

reference numeric vector. Spectre to use as reference. If NULL, the column means of X are

used.

object an object inheriting from class "msc", normally the result of a call to msc with a

single matrix argument.

var A variable.

call The term in the formula, as a call.
... other arguments. Currently ignored.

# **Details**

makepredictcall.msc is an internal utility function; it is not meant for interactive use. See makepredictcall for details.

#### Value

Both msc and predict.msc return a multiplicative scatter corrected matrix, with attribute "reference" the vector used as reference spectre. The matrix is given class c("msc", "matrix"). For predict.msc, the "reference" attribute of object is used as reference spectre.

#### Author(s)

Bjørn-Helge Mevik and Ron Wehrens

#### References

Martens, H., Næs, T. (1989) Multivariate calibration. Chichester: Wiley.

#### See Also

```
mvr, pcr, plsr, stdize
```

## **Examples**

```
data(yarn)
## Direct correction:
Ztrain <- msc(yarn$NIR[yarn$train,])
Ztest <- predict(Ztrain, yarn$NIR[!yarn$train,])

## Used in formula:
mod <- plsr(density ~ msc(NIR), ncomp = 6, data = yarn[yarn$train,])
pred <- predict(mod, newdata = yarn[!yarn$train,]) # Automatically scatter corrected</pre>
```

mvr

Partial Least Squares and Principal Component Regression

# Description

Functions to perform partial least squares regression (PLSR), canonical powered partial least squares (CPPLS) or principal component regression (PCR), with a formula interface. Cross-validation can be used. Prediction, model extraction, plot, print and summary methods exist.

## Usage

```
mvr(formula, ncomp, Y.add, data, subset, na.action,
    method = pls.options()$mvralg,
    scale = FALSE, center = TRUE, validation = c("none", "CV", "L00"),
    model = TRUE, x = FALSE, y = FALSE, ...)
plsr(..., method = pls.options()$plsralg)
cppls(..., Y.add, weights, method = pls.options()$cpplsalg)
pcr(..., method = pls.options()$pcralg)
```

#### **Arguments**

formula a model formula. Most of the 1m formula constructs are supported. See below.

ncomp the number of components to include in the model (see below).

Y. add a vector or matrix of additional responses containing relevant information about

the observations. Only used for cppls.

data an optional data frame with the data to fit the model from.

subset an optional vector specifying a subset of observations to be used in the fitting

process.

na.action a function which indicates what should happen when the data contain missing

values. The default is set by the na.action setting of options, and is na.fail if that is unset. The 'factory-fresh' default is na.omit. Another possible value is NULL, no action. Value na.exclude can be useful. See na.omit for other

alternatives.

method the multivariate regression method to be used. If "model.frame", the model

frame is returned.

scale numeric vector, or logical. If numeric vector, X is scaled by dividing each

variable with the corresponding element of scale. If scale is TRUE, X is scaled by dividing each variable by its sample standard deviation. If cross-validation is

selected, scaling by the standard deviation is done for every segment.

center logical, determines if the X and Y matrices are mean centered or not. Default

is to perform mean centering.

validation character. What kind of (internal) validation to use. See below.

model a logical. If TRUE, the model frame is returned.

x a logical. If TRUE, the model matrix is returned.

y a logical. If TRUE, the response is returned.

weights a vector of individual weights for the observations. Only used for cppls. (Op-

tional)

.. additional optional arguments, passed to the underlying fit functions, and mvrCv.

 $Currently, \ the \ fit \ functions \ oscorespls.fit \ and \ wide kernelpls.fit \ implementations \ oscorespls.fit \ and \ wide kernelpls.fit \ implementation \ oscorespls.fit \ and \ wide kernelpls.fit \ implementation \ oscorespls.fit \ and \ wide kernelpls.fit \ implementation \ oscorespls.fit \ oscorespls.$ 

ment these extra arguments:

tol: numeric. Tolerance used for determining convergence.

**maxit:** positive integer. The maximal number of iterations used.

and cppls. fit implements:

**lower:** a vector of lower limits for power optimisation.

**upper:** a vector of upper limits for power optimisation.

trunc.pow: logical. Whether to use an experimental alternative power algo-

rithm.

mvrCv implements several arguments; the following are probably the most useful of them:

**segments:** the number of segments to use, or a list with segments.

**segment.type:** the type of segments to use.

**length.seg:** Positive integer. The length of the segments to use.

**jackknife:** logical. Whether to perform jackknifing of regression coefficients.

See the functions' documentation for details.

#### **Details**

The functions fit PLSR, CPPLS or PCR models with 1, ..., ncomp number of components. Multi-response models are fully supported.

The type of model to fit is specified with the method argument. Four PLSR algorithms are available: the kernel algorithm ("kernelpls"), the wide kernel algorithm ("widekernelpls"), SIMPLS ("simpls") and the classical orthogonal scores algorithm ("oscorespls"). One CPPLS algorithm is available ("cppls") providing several extensions to PLS. One PCR algorithm is available: using the singular value decomposition ("svdpc"). If method is "model.frame", the model frame is returned. The functions pcr, plsr and cppls are wrappers for mvr, with different values for method.

The formula argument should be a symbolic formula of the form response  $^{\sim}$  terms, where response is the name of the response vector or matrix (for multi-response models) and terms is the name of one or more predictor matrices, usually separated by +, e.g., water  $^{\sim}$  FTIR or y  $^{\sim}$  X + Z. See lm for a detailed description. The named variables should exist in the supplied data data frame or in the global environment. Note: Do not use mvr(mydata\$y  $^{\sim}$  mydata\$X,...), instead use mvr(y  $^{\sim}$  X, data = mydata,...). Otherwise, predict.mvr will not work properly. The chapter 'Statistical models in R' of the manual 'An Introduction to R' distributed with R is a good reference on formulas in R.

The number of components to fit is specified with the argument ncomp. It this is not supplied, the maximal number of components is used (taking account of any cross-validation).

All implemented algorithms mean-center both predictor and response matrices. This can be turned off by specifying center = FALSE. See Seasholtz and Kowalski for a discussion about centering in PLS regression.

If validation = "CV", cross-validation is performed. The number and type of cross-validation segments are specified with the arguments segments and segment.type. See mvrCv for details. If validation = "L00", leave-one-out cross-validation is performed. It is an error to specify the segments when validation = "L00" is specified.

By default, the cross-validation will be performed serially. However, it can be done in parallel using functionality in the parallel package by setting the option parallel in pls.options. See pls.options for the differnt ways to specify the parallelism. See also Examples below.

Note that the cross-validation is optimised for speed, and some generality has been sacrificed. Especially, the model matrix is calculated only once for the complete cross-validation, so models like  $y \sim msc(X)$  will not be properly cross-validated. However, scaling requested by scale = TRUE is properly cross-validated. For proper cross-validation of models where the model matrix must be updated/regenerated for each segment, use the separate function crossval.

## Value

If method = "model.frame", the model frame is returned. Otherwise, an object of class mvr is returned. The object contains all components returned by the underlying fit function. In addition, it contains the following components:

validation if validation was requested, the results of the cross-validation. See mvrCv for

fit.time the elapsed time for the fit. This is used by crossval to decide whether to turn

on tracing.

na.action	if observations with missing values were removed, na.action contains a vector with their indices. The class of this vector is used by functions like fitted to decide how to treat the observations.
ncomp	the number of components of the model.
method	the method used to fit the model. See the argument method for possible values.
scale	if scaling was requested (with scale), the scaling used.
call	the function call.
terms	the model terms.
model	if model = TRUE, the model frame.
x	if $x = TRUE$ , the model matrix.
У	if y = TRUE, the model response.

#### Author(s)

Ron Wehrens and Bjørn-Helge Mevik

#### References

Martens, H., Næs, T. (1989) Multivariate calibration. Chichester: Wiley.

Seasholtz, M. B. and Kowalski, B. R. (1992) The effect of mean centering on prediction in multivariate calibration. *Journal of Chemometrics*, **6**(2), 103–111.

## See Also

```
kernelpls.fit, widekernelpls.fit, simpls.fit, oscorespls.fit, cppls.fit, svdpc.fit, mvrCv, crossval, loadings, scores, loading.weights, coef.mvr, predict.mvr, R2, MSEP, RMSEP, plot.mvr
```

# **Examples**

```
data(yarn)
## Default methods:
yarn.pcr <- pcr(density ~ NIR, 6, data = yarn, validation = "CV")</pre>
yarn.pls <- plsr(density ~ NIR, 6, data = yarn, validation = "CV")</pre>
yarn.cppls <- cppls(density ~ NIR, 6, data = yarn, validation = "CV")</pre>
## Alternative methods:
yarn.oscorespls <- mvr(density ~ NIR, 6, data = yarn, validation = "CV",</pre>
                      method = "oscorespls")
yarn.simpls <- mvr(density ~ NIR, 6, data = yarn, validation = "CV",</pre>
                  method = "simpls")
## Not run:
## Parallelised cross-validation, using transient cluster:
pls.options(parallel = 4) # use mclapply
pls.options(parallel = quote(makeCluster(4, type = "PSOCK"))) # use parLapply
## A new cluster is created and stopped for each cross-validation:
yarn.pls <- plsr(density ~ NIR, 6, data = yarn, validation = "CV")</pre>
```

mvrCv 25

```
yarn.pcr <- pcr(density ~ NIR, 6, data = yarn, validation = "CV")</pre>
## Parallelised cross-validation, using persistent cluster:
library(parallel)
## This creates the cluster:
pls.options(parallel = makeCluster(4, type = "PSOCK"))
## The cluster can be used several times:
yarn.pls <- plsr(density ~ NIR, 6, data = yarn, validation = "CV")
yarn.pcr <- pcr(density ~ NIR, 6, data = yarn, validation = "CV")</pre>
## The cluster should be stopped manually afterwards:
stopCluster(pls.options()$parallel)
## Parallelised cross-validation, using persistent MPI cluster:
## This requires the packages snow and Rmpi to be installed
library(parallel)
## This creates the cluster:
pls.options(parallel = makeCluster(4, type = "MPI"))
## The cluster can be used several times:
yarn.pls <- plsr(density ~ NIR, 6, data = yarn, validation = "CV")</pre>
yarn.pcr <- pcr(density ~ NIR, 6, data = yarn, validation = "CV")</pre>
## The cluster should be stopped manually afterwards:
stopCluster(pls.options()$parallel)
## It is good practice to call mpi.exit() or mpi.quit() afterwards:
mpi.exit()
## End(Not run)
## Multi-response models:
data(oliveoil)
sens.pcr <- pcr(sensory ~ chemical, ncomp = 4, scale = TRUE, data = oliveoil)</pre>
sens.pls <- plsr(sensory ~ chemical, ncomp = 4, scale = TRUE, data = oliveoil)</pre>
## Classification
# A classification example utilizing additional response information
# (Y.add) is found in the cppls.fit manual ('See also' above).
```

mvrCv

Cross-validation

# Description

Performs the cross-validation calculations for mvr.

## Usage

```
mvrCv(X, Y, ncomp, Y.add = NULL, weights = NULL,
    method = pls.options()$mvralg, scale = FALSE,
    segments = 10, segment.type = c("random", "consecutive", "interleaved"),
    length.seg, jackknife = FALSE, trace = FALSE, ...)
```

26 mvrCv

## **Arguments**

X a matrix of observations. NAs and Infs are not allowed.
Y a vector or matrix of responses. NAs and Infs are not allowed.
ncomp the number of components to be used in the modelling.

Y. add a vector or matrix of additional responses containing relevant information about

the observations. Only used for cppls.

weights a vector of individual weights for the observations. Only used for cppls. (Op-

tional)

method the multivariate regression method to be used.

scale  $\log$  logical. If TRUE, the learning X data for each segment is scaled by dividing each

variable by its sample standard deviation. The prediction data is scaled by the

same amount.

segments the number of segments to use, or a list with segments (see below).

segment. type the type of segments to use. Ignored if segments is a list.

length.seg Positive integer. The length of the segments to use. If specified, it overrides

segments unless segments is a list.

jackknife logical. Whether jackknifing of regression coefficients should be performed.

trace logical; if TRUE, the segment number is printed for each segment.

. . . additional arguments, sent to the underlying fit function.

#### **Details**

This function is not meant to be called directly, but through the generic functions pcr, plsr, cppls or mvr with the argument validation set to "CV" or "LOO". All arguments to mvrCv can be specified in the generic function call.

If segments is a list, the arguments segment.type and length.seg are ignored. The elements of the list should be integer vectors specifying the indices of the segments. See cvsegments for details.

Otherwise, segments of type segment.type are generated. How many segments to generate is selected by specifying the number of segments in segments, or giving the segment length in length.seg. If both are specified, segments is ignored.

If jackknife is TRUE, jackknifed regression coefficients are returned, which can be used for for variance estimation (var.jack) or hypothesis testing (jack.test).

X and Y do not need to be centered.

Note that this function cannot be used in situations where X needs to be recalculated for each segment (except for scaling by the standard deviation), for instance with msc or other preprocessing. For such models, use the more general (but slower) function crossval.

Also note that if needed, the function will silently(!) reduce ncomp to the maximal number of components that can be cross-validated, which is n-l-1, where n is the number of observations and l is the length of the longest segment. The (possibly reduced) number of components is returned as the component ncomp.

By default, the cross-validation will be performed serially. However, it can be done in parallel using functionality in the parallel package by setting the option parallel in pls.options. See pls.options for the different ways to specify the parallelism.

mvrCv 27

#### Value

A list with the following components:

method equals "CV" for cross-validation.

pred an array with the cross-validated predictions.

coefficients (only if jackknife is TRUE) an array with the jackknifed regression coefficients.

The dimensions correspond to the predictors, responses, number of components,

and segments, respectively.

PRESS0 a vector of PRESS values (one for each response variable) for a model with zero

components, i.e., only the intercept.

PRESS a matrix of PRESS values for models with 1, ..., ncomp components. Each row

corresponds to one response variable.

adj a matrix of adjustment values for calculating bias corrected MSEP. MSEP uses

this.

segments the list of segments used in the cross-validation.

ncomp the actual number of components used.

gamma if method cppls is used, gamma values for the powers of each CV segment are

returned.

#### Note

The PRESS0 is always cross-validated using leave-one-out cross-validation. This usually makes little difference in practice, but should be fixed for correctness.

The current implementation of the jackknife stores all jackknife-replicates of the regression coefficients, which can be very costly for large matrices. This might change in a future version.

#### Author(s)

Ron Wehrens and Bjørn-Helge Mevik

#### References

Mevik, B.-H., Cederkvist, H. R. (2004) Mean Squared Error of Prediction (MSEP) Estimates for Principal Component Regression (PCR) and Partial Least Squares Regression (PLSR). *Journal of Chemometrics*, **18**(9), 422–429.

## See Also

```
mvr crossval cvsegments MSEP var.jack jack.test
```

# **Examples**

```
data(yarn)
yarn.pcr <- pcr(density ~ NIR, 6, data = yarn, validation = "CV", segments = 10)
## Not run: plot(MSEP(yarn.pcr))</pre>
```

28 mvrVal

mvrVal

MSEP, RMSEP and R2 of PLSR and PCR models

# **Description**

Functions to estimate the mean squared error of prediction (MSEP), root mean squared error of prediction (RMSEP) and  $\mathbb{R}^2$  (A.K.A. coefficient of multiple determination) for fitted PCR and PLSR models. Test-set, cross-validation and calibration-set estimates are implemented.

# Usage

# **Arguments**

se

an mvr object
a character vector. Which estimators to use. Should be a subset of c("all", "train", "CV", "adjCV", "adjCV" is only available for (R)MSEP. See below for how the estimators are chosen.
a data frame with test set data.
a vector of positive integers. The components or number of components to use. See below.
logical. Whether estimates for a model with zero components should be returned as well.

logical. Whether estimated standard errors of the estimates should be calculated.

,"t∈

. . further arguments sent to underlying functions or (for RMSEP) to MSEP

Not implemented yet.

mvrVal 29

#### **Details**

RMSEP simply calls MSEP and takes the square root of the estimates. It therefore accepts the same arguments as MSEP.

Several estimators can be used. "train" is the training or calibration data estimate, also called (R)MSEC. For R2, this is the unadjusted  $R^2$ . It is overoptimistic and should not be used for assessing models. "CV" is the cross-validation estimate, and "adjCV" (for RMSEP and MSEP) is the bias-corrected cross-validation estimate. They can only be calculated if the model has been cross-validated. Finally, "test" is the test set estimate, using newdata as test set.

Which estimators to use is decided as follows (see below for mvrValstats). If estimate is not specified, the test set estimate is returned if newdata is specified, otherwise the CV and adjusted CV (for RMSEP and MSEP) estimates if the model has been cross-validated, otherwise the training data estimate. If estimate is "all", all possible estimates are calculated. Otherwise, the specified estimates are calculated.

Several model sizes can also be specified. If comps is missing (or is NULL), length(ncomp) models are used, with ncomp[1] components, ..., ncomp[length(ncomp)] components. Otherwise, a single model with the components comps[1], ..., comps[length(comps)] is used. If intercept is TRUE, a model with zero components is also used (in addition to the above).

The  $R^2$  values returned by "R2" are calculated as 1-SSE/SST, where SST is the (corrected) total sum of squares of the response, and SSE is the sum of squared errors for either the fitted values (i.e., the residual sum of squares), test set predictions or cross-validated predictions (i.e., the PRESS). For estimate = "train", this is equivalent to the squared correlation between the fitted values and the response. For estimate = "train", the estimate is often called the prediction  $R^2$ .

mvrValstats is a utility function that calculates the statistics needed by MSEP and R2. It is not intended to be used interactively. It accepts the same arguments as MSEP and R2. However, the estimate argument must be specified explicitly: no partial matching and no automatic choice is made. The function simply calculates the types of estimates it knows, and leaves the other untouched.

#### Value

mvrValstats returns a list with components

**SSE** three-dimensional array of SSE values. The first dimension is the different estimators, the second is the response variables and the third is the models.

**SST** matrix of SST values. The first dimension is the different estimators and the second is the response variables.

**nobj** a numeric vector giving the number of objects used for each estimator.

**comps** the components specified, with 0 prepended if intercept is TRUE.

cumulative TRUE if comps was NULL or not specified.

The other functions return an object of class "mvrVal", with components

**val** three-dimensional array of estimates. The first dimension is the different estimators, the second is the response variables and the third is the models.

type "MSEP", "RMSEP" or "R2".

**comps** the components specified, with 0 prepended if intercept is TRUE.

30 oliveoil

```
cumulative TRUE if comps was NULL or not specified. call the function call
```

#### Author(s)

Ron Wehrens and Bjørn-Helge Mevik

#### References

Mevik, B.-H., Cederkvist, H. R. (2004) Mean Squared Error of Prediction (MSEP) Estimates for Principal Component Regression (PCR) and Partial Least Squares Regression (PLSR). *Journal of Chemometrics*, **18**(9), 422–429.

#### See Also

```
mvr, crossval, mvrCv, validationplot, plot.mvrVal
```

## **Examples**

```
data(oliveoil)
mod <- plsr(sensory ~ chemical, ncomp = 4, data = oliveoil, validation = "L00")
RMSEP(mod)
## Not run: plot(R2(mod))</pre>
```

oliveoil

Sensory and physico-chemical data of olive oils

## **Description**

A data set with scores on 6 attributes from a sensory panel and measurements of 5 physico-chemical quality parameters on 16 olive oil samples. The first five oils are Greek, the next five are Italian and the last six are Spanish.

## Usage

oliveoil

## Format

A data frame with 16 observations on the following 2 variables.

```
sensory a matrix with 6 columns. Scores for attributes 'yellow', 'green', 'brown', 'glossy', 'transp', and 'syrup'.
```

chemical a matrix with 5 columns. Measurements of acidity, peroxide, K232, K270, and DK.

## Source

Massart, D. L., Vandeginste, B. G. M., Buydens, L. M. C., de Jong, S., Lewi, P. J., Smeyers-Verbeke, J. (1998) *Handbook of Chemometrics and Qualimetrics: Part B.* Elsevier. Tables 35.1 and 35.4.

oscorespls.fit 31

|--|

# Description

Fits a PLSR model with the orthogonal scores algorithm (aka the NIPALS algorithm).

# Usage

## **Arguments**

Χ	a matrix of observations. NAs and Infs are not allowed.
Υ	a vector or matrix of responses. NAs and Infs are not allowed.
ncomp	the number of components to be used in the modelling.
center	logical, determines if the $X$ and $Y$ matrices are mean centered or not. Default is to perform mean centering.
stripped	logical. If TRUE the calculations are stripped as much as possible for speed; this is meant for use with cross-validation or simulations when only the coefficients are needed. Defaults to FALSE.
tol	numeric. The tolerance used for determining convergence in multi-response models.
maxit	positive integer. The maximal number of iterations used in the internal Eigenvector calculation.
	other arguments. Currently ignored.

## **Details**

This function should not be called directly, but through the generic functions plsr or mvr with the argument method="oscorespls". It implements the orthogonal scores algorithm, as described in *Martens and Næs (1989)*. This is one of the two "classical" PLSR algorithms, the other being the orthogonal loadings algorithm.

# Value

A list containing the following components is returned:

coefficients	an array of regression coefficients for 1,, ncomp components. The dimen-
	sions of coefficients are c(nvar,npred,ncomp) with nvar the number of X
	variables and npred the number of variables to be predicted in Y.

scores a matrix of scores.

loadings a matrix of loadings.

32 plot.mvr

loading.weights

a matrix of loading weights.

Yscores a matrix of Y-scores.
Yloadings a matrix of Y-loadings.

projection the projection matrix used to convert X to scores.

Xmeans a vector of means of the X variables.
Ymeans a vector of means of the Y variables.

fitted.values an array of fitted values. The dimensions of fitted.values are c(nobj,npred,ncomp)

with nobj the number samples and npred the number of Y variables.

residuals an array of regression residuals. It has the same dimensions as fitted.values.

Xvar a vector with the amount of X-variance explained by each component.

Xtotvar Total variance in X.

If stripped is TRUE, only the components coefficients, Xmeans and Ymeans are returned.

#### Author(s)

Ron Wehrens and Bjørn-Helge Mevik

#### References

Martens, H., Næs, T. (1989) Multivariate calibration. Chichester: Wiley.

#### See Also

```
mvr plsr pcr kernelpls.fit widekernelpls.fit simpls.fit
```

plot.mvr

Plot Method for MVR objects

#### **Description**

plot.mvr plots predictions, coefficients, scores, loadings, biplots, correlation loadings or validation plots (RMSEP curves, etc.).

# Usage

#### **Arguments**

x an object of class mvr. The fitted model to plot.

plottype character. What kind of plot to plot.

. . . further arguments, sent to the underlying plot functions.

pls.options 33

## **Details**

The function is simply a wrapper for the underlying plot functions used to make the selected plots. See predplot.mvr, validationplot, coefplot, scoreplot, loadingplot, biplot.mvr or corrplot for details. Note that all arguments except x and plottype must be named.

#### Value

plot.mvr returns whatever the underlying plot function returns.

# Author(s)

Ron Wehrens and Bjørn-Helge Mevik

#### See Also

mvr, predplot.mvr, validationplot, coefplot, scoreplot, loadingplot, biplot.mvr, corrplot

## **Examples**

```
data(yarn)
nir.pcr <- pcr(density ~ NIR, ncomp = 9, data = yarn, validation = "CV")
## Not run:
plot(nir.pcr, ncomp = 5) # Plot of cross-validated predictions
plot(nir.pcr, "scores") # Score plot
plot(nir.pcr, "loadings", comps = 1:3) # The three first loadings
plot(nir.pcr, "coef", ncomp = 5) # Coefficients
plot(nir.pcr, "val") # RMSEP curves
plot(nir.pcr, "val", val.type = "MSEP", estimate = "CV") # CV MSEP
## End(Not run)</pre>
```

pls.options

Set or return options for the pls package

# Description

A function to set options for the **pls** package, or to return the current options.

#### **Usage**

```
pls.options(...)
```

# Arguments

a single list, a single character vector, or any number of named arguments (name = value).

34 pls.options

#### **Details**

If called with no arguments, or with an empty list as the single argument, pls.options returns the current options.

If called with a character vector as the single argument, a list with the arguments named in the vector are returned.

If called with a non-empty list as the single argument, the list elements should be named, and are treated as named arguments to the function.

Otherwise, pls.options should be called with one or more named arguments *name* = *value*. For each argument, the option named *name* will be given the value *value*.

The recognised options are:

**mvralg** The fit method to use in mvr and mvrCv. The value should be one of the allowed methods. Defaults to "kernelpls". Can be overridden with the argument method in mvr and mvrCv.

**pcralg** The fit method to use in pcr. The value should be one of the allowed methods. Defaults to "svdpc". Can be overridden with the argument method in pcr.

**plsralg** The fit method to use in plsr. The value should be one of the allowed methods. Defaults to "kernelpls". Can be overridden with the argument method in plsr.

**cpplsalg** The fit method to use in cppls. The value should be one of the allowed methods. Defaults to "cppls". Can be overridden with the argument method in cppls.

**parallel** Specification of how the cross-validation (CV) in mvr should be performed. If the specification is NULL (default) or 1, the CV is done serially, otherwise it is done in parallel using functionality from the parallel package.

If it is an integer greater than 1, the CV is done in parallel with the specified number of processes, using mclapply.

If it is a cluster object created by makeCluster, the CV is done in parallel on that cluster, using parLapply. The user should stop the cluster herself when it is no longer needed, using stopCluster.

Finally, if the specification is an unevaluated call to makeCluster, the call is evaluated, and the CV is done in parallel on the resulting cluster, using parLapply. In this case, the cluster will be stopped (with stopCluster) after the CV. Thus, in the final case, the cluster is created and destroyed for each CV, just like when using mclapply.

**w.tol** The tolerance used for removing values close to 0 in the vectors of loading weights in cppls. Defaults to .Machine\$double.eps.

**X.tol** The tolerance used for removing predictor variables with L1 norms close to 0 in cppls. Defaults to 10^-12.

#### Value

A list with the (possibly changed) options. If any named argument (or list element) was provided, the list is returned invisibly.

#### Note

The function is a slight modification of the function sm. options from the package sm.

predict.mvr 35

## Author(s)

Bjørn-Helge Mevik and Ron Wehrens

# **Examples**

```
## Return current options:
pls.options()
pls.options("plsralg")
pls.options(c("plsralg", "pcralg"))

## Set options:
pls.options(plsralg = "simpls", mvralg = "simpls")
pls.options(list(plsralg = "simpls", mvralg = "simpls")) # Equivalent
pls.options()

## Restore `factory settings':
rm(.pls.Options)
pls.options()
```

predict.mvr

Predict Method for PLSR and PCR

# Description

Prediction for mvr (PCR, PLSR) models. New responses or scores are predicted using a fitted model and a new matrix of observations.

# Usage

## **Arguments**

object	an mvr object. The fitted model
newdata	a data frame. The new data. If missing, the training data is used.
ncomp, comps	vector of positive integers. The components to use in the prediction. See below.
type	character. Whether to predict scores or response values
na.action	function determining what should be done with missing values in newdata. The default is to predict NA. See na.omit for alternatives.
	further arguments. Currently not used

36 predict.mvr

#### **Details**

When type is "response" (default), predicted response values are returned. If comps is missing (or is NULL), predictions for length(ncomp) models with ncomp[1] components, ncomp[2] components, etc., are returned. Otherwise, predictions for a single model with the exact components in comps are returned. (Note that in both cases, the intercept is always included in the predictions. It can be removed by subtracting the Ymeans component of the fitted model.)

When type is "scores", predicted score values are returned for the components given in comps. If comps is missing or NULL, ncomps is used instead.

It is also possible to supply a matrix instead of a data frame as newdata, which is then assumed to be the X data matrix. Note that the usual checks for the type of the data are then omitted. Also note that this is *only* possible with predict; it will not work in functions like predplot, RMSEP or R2, because they also need the response variable of the new data.

#### Value

When type is "response", a three dimensional array of predicted response values is returned. The dimensions correspond to the observations, the response variables and the model sizes, respectively.

When type is "scores", a score matrix is returned.

#### Note

A warning message like ''newdata' had 10 rows but variable(s) found have 106 rows' means that not all variables were found in the newdata data frame. This (usually) happens if the formula contains terms like yarn\$NIR. Do not use such terms; use the data argument instead. See mvr for details.

#### Author(s)

Ron Wehrens and Bjørn-Helge Mevik

#### See Also

```
mvr, summary.mvr, coef.mvr, plot.mvr
```

# **Examples**

```
data(yarn)
nir.mvr <- mvr(density ~ NIR, ncomp = 5, data = yarn[yarn$train,])
## Predicted responses for models with 1, 2, 3 and 4 components
pred.resp <- predict(nir.mvr, ncomp = 1:4, newdata = yarn[!yarn$train,])
## Predicted responses for a single model with components 1, 2, 3, 4
predict(nir.mvr, comps = 1:4, newdata = yarn[!yarn$train,])
## Predicted scores
predict(nir.mvr, comps = 1:3, type = "scores", newdata = yarn[!yarn$train,])</pre>
```

predplot 37

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# **Description**

Functions to plot predicted values against measured values for a fitted model.

# Usage

# **Arguments**

object	a fitted model.
ncomp	integer vector. The model sizes (numbers of components) to use for prediction.
which	character vector. Which types of predictions to plot. Should be a subset of c("train", "validation", "test"). If not specified, plot.mvr selects test set predictions if newdata is supplied, otherwise cross-validated predictions if the model has been cross-validated, otherwise fitted values from the calibration data.
newdata	data frame. New data to predict.
nCols, nRows	integer. The number of coloumns and rows the plots will be laid out in. If not specified, plot.mvr tries to be intelligent.
xlab,ylab	titles for $x$ and $y$ axes. Typically character strings, but can be expressions or lists. See title for details.
labels	optional. Alternative plot labels to use. Either a vector of labels, or "names" or "numbers" to use the row names or row numbers of the data as labels.
type	character. What type of plot to make. Defaults to "p" (points). See plot for a complete list of types. The argument is ignored if labels is specified.
main	optional main title for the plot. See Details.
ask	logical. Whether to ask the user before each page of a plot.
font.main	font to use for main titles. See par for details. Also see Details below.
cex.main	numeric. The magnification to be used for main titles relative to the current size. Also see Details below.

38 predplot

x numeric vector. The observed response values.
 y numeric vector. The predicted response values.
 logical. Whether a target line should be drawn.

line.col, line.lty, line.lwd

character or numeric. The col, 1ty and 1wd parametres for the target line. See

par for details.

... further arguments sent to underlying plot functions.

#### **Details**

predplot is a generic function for plotting predicted versus measured response values, with default and mvr methods currently implemented. The default method is very simple, and doesn't handle multiple responses or new data.

The mvr method, handles multiple responses, model sizes and types of predictions by making one plot for each combination. It can also be called through the plot method for mvr, by specifying plottype = "prediction" (the default).

The argument main can be used to specify the main title of the plot. It is handled in a non-standard way. If there is only on (sub) plot, main will be used as the main title of the plot. If there is *more* than one (sub) plot, however, the presence of main will produce a corresponding 'global' title on the page. Any graphical parametres, e.g., cex.main, supplied to coefplot will only affect the 'ordinary' plot titles, not the 'global' one. Its appearance can be changed by setting the parameters with par, which will affect *both* titles (with the exception of font.main and cex.main, which will only affect the 'global' title when there is more than one plot). (To have different settings for the two titles, one can override the par settings with arguments to predplot.)

predplotXy is an internal function and is not meant for interactive use. It is called by the predplot methods, and its arguments, e.g, line, can be given in the predplot call.

## Value

The functions invisibly return a matrix with the (last) plotted data.

#### Note

The font.main and cex.main must be (completely) named. This is to avoid that any argument cex or font matches them.

Tip: If the labels specified with labels are too long, they get clipped at the border of the plot region. This can be avoided by supplying the graphical parameter xpd = TRUE in the plot call.

## Author(s)

Ron Wehrens and Bjørn-Helge Mevik

#### See Also

```
mvr, plot.mvr
```

scoreplot 39

## **Examples**

scoreplot

Plots of Scores, Loadings and Correlation Loadings

## **Description**

Functions to make scatter plots of scores or correlation loadings, and scatter or line plots of loadings.

## Usage

```
scoreplot(object, ...)
## Default S3 method:
scoreplot(object, comps = 1:2, labels, identify = FALSE, type = "p",
          xlab, ylab, ...)
## S3 method for class 'scores'
plot(x, ...)
loadingplot(object, ...)
## Default S3 method:
loadingplot(object, comps = 1:2, scatter = FALSE, labels,
            identify = FALSE, type, lty, lwd = NULL, pch, cex = NULL,
            col, legendpos, xlab, ylab, pretty.xlabels = TRUE, xlim, ...)
## S3 method for class 'loadings'
plot(x, ...)
corrplot(object, comps = 1:2, labels, plotx = TRUE, ploty = FALSE,
         radii = c(sqrt(1/2), 1), identify = FALSE, type = "p",
         xlab, ylab, col, ...)
```

## **Arguments**

```
object an R object. The fitted model.

comps integer vector. The components to plot.
```

40 scoreplot

scatter	logical. Whether the loadings should be plotted as a scatter instead of as lines.
labels	optional. Alternative plot labels or $x$ axis labels. See Details.
plotx	locical. Whether to plot the $X$ correlation loadings. Defaults to TRUE.
ploty	locical. Whether to plot the $Y$ correlation loadings. Defaults to FALSE.
radii	numeric vector, giving the radii of the circles drawn in corrplot. The default radii represent $50\%$ and $100\%$ explained variance of the $X$ variables by the chosen components.
identify	logical. Whether to use identify to interactively identify points. See below.
type	character. What type of plot to make. Defaults to "p" (points) for scatter plots and "1" (lines) for line plots. See plot for a complete list of types (not all types are possible/meaningful for all plots).
lty	vector of line types (recycled as neccessary). Line types can be specified as integers or character strings (see par for the details).
lwd	vector of positive numbers (recycled as neccessary), giving the width of the lines.
pch	plot character. A character string or a vector of single characters or integers (recycled as neccessary). See points for all alternatives.
cex	numeric vector of character expansion sizes (recycled as neccessary) for the plotted symbols.
col	character or integer vector of colors for plotted lines and symbols (recycled as neccessary). See par for the details.
legendpos	Legend position. Optional. Ignored if scatter is TRUE. If present, a legend is drawn at the given position. The position can be specified symbolically (e.g., legendpos = "topright"). This requires $R >= 2.1.0$ . Alternatively, the position can be specified explicitly (legendpos = $t(c(x,y))$ ) or interactively (legendpos = $locator()$ ).
xlab,ylab	titles for $x$ and $y$ axes. Typically character strings, but can be expressions or lists. See title for details.
pretty.xlabels	logical. If TRUE, loadingplot tries to plot the $\boldsymbol{x}$ labels more nicely. See Details.
xlim	optional vector of length two, with the $x$ limits of the plot.
X	a scores or loadings object. The scores or loadings to plot.
• • •	further arguments sent to the underlying plot function(s).

## **Details**

plot. scores is simply a wrapper calling scoreplot, passing all arguments. Similarly for plot.loadings.

scoreplot is generic, currently with a default method that works for matrices and any object for which scores returns a matrix. The default scoreplot method makes one or more scatter plots of the scores, depending on how many components are selected. If one or two components are selected, and identify is TRUE, the function identify is used to interactively identify points.

Also loadingplot is generic, with a default method that works for matrices and any object where loadings returns a matrix. If scatter is TRUE, the default method works exactly like the default scoreplot method. Otherwise, it makes a lineplot of the selected loading vectors, and if identify

scoreplot 41

is TRUE, uses identify to interactively identify points. Also, if legendpos is given, a legend is drawn at the position indicated.

corrplot works exactly like the default scoreplot method, except that at least two components must be selected. The "correlation loadings", i.e. the correlations between each variable and the selected components (see References), are plotted as pairwise scatter plots, with concentric circles of radii given by radii. Each point corresponds to a variable. The squared distance between the point and origin equals the fraction of the variance of the variable explained by the components in the panel. The default radii corresponds to 50% and 100% explained variance. By default, only the correlation loadings of the X variables are plotted, but if ploty is TRUE, also the Y correlation loadings are plotted.

scoreplot, loadingplot and corrplot can also be called through the plot method for mvr objects, by specifying plottype as "scores", "loadings" or "correlation", respectively. See plot.mvr.

The argument labels can be a vector of labels or one of "names" and "numbers".

If a scatter plot is produced (i.e., scoreplot, corrplot, or loadingplot with scatter = TRUE), the labels are used instead of plot symbols for the points plotted. If labels is "names" or "numbers", the row names or row numbers of the matrix (scores, loadings or correlation loadings) are used.

If a line plot is produced (i.e., loadingplot), the labels are used as x axis labels. If labels is "names" or "numbers", the variable names are used as labels, the difference being that with "numbers", the variable names are converted to numbers, if possible. Variable names of the forms "number" or "number text" (where the space is optional), are handled.

The argument pretty.xlabels is only used when labels is specified for a line plot. If TRUE (default), the code tries to use a 'pretty' selection of labels. If labels is "numbers", it also uses the numerical values of the labels for horisontal spacing. If one has excluded parts of the spectral region, one might therefore want to use pretty.xlabels = FALSE.

#### Value

The functions return whatever the underlying plot function (or identify) returns.

## Note

legend has many options. If you want greater control over the appearance of the legend, omit the legendpos argument and call legend manually.

Graphical parametres (such as pch and cex) can also be used with scoreplot and corrplot. They are not listed in the argument list simply because they are not handled specifically in the function (unlike in loadingplot), but passed directly to the underlying plot functions by . . . .

Tip: If the labels specified with labels are too long, they get clipped at the border of the plot region. This can be avoided by supplying the graphical parameter xpd = TRUE in the plot call.

The handling of labels and pretty.xlabels in coefplot is experimental.

#### Author(s)

Ron Wehrens and Bjørn-Helge Mevik

42 scores

## References

Martens, H., Martens, M. (2000) Modified Jack-knife Estimation of Parameter Uncertainty in Bilinear Modelling by Partial Least Squares Regression (PLSR). *Food Quality and Preference*, **11**(1–2), 5–16.

#### See Also

```
mvr, plot.mvr, scores, loadings, identify, legend
```

# **Examples**

```
data(yarn)
mod <- plsr(density ~ NIR, ncomp = 10, data = yarn)
## These three are equivalent:
## Not run:
scoreplot(mod, comps = 1:5)
plot(scores(mod), comps = 1:5)
plot(mod, plottype = "scores", comps = 1:5)

loadingplot(mod, comps = 1:5)
loadingplot(mod, comps = 1:5, legendpos = "topright") # With legend
loadingplot(mod, comps = 1:5, scatter = TRUE) # Plot as scatterplots

corrplot(mod, comps = 1:2)
corrplot(mod, comps = 1:3)
## End(Not run)</pre>
```

scores

Extract Scores and Loadings from PLSR and PCR Models

## **Description**

These functions extract score and loading matrices from fitted mvr models.

# Usage

```
scores(object, ...)
## Default S3 method:
scores(object, ...)

loadings(object, ...)
## Default S3 method:
loadings(object, ...)

loading.weights(object)

Yscores(object)

Yloadings(object)
```

selectNcomp 43

## Arguments

```
object a fitted model to extract from.
... extra arguments, currently not used.
```

#### **Details**

All functions extract the indicated matrix from the fitted model, and will work with any object having a suitably named component.

The default scores and loadings methods also handle prcomp objects (their scores and loadings components are called x and rotation, resp.), and add an attribute "explvar" with the variance explained by each component, if this is available. (See explvar for details.)

#### Value

A matrix with scores or loadings.

#### Note

There is a loadings function in package **stats**. It simply returns any element named "loadings". See loadings for details. The function can be accessed as stats::loadings(...).

# Author(s)

Ron Wehrens and Bjørn-Helge Mevik

# See Also

```
mvr, coef.mvr
```

## **Examples**

```
data(yarn)
plsmod <- plsr(density ~ NIR, 6, data = yarn)
scores(plsmod)
loadings(plsmod)[,1:4]</pre>
```

selectNcomp

Suggestions for the optimal number of components in PCR and PLSR models

# **Description**

Choosing the best number of components in PCR and PLSR models is difficult and usually done on the basis of visual inspection of the validation plots. In cases where large numbers of models are built this choice needs to be automated. This function implements two proposals, one based on randomization (permutation) testing, and an approach based on the standard error of the cross-validation residuals.

44 selectNcomp

#### Usage

```
selectNcomp(object, method = c("randomization", "onesigma"),
           nperm = 999, alpha = 0.01, ncomp = object$ncomp,
           plot = FALSE, ...)
```

## **Arguments**

object an myr object. The fitted model. It should contain a validation element. method character string, indicating the heuristic to use. nperm number of permutations in the "randomization" approach - not used in the "onesigma" approach. alpha cutoff for p values in the "randomization" approach - not used in the "one sigma" approach. ncomp maximum number of components to consider when determining the global minimum in the cross-validation curve. plot whether or not to show a cross-validation plot. The plot for the "randomization"

approach shows models that do not differ significantly from the global RMSEP minimum with open circles; the "onesigma" approach shows the one-sigma bands around the RMSEP values. In both cases, the selection is indicated with a blue dashed line.

Further plotting arguments, e.g., to add a title to the plot, or to limit the plotting

range.

## **Details**

In both approaches the results of cross-validation are used, so the model should have been calculated with some form of cross-validation. First, the absolute minimum in the CV curve is determined (considering only the first noomp components), leading to the reference model. The randomization test approach (Van der Voet, 1994) checks whether the squared prediction errors of models with fewer components are significantly larger than in the reference model. This leads for each model considered to a p value; the smallest model not significantly worse than the reference model is returned as the selected one.

The approach "onesigma" simply returns the first model where the optimal CV is within one standard error of the absolute optimum (Hastie, Tibshirani and Friedman, 2009). Note that here we simply use the standard deviation of the cross-validation residuals, in line with the procedure used to calculate the error measure itself. Some other packages implementing similar procedures (such as glmnet) calculate an error measure for each validation segment separately and use the average as the final estimate. In such cases the standard error across segments is the relevant measure of spread. For LOO, the two procedures are identical. In other forms of validation, small differences will occur.

#### Value

A number indicating the suggested number of components in the model.

simpls.fit 45

#### Author(s)

Ron Wehrens, Hilko van der Voet and Gerie van der Heijden

#### References

Van der Voet, H. (1994) Comparing the predictive accuracy of models using a simple randomization test. Chemom. Intell. Lab. Syst. 25 (2), 313-323

Hastie, T., Friedman, J. and Tibshirani, R. The Elements of Statistical Learning: data mining, inference, and prediction, Springer (2013), 10th printing with corrections, paragraph 7.10.

#### See Also

```
mvr, summary.mvr
```

# **Examples**

simpls.fit

Sijmen de Jong's SIMPLS

## **Description**

Fits a PLSR model with the SIMPLS algorithm.

#### Usage

```
simpls.fit(X, Y, ncomp, center = TRUE, stripped = FALSE, ...)
```

## **Arguments**

Χ	a matrix of observations. NAs and Infs are not allowed.
Υ	a vector or matrix of responses. NAs and Infs are not allowed. $% \label{eq:continuous}%$

ncomp the number of components to be used in the modelling.

center logical, determines if the X and Y matrices are mean centered or not. Default

is to perform mean centering.

stripped logical. If TRUE the calculations are stripped as much as possible for speed; this

is meant for use with cross-validation or simulations when only the coefficients

are needed. Defaults to FALSE.

... other arguments. Currently ignored.

46 simpls.fit

#### **Details**

This function should not be called directly, but through the generic functions plsr or mvr with the argument method="simpls". SIMPLS is much faster than the NIPALS algorithm, especially when the number of X variables increases, but gives slightly different results in the case of multivariate Y. SIMPLS truly maximises the covariance criterion. According to de Jong, the standard PLS2 algorithms lie closer to ordinary least-squares regression where a precise fit is sought; SIMPLS lies closer to PCR with stable predictions.

#### Value

A list containing the following components is returned:

coefficients an array of regression coefficients for 1, ..., ncomp components. The dimen-

sions of coefficients are c(nvar, npred, ncomp) with nvar the number of X

variables and npred the number of variables to be predicted in Y.

scores a matrix of scores.

loadings a matrix of loadings.

Yscores a matrix of Y-scores.

Yloadings a matrix of Y-loadings.

projection the projection matrix used to convert X to scores.

Xmeans a vector of means of the X variables.

Ymeans a vector of means of the Y variables.

fitted.values an array of fitted values. The dimensions of fitted.values are c(nobj, npred, ncomp)

with nobj the number samples and npred the number of Y variables.

residuals an array of regression residuals. It has the same dimensions as fitted.values.

Xvar a vector with the amount of X-variance explained by each component.

Xtotvar Total variance in X.

If stripped is TRUE, only the components coefficients, Xmeans and Ymeans are returned.

## Author(s)

Ron Wehrens and Bjørn-Helge Mevik

## References

de Jong, S. (1993) SIMPLS: an alternative approach to partial least squares regression. *Chemometrics and Intelligent Laboratory Systems*, **18**, 251–263.

#### See Also

mvr plsr pcr kernelpls.fit widekernelpls.fit oscorespls.fit

stdize 47

stdize	Standardization of Data Matrices	

## **Description**

Performs standardization (centering and scaling) of a data matrix.

# Usage

```
stdize(x, center = TRUE, scale = TRUE)
## S3 method for class 'stdized'
predict(object, newdata, ...)
## S3 method for class 'stdized'
makepredictcall(var, call)
```

#### Arguments

x, newdata	numeric matrices. The data to standardize.
center	logical value or numeric vector of length equal to the number of coloumns of x.
scale	logical value or numeric vector of length equal to the number of coloumns of x.
object	an object inheriting from class "stdized", normally the result of a call to stdize.
var	A variable.
call	The term in the formula, as a call.
	other arguments. Currently ignored.

## **Details**

makepredictcall.stdized is an internal utility function; it is not meant for interactive use. See makepredictcall for details.

If center is TRUE, x is centered by subtracting the coloumn mean from each coloumn. If center is a numeric vector, it is used in place of the coloumn means.

If scale is TRUE, x is scaled by dividing each coloumn by its sample standard deviation. If scale is a numeric vector, it is used in place of the standard deviations.

## Value

Both stdize and predict.stdized return a scaled and/or centered matrix, with attributes "stdized:center" and/or "stdized:scale" the vector used for centering and/or scaling. The matrix is given class c("stdized", "matrix").

#### Note

stdize is very similar to scale. The difference is that when scale = TRUE, stdize divides the coloumns by their standard deviation, while scale uses the root-mean-square of the coloumns. If center is TRUE, this is equivalent, but in general it is not.

48 summary.mvr

#### Author(s)

Bjørn-Helge Mevik and Ron Wehrens

#### See Also

```
mvr, pcr, plsr, msc, scale
```

## **Examples**

```
data(yarn)
## Direct standardization:
Ztrain <- stdize(yarn$NIR[yarn$train,])
Ztest <- predict(Ztrain, yarn$NIR[!yarn$train,])

## Used in formula:
mod <- plsr(density ~ stdize(NIR), ncomp = 6, data = yarn[yarn$train,])
pred <- predict(mod, newdata = yarn[!yarn$train,]) # Automatically standardized</pre>
```

summary.mvr

Summary and Print Methods for PLSR and PCR objects

## Description

Summary and print methods for mvr and mvrVal objects.

#### Usage

# Arguments

```
x, object an mvr object
what one of "all", "validation" or "training"
digits integer. Minimum number of significant digits in the output. Default is 4.
print.gap Integer. Gap between coloumns of the printed tables.
... Other arguments sent to underlying methods.
```

#### **Details**

If what is "training", the explained variances are given; if it is "validation", the cross-validated RMSEPs (if available) are given; if it is "all", both are given.

svdpc.fit 49

## Value

print.mvr and print.mvrVal return the object invisibly.

#### Author(s)

Ron Wehrens and Bjørn-Helge Mevik

#### See Also

```
mvr, pcr, plsr, RMSEP, MSEP
```

# Examples

```
data(yarn)
nir.mvr <- mvr(density ~ NIR, ncomp = 8, validation = "L00", data = yarn)
nir.mvr
summary(nir.mvr)
RMSEP(nir.mvr)</pre>
```

svdpc.fit

Principal Component Regression

# **Description**

Fits a PCR model using the singular value decomposition.

## Usage

```
svdpc.fit(X, Y, ncomp, center = TRUE, stripped = FALSE, ...)
```

other arguments. Currently ignored.

## **Arguments**

X a matrix of observations. NAs and Infs are not allowed.

Y a vector or matrix of responses. NAs and Infs are not allowed.

ncomp the number of components to be used in the modelling.

center logical, determines if the X and Y matrices are mean centered or not. Default is to perform mean centering.

stripped logical. If TRUE the calculations are stripped as much as possible for speed; this is meant for use with cross-validation or simulations when only the coefficients are needed. Defaults to FALSE.

## **Details**

This function should not be called directly, but through the generic functions pcr or mvr with the argument method="svdpc". The singular value decomposition is used to calculate the principal components.

50 validationplot

## Value

A list containing the following components is returned:

coefficients an array of regression coefficients for 1, ..., ncomp components. The dimen-

sions of coefficients are c(nvar, npred, ncomp) with nvar the number of X

variables and npred the number of variables to be predicted in Y.

scores a matrix of scores.

loadings a matrix of loadings.

Yloadings a matrix of Y-loadings.

projection the projection matrix used to convert X to scores.

Xmeans a vector of means of the X variables.

Ymeans a vector of means of the Y variables.

fitted.values an array of fitted values. The dimensions of fitted.values are c(nobj,npred,ncomp)

with nobj the number samples and npred the number of Y variables.

residuals an array of regression residuals. It has the same dimensions as fitted.values.

Xvar a vector with the amount of X-variance explained by each component.

Xtotvar Total variance in X.

If stripped is TRUE, only the components coefficients, Xmeans and Ymeans are returned.

## Author(s)

Ron Wehrens and Bjørn-Helge Mevik

#### References

Martens, H., Næs, T. (1989) Multivariate calibration. Chichester: Wiley.

## See Also

mvr plsr pcr cppls

validationplot Validation Plots

## Description

Functions to plot validation statistics, such as RMSEP or  $\mathbb{R}^2$ , as a function of the number of components.

validationplot 51

# Usage

# **Arguments**

8	
object	an mvr object.
val.type	character. What type of validation statistic to plot.
estimate	character. Which estimates of the statistic to calculate. See RMSEP.
newdata	data frame. Optional new data used to calculate statistic.
ncomp, comps	integer vector. The model sizes to compute the statistic for. See RMSEP.
intercept	logical. Whether estimates for a model with zero components should be calculated as well.
x	an mvrVal object. Usually the result of a RMSEP, MSEP or R2 call.
nCols, nRows	integers. The number of coloumns and rows the plots will be laid out in. If not specified, plot.mvrVal tries to be intelligent.
type	character. What type of plots to create. Defaults to "1" (lines). Alternative types include "p" (points) and "b" (both). See plot for a complete list of types.
lty	vector of line types (recycled as neccessary). Line types can be specified as integers or character strings (see par for the details).
lwd	vector of positive numbers (recycled as neccessary), giving the width of the lines.
pch	plot character. A character string or a vector of single characters or integers (recycled as neccessary). See points for all alternatives.
cex	numeric vector of character expansion sizes (recycled as neccessary) for the plotted symbols.
col	character or integer vector of colors for plotted lines and symbols (recycled as neccessary). See par for the details.
legendpos	Legend position. Optional. If present, a legend is drawn at the given position. The position can be specified symbolically (e.g., legendpos = "topright"). This requires $R >= 2.1.0$ . Alternatively, the position can be specified explicitly (legendpos = $t(c(x,y))$ ) or interactively (legendpos = $locator()$ ). This only works well for plots of single-response models.
xlab,ylab	titles for $x$ and $y$ axes. Typically character strings, but can be expressions (e.g., expression(R^2) or lists. See title for details.
main	optional main title for the plot. See Details.
ask	logical. Whether to ask the user before each page of a plot.

Further arguments sent to underlying plot functions.

52 validationplot

#### **Details**

validationplot calls the proper validation function (currently MSEP, RMSEP or R2) and plots the results with plot.mvrVal. validationplot can be called through the mvr plot method, by specifying plottype = "validation".

plot.mvrVal creates one plot for each response variable in the model, laid out in a rectangle. It uses matplot for performing the actual plotting. If legendpos is given, a legend is drawn at the given position.

The argument main can be used to specify the main title of the plot. It is handled in a non-standard way. If there is only on (sub) plot, main will be used as the main title of the plot. If there is *more* than one (sub) plot, however, the presence of main will produce a corresponding 'global' title on the page. Any graphical parametres, e.g., cex.main, supplied to coefplot will only affect the 'ordinary' plot titles, not the 'global' one. Its appearance can be changed by setting the parameters with par, which will affect *both* titles. (To have different settings for the two titles, one can override the par settings with arguments to the plot function.)

#### Note

legend has many options. If you want greater control over the appearance of the legend, omit the legendpos argument and call legend manually.

#### Author(s)

Ron Wehrens and Bjørn-Helge Mevik

#### See Also

```
mvr, plot.mvr, RMSEP, MSEP, R2, matplot, legend
```

## **Examples**

```
data(oliveoil)
mod <- plsr(sensory ~ chemical, data = oliveoil, validation = "L00")
## Not run:
## These three are equivalent:
validationplot(mod, estimate = "all")
plot(mod, "validation", estimate = "all")
plot(RMSEP(mod, estimate = "all"))
## Plot R2:
plot(mod, "validation", val.type = "R2")
## Plot R2, with a legend:
plot(mod, "validation", val.type = "MSEP", legendpos = "top") # R >= 2.1.0
## End(Not run)
```

var.jack 53

var.jack	Jackknife Variance Estimates of Regression Coefficients	
· ·	• • • • • • • • • • • • • • • • • • •	

#### **Description**

Calculates jackknife variance or covariance estimates of regression coefficients.

#### Usage

```
var.jack(object, ncomp = object$ncomp, covariance = FALSE, use.mean = TRUE)
```

## Arguments

object an mvr object. A cross-validated model fitted with jackknife = TRUE.

ncomp the number of components to use for estimating the (co)variances

covariance logical. If TRUE, covariances are calculated; otherwise only variances. The default is FALSE.

use.mean logical. If TRUE (default), the mean coefficients are used when estimating the (co)variances; otherwise the coefficients from a model fitted to the entire data

set. See Details.

## **Details**

The original (Tukey) jackknife variance estimator is defined as  $(g-1)/g\sum_{i=1}^g (\tilde{\beta}_{-i} - \bar{\beta})^2$ , where g is the number of segments,  $\tilde{\beta}_{-i}$  is the estimated coefficient when segment i is left out (called the jackknife replicates), and  $\bar{\beta}$  is the mean of the  $\tilde{\beta}_{-i}$ . The most common case is delete-one jackknife, with g=n, the number of observations.

This is the definition var. jack uses by default.

However, Martens and Martens (2000) defined the estimator as  $(g-1)/g\sum_{i=1}^g (\tilde{\beta}_{-i}-\hat{\beta})^2$ , where  $\hat{\beta}$  is the coefficient estimate using the entire data set. I.e., they use the original fitted coefficients instead of the mean of the jackknife replicates. Most (all?) other jackknife implementations for PLSR use this estimator. var. jack can be made to use this definition with use.mean = FALSE. In practice, the difference should be small if the number of observations is sufficiently large. Note, however, that all theoretical results about the jackknife refer to the 'proper' definition. (Also note that this option might disappear in a future version.)

#### Value

If covariance is FALSE, an  $p \times q \times c$  array of variance estimates, where p is the number of predictors, q is the number of responses, and c is the number of components.

If covariance id TRUE, an  $pq \times pq \times c$  array of variance-covariance estimates.

54 widekernelpls.fit

## Warning

Note that the Tukey jackknife variance estimator is not unbiased for the variance of regression coefficients (Hinkley 1977). The bias depends on the X matrix. For ordinary least squares regression (OLSR), the bias can be calculated, and depends on the number of observations n and the number of parameters k in the mode. For the common case of an orthogonal design matrix with  $\pm 1$  levels, the delete-one jackknife estimate equals (n-1)/(n-k) times the classical variance estimate for the regression coefficients in OLSR. Similar expressions hold for delete-d estimates. Modifications have been proposed to reduce or eliminate the bias for the OLSR case, however, they depend on the number of parameters used in the model. See e.g. Hinkley (1977) or Wu (1986).

Thus, the results of var. jack should be used with caution.

#### Author(s)

Bjørn-Helge Mevik

#### References

Tukey J.W. (1958) Bias and Confidence in Not-quite Large Samples. (Abstract of Preliminary Report). *Annals of Mathematical Statistics*, **29**(2), 614.

Martens H. and Martens M. (2000) Modified Jack-knife Estimation of Parameter Uncertainty in Bilinear Modelling by Partial Least Squares Regression (PLSR). *Food Quality and Preference*, **11**, 5–16.

Hinkley D.V. (1977), Jackknifing in Unbalanced Situations. Technometrics, 19(3), 285–292.

Wu C.F.J. (1986) Jackknife, Bootstrap and Other Resampling Methods in Regression Analysis. *Te Annals of Statistics*, **14**(4), 1261–1295.

#### See Also

```
mvrCv, jack.test
```

## **Examples**

widekernelpls.fit

Wide Kernel PLS (Rännar et al.)

## Description

Fits a PLSR model with the wide kernel algorithm.

widekernelpls.fit 55

#### Usage

## **Arguments**

X a matrix of observations. NAs and Infs are not allowed.

Y a vector or matrix of responses. NAs and Infs are not allowed.

ncomp the number of components to be used in the modelling.

center logical, determines if the X and Y matrices are mean centered or not. Default

is to perform mean centering.

stripped logical. If TRUE the calculations are stripped as much as possible for speed; this

is meant for use with cross-validation or simulations when only the coefficients

are needed. Defaults to FALSE.

tol numeric. The tolerance used for determining convergence in the algorithm.

maxit positive integer. The maximal number of iterations used in the internal Eigen-

vector calculation.

... other arguments. Currently ignored.

#### **Details**

This function should not be called directly, but through the generic functions plsr or mvr with the argument method="widekernelpls". The wide kernel PLS algorithm is efficient when the number of variables is (much) larger than the number of observations. For very wide X, for instance 12x18000, it can be twice as fast as kernelpls.fit and simpls.fit. For other matrices, however, it can be much slower. The results are equal to the results of the NIPALS algorithm.

## Value

A list containing the following components is returned:

coefficients an array of regression coefficients for 1, ..., ncomp components. The dimen-

sions of coefficients are c(nvar, npred, ncomp) with nvar the number of X

variables and npred the number of variables to be predicted in Y.

scores a matrix of scores.

loadings a matrix of loadings.

loading.weights

a matrix of loading weights.

Yscores a matrix of Y-scores.
Yloadings a matrix of Y-loadings.

projection the projection matrix used to convert X to scores.

Xmeans a vector of means of the X variables.

Ymeans a vector of means of the Y variables.

56 yarn

fitted.values an array of fitted values. The dimensions of fitted.values are c(nobj, npred, ncomp)

with nobj the number samples and npred the number of Y variables.

residuals an array of regression residuals. It has the same dimensions as fitted.values.

Xvar a vector with the amount of X-variance explained by each component.

Xtotvar Total variance in X.

If stripped is TRUE, only the components coefficients, Xmeans and Ymeans are returned.

## Note

The current implementation has not undergone extensive testing yet, and should perhaps be regarded as experimental. Specifically, the internal Eigenvector calculation does not always converge in extreme cases where the Eigenvalue is close to zero. However, when it does converge, it always converges to the same results as kernelpls.fit, up to numerical inacurracies.

The algorithm also has a bit of overhead, so when the number of observations is moderately high, kernelpls.fit can be faster even if the number of predictors is much higher. The relative speed of the algorithms can also depend greatly on which BLAS and/or LAPACK library R is linked against.

#### Author(s)

Bjørn-Helge Mevik

# References

Rännar, S., Lindgren, F., Geladi, P. and Wold, S. (1994) A PLS Kernel Algorithm for Data Sets with Many Variables and Fewer Objects. Part 1: Theory and Algorithm. *Journal of Chemometrics*, **8**, 111–125.

#### See Also

mvr plsr cppls pcr kernelpls.fit simpls.fit oscorespls.fit

yarn NIR spectra and density measurements of PET yarns

# Description

A training set consisting of 21 NIR spectra of PET yarns, measured at 268 wavelengths, and 21 corresponding densities. A test set of 7 samples is also provided. Many thanks to Erik Swierenga.

#### Usage

yarn

yarn 57

# **Format**

A data frame with components

NIR Numeric matrix of NIR measurements

density Numeric vector of densities

train Logical vector with TRUE for the training samples and FALSE for the test samples

# Source

Swierenga H., de Weijer A. P., van Wijk R. J., Buydens L. M. C. (1999) Strategy for constructing robust multivariate calibration models *Chemometrics and Intelligent Laboratoryy Systems*, **49**(1), 1–17.

# **Index**

* classification	summary.mvr, 48
cppls.fit,8	svdpc.fit,49
* datasets	validationplot, 50
gasoline, 15	widekernelpls.fit,54
mayonnaise, 19	* regression
oliveoil, 30	biplot.mvr, 2
yarn, <u>56</u>	coef.mvr,4
* hplot	coefplot, 6
biplot.mvr, 2	cppls.fit,8
coefplot, 6	crossval, 11
plot.mvr, 32	kernelpls.fit,18
predplot, 37	msc, 20
scoreplot, 39	mvr, 21
validationplot, $50$	mvrCv, 25
* htest	mvrVal, 28
jack.test, 16	oscorespls.fit,31
* models	plot.mvr, 32
cvsegments, 14	pls.options, 33
* multivariate	predict.mvr, 35
biplot.mvr, 2	predplot, 37
coef.mvr, 4	scoreplot, 39
coefplot, 6	scores, 42
cppls.fit,8	selectNcomp, 43
crossval, 11	simpls.fit,45
kernelpls.fit, 18	stdize, 47
msc, 20	summary.mvr, 48
mvr, 21	svdpc.fit,49
mvrCv, 25	validationplot, 50
mvrVal, 28	widekernelpls.fit,54
oscorespls.fit,31	* univar
plot.mvr, 32	var.jack,53
pls.options, 33	biplot.default, 3
predict.mvr, 35	biplot.mvr, 2, 33
predplot, 37	bipiot. iivi, 2, 33
scoreplot, 39	coef, 4, 5
scores, 42	coef.mvr, 4, 6, 8, 24, 36, 43
selectNcomp, 43	coefplot, 6, 33
simpls.fit, 45	compnames (coef.mvr), 4
stdize, 47	corrplot, 33
, · · ·	p 100, 00

INDEX 59

corrplot (scoreplot), 39	na.exclude, 22
cppls, 19, 34, 50, 56	na.fail, <u>22</u>
cppls (mvr), 21	na.omit, <i>5</i> , <i>22</i> , <i>35</i>
cppls.fit, 8, 22, 24	
crossval, 11, 23, 24, 26, 27, 30	oliveoil, 30
cvsegments, 12, 13, 14, 26, 27	options, <i>5</i> , <i>22</i>
	oscorespls.fit, 10, 19, 22, 24, 31, 46, 56
explvar, 43	
explvar (coef.mvr), 4	par, 7, 37, 38, 40, 51, 52
	parallel, <i>12</i> , <i>23</i> , <i>26</i> , <i>34</i>
fitted, 4, 5	parLapply, 34
fitted.mvr (coef.mvr), 4	pcr, 10, 19, 21, 32, 34, 46, 48–50, 56
	pcr (mvr), 21
gasoline, 15	plot, 6, 8, 37, 40, 51
	plot.loadings (scoreplot), 39
identify, 40-42	plot.mvr, 3, 8, 24, 32, 36, 38, 41, 42, 52
10 10 10 00 07 54	plot.mvrVal, 30
jack.test, 12, 13, 16, 26, 27, 54	plot.mvrVal(validationplot), 50
Leave 1-1- Cit 10 24 22 46 55 56	plot.scores (scoreplot), 39
kernelpls.fit, 18, 24, 32, 46, 55, 56	pls.options, 12, 23, 26, 33
legend, 8, 41, 42, 52	plsr, 10, 19, 21, 32, 34, 46, 48–50, 56
_	plsr (mvr), 21
1m, 22, 23	
loading.weights, 24	points, 7, 40, 51
loading.weights (scores), 42	predict.msc (msc), 20
loadingplot, 33	predict.mvr, 23, 24, 35
loadingplot (scoreplot), 39	predict.stdized(stdize),47
loadings, 5, 24, 40, 42, 43	prednames (coef.mvr), 4
loadings (scores), 42	predplot, 36, 37
locator, 7, 40, 51	predplot.mvr, 33
1 01 4 24	predplotXy (predplot), 37
makeCluster, 34	<pre>print.jacktest(jack.test), 16</pre>
makepredictcall, 20, 47	print.mvr(summary.mvr),48
makepredictcall.msc(msc), 20	<pre>print.mvrVal (summary.mvr), 48</pre>
makepredictcall.stdized(stdize),47	printCoefmat, <u>16</u>
matplot, 52	
mayonnaise, 19	R2, 24, 36, 51, 52
mclapply, 34	R2 (mvrVal), 28
model.frame, 5	residuals, 4, 5
<pre>model.frame.mvr (coef.mvr), 4</pre>	residuals.mvr(coef.mvr),4
model.matrix, 5	respnames (coef.mvr), 4
<pre>model.matrix.mvr (coef.mvr), 4</pre>	RMSEP, 24, 36, 49, 51, 52
msc, 20, 48	RMSEP (mvrVal), 28
MSEP, 13, 24, 27, 49, 51, 52	
MSEP (mvrVal), 28	scale, <i>47</i> , <i>48</i>
mvr, 3, 5, 8, 10, 13, 19, 21, 21, 27, 30, 32–34,	scoreplot, <i>33</i> , 39
36, 38, 42, 43, 45, 46, 48–50, 52, 56	scores, 5, 24, 40, 42, 42
mvrCv, 13, 17, 22-24, 25, 30, 34, 54	selectNcomp, 43
mvrVal, 28	simpls.fit, 10, 19, 24, 32, 45, 55, 56
mvrValstats (mvrVal), 28	sm.options, 34

INDEX

```
stdize, 21, 47

stopCluster, 34

summary.mvr, 36, 45, 48

svdpc.fit, 24, 49

title, 7, 37, 40, 51

validationplot, 30, 33, 50

var.jack, 12, 13, 16, 17, 26, 27, 53

widekernelpls.fit, 10, 19, 22, 24, 32, 46, 54

yarn, 56

Yloadings, 5

Yloadings (scores), 42

Yscores (scores), 42
```