## PrimeGrid's Generalized Cullen/Woodall Prime Search

On 21 August 2017, 14:51:43 UTC, PrimeGrid's Generalized Cullen/Woodall Prime Search found the largest known generalized Cullen prime:

$$
1341174^{*} 53^{1341174}+1
$$

Generalized Cullen numbers are of the form: $n^{*} b^{\wedge} n+1$. Generalized Cullen numbers that are prime are called generalized Cullen primes. For more information, please see "Cullen prime" in The Prime Glossary (http://primes.utm.edu/glossary).

The prime is $2,312,561$ digits long and enters Chris Caldwell's "The Largest Known Primes Database" (http://primes.utm.edu/primes) ranked $1^{\text {st }}$ for Generalized Cullen primes and $30^{\text {th }}$ overall.

The discovery was made by Hiroyuki Okazaki of Japan using an Intel(R) CPU @ 2.90 GHz with 16GB RAM, running Linux. This computer took about 12 hours and 39 minutes to complete the primality test using multithreaded LLR. Hiroyuki is a member of the Aggie The Pew team.

The prime was verified on 22 August 2017 17:24:17 UTC by user "wuzzat" of Australia using an Intel(R) Xeon(R) E5-2620 v3 CPU @ 2.40 GHz with 256GB RAM, running Microsoft Windows Server 2008R2. This computer took about 31 hours 41 minutes to complete the primality test using LLR. "wuzzat" is a member of the BOINC@AUSTRALIA team.

The credits for the discovery are as follows:

1. Hiroyuki Okazaki (Japan), discoverer
2. PrimeGrid, et al.
3. MultiSieve, sieve program developed by Mark Rodenkirch
4. gcwsieve, sieve program developed by Geoff Reynolds
5. LLR, primality program developed by Jean Penné

Entry in "The Largest Known Primes Database" can be found here:
http://primes.utm.edu/primes/page.php?id=123862
Base 53 was one of 14 prime-less generalized Cullen bases below $b=121$ that PrimeGrid is searching. The remaining bases are $13,25,29,41,47,49,55,69,73,101,109,116 \& 121$.

Using a single PC would have taken years to find this prime. So this timely discovery would not have been possible without the thousands of volunteers who contributed their spare CPU cycles. A special thanks to everyone who contributed their advice and/or computing power to the search especially all the sievers who work behind the scenes to make a find like this possible.

PrimeGrid's Generalized Cullen/Woodall Prime Search will continue seeking primes for other primeless bases. To join the search please visit PrimeGrid: http://www.primegrid.com

# PrimeGrid's Generalized Cullen/Woodall Prime Search 


#### Abstract

About PrimeGrid PrimeGrid is a distributed computing project, developed by Rytis Slatkevičius and currently administered by lain Bethune, James Breslin, Scott Brown, Ulrich Fries, Charley Gielkens, Michael Goetz, Roger Karpin, Rytis Slatkevičius, and Van Zimmerman.

PrimeGrid is hosted by Rackspace, and their generous contributions have helped make this project possible.

PrimeGrid utilizes BOINC and PRPNet to search for primes with the primary goal of bringing the excitement of prime finding to the "everyday" computer user. Simply download the software and let your computer do the rest. Participants can choose from a variety of prime forms to search. With a little patience, you may find a large or even record breaking prime.


## BOINC

The Berkeley Open Infrastructure for Network Computing (BOINC) is a software platform for distributed computing using volunteered computer resources. It allows users to participate in multiple distributed computing projects through a single program. Currently BOINC is being developed by a team based at the University of California, Berkeley led by David Anderson.

This platform currently supports projects from biology to math to astronomy. For more information, please visit BOINC: http://boinc.berkeley.edu

## PRPNet

PRPNet is a client/server application written by Mark Rodenkirch that is specifically designed to help find prime numbers of various forms. It is easily ported between various OS/hardware combinations. PRPNet does not run each PRP test itself, but relies on helper programs, such as LLR, PFGW, phrot, wwww, and genefer to do the work.

For more information, please visit PrimeGrid's PRPNet forum thread:
http://www.primegrid.com/forum_thread.php?id=1215
For more information about PrimeGrid and a complete list of available prime search projects, please visit: http://www.primegrid.com

