1 Computational epitope mapping of class I fusion proteins using Bayes classification 2 Marion F.S. Fischer^{1,2,*}, James E. Crowe, Jr.^{3,4,5}, and Jens Meiler^{1,2,6} 3 4 ¹ Department of Chemistry, Vanderbilt University, Nashville, Tennessee, United States of America 5 6 ² Center for Structural Biology, Vanderbilt University, Nashville, Tennessee, United States of 7 America 8 9 ³ Vanderbilt Vaccine Center, Vanderbilt University Medical Center, Nashville, Tennessee, United 10 States of America 11 12 ⁴ Department of Pediatrics, Vanderbilt University Medical Center, Nashville, Tennessee, United 13 States of America 14 ⁵ Department of Pathology, Microbiology and Immunology, Vanderbilt University Medical 15 16 Center, Nashville, Tennessee, United States of America 17 18 ⁶ Institute for Drug Discovery, Leipzig University Medical School, 04103, Leipzig, Saxony, 19 Germany 20 21 * Corresponding author

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Abstract

Antibody epitope mapping of viral proteins plays a vital role in understanding immune system mechanisms of protection. In the case of class I viral fusion proteins, recent advances in cryoelectron microscopy and protein stabilization techniques have highlighted the importance of cryptic or 'alternative' conformations that expose epitopes targeted by potent neutralizing antibodies. Thorough epitope mapping of such metastable conformations is difficult, but is critical for understanding sites of vulnerability in class I fusion proteins that occur as transient conformational states during viral attachment and fusion. We introduce a novel method Accelerated class I fusion protein Epitope Mapping (AxIEM) that accounts for fusion protein flexibility to significantly improve out-of-sample prediction of discontinuous antibody epitopes. Harnessing data from previous experimental epitope mapping efforts of several class I fusion proteins, we demonstrate that accuracy of epitope prediction depends on residue environment and allows for the precise prediction of conformation-dependent antibody target residues. We also show that AxIEM can to identify common epitopes and provide structural insights for the development and rational design of vaccines.

Author Summary

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Efficient determination of neutralizing epitopes of viral fusion proteins is paramount in the development of antibody-based therapeutics against rapidly evolving or undercharacterized viral pathogens. Advances in the determination of viral fusion proteins in multiple conformations with 'cryptic epitopes' during attachment and fusion has highlighted the importance of epitope accessibility due to viral fusion protein flexibility, a physical trait not accounted for in previous Bcell epitope prediction methods. Given the relatively limited number of viral fusion proteins that have been determined in multiple conformations that also have been extensively subjected to epitope mapping techniques,, which are predominantly class I fusion proteins, we chose a limited feature set in combination with a low-complexity Bayesian classifier model to avoid overfitting. We show that this model demonstrates higher accuracy in out-of-sample performance than publicly available epitope prediction methods. Additionally, due to limited structural annotation of neutralizing epitope residues, we provide examples of how our model better discerns conformation-specific epitopes, which is critical for subunit vaccine design, and how this may provide a novel approach to assess the structural changes of antigenicity of viral fusion protein homologues.

Introduction

Successful structure-based vaccine design relies on the identification of antigenic determinants that are most likely to elicit a humoral immune response, which can be achieved through the process of epitope mapping(1). Given the time and cost of experimental methods used for epitope mapping, computational B-cell epitope prediction may provide a more practical starting point to narrow the search for commonly conserved or novel epitope targets. Although B-cell epitopes are typically defined as a spatially clustered set of residues with a surface area of 600 Å² to 1,000 Å²,(2) the precise definition of both an epitope's size and residue composition are not always readily known. Therefore, the major challenge of B-cell epitope prediction is making a precise and accurate distinction between residues that are or are unlikely to contact an antibody and whether epitope residues are contiguous in sequence or not.

Data collections for structural epitopes, especially residue-specific data, have increased in the past several years through the curation of databases such as the Immune Epitope Data Base (iedb.org). This availability of data has permitted more accurate epitope prediction models, such as those provided by publicly available Discotope or Ellipro discontinuous epitope prediction servers(3,4). Even so, these epitope prediction models are limited to predicting epitopes of a single protein structure or even a single protein chain, which hinders the prediction of quaternary B-cell epitopes. Moreover, proteins are dynamic, *i.e.*, they assume more than one conformation, and a single conformation of a protein may not be sufficient to predict all possible epitopes. For instance, the stabilization of the respiratory syncytial virus (RSV) fusion (F) protein in its meta-stable prefusion conformation coincided with the identification of a broadly-neutralizing epitope

designated Site \emptyset , which is surface-inaccessible in the more stable postfusion F protein conformation(5).

The innate flexibility of class I viral fusion glycoproteins facilitates the entropy-driven process of membrane fusion to achieve cellular entry and host infection despite distinct fusion mechanisms. Compared to other proteins with antigenic determinants within a viral quasispecies, fusion proteins are more frequently targeted by broadly neutralizing antibodies, and therefore are prime candidates for rational structure-based viral vaccine design (so-called 'reverse vaccinology'). As most viral fusion proteins are oligomeric and flexible, computational B-cell epitope prediction for these targets faces unique challenges. For thorough epitope mapping and prediction, the model should account for not only the prefusion quaternary structure of the target antigen, but also the changes in quaternary structure during attachment and fusion. Recent advances in experimental design and cryogenic electron microscopy (cryo-EM) allow discovery of cryptic epitopes in 'alternative' conformations of viral fusion proteins. It is now feasible to identify residue-specific epitope accessibility changes during the fusion process, albeit with great effort for each antibody-antigen interaction.

We developed a machine learning approach designated Accelerated class I fusion protein Epitope Mapping (AxIEM) that harnesses evolutionary and structural features to classify whether a residue will reside within an epitope depending on the conformation of the fusion protein. We applied AxIEM to seven class I viral fusion proteins for which structures have been determined in at least two conformations and have been extensively subjected to experimental epitope mapping techniques. We show that AxIEM enables a much higher out-of-sample success rate in defining viral fusion epitopes than previous methods and provides a computational tool to identify antigenic determinants of novel or under-characterized viral fusion proteins.

Results

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Description of AxIEM Dataset

The dataset used to build the training and test sets of the AxIEM model included seven class I fusion proteins (S1 Table), where each trimeric protein included at least two conformations of greater than 2.00 Å root mean square deviation (RMSD) and no two conformations of less than 1.00 Å RMSD(6-26). For all 46,710 residues within the dataset, each residue possessed an expected classifier label that indicates the residue as an experimentally determined residue to be part of an epitope or not, plus a feature set of four metric values that account for the conformation and associated energetic changes each residue undergoes during various stages of attachment and fusion (Fig 1). Three of the four features were calculated to describe the residue alone in terms of its relative surface exposure, stability, and contact changes within the protein ensemble by using the metrics Neighbor Vector (NV)(27), the Rosetta-based per-residue total energy score (REU)(28), and contact proximity root mean square deviation (CP_{RMSD})(29), respectively. Comparison by a Welch's two-tailed t-test for each residue-specific feature indicated that the mean value differed significantly between residues that have and have not been experimentally determined to form an antibody (Ab) binding interaction, with $p < 1.00 \times 10^{-4}$ for all three features (S1 Fig). Under the assumption that a residue is more likely to form an epitope if its surrounding residues are also likely to do so, we created the Neighbor Sum (NS) metric to estimate the antigenicity of the volume surrounding a single residue as a cosine-weighted linear sum of a residue's own and surrounding NV, REU, and CP_{RMSD} values, which increased the separation of epitope and nonepitope scores with a Welch's paired t-test $p < 1.00 \times 10^{-10}$ (S2 Fig). Please refer to Methods and

supplementary information for the detailed description of each metric and definition of epitope residues.

Given the significant differentiation of epitope from non-epitope residues using each metric, we calculated a multivariate Gaussian distribution for each training data's feature sets and used a Bayes classifier to build a probability model to test for out-of-sample performance on the left-out protein ensemble (30). Performance accuracy relied on the definition of a true positive (TP) as a residue with a prediction score above a certain threshold value and also was designated as an expected epitope residue given a specific conformation with a classifier label of '1' prior to building the model. A true negative (TN) is a residue with opposite characteristics of a TP, although this definition is not as rigid given the possibility of unidentified or incomplete characterization of antigenic sites. A false negative (FN) or false positive (FP) is any residue that scores incorrectly below or above, respectively, of a given threshold.

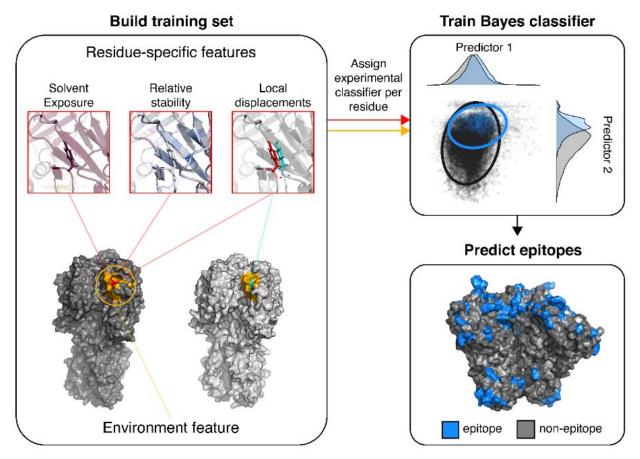


Fig 1

Overview of AxIEM. For each residue within the dataset, a set of four features was calculated that included three residue-specific features (outlined in red) and one environment feature (outlined in dark yellow). Two of the residue specific features that measured relative solvent exposure (as Neighbor Vector) and stability (as Rosetta Energy Unit) are unique to that residue as a part of a single protein conformation. The feature measuring local displacements (as Contact Proximity RMSD) quantifies a residue's contact changes within an ensemble, and relies on at least two conformations of aligned sequence for calculation. The environment feature (as Neighbor Sum) approximates the relative antigenicity of an area surrounding the residue of interest. A classifier label is assigned to each residue's calculated feature set for six of the seven protein ensembles. For

training the Bayes classifier, the distribution of each of the four features is transformed into a multivariate gaussian distribution, from which a Bayes classifier model is trained to minimize classification error given the training data. For simplicity, only the kernel density estimates of two features are shown. Afterwards, the trained Bayes classifier model is used to predict classification of the left-out protein ensemble. The bottom right panel depicts AxIEM positive predictions for the HIV-1 Env trimer PDB ID 6CM3.

Accuracy of epitope prediction depends on environment score and protein size

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We initially chose the metrics that calculated per-residue properties to avoid making assumptions about epitope size or total antigenic surface area. Even though the mean per-residue metric values were significantly different between epitope and non-epitope residues for NV, REU, and CP_{RMSD} , the overlapping coefficient $\eta(31)$ was high with values of 0.733, 0.685, or 0.792, respectively, indicating that each residue-specific feature has a relatively weak predictive value. With the metric Neighbor Sum (NS), we found that increasing the radius size of the neighboring residues' contributions to the NS value of a single residue resulted in a further separation of mean NS values between experimentally determined epitope and non-epitope residues up to $\eta = 0.333$ at a radius of 40 Å. Evaluation of the receiver operator characteristic (ROC) area under the curve (AUC) values for each viral protein ensemble, however, indicated non-uniform maximal AUC values given the upper boundary radius used to calculate NS, despite that cumulative maximal performance converged when using an upper boundary radii greater than 32 Å (Fig 2). We found that maximal performance was strongly determined by the number of amino acids within each conformation, with $R^2 = 0.76$ and p = 0.011 (S3 Fig). Using the linear regression model described by the correlation of protein amino acid number n and maximal upper boundary performance u,

with u = 15.1 + 0.0147n to determine the optimal upper boundary radius to calculate NS for each protein ensemble, overall performance of the AxIEM method significantly outperformed existing discontinuous epitope prediction methods, Discotope and Ellipro, as summarized in **Table 1**.

Method	Included Feature	AUC	DeLong's p	J	$\mathrm{MCC}_{\mathrm{max}}$	$Threshold_{MCC}$	η
Discotope*	default	0.633	$< 1.00 \times 10^{-214}$	0.210	0.144	-13.5	0.649
Ellipro	default	0.747	$< 1.00 \times 10^{-214}$	0.370	0.208	0.729	0.466
AxIEM	all	0.836	n/a	0.577	0.319	0.119	0.272
$AxIEM_{1 \text{ out}}$	no REU	0.802	4.80×10^{-21}	0.542	0.277	0.0948	0.309
	no CP_{RMSD}	0.829	0.077	0.565	0.301	0.105	0.284
	no NV	0.837	0.684	0.591	0.332	0.131	0.259
$AxIEM_{2 out}$	REU	0.829	0.040	0.646	0.307	0.122	0.278
	CP_{RMSD}	0.771	4.26×10^{-91}	0.574	0.265	0.0936	0.316
	NV	0.800	3.18×10^{-25}	0.638	0.270	0.0820	0.315
$AxIEM_{environ}$	NS	0.820	1.02×10^{-6}	0.673	0.319	0.131	0.262

Table 1

Performance evaluation summary of cumulative predictions.

For methods AxIEM_{1 out} and AxIEM_{2 out}, one or two of the per-residue features were excluded in the feature set and also from the environment *NS* calculations. The AxIEM_{environ} method excludes all AxIEM per-residue features. Note (*), evaluation of Discotope does not include SARS-CoV S protein epitope predictions.

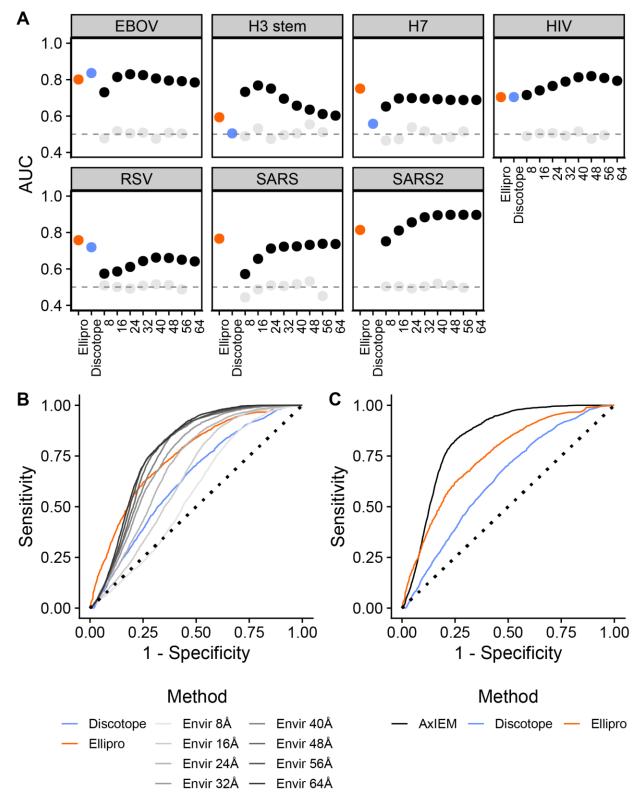


Fig 2

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Performance comparison of discontinuous epitope prediction methods. A) Comparison of AUC values by virus. Each panel represents the determined AUC value for an individual test set given the employed method. Black indicates that the feature set $\{NV, REU, CP_{RMSD}, NS_u\}$ was used to train a Bayes classifier model, with u as the upper boundary radius listed along the x axis. Light grey represents a negative control for which each residue was assigned a random value for each of the features, NV, REU, and CP_{RMSD} from a normal Gaussian distribution as determined by the mean and standard deviation of each feature's original values for a single protein. AUC values of Ellipro and Discotope are also listed by protein ensemble test set. Note that Discotope was not able to evaluate predictions for SARS-CoV and SARS-CoV-2 S proteins due to protein size and server time limits. B) Comparison of ROC curves by method. Light to dark gray represents increasing upper boundary conditions when used to determine the environment (Envir) feature NS_u . In both panel B and C, the x axis represents the false positive rate calculated as FP/(FP+TN), and the y axis represents the true positive rate calculated as TP/(TP+FN). C) Comparison of AxIEM to publically available discontinuous epitope prediction methods. The method AxIEM uses the feature set {NV, REU, CP_{RMSD} , NS_u } where u is determined as u = 15.1 + 0.0147n, with n being the number of residues of a single protein conformation.

AxIEM clarifies conformation specificity of common epitopes

Correct assignment of a classifier label, or in other words, what range and combination of feature values the model is instructed to classify as an epitope or not, is crucial in assessing model accuracy. In the case of SARS-CoV or SARS-CoV-2 Spike (S) proteins, most available structures of Ab-antigen interactions exist as fragment Ab and receptor binding domain (RBD) complexes, which disallows the certainty of classifier assignment of experimentally determined epitope

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residues to any one or more S protein trimeric conformation species. Given the experimental information available and the definition of an epitope residue used for the curation of the AxIEM dataset, the closed conformations of both SARS-related S proteins were labelled to be antigenic, while only the 2- or 3-RBD up or open conformations of the SARS-CoV-2 S protein were labelled to be antigenic. Although the AUC values of S protein-specific predictions were relatively high for SARS-CoV and SARS-CoV 2, with values of 0.759 and 0.908, up to 65.3% of false prediction assessment types could possibly be attributed to incorrect classifier label assignment, suggesting that the feature set used by AxIEM is sufficient to discern relevant conformations that will also give rise to an antigenic response (Fig 3 and Table 2). More importantly, AxIEM allows for the comparison of antigenic sites between homologs, since the AxIEM feature set is agnostic to sequence identity. Sequence alignment of predicted positives indicated only eleven aligned predicted positive residues between S protein monomers are structurally available to form an Abantigen interaction when in the up or open conformation (Fig. 3B). Geographically speaking, aligned 'up'-conformation positives share a relative constellation pattern, but differ in their relative orientation to each other by a root mean squared difference in pairwise distances of 19.4 Å (as calculated in **Equation 7**. Of the eleven aligned positives, only six residues share the same sequence identify with a root mean squared difference in epitope residues' pairwise distances of 3.64 Å (S2 Table), indicating that RBD epitope similarity is relatively low between SARS-related S proteins. Besides predicting experimentally determined RBD epitopes, AxIEM also predicted a novel common site of vulnerability within the N-terminal domain (NTD) of the S1 subunit for both SARS-CoV-2 and SARS-CoV S proteins, although the sequence identity and alignment differed for all predicted NTD epitope residues (Fig. 3C). Given these data, identification of a broadlyneutralizing Ab against multiple SARS-related S proteins is constrained not only by sequence

similarity, but also conformation similarity and availability as metastable up or open conformations.

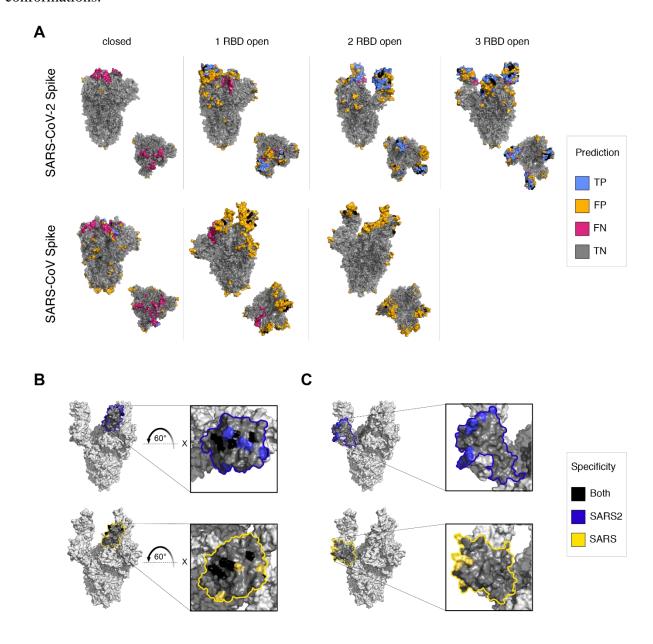


Fig 3

Overview of AxIEM predictions of coronavirus Spike protein epitopes. A) Predictions mapped to conformation models. Side and top views are shown for each protein and conformation. Black indicates alignment of positive predictions. B) Alignment of common RBD epitopes. Highlighted

area represents all residues that are within 16 Å of the geometric centroid of identified common epitopes. The models used to represent the SARS-CoV-2 (top) or SARS-CoV (bottom) include PDB models 7CAK and 6NB7. Black indicates alignment of positive predictions sharing the same sequence identity. Blue and yellow indicate sequence position alignment only. **C**) Alignment of novel NTD epitopes. Highlighted areas, model representation, and coloring are the same as in panel B.

Method	Virus	№ False predictions		'Mis'-classified false predictions (fraction)			
		FP	FN	$\text{FP}_{\text{FP}} \leftrightarrow_{\text{FN}}$	$FN_{FP} \leftrightarrow_{FN}$	$FN_{FN \to TP}$	
AxIEM	EBOV	1169	56	0.00	0.00	0.357	
	Н3	629	0	0.00	0.00	0.00	
	H7	1601	11	3.75×10^{-3}	0.545	0.00	
	HIV-1	4134	104	1.69×10^{-3}	$8.65 imes 10^{-2}$	0.577	
	RSV	1809	13	0.00	0.00	7.69×10^{-2}	
	SARS-CoV	543	124	0.171	0.653	0.00	
	SARS-CoV-2	1002	211	0.00	0.00	0.588	
Ellipro	EBOV	577	103	9.19×10^{-2}	0.407	9.71×10^{-2}	
	Н3	173	37	6.93×10^{-2}	0.324	$5.41 imes 10^{-2}$	
	H7	716	113	3.63×10^{-2}	0.230	6.19×10^{-2}	
	HIV-1	1879	467	2.98×10^{-2}	0.278	0.197	
	RSV	745	25	1.07×10^{-2}	0.320	$8.00 imes 10^{-2}$	
	SARS-CoV	2427	300	5.68×10^{-2}	8.00×10^{-2}	0.397	
	SARS-Cov-2	4729	178	2.80×10^{-2}	3.90×10^{-2}	0.376	
Discotope	EBOV	1574	10	1.02×10^{-2}	0.800	0.00	
	H3	257	25	$3.45 imes 10^{-2}$	0.560	$8.00 imes 10^{-2}$	
	H7	1257	84	4.77×10^{-2}	0.714	3.57×10^{-2}	
	HIV-1	2217	475	6.22×10^{-2}	0.236	0.371	
	RSV	1923	13	6.76×10^{-3}	0.00	1.00	
	SARS-CoV	-	-	_	-	-	
	SARS-CoV	-	-	-	-	-	

Table 2
Summary of false predictions.

 $FP_{FP \leftrightarrow FN}$ and $FN_{FP \leftrightarrow FN}$ represents the fraction of FP and FN, respectively, where for each residue within an ensemble, the residue was labeled as an expected negative for one conformation and predicted to a positive, while also labeled as an expected positive in another conformation that was predicted to be a negative. $FN_{FN \to TP}$ represents the fraction of FN that were not labeled as

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expected positives for additional conformations, while in other other conformations that residue was correctly predicted as a positive with no FP. Discussion AxIEM provides a low complexity solution to epitope mapping For this study, we chose a final model that employs a Bayes classifier, which has been shown to optimally minimize classification error (32), in conjunction with a limited feature set to avoid overfitting from the experimentally validated dataset. Despite its low complexity, the AxIEM model improves prediction of tertiary and quarternary epitopes of class I viral fusion proteins compared to the IEDB sponsored discontinuous epitope prediction methods, Ellipro and Discotope 2.0. The limited computational requirements of AxIEM, either to use as is or retrain, provides an accessible tool for vaccine development strategies such as screening for novel or cryptic antigenic sites of newly determined class I viral fusion proteins, comparing fusion protein homologues as demonstrated in Fig 3, or employing AxIEM within subunit vaccine design platforms. The further use of AxIEM as a computational epitope mapping strategy, however, requires further consideration of aspects of viral structural biology and poses future challenges to generalize epitope prediction, as discussed in the following sections. Blocking the moving target requires dynamic precision To model viral fusion protein flexibility, AxIEM requires at least two conformations to represent major conformation populations during fusion protein-mediated cellular entry and relies on the coarse-grained flexibility metric CP_{RMSD} to estimate cumulative local residue displaced contacts

as previously described. Almost certainly, two conformations are insufficient to fully summarize the biophysical changes of viral entry in terms of representing the major subpopulations, dynamics, and various other gradients like pH when entering the host cell.. Exclusion of CP_{RMSD} from the AxIEM feature set insignificantly affected overall performance (**Table 1**), and therefore could be excluded when only a single conformation is known. However, AxIEM exceeds in classifying protein antigenic residues when prefusion conformation heterogeneity is more thoroughly represented, such as in the case of ebola glycoprotein, HIV Env, or SARS-CoV-related S proteins that have multiple prefusion conformations included in the datasets. In these cases, the diverging overlap of epitope and non-epitope residue feature distributions is more pronounced, with $\eta < 0.300$ for all AxIEM features, compared to the cumulate *NS* feature overlap of $\eta = 0.333$.

Conversely, the AxIEM model overestimates the probability of antigenicity of postfusion and membrane-proximal external region (MPER) protein surfaces regardless of conformation, as displayed in S4-8 Fig, possibly due to the fact that these regions are not truly surface-accessible to an antibody in a cellular environment. This is supported by the findings summarized in Table 1, where exclusion of NV had no effect on AxIEM's AUC with De Long's p = 0.684, and explains the poor individual performance of predicting RSV and influenza H3 stem epitopes due to the large fraction of surface-accessible residues within each represented protein ensemble. However, in the case of HIV Env MPER, antibodies like 10E8 require HIV Env to 'tilt' in relation to the lipid bilayer to gain surface accessibility (33), and it is possible that similar regions may present true sites of vulnerability. Further validation would require either identification of novel neutralizing antibodies like 10E8 or better quantification of membrane or protein crowding. Furthermore, any information regarding glycosylation patterns was not included in the AxIEM model due to the lack of high resolution (< 3.0 Å) determination of most glycosylation sites, and

therefore any predictions made by AxIEM would need to be supplemented with glycosylation modeling to further assess validity of any initial AxIEM predictions. Overall, AxIEM's performance and other computational epitope prediction methods would likely benefit from modeling of protein target dynamics and major subpopulation states to better interrogate how protein flexibility affects antigenicity and which major subpopulation states are most likely to illicit a strong neutralizing response.

Subunit vaccine design may improve by considering protein size

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Subunit vaccines rely on the adaptive immune response to produce antibodies against a protein domain or scaffold, which can subsequently elicit a neutralizing antibody response during natural infection. Sites of vulnerability are viral protein surfaces that have been shown to form more than one neutralizing antibody binding interaction and are prime candidates for serving as antigen targets for subunit vaccines. Rather than assuming that proximity features for antigenicity prediction are constrained by the surface area of an antibody binding footprint like Ellipro or Discotope 2.0, AxIEM improves epitope residue classification prediction by employing physicochemical proximity features in relation to the total number of residues within a fusion protein (Fig 2). Given that AxIEM positive predictions tend to be clustered within local domains, many of which are known to form epitope-paratope interactions with multiple neutralizing antibodies, AxIEM may be better suited for the task of identifying conformation-specific sites of vulnerability than the task of B-cell epitope prediction. In this case, subunit vaccine design strategies might benefit from the construction of antigens that account for the relative structural antigenicity of a fusion protein rather than the highly specific identification of a potential epitope region..

Methods

Explanation of epitope predictors

Neighbor Vector (NV) The per-residue solvent-accessible surface area (SASA) metric NV approximates the proximity and spatial orientation of surrounding residues to estimate relative surface exposure of a residue, as previously described(27). In brief, NV employs the Contact Proximity (CP) and Neighbor Count (NC) algorithms to calculate the sum of each surrounding residue's C_{β} - C_{β} distance (d) unit vector weighted by its likelihood to make a contact with the reference residue, calculated as CP (Equation 1), and is normalized by the sum of all possible contacts within the residue's vicinity, calculated as NC (Equation 2). In other words, for a highly buried residue, the weighted d unit vectors of all C_{β} - C_{β} distances will be directed outwards in many directions so that its NV score ≈ \cong 0, whereas a highly exposed residue's weighted d unit vectors will be directed uniformly so that its NV score \cong 1. We use the lower and upper boundaries of 4.00 Å and 12.8 Å, respectively, because 4.00 Å was shown to be the optimal lower boundary to accurately assess per-residue SASA using NC and 12.8 Å is the maximum length of a C_{β} - C_{β} distance where any atom of one amino acid's side chain has been shown to make a direct interaction with another amino acid's side chain (Equation 3).

Equation 1

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$$CP = \begin{cases} 1, & \text{if } d \leq 4.00 \text{ Å} \\ 0, & \text{if } d \geq 12.8 \text{ Å} \\ \frac{1}{2} \left[\cos \left(\frac{d - 4.00 \text{ Å}}{12.8 \text{ Å} - 4.00 \text{ Å}} \times \pi \right) + 1 \right], & \text{if } 4.00 \text{ Å} < d < 12.8 \text{ Å} \end{cases}$$

- Where d is the geometric distance between two C_{β} atoms of two residues. In the case of glycine, a
- dummy C_{β} atom was used in place of its hydrogen.
- 334 Equation 2

$$NC_i = \sum CP_j(d(i,j), lower, upper)$$

- Where CP_i is the evaluated CP score of the *j*th residue in relation to the residue of interest *i* given
- the lower boundary of 4.00 Å and the upper boundary of 12.8 Å.
- 338 Equation 3

$$NV_i = \frac{\sum_{i=1}^{j} (\overrightarrow{v_{ij}} / ||\overrightarrow{v_{ji}}|| \times CP_j)}{NC_i}$$

- 340 where $\overrightarrow{v_{ij}}/\|\overrightarrow{v_{ji}}\|$ is the unit vector of the *j*th residue multiplied by the *CP* score of the *j*th residue,
- both terms in relation to the *i*th residue.
- 342 Per-residue Rosetta Energy Unit (REU) The relative stability for each residue of a minimized
- single protein conformation was calculated with the Rosetta *ref2015* energy function and using the
- 344 jd2 scoring application to estimate the single body and pairwise interaction energies of a residue
- as the Rosetta per-residue total energy score, which is reported in Rosetta Energy Units (*REU*).
- 346 Contact Proximity Root Mean Square Deviation (CP_{RMSD}) The metric CP_{RMSD} has previously
- been used to estimate the relative local side chain contact changes of a single residue experiences
- as part of a protein ensemble, and was calculated as the sum of all root mean square deviations of
- 349 likely contacts a single residue will form (**Equation 4**)(29). This was estimated by *CP* for each
- C_{β} - C_{β} distance, again using 4.00 Å and 12.8 Å as the lower and upper boundaries.
- 351 Equation 4

$$CP_{RMSD}(i) = \sum_{n} \sqrt{\frac{1}{n} \sum_{j=1}^{n} (\overline{CP(ji)} - CP(ji)_n)^2}$$

where i is the residue of interest, j is another residue in the same protein conformation, n is the number of protein conformations within the protein ensemble, and $(\overline{CP(ji)} - CP(ji)_n)^2$ is the variance of the CP value of residue j with respect to residue i within n conformations. In the case where only two conformations were used, only the mean CP value was calculated.

Neighbor Sum (NS) The NS metric was calculated as a weighted linear sum of NV, REU, and CP_{RMSD} (Equation 5). In the Results section, we reported NS using a fixed lower boundary of 4.00 Å and adjusted the upper boundary to test for epitope radius size as noted (Equation 6). We also tested for adjusting the lower boundary to 6.00 Å and 8.00 Å as well as using a linear weighted function instead of a cosine weighted function and found an increase in classification overlap of

Equation 5

$$NS_u(i) = \sum_{i=1}^{j} NV(j) + REU(j) + CP_{RMSD}(j)$$

NS values provided that the same upper boundary condition was used.

where i is the residue of interest, j is another residue in the same protein conformation, u is the upper boundary radius at which surrounding residues contribute to i residue's NS value, and j residue's weighted contribution w to residue i is determined in **Equation 6**.

Equation 6

$$w = \begin{cases} 1, & \text{if } d \leq lower \\ 0, & \text{if } d \geq upper \end{cases}$$

$$\frac{1}{2} \left[\cos \left(\frac{d - lower}{upper - lower} \times \pi \right) + 1 \right], & \text{if } lower < d < upper \end{cases}$$

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Definition of conformation-specific epitopes All residues classified as an "epitope" have been listed within a publicly available online database as experimentally validated discontinuous B-cell epitopes, whose database identifications have been listed in Online Methods. The definition of an epitope was further refined as any residue identified as a discontinuous epitope that also retained a structural similarity to the conformation of the antigen experimentally determined to interact with a specific antibody and that the binding orientation of the antibody did not occupy the same space, or intersect, with any part of the fulllength viral protein in that conformation when aligned using PyMOL. Residues that did not fit these criteria were classified as a "non-epitope". Model preparation Protein structures were downloaded from the Protein Data Bank (PDB; rcsb.org) and aligned using Clustal Omega (www.ebi.ac.uk/Tools/msa/clustalo/) to identify residues that were structurally determined for all equivalent chains and in all conformations of each viral protein. Residues that were not determined as such were manually removed using PyMOL (https://pymol.org/2/) to generate an aligned pdb file. Since some structural models contained mutations for stabilization, the consensus sequence was used to replace the initial sequence. The consensus sequence was obtained by performing a multiple sequence alignment of all available full-length sequences with Clustal Omega and using the EMBOSS cons package (ftp://emboss.open-bio.org/pub/EMBOSS) to identify the consensus sequence. The Rosetta partial_thread application was used to thread, or replace, each residue with the corresponding consensus sequence. Afterwards, the threaded structures were subjected to a constrained relax using the Rosetta FastRelax application to generate 100 models for each protein. From the generated models, the model with the combined lowest energy and lowest structural RMSD to the respective aligned structure was selected as the final model used to evaluate NV, REU, CP_{RMSD} , and NS. For a complete guide to which residues and methods were used for model generation, please refer to the Online Methods section.

Statistical Information

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399 A DeLong's test was used to compute significance in differences of AUC between AxIEM performance and other method, where a z $score = \frac{AUC_A - AUC_B}{\left(\sigma_A^2 + \sigma_B^2 - 2Cov(AB)\right)^{0.5}}$. Youden's J statistic was 400 measured as max (sensitivity + specificity -1). A Matthew's correlation coefficient (MCC) 401 402 ROC MCC =calculated each threshold along where was curve $\frac{TP \times TN - FP \times FN}{\sqrt{(TP + FP)(TP + FN)(TN + FP)(TN + FN)}}$. The maximum MCC value is reported along with the associated 403 404 threshold value in **Table 1**. The overlapping index η represents the overlap of prediction scores of 405 expected classifications. Root mean square differences of pairwise epitope geometric distances, 406 denoted as $rmsd_p$ in **Equation 7**, represents the average difference in geometric distance d 407 (**Equation 8**) of each aligned residue i to all other residues j between epitopes a and b containing 408 equal number of n residues. For a complete description of library and package dependencies and 409 software versions, please see the supplementary protocol capture. All scripts and curated datasets 410 for the development of AxIEM are available at https://github.com/mfsfischer/AxIEM/.

Equation 7

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$$rmsd_{p} = \frac{1}{n} \sqrt{\sum_{i=1}^{n} \left| \sum_{j=1}^{n} d_{a}(i,j) - d_{b}(i,j) \right|}$$

413 Equation 8

$$d = (x_j - x_i)^2 + (y_j - y_i)^2 + (z_j - z_i)^2$$

Computational resources

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All calculations were performed on a Core i9-9980HK laptop with 16 GB RAM and Gentoo Linux operating system. Transformation of the feature set to a multivariate Gaussian distribution and training of Bayes classifier models were implemented in Python using the pomegranate package(30). Statistical analysis for ROC curves, AUC values, DeLong's test(34), Youden's J index(35), maximal Matthews correlation coefficient(36) and the associated threshold was performed using Python. Conductance of the Welch's two-tailed t-test, Pearson's correlation (to determine R², p value, and linear model to determine optimal upper boundary radii), and calculation of the distribution-free overlapping index n were performed in R. All datasets, code, documentation this publicly available and used for study are at https://github.com/mfsfischer/AxIEM.

Acknowledgements

We thank Dr. Axel Fischer for his helpful insights.

Author contributions

429 M.F. curated the structure-based epitope data set, implemented code, conducted analysis, and

wrote the manuscript. J.M and J.C. contributed to the review of the manuscript.

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