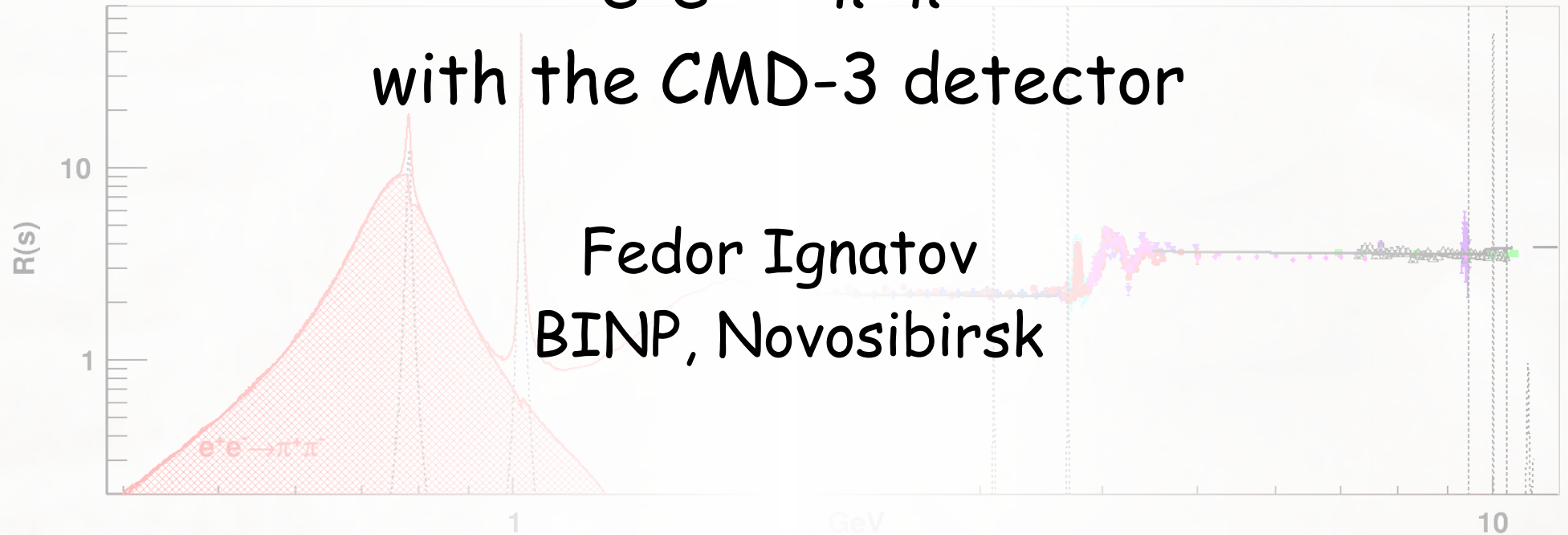


$$e^+e^- \rightarrow \pi^+\pi^-$$

with the CMD-3 detector



Fedor Ignatov  
BINP, Novosibirsk

17 March 2023

The Muon  $g-2$  Theory Initiative Seminar

# 55 years of hadron production at colliders

## INVESTIGATION OF THE $\rho$ -MESON RESONANCE WITH ELECTRON-POSITRON COLLIDING BEAMS

V. L. AUSLANDER, G. I. BUDKER, Ju. N. PESTOV, V. A. SIDOROV, A. N. SKRINSKY and A. G. KHABAKHPASHEV

*Institute of Nuclear Physics, Siberian Branch of the USSR Academy of Sciences, Novosibirsk, USSR*

Received 1 September 1967

Preliminary results on the determination of the position and shape of the  $\rho$ -meson resonance with electron-positron colliding beams are presented.

When experiments with electron-positron colliding beams were planned [1, 2] investigation of the process

$$e^- + e^+ \rightarrow \pi^- + \pi^+$$

$$e^- + e^+ \rightarrow K^- + K^+$$

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Detector was made from different layers of Spark chambers, readouts by photo camera

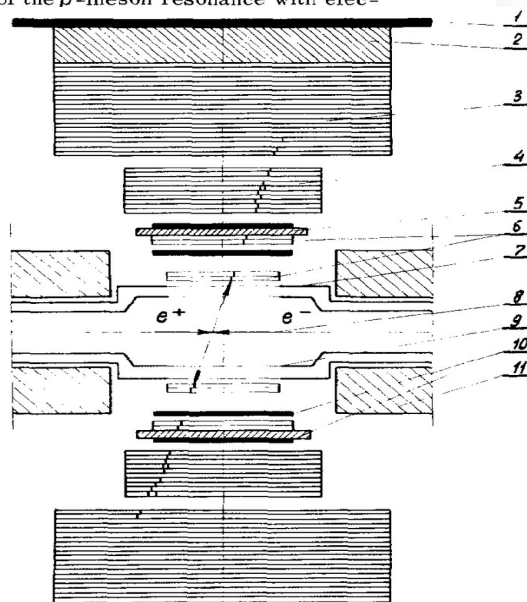


Fig. 1. Spark chambers system:  
1) Anticoincidence scintillation counter  
2) Lead absorber 20 cm thick  
3) "Range" spark chamber  
4) "Shower" spark chamber  
5) Duraluminium absorber 2 cm thick  
6) Thin-plate spark chambers

1 September 1967

Start of  $e^+e^- \rightarrow$  hadrons measurements

Phys.Lett. 25B (1967) no.6, 433-435

VEPP-2, Novosibirsk

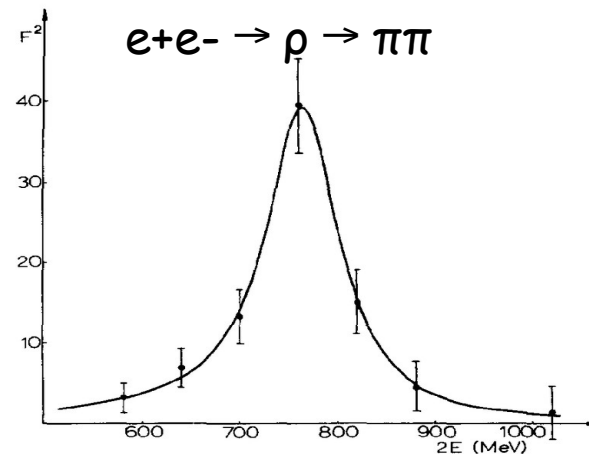
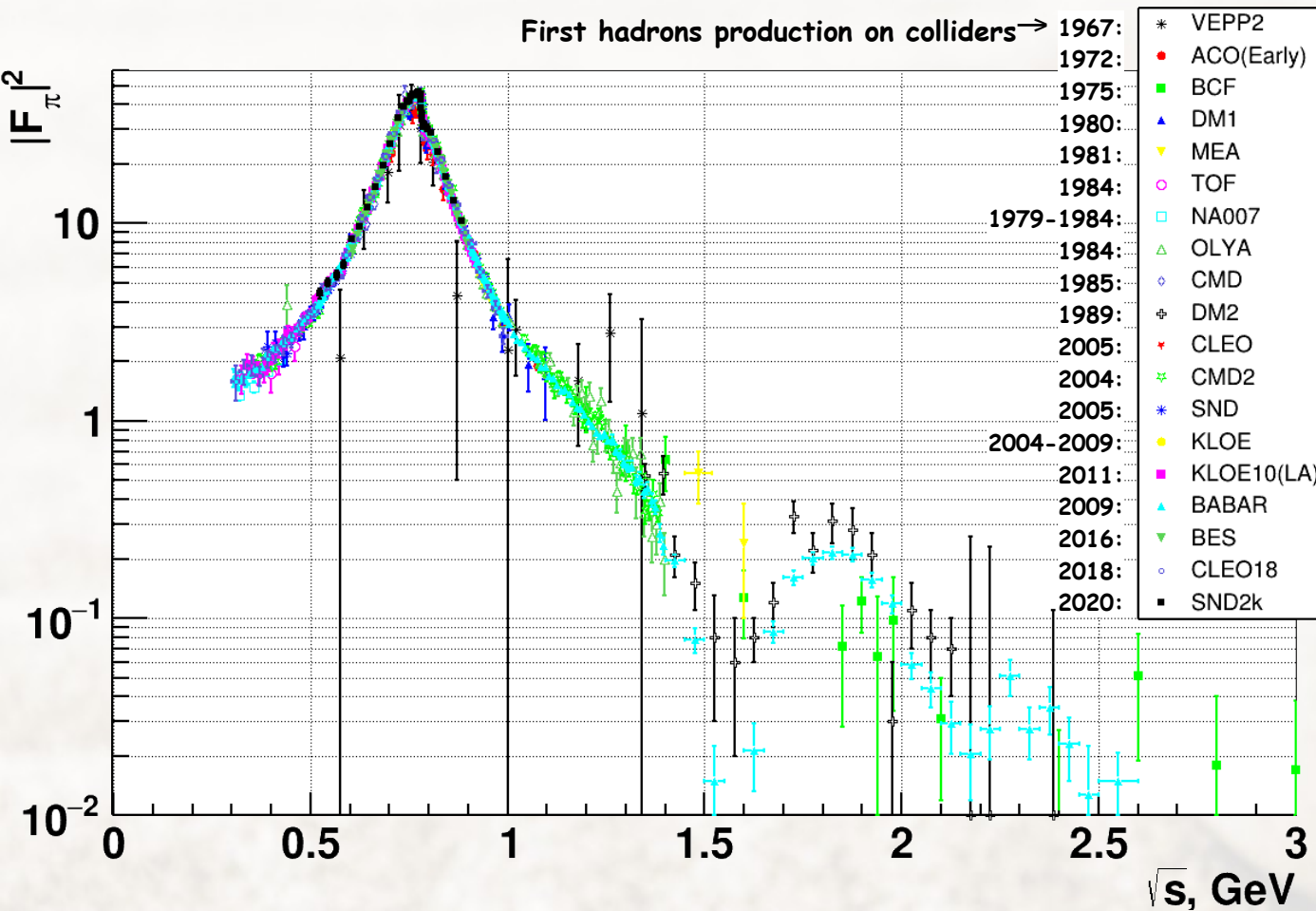


Fig. 2. Experimental values of  $F^2(E)$  approximated by the Breit-Wigner formula.

ment geometry and  $F$ - modulus of the form factor for pion pair production [1]. In the case of QED with no other forces  $F=1$ . If the particles are produced at the angle  $90^\circ$  with respect to the beam axis then  $a=18$ . Integration over the solid angle gives  $a=20.4$ .

# $e^+ e^- \rightarrow \pi^+ \pi^-$ today



## Before 1985

Low statistical precision

Systematics >10%

NA7 A few points with >1-5%

## 1985 - VEPP-2M

with more detailed scan

OLYA systematics 4%

CMD 2%

## 2004 with CMD2 at VEPP-2M

was boost to systematics: 0.6%

(near same total statistic)

The uncertainty in  $a_\mu(\text{had})$  was improved by factor 3 as the result of VEPP-2M measurements

## New ISR method

$e^+e^- \rightarrow \gamma + \text{hadrons}$  (limited only by systematics):

KLOE: 0.8%

BaBar: 0.5%

BES: 0.9%

CLEO: 1.5%

## New direct data:

SND2k : 0.8% (with 1./10 of avail. data)

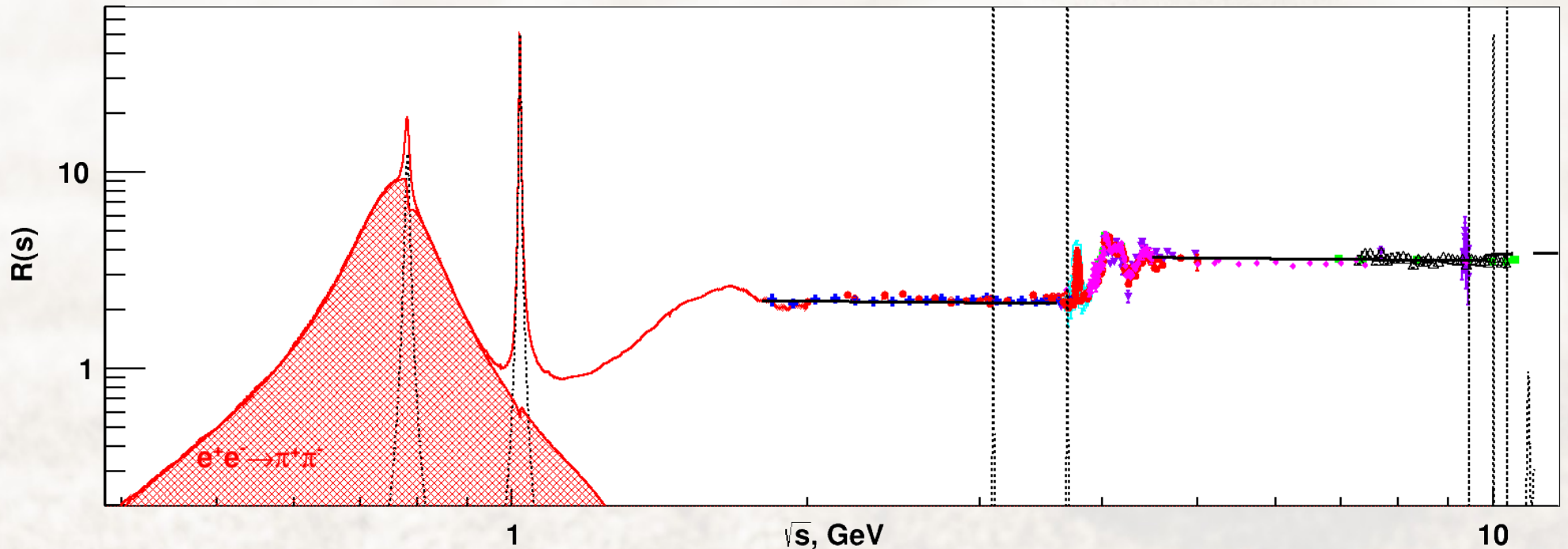
New  $g-2$  experiments and future  $e^+e^-$  as ILC, FCC-ee require average precision  $\sim 0.2\%$

$$R(s) = \frac{\sigma^0(e^+ e^- \rightarrow \gamma^* \rightarrow \text{hadrons})}{\sigma^0(e^+ e^- \rightarrow \gamma^* \rightarrow \mu^+ \mu^-)}$$

$R(s)$  is one of the fundamental quantities in high energy physics:  
 it reflects number of quarks and colors  $\rightarrow$  pQCD tests;

QCD sum rules  $\rightarrow$  quark masses, quark and gluon condensates,  $\Lambda_{\text{QCD}}$

Dispersion relations  $\rightarrow \alpha_{\text{QED}}(M_Z)$ , hyperfine muonium splitting, **muon (g-2)**



$e^+e^- \rightarrow \pi^+\pi^-$  gives main contribution to  $R(s)$  at  $\sqrt{s} < 1 \text{ GeV}$

# SM prediction for muon g-2

White Paper 2020 (e-Print: 2006.04822)

Experimental world average (E821+E989)

$$a_\mu = 11\,659\,206.1 \pm 4.1 \times 10^{-10}$$

Theoretical prediction data driven

$$a_\mu = 11\,659\,181.0 \pm 4.3 \times 10^{-10} \quad (\text{WP20})$$

$$\Delta a_\mu = 25.1 \pm 5.9 \times 10^{-10}$$

Hadronic part from measured cross-section

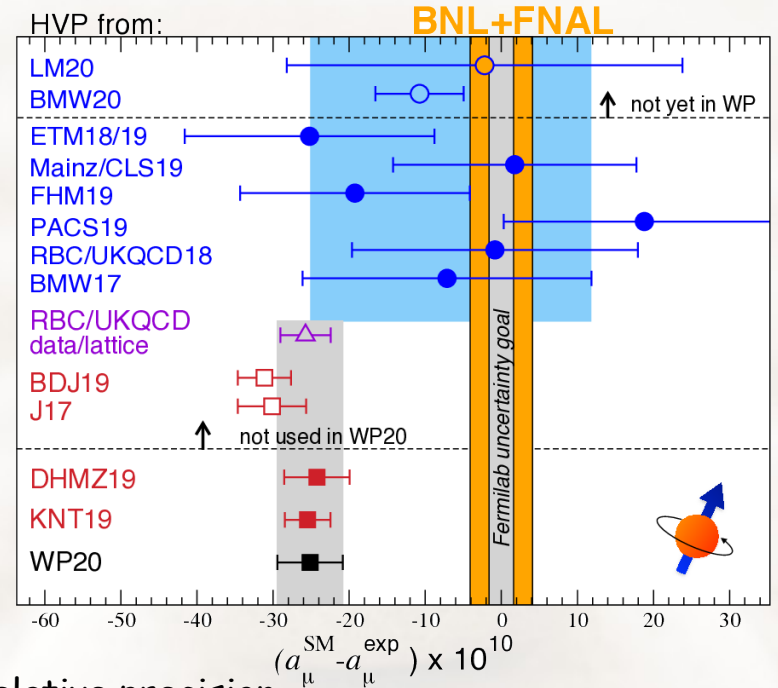
$$\text{LO hadronic } 693.1 \pm 4.0 \times 10^{-10}$$

	<b>KLOE/BABAR difference</b>	
$\pi^+\pi^-$	$506.0 \pm 1.9 \pm 2.8$	<b>0.7%</b>
$\pi^+\pi^-\pi^0$	$46.4 \pm 1.5$ (mostly from omega region)	<b>3.2%</b>
$\pi^+\pi^-\pi^0\pi^0$	$18.1 \pm 0.7$	<b>3.9%</b>
Inclusive ( $\sqrt{s} > 1.8\text{-}3.7 \text{ GeV}$ )	$34.0 \pm 0.7 \pm 0.7$ <b>DV+QCD</b>	<b>2.9%</b>

.....

---


$$\text{Light-by-light } 9.2 \pm 1.9$$

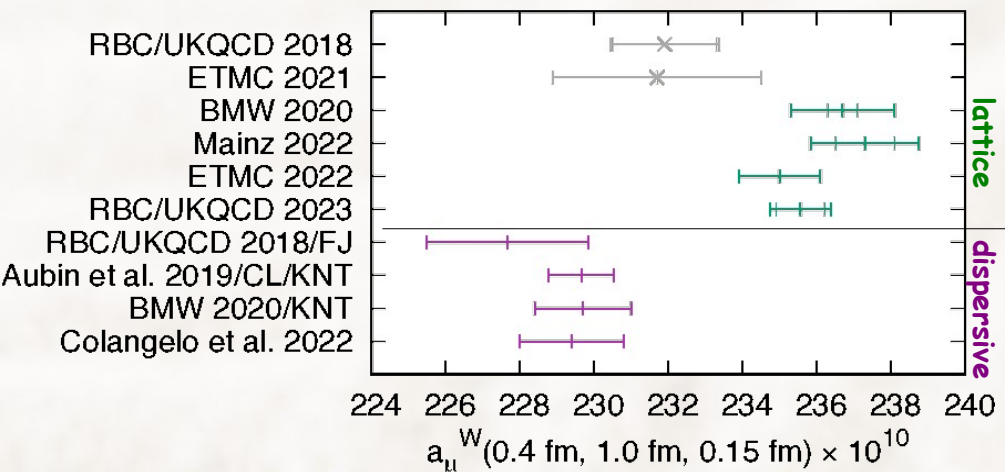


e-Print: 2203.15810

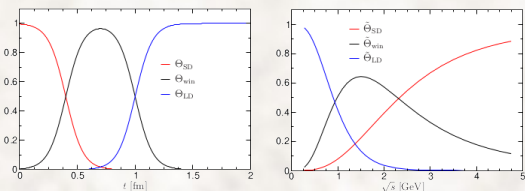
# Dispersive vs Lattice

T.Blum et al, [e-Print: 2301.08696 \[hep-lat\]](#)

$a_\mu^{\text{HVP}}$  contribution from intermediate window in Euclidean time



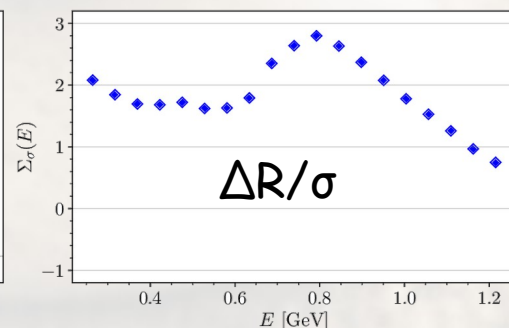
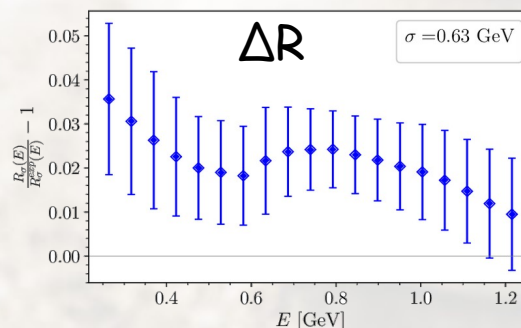
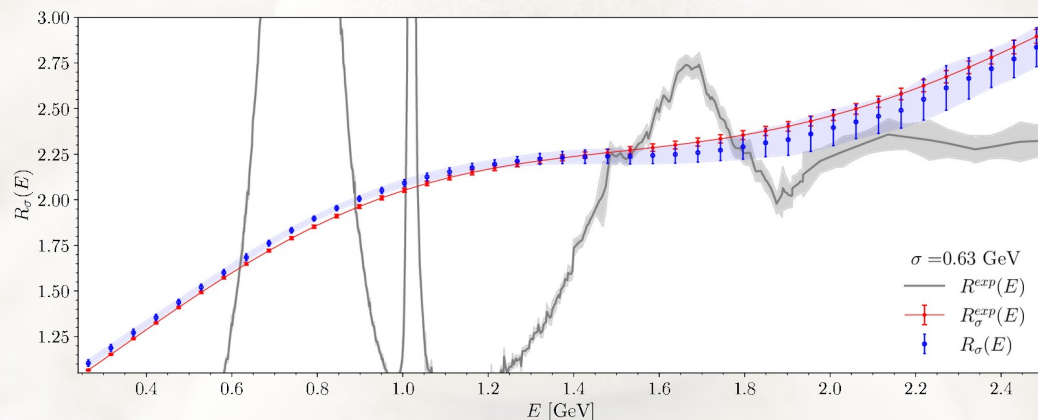
Windows definition



$\sim 4\sigma$  tension between Lattice/Dispersive

C. Alexandrou et al, [e-Print: 2212.08467 \[hep-lat\]](#)

$R(s)$  is convolved with Gaussian kernel

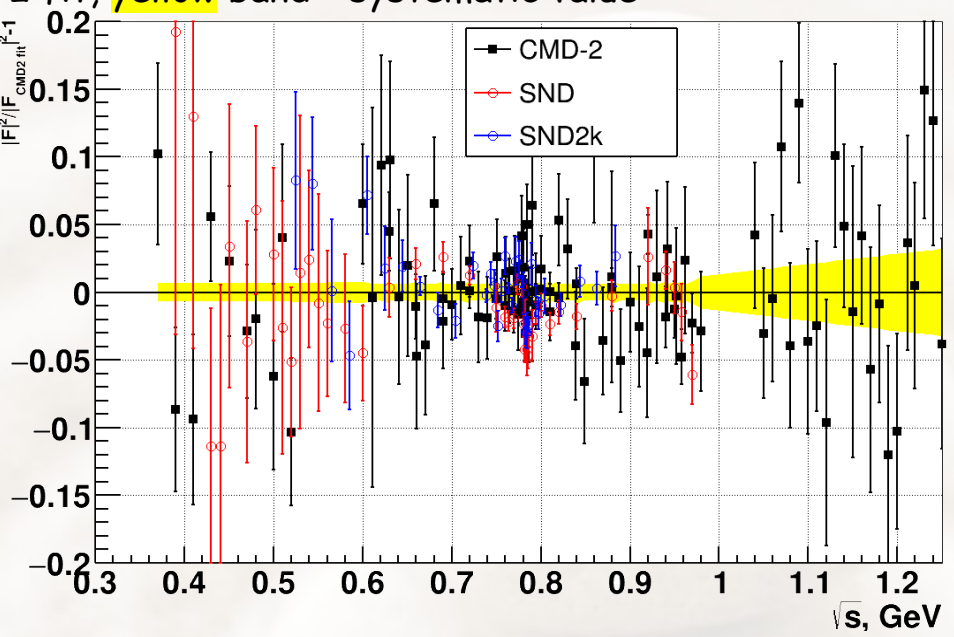
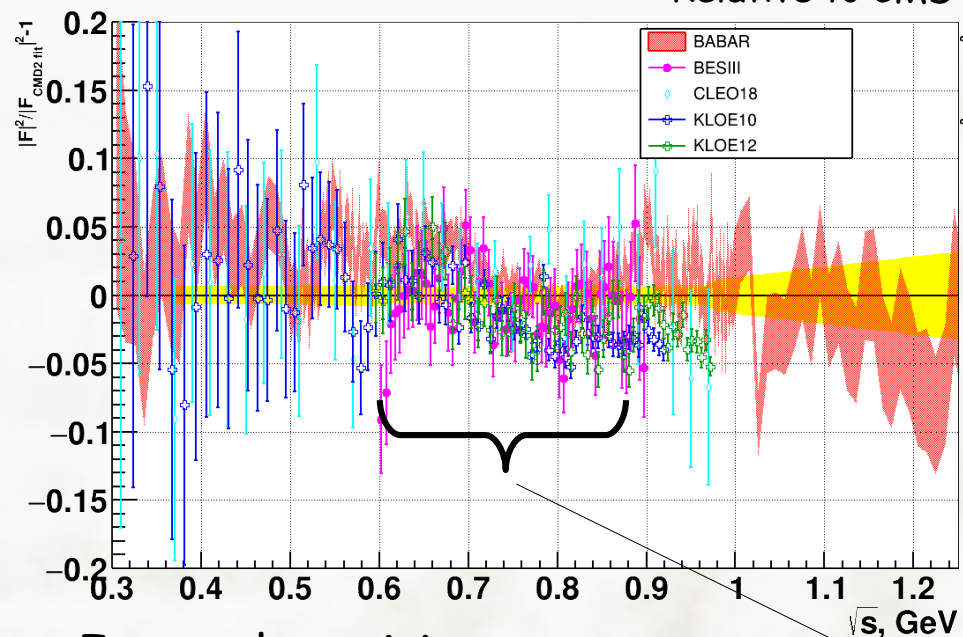


$\sim 3\sigma$  tension at rho energies

Question of comparison:  $e+e^-$  vs  $(g-2)_\mu$  vs lattice

# The $\pi^+ \pi^-$ contribution to $a_\mu^{\text{had}}$

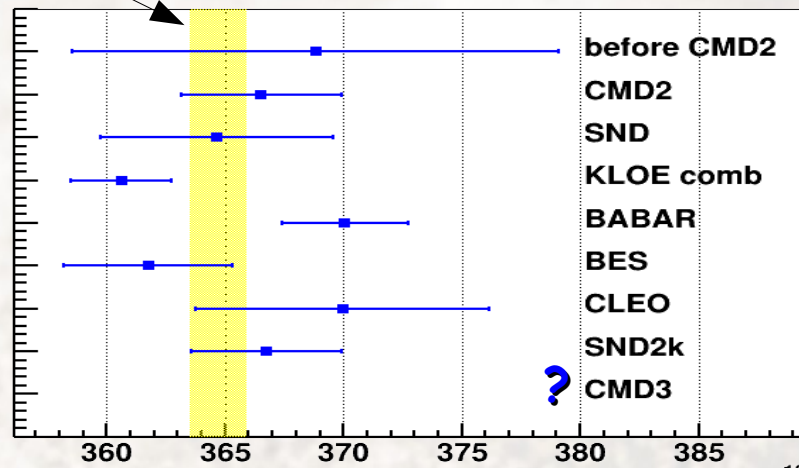
Relative to CMD-2 fit, **yellow** band - systematic value



Integral precision  
is limited by systematics

local inconsistencies larger  
than claimed systematic errors  
→ additional scale factor

Seen  $2.9\sigma$  tension KLOE vs BaBar



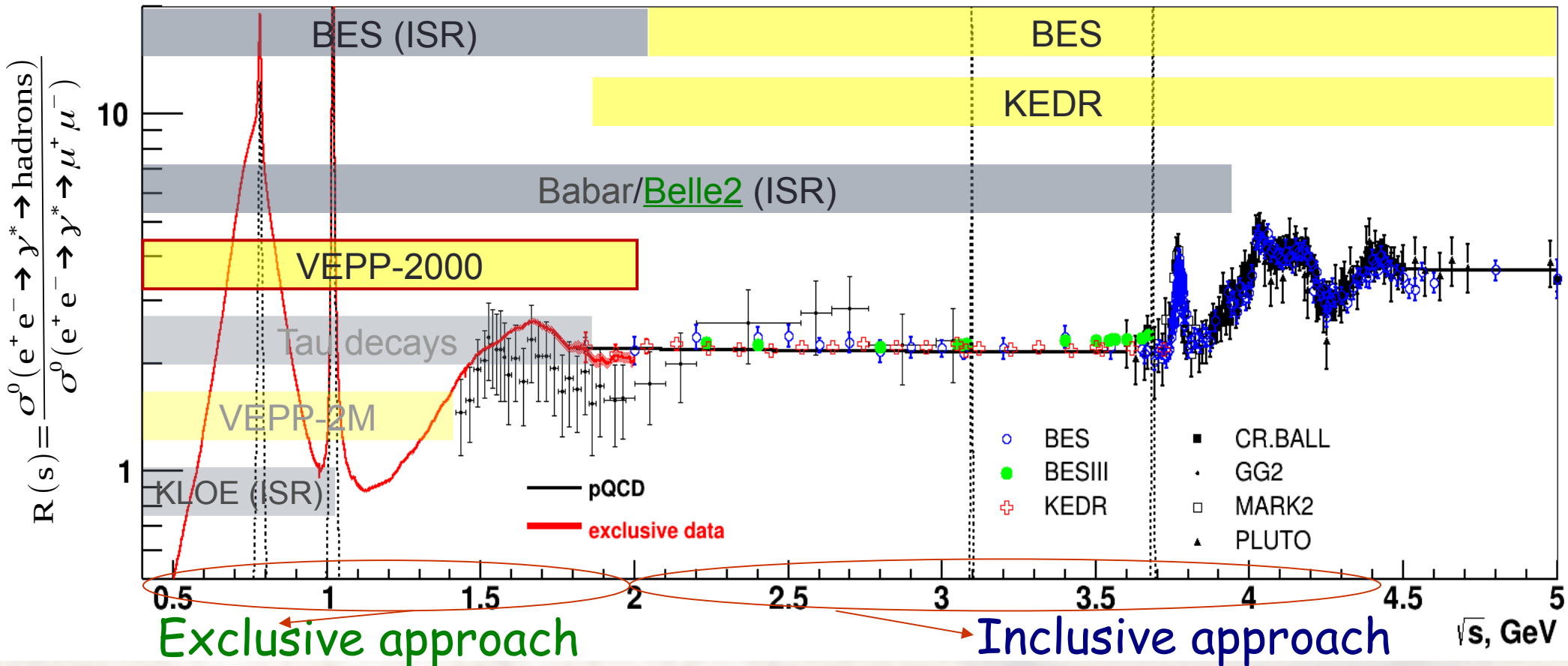
Experiment	Systematic Error (p-region)
CMD2	0.6-0.8%
SND	1.5%
KLOE comb	0.8%
BABAR	0.5%
BES	0.9%
CLEO	1.5%
SND2k	0.8%
CMD3	

KLOE/BABAR  
difference

$$a_\mu(\pi^+\pi^-) = 506.0 \pm 1.9 + 2.8 \times 10^{-10} (\pm 0.7\%)$$

# R(s) measurement

Two techniques: ISR vs Energy scan



VEPP-2000: direct exclusive measurement of  $\sigma(e+e^- \rightarrow \text{hadrons})$

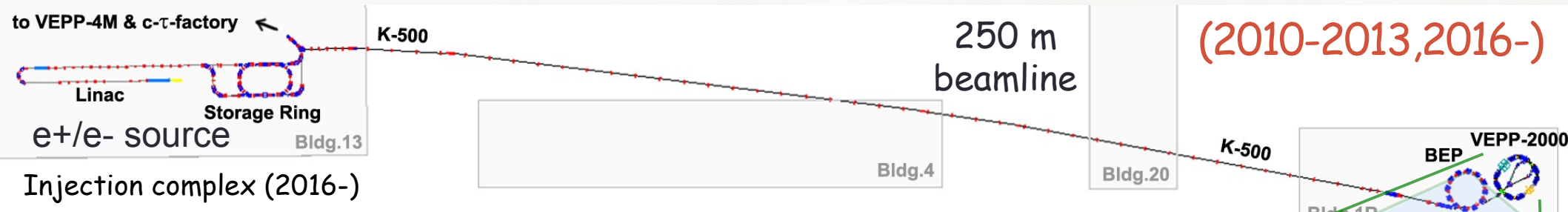
Only one working these days on scanning below  $< 2$  GeV

World-best luminosity below 2 GeV (except 1 GeV - where KLOE outperformed everybody)

BESIII, KEDR - inclusive measurement of R(s) from 2 GeV to 5 GeV



# VEPP-2000 e+e- collider

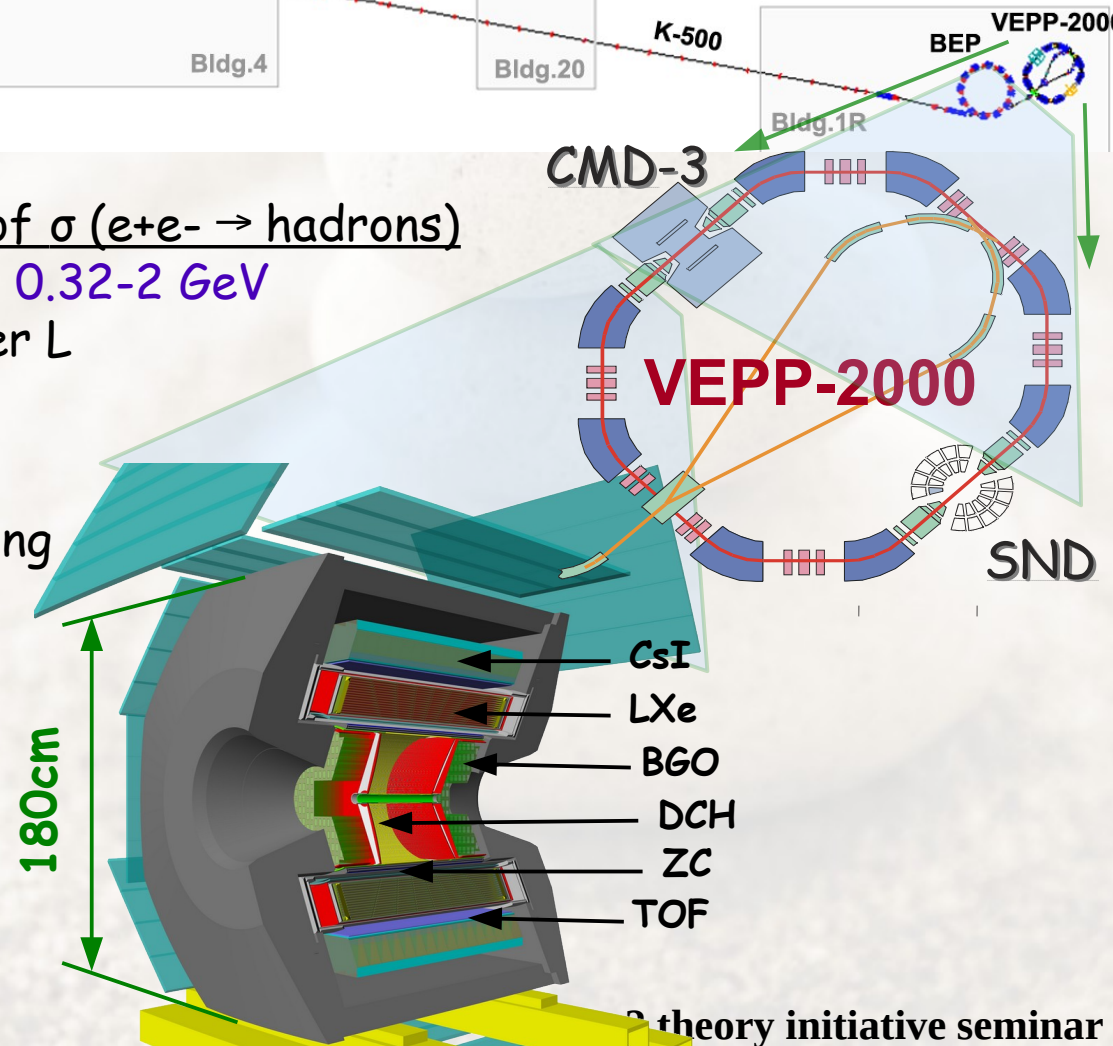


VEPP-2000: direct exclusive measurement of  $\sigma(e+e- \rightarrow \text{hadrons})$   
 Only one working this days on scanning  $2E = 0.32-2 \text{ GeV}$   
 Unique optics, "round beams" to reach higher L

$$L = 0.8 \times 10^{32} \text{ cm}^{-2}\text{s}^{-1} \text{ at } 2E = 2 \text{ GeV}$$

Energy monitoring by Compton backscattering  
 $\sigma_{fs} \approx 0.1 \text{ MeV}$

Two detectors: CMD-3 and SND  
 started by the end of 2010

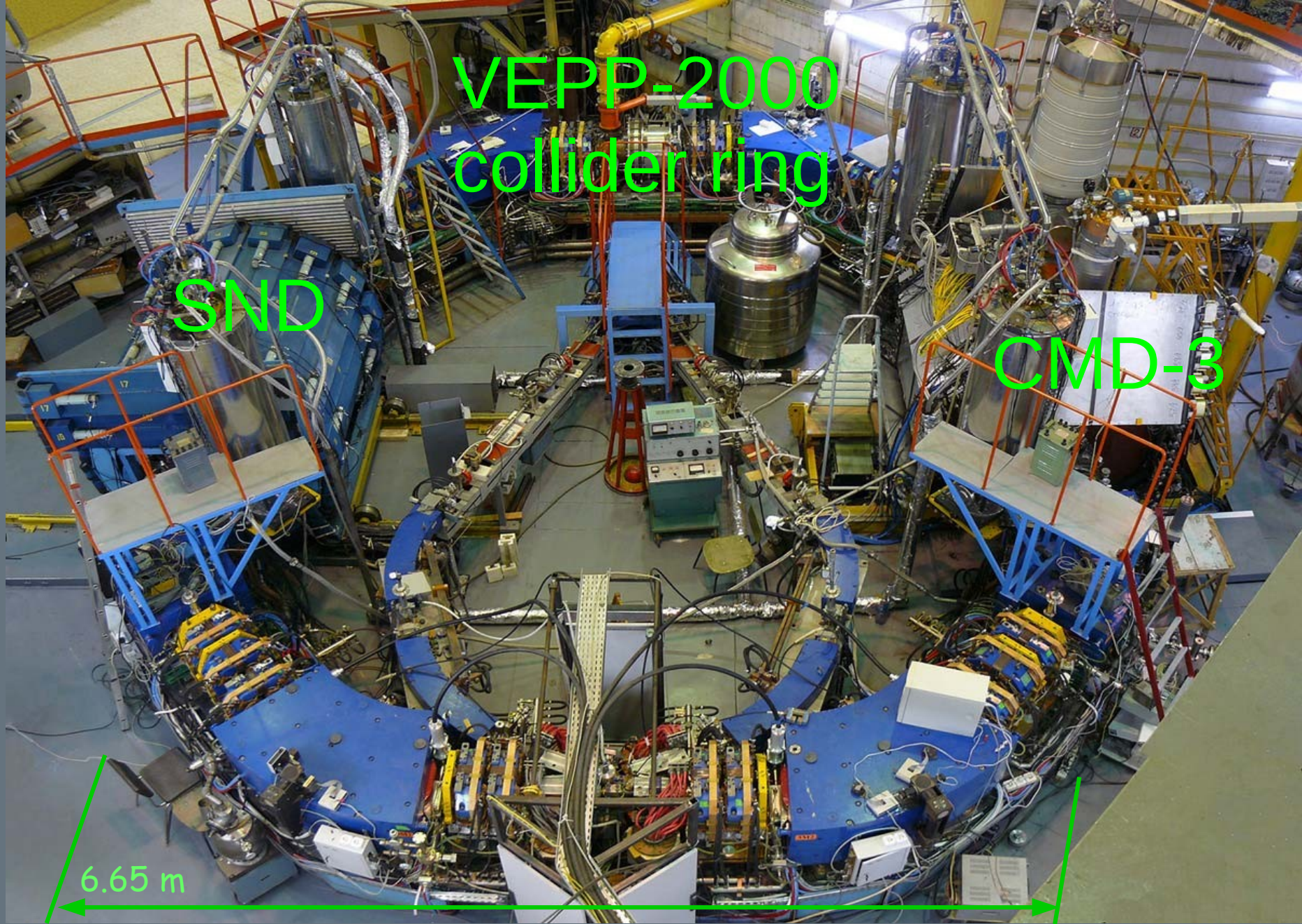


VEPP-2000  
collider ring

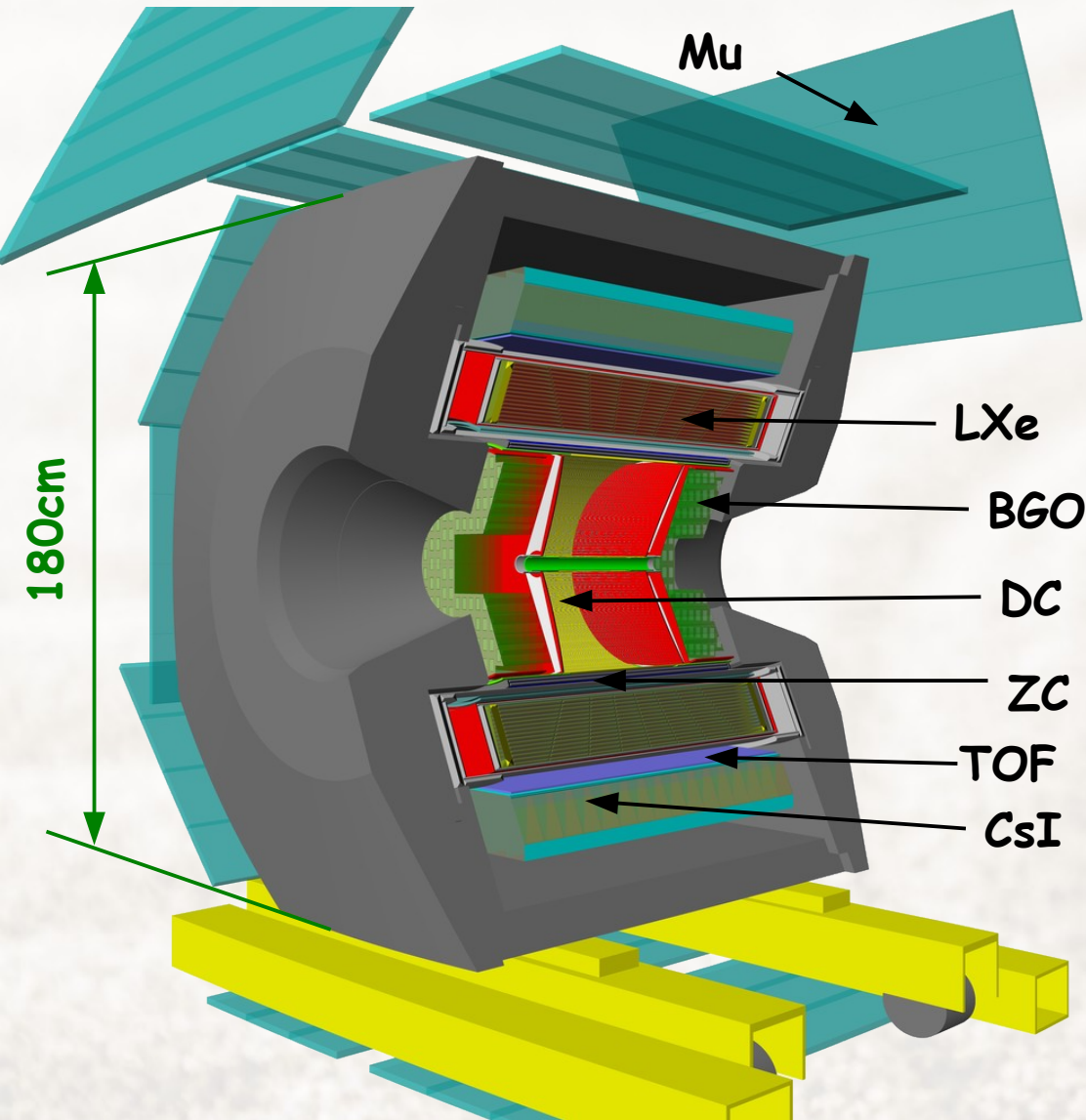
SND

CMD-3

6.65 m



# CMD-3 detector



## Tracking:

x Drift Chamber in 1.3 T magnetic field

$$\sigma_{R\phi} \sim 100 \mu\text{m}, \sigma_z \sim 2.5\text{mm}$$

$$\sigma_p/P \sim \sqrt{0.6^2 + (4.4 \cdot p[\text{GeV}])^2}, \%$$

x ZC-chamber worked until summer 2017

$$\sigma_z \sim 0.7\text{mm by strip readout}$$

## Calorimetry:

x Combined EM calorimeter (LXe, CsI, BGO)  
13.5  $X_0$  in barrel part

$$\sigma_E/E \sim 0.034/\sqrt{E [\text{GeV}]} \oplus 0.020 - \text{barrel}$$

$$\sigma_E/E \sim 0.024/\sqrt{E [\text{GeV}]} \oplus 0.023 - \text{endcap}$$

x LXe calorimeter with 7 ionization layers  
with strip readout

~2mm measurement of conversion point,  
tracking capability,  
shower profile (from 7 layers + CsI)

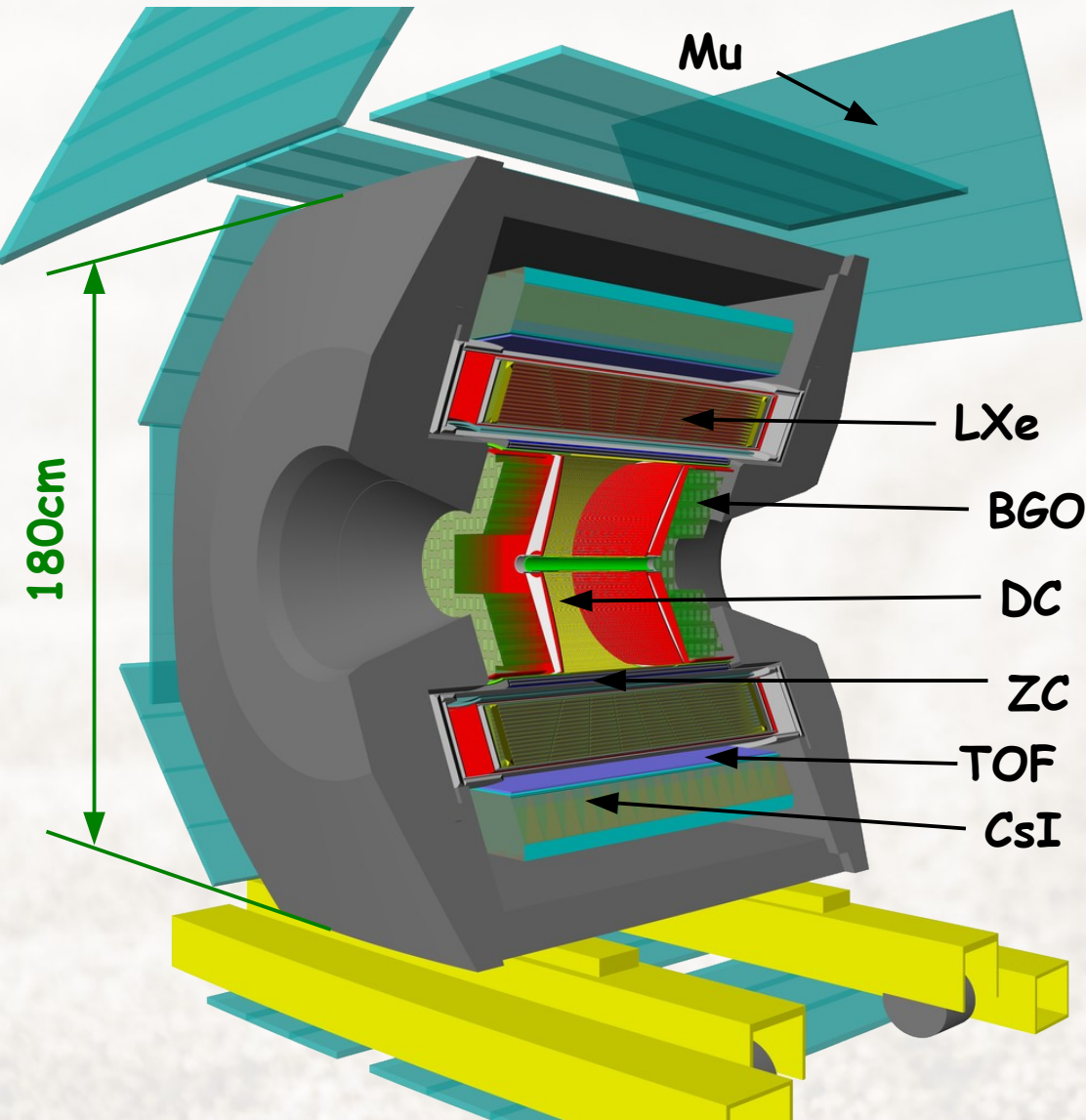
## PID:

x TOF system ( $\sigma_T \sim 0.4 \text{ nsec}$ )

particle id mainly for p, n

x Muon system

# CMD-3 detector



Advantages compared to previous CMD-2:

- x new drift chamber with x2 better spatial resolution, higher B field  
better rec. efficiency (factor ~2-5)  
better momentum resolution (factor ~ 2)

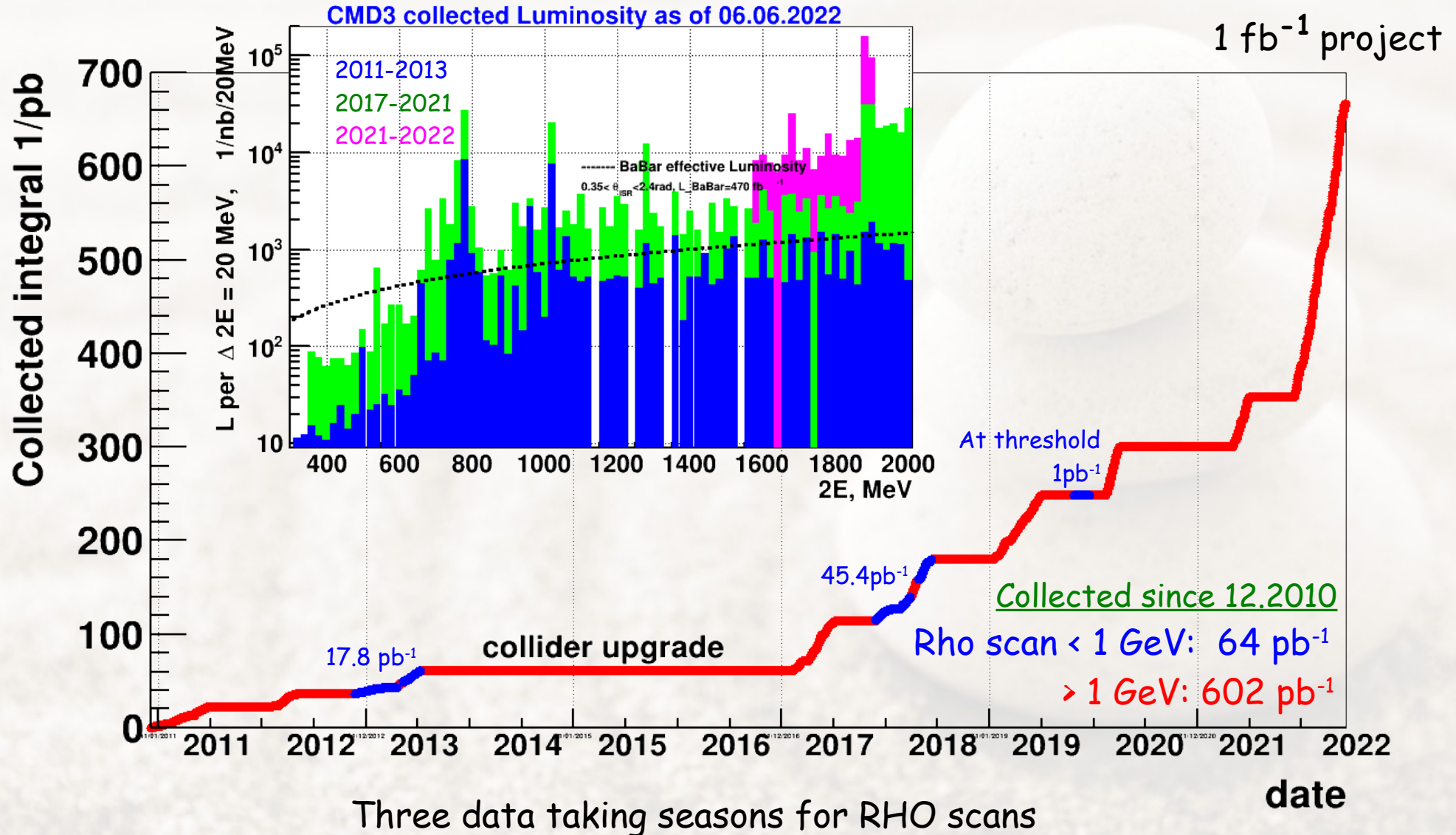
- x Unique LXe calorimeter with 7 ionization layers with strip readout  
~2mm measurement of conversion point, tracking capability, shower profile (from 7 layers + CsI)

- x thicker barrel calorimeter,  $8.3 X_0 \rightarrow 13.4 X_0$

better particle separation

- x TOF system  
particle id (mainly p, n)

# Overview of CMD-3 data taking runs

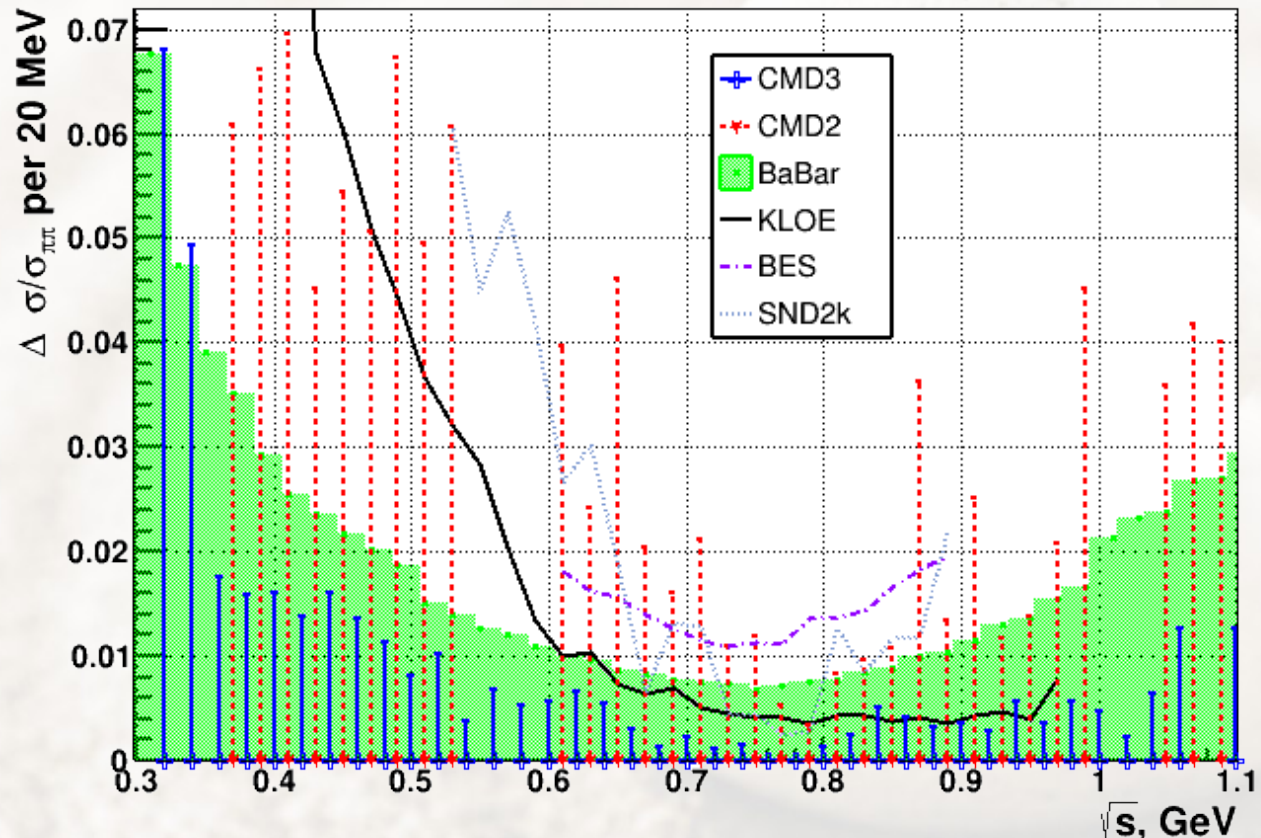


# $e^+e^- \rightarrow \pi^+\pi^-$ by CMD-3

Statistical precision of cross section measurement for seasons at  $< 1 \text{ GeV}$  (2013+2018+2020)  
a few times better than any other experiments

Full statistic up to date  
with  $\rho$  scans

RHO2013  
RHO2018  
LOW2020



Analysis based on  $L = 61.9 \text{ pb}^{-1}$  at  $\sqrt{s} < 1 \text{ GeV}$  (+25.7  $\text{pb}^{-1}$ , 1.0-1.2  $\text{GeV}$ )

$34 \times 10^6 \pi^+\pi^-$ ,  $3.7 \times 10^6 \mu^+\mu^-$ ,  $44 \times 10^6 e^+e^-$   
events selected at  $\sqrt{s} < 1 \text{ GeV}$

# $e^+e^- \rightarrow \pi^+\pi^-$ by CMD3

Very simple topology (just 2 tracks back to back),  
but the most challenging channel  
due to high precision requirement.

Analysis was performed trying to reach systematic  
 $\sim 0.35\text{-}0.5\%$

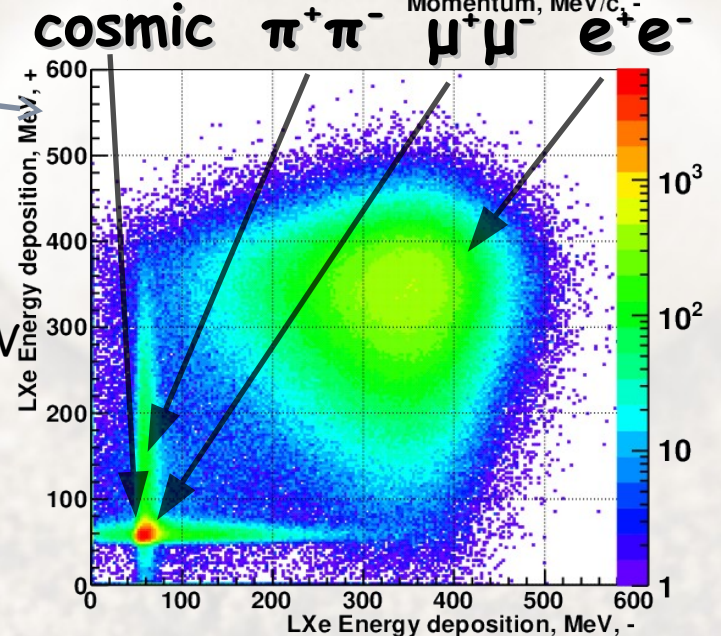
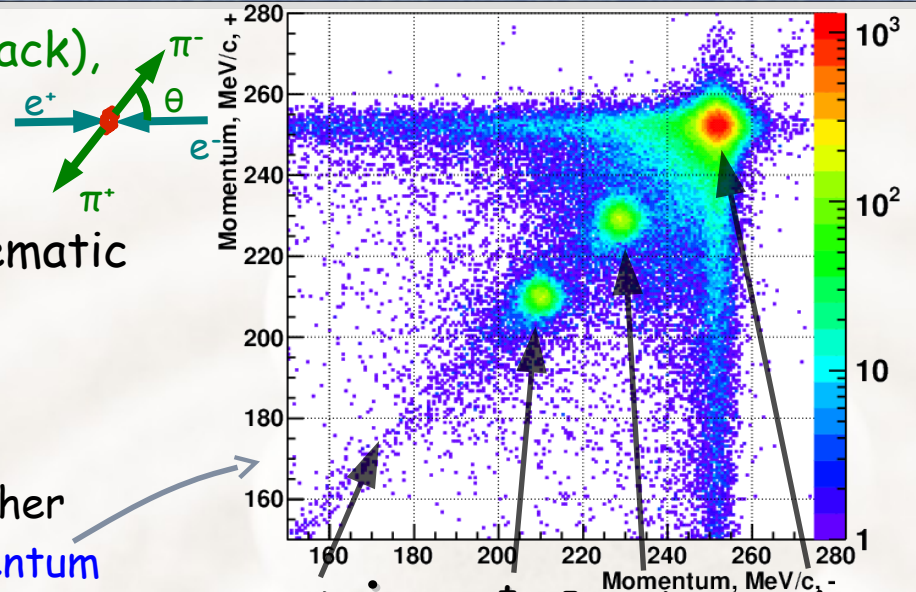
## Crucial pieces of analysis:

- x  $e/\mu/\pi$  separation
- x radiative corrections
- x precise fiducial volume
- x ...

events separation either

- 1) by momentum
- 2) or by energy deposition
- 3) additional cross-check  
by angle distribution

4) using shower profile at  $>1\text{GeV}$



$P^+ \times P^-$   $E_{\text{beam}} = 250 \text{ MeV}$

$E^+_{\text{LXe}} \times E^-_{\text{LXe}}$   $E_{\text{beam}} = 480 \text{ MeV}$

# Form Factor evaluation

$$\sigma_{e^+e^- \rightarrow \gamma \rightarrow \pi^+ \pi^-} = \frac{\pi \alpha^2}{3s} \beta_\pi^3 |F_\pi|^2$$

$$|F_\pi|^2 = \left( \frac{N_{\pi^+ \pi^-}}{N_{e^+ e^-}} - \Delta^{bg} \right) \frac{\sigma_{e^+ e^-}^0 \cdot (1 + \delta_{e^+ e^-}^{rad})}{\sigma_{\pi^+ \pi^-}^0 \cdot (1 + \delta_{\pi^+ \pi^-}^{rad})} \frac{\epsilon_{e^+ e^-}}{\epsilon_{\pi^+ \pi^-}}$$

Ratio  $N_{\pi\pi}/N_{ee}$  is measured directly  $\rightarrow$  detector inefficiencies are partially cancelled out

Mostly no background, Applied if not accounted in particle separation

$$\Delta^{BG} = (N_{bg} / N_{ee})^{simul}$$

Evaluated as ratio to  $e^+e^-$  by simulation. Both BG and  $e^+e^-$  are taken from sim, inefficiencies cancelled out in same way

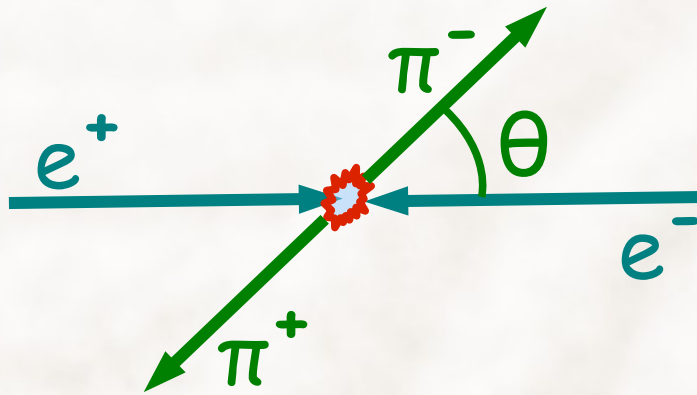
Radiative corrections defined in used acceptance, account for ISR and FSR effects, VP included in  $F_\pi$  definition.

Efficiency analysis rely mostly on the data. Important only difference between  $\pi^+\pi^- / e^+e^-$  (common cancelled out)



# Event selection

Simple event signature with  
2 back-to-back  
charged particles



- Two charged collinear tracks:  
 $|\Delta\phi| < 0.15$ ,  $|\Delta\theta| < 0.25$       $Q_1 + Q_2 = 0$ ,  $|\Delta t| < 20 \text{ nsec}$
- Vertex position close to interaction point:  
 $\rho_{\text{average}} < 0.3 \text{ cm}$ ,  $|Z_{\text{average}}| < 5 \text{ cm}$   
 $|\Delta\rho| < 0.3 \text{ cm}$ ,  $|\Delta Z| < 5 \text{ cm}$
- Fiducial volume inside good region of the DCH:  
 $1. < (\pi + \theta^+ - \theta^-) / 2 < \pi - 1. \text{ rad}$
- Quality of selected tracks:  
 $\chi^2 / \text{ndf} < 10$ ,  $N_{\text{hits}} \geq 10$
- Filtration of low momentum and cosmic background:  
 $0.45 E_{\text{beam}} < p^\pm < E_{\text{beam}} + 100 \text{ MeV}/c$ ,  $p^\pm > 1.15 p_{K^\pm}$

Data sample includes events with:  $e^+e^-$ ,  $\mu^+\mu^-$ ,  $\pi^+\pi^-$ , cosmic muons

Almost no other background at  $\sqrt{s} < 1 \text{ GeV}$

$34 \times 10^6 \pi^+\pi^-$ ,  $3.7 \times 10^6 \mu^+\mu^-$ ,  $44 \times 10^6 e^+e^-$  events selected at  $\sqrt{s} < 1 \text{ GeV}$

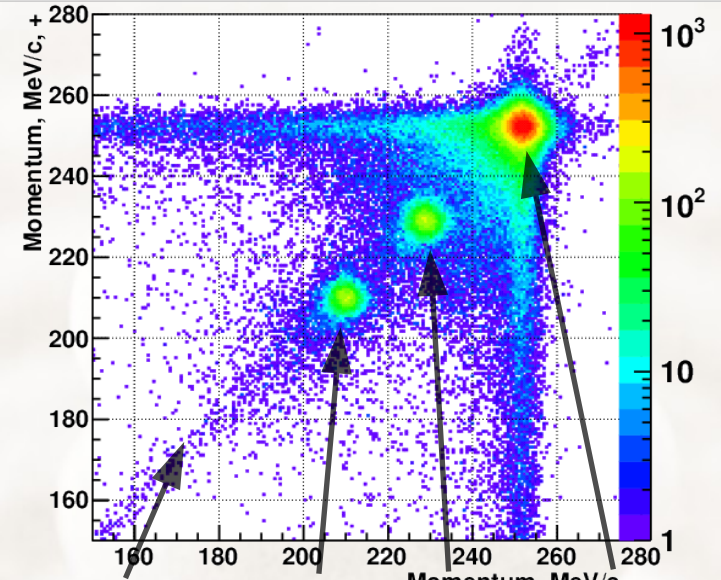
# Event separation

events separation either

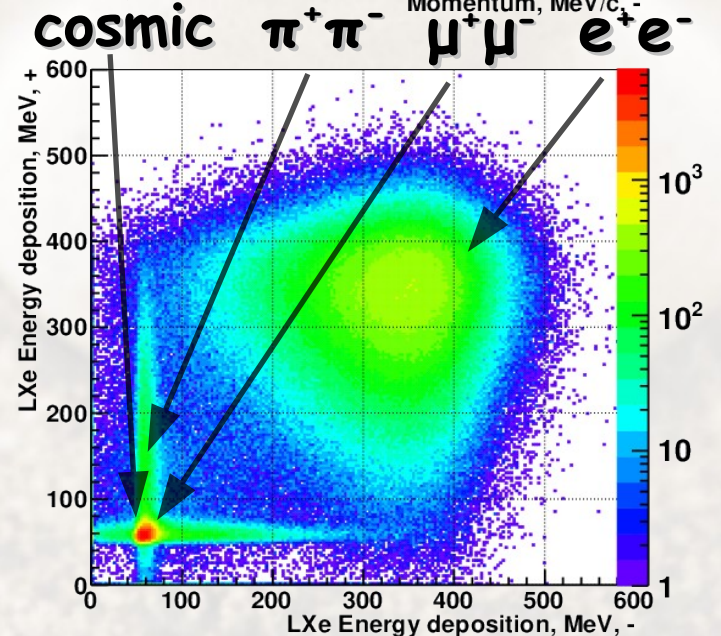
- 1) by momentum
- 2) or by energy deposition

Separation of  $\pi^+\pi^-$ ,  $\mu^+\mu^-$ ,  $e^+e^-$ , ... final states is based on likelihood minimization:

$$-\ln L = - \sum_{events} \ln \left[ \sum_i N_i f_i(X^+, X^-) \right] + \sum_i N_i$$



$P^+ X P^-$   $E_{beam} = 2550 \text{ MeV}$



$E^+ X E^-$   $E_{beam} = 480 \text{ MeV}$

# Event separation

Separation of  $\pi^+\pi^-$ ,  $\mu^+\mu^-$ ,  $e^+e^-$ , ... final states is based on likelihood minimization:

$$-\ln L = - \sum_{\text{events}} \ln \left[ \sum_i N_i f_i(X^+, X^-) \right] + \sum_i N_i$$

Momentum-based separation:

PDFs are constructed as:

MC generator spectra are convolved with detector response function (momentum resolution, bremsstrahlung, pion decays)

36 free parameters in fit per each point

Energy deposition-base separation:

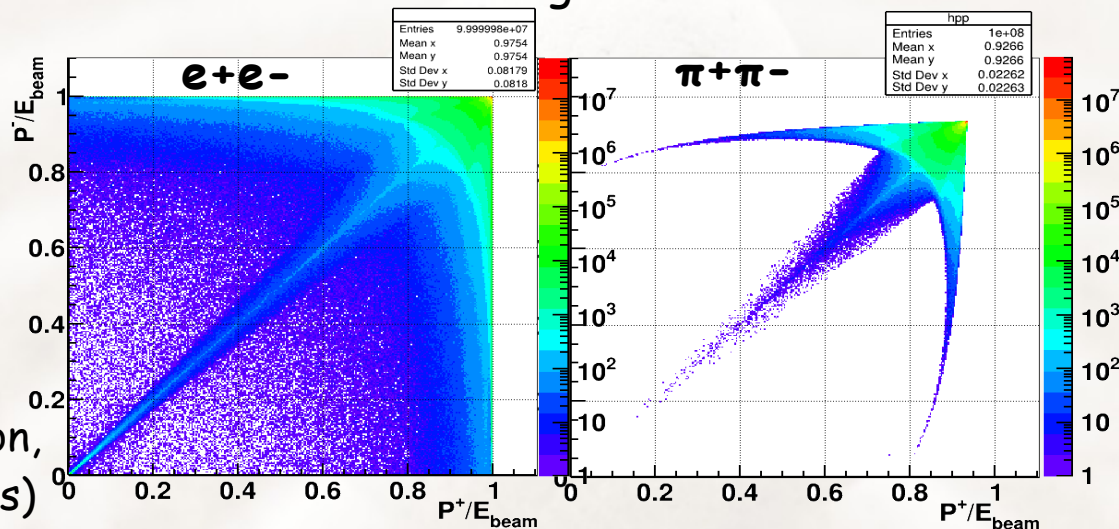
PDFs is described by a generic functional form (log-gaus, etc), trained on the data: by tagged electron, cosmic muons

56 free parameters in fit

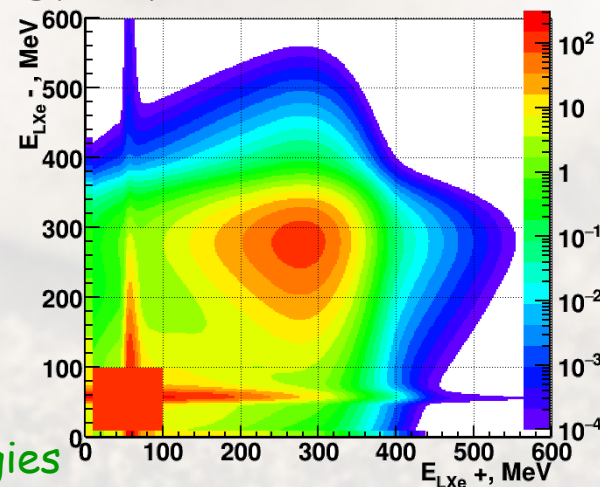
$N_{\pi\pi}/N_{ee}$  - one of the free parameters,

$N_{\mu\mu}/N_{ee}$  - fixed from QED (free at  $\sqrt{s} < 0.7 \text{ GeV}$ )

Momentum PDF's ingredients from MC generator



Energy deposition summed PDF



Possible biases are checked on full MC  $\rightarrow$  systematics 0.2% at  $\rho$  energies

# Angle distribution fit

$d\sigma/d\theta$  spectra from MC Generators  
 + all efficiencies/smearing effects  
 extracted from data and full simulation  
 (cosmic is taken from data itself)

$N_{\mu\mu} / N_{ee}$  - fixed from QED (+efficiencies)

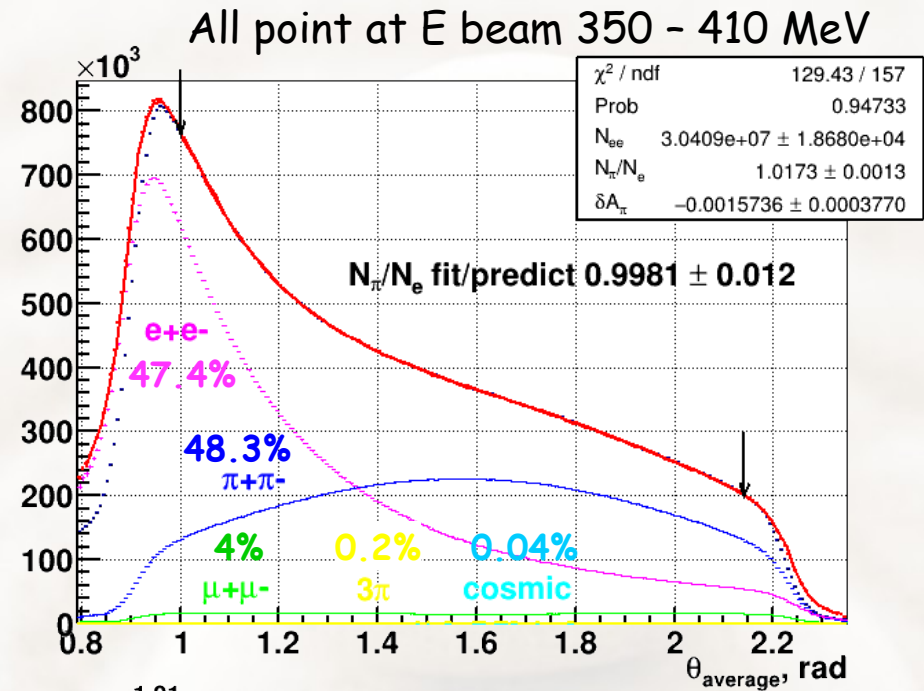
$N$  cosmic,  $3\pi$  - from momentum based  
 separation

$N_{\pi\pi} / N_{ee}$ ,  $\delta A$  - free parameters

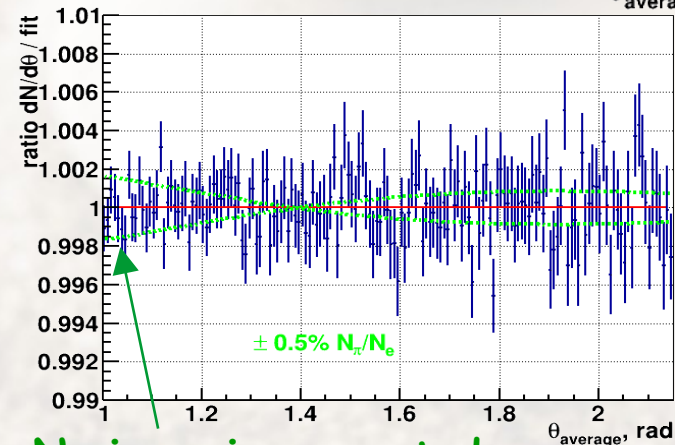
Combined fit on all points around  $\rho$ -peak

$\sqrt{s} = 0.7 - 0.82 \text{ GeV}$

$$N_{\pi\pi} / N_{ee} = 1.0173 \pm 0.0013$$



Fit by  $\theta$  distribution



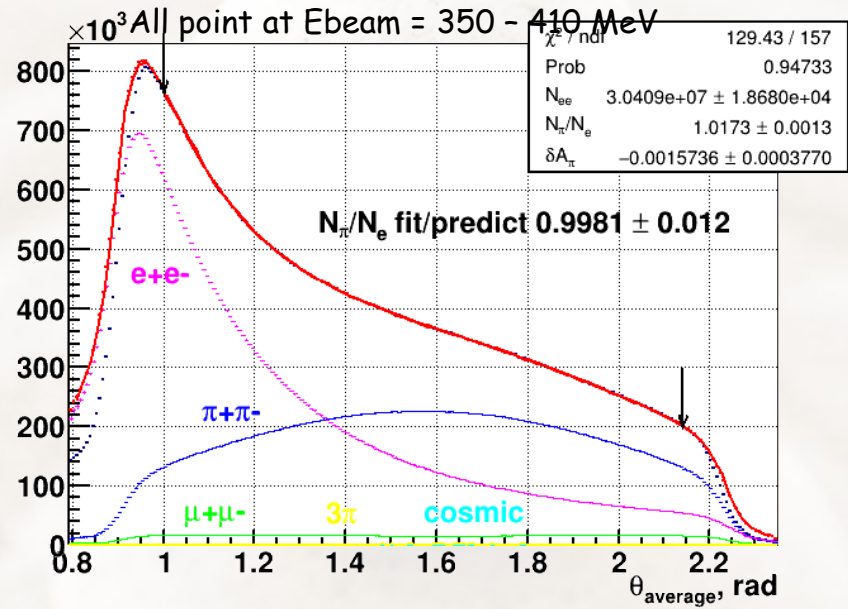
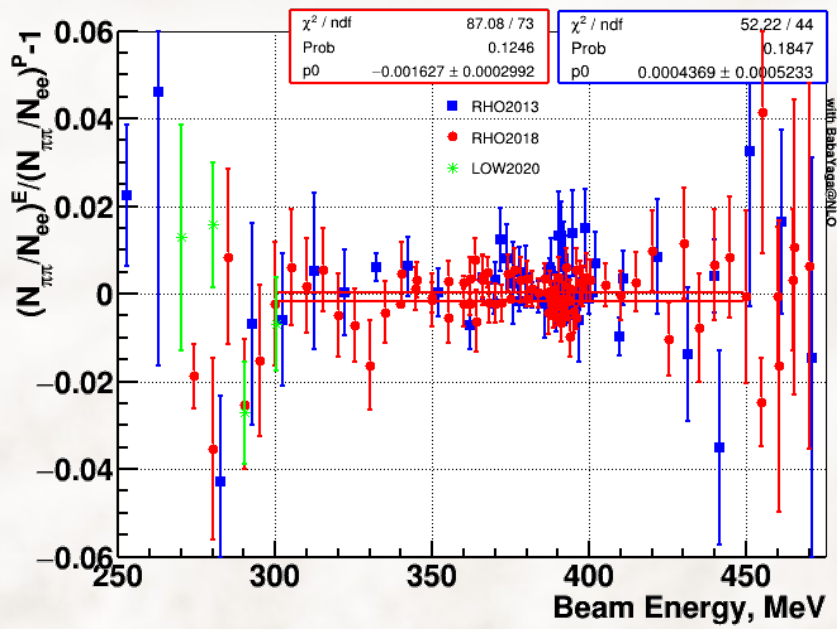
No issue in accounted  
 efficiency at  $\theta = 1 \text{ rad}$

# e/ $\mu$ / $\pi$ separation

3 methods for  $N_{\pi\pi} / N_{ee}$  determination based on independent informations:

- 1) Momentum from DCH
- 2) Energy deposition in LXe
- 3) angles in DCH

E vs P separations



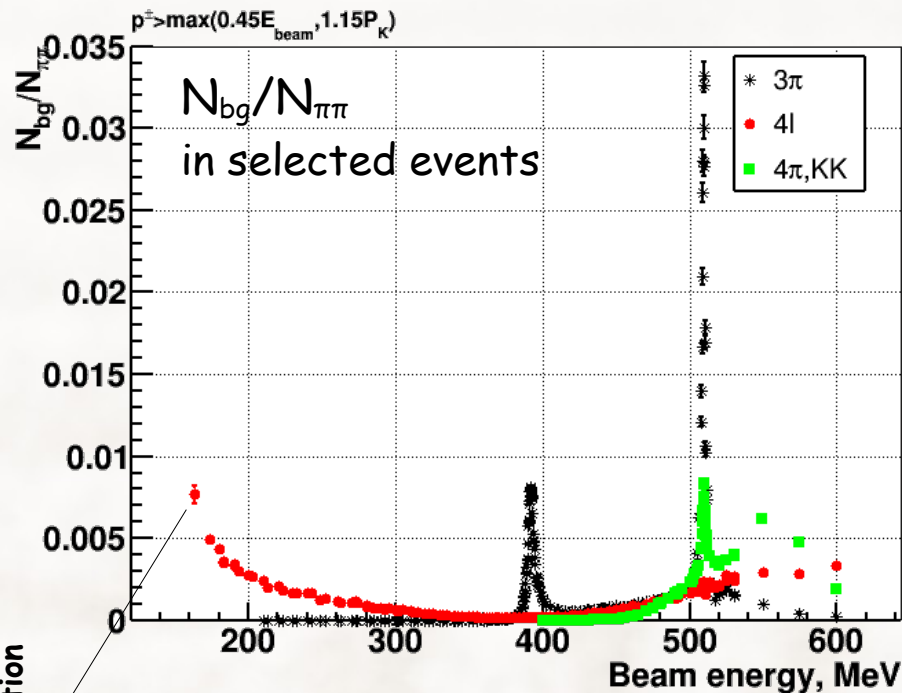
Fit by  $\theta$  distribution

For sum of  $\sqrt{s} = 0.7 - 0.82$  GeV points  
by momenta in DCH:  $N_{\pi\pi} / N_{ee} = 1.0193 \pm 0.00030$   
by energies in LXe  $\Delta N_{\pi\pi} / N_{ee} = -0.09 \pm 0.024\%$   
from theta with free  $\delta A$ :  $= -0.20 \pm 0.12\%$   
 with fixed  $\delta A=0$ :  $= +0.21 \pm 0.07\%$

consistency at  $\sim 0.2\%$

Common stat from  $\sqrt{N}$ :  
0.026%

# Background



All possible background contributions to the selected collinear data sample:

$$e^+e^- \rightarrow \pi^+\pi^-\pi^0$$

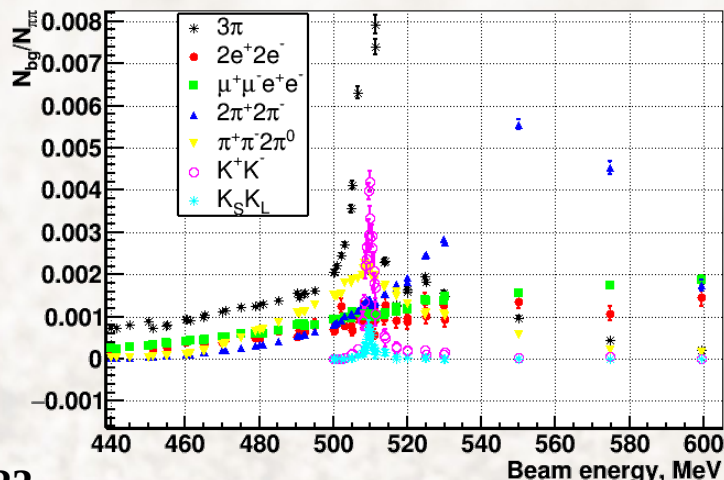
$$e^+e^- \rightarrow e^+e^-e^+e^-, e^+e^-\mu^+\mu^-$$

$$e^+e^- \rightarrow K^+K^-, K_S K_L, \pi^+\pi^-\pi^+\pi^-, \pi^+\pi^-\pi^0\pi^0$$

Cross-check of proper accounting with stronger momentum cut:

$P^+ > 0.45 E_{\text{beam}} \rightarrow > 0.6 E_{\text{beam}} (> 1.15 p_K \rightarrow > 1.2 p_K)$   
 reduces by **30-50%**  $3\pi$  and to **1./5** of  $2K, 4\pi$   
 $\rightarrow \Delta|F|^2/|F|^2 \sim 0.02\%$  (at  $\omega$ )  
 0.05% (at  $\phi$ )

Effect on  $N_{\pi\pi}/N_{ee}$   
after separation  
only  $\sim 0.2\%$



BG systematic error to  $F_\pi$ :

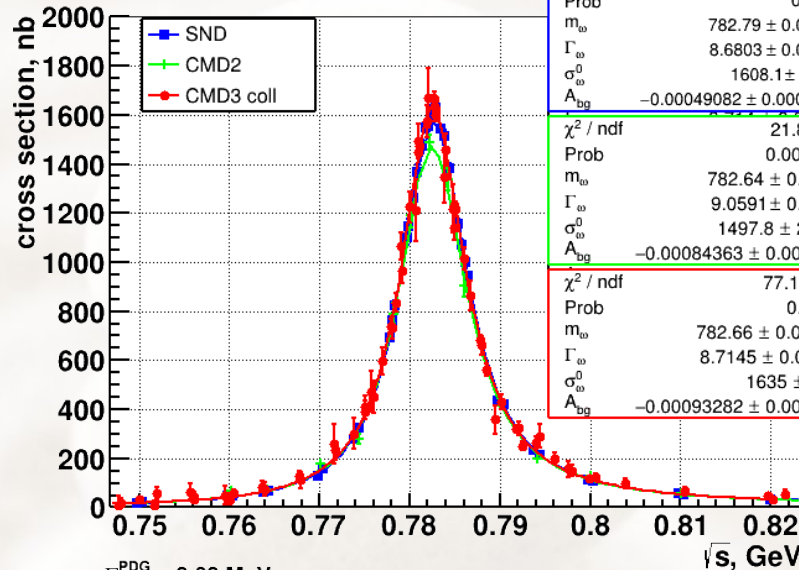
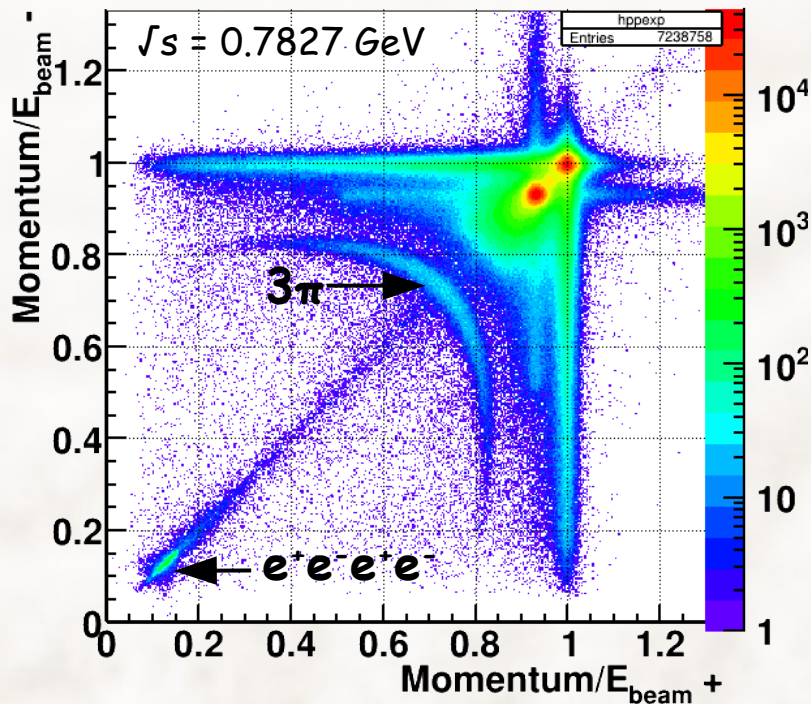
0.05% (at  $\omega$ ), 0.2% (at  $\phi$ ),

0.-0.15% ( $\sqrt{s}=0.9-1.2\text{GeV}$ )

$$e^+e^- \rightarrow \pi^+\pi^-\pi^0$$

$\sigma(e^+e^- \rightarrow \pi^+\pi^-\pi^0)$  within collinear events

Collinear events are selected for  $2\pi$  analysis

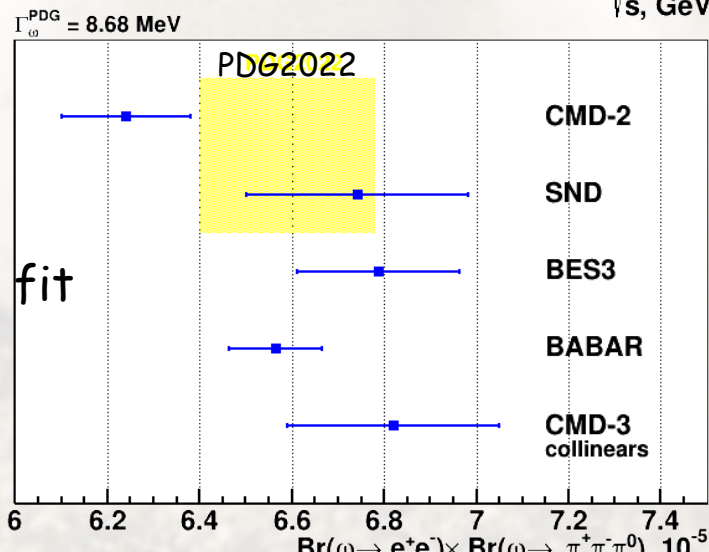


$\chi^2 / \text{ndf}$	40.733 / 37
Prob	0.30956
$m_\omega$	$782.79 \pm 0.025632$
$\Gamma_\omega$	$8.6803 \pm 0.037507$
$\sigma_\omega^0$	$1608.1 \pm 7.1207$
$A_{\text{bg}}$	$-0.00049082 \pm 0.00023768$
$\chi^2 / \text{ndf}$	21.868 / 9
Prob	0.0093073
$m_\omega$	$782.64 \pm 0.11782$
$\Gamma_\omega$	$9.0591 \pm 0.18778$
$\sigma_\omega^0$	$1497.8 \pm 26.255$
$A_{\text{bg}}$	$-0.00084363 \pm 0.0026238$
$\chi^2 / \text{ndf}$	77.152 / 71
Prob	0.28853
$m_\omega$	$782.66 \pm 0.048209$
$\Gamma_\omega$	$8.7145 \pm 0.095681$
$\sigma_\omega^0$	$1635 \pm 9.271$
$A_{\text{bg}}$	$-0.00093282 \pm 0.0024148$

$e^+e^- \rightarrow \pi^+\pi^-\pi^0$  is background for  $\pi^+\pi^-$  analysis (0.8% at  $\omega$ )  
 Number of  $3\pi$  events is additional parameter in likelihood fit  
 Main systematics (2.4%) inaccuracy of  $\rho\pi$  - model for efficiency determination, **total 3.3%**

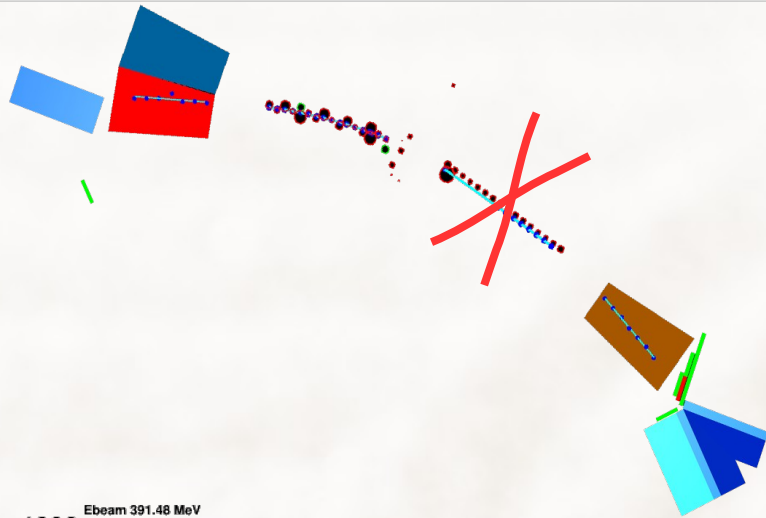
$$B(\omega \rightarrow e^+e^-)B(\omega \rightarrow \pi^+\pi^-\pi^0) = (6.82 \pm 0.04 \pm 0.23) \times 10^{-5}$$

confirm SND@VEPP-2M result



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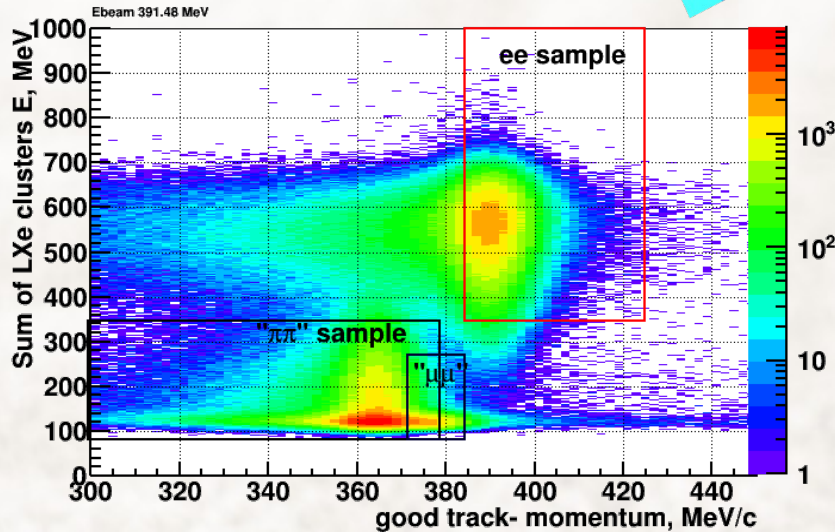
# Efficiency



Assuming independence of Calorimeter & Tracker,  
Using the "test" sample based on LXe information:

**two collinear clusters are detected + one good track**

gives possibility to study track reconstruction  
inefficiency



Event type is tagged by  
energy deposition and momentum of good track

The "test" sample includes only partially some specific  
losses (when second compatible cluster is not produced):  
pion decay, nuclear interaction, .. (~30% ineff. accounted)  
electron bremsstrahlung (~5% accounted)

N.B. Correlated inefficiency study was also performed  
without requirement on detection of one good track



# Inefficiency of Nhit cut

Number of hits on track starts to decrease at edge of the DCH

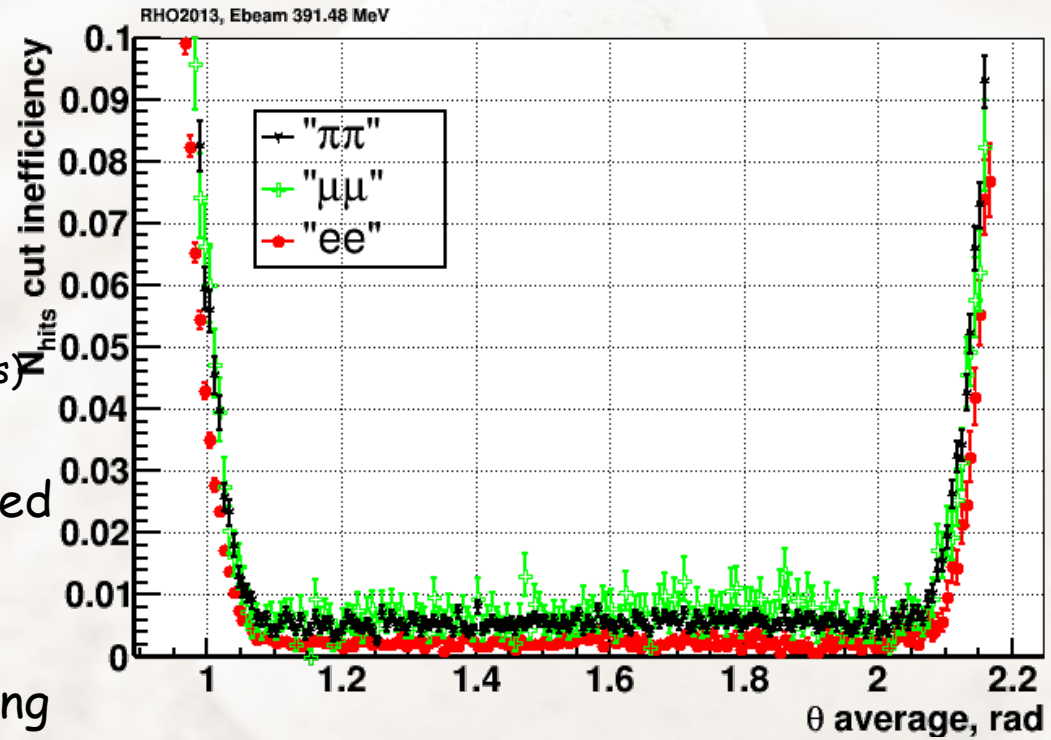
Inefficiency need to be taken into account in same  $\theta_{event}$  definition (as average over two tracks)

Evaluated on the same collinear sample as used in the  $|F_{\pi}|^2$  measurement

Event types are tagged by Edep, P

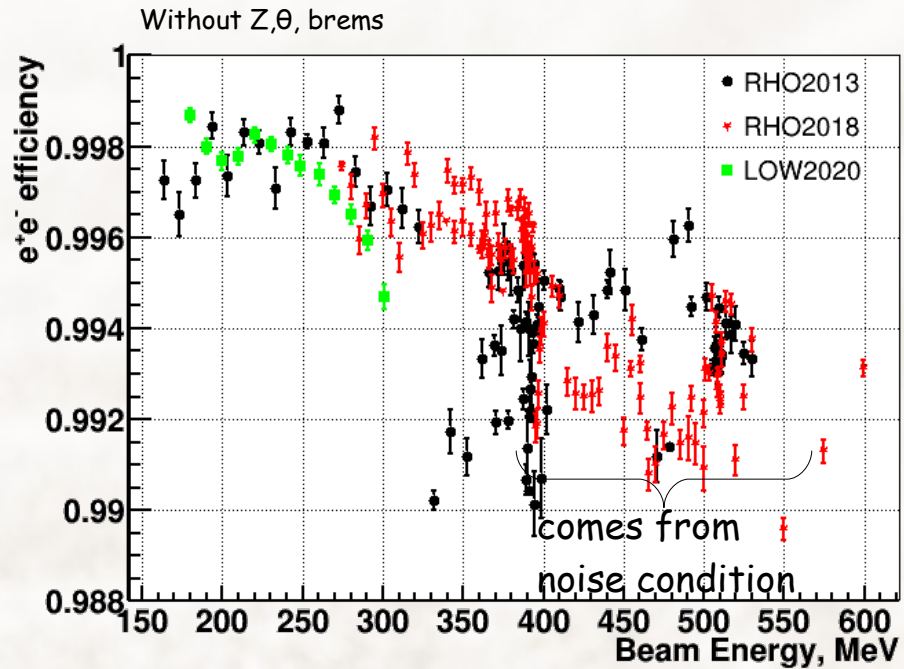
Inefficiency is evaluated by Nhit cut releasing

$$\varepsilon^{nhits} = \frac{N^{events}(\text{tracks with } nhit \geq 10)}{N^{events}(\text{tracks just reconstructed})}$$



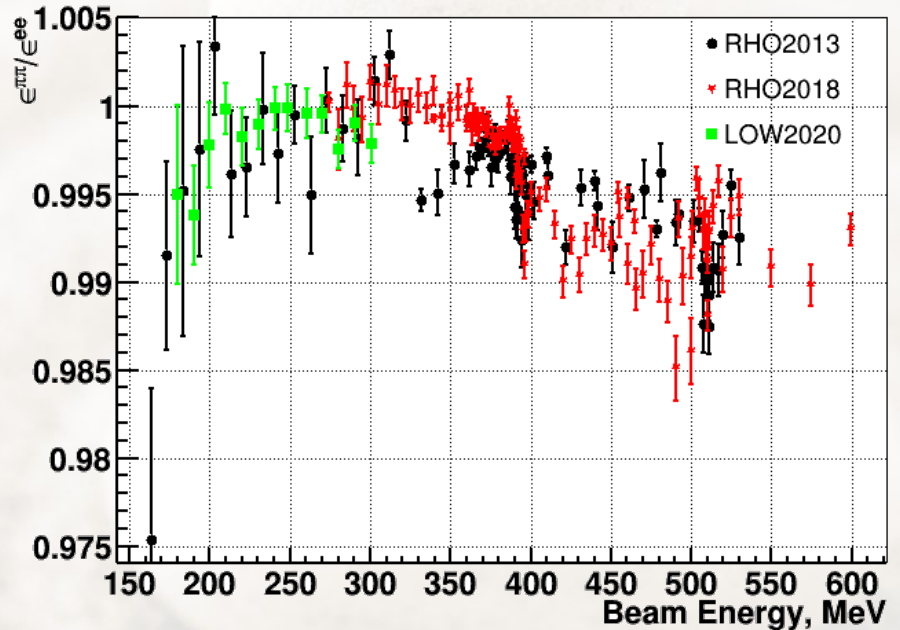
# Base efficiencies

$$\epsilon_{e^+e^-}$$



$$\epsilon_{\pi^+\pi^-} / \epsilon_{e^+e^-}$$

Efficiency without particles specific losses

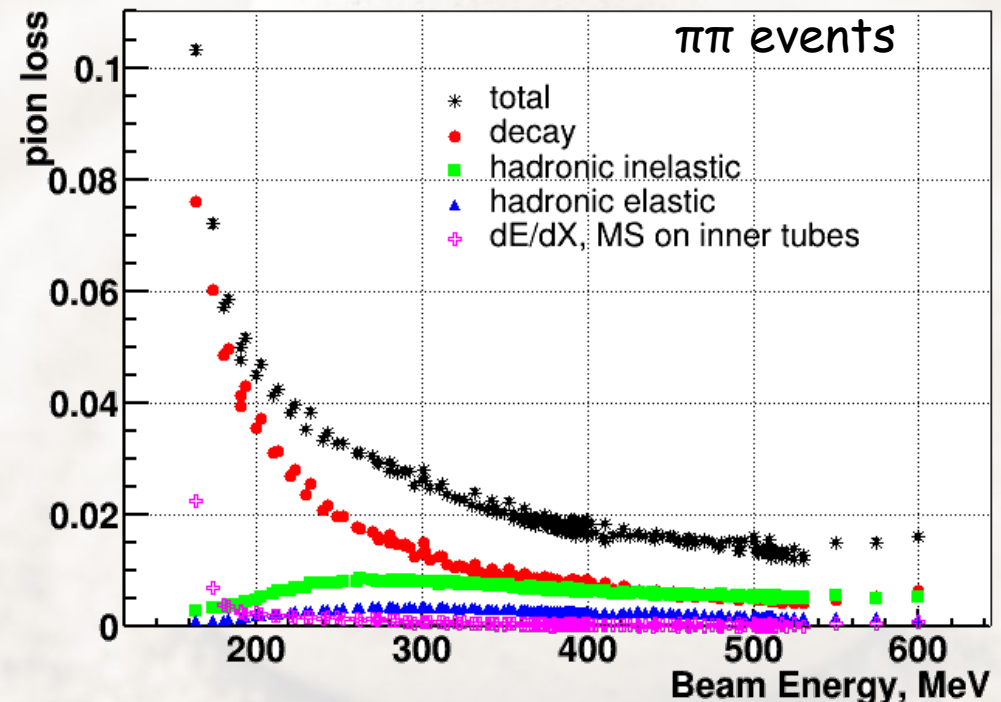
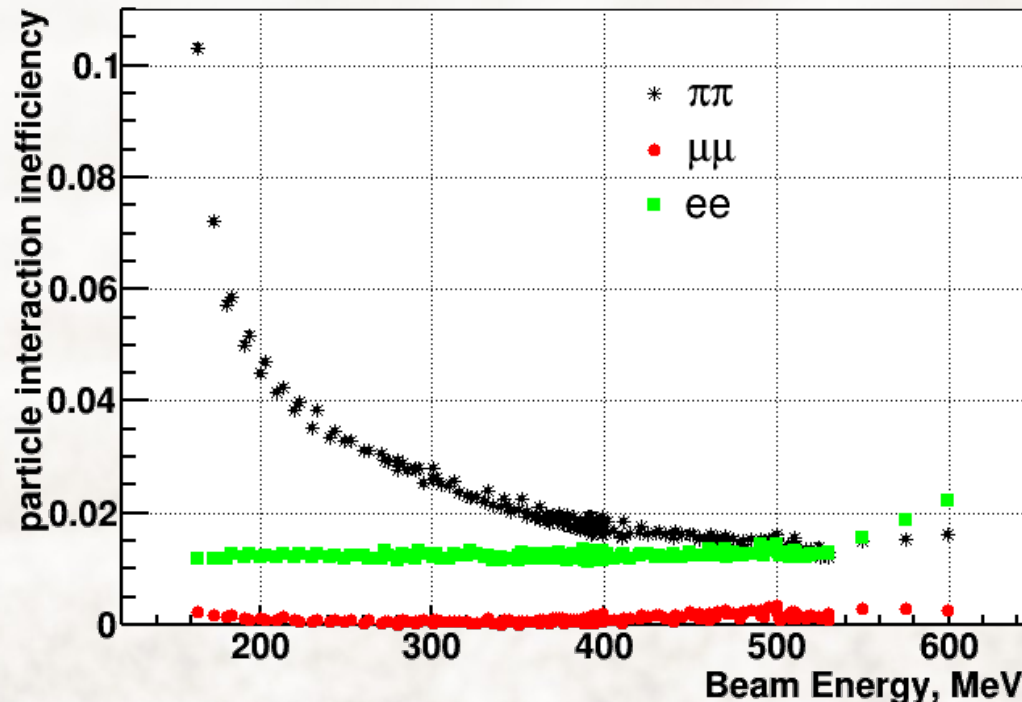


# Particle specific losses

bremsstrahlung energy loss, decay in flight, nuclear interaction with materials, MS on the inner vacuum tube, ...

Taken from detailed full MC (includes detector conditions with time)

but it is also controlled by the data

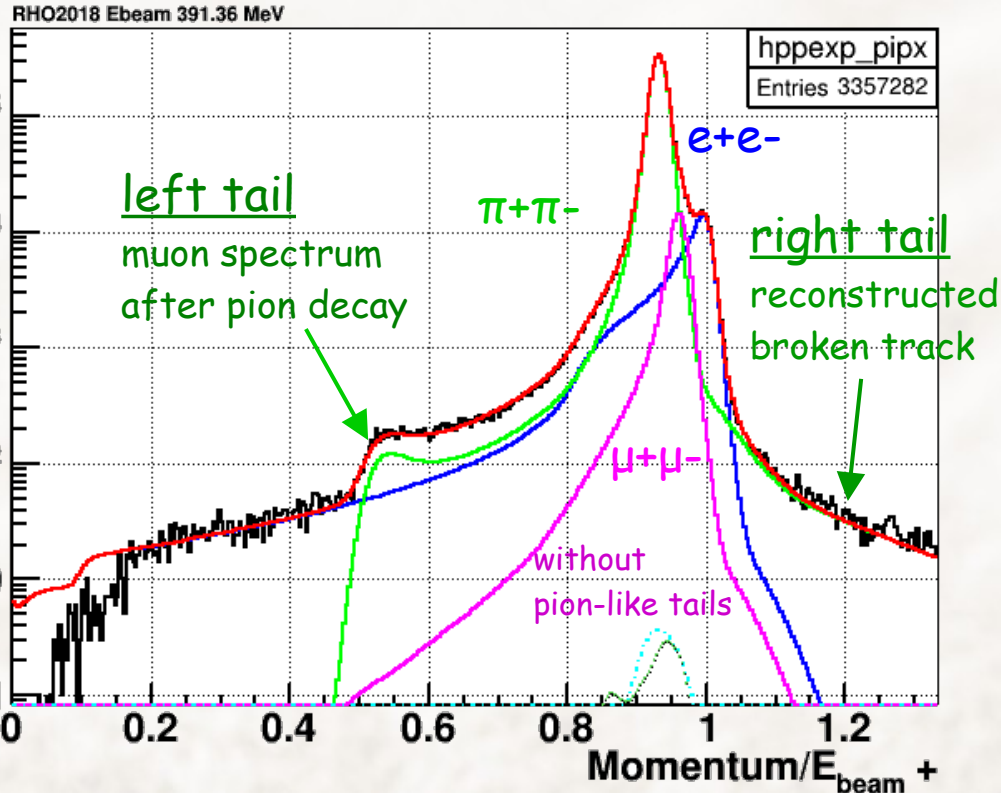


nuclear interactions mostly on inner tube (systematics 0.2%)

most dangerous is decay in flight as it depends on detector conditions (syst. 0.2-0.1%)

# Pion decay inefficiency

Experimental  $P^+$  spectrum  
with  $|P^- - P_\pi| < 10 \text{ MeV}$



Decay in flight - depends on DCH efficiency

controlled by number of events in tails  
in the data vs simulation

Tails function taken from full MC  
(include DCH inefficiencies, resolutions,  
amplitudes, correlated noises per layers, etc..)  
Number of events in tails are free parameters  
in momentum-based separation

$N_{\text{event}}^{\text{in tails}}$  consistent with sim at  $\sim 3\%$

$\rightarrow$  systematic uncertainty of  $N_{\pi\pi}$

0.2-0.1% (from low to  $\rho$ )

(N.B. simplified DCH descriptions gives 15% discrepancies on tails)

Additional crosscheck with «weak» cuts:

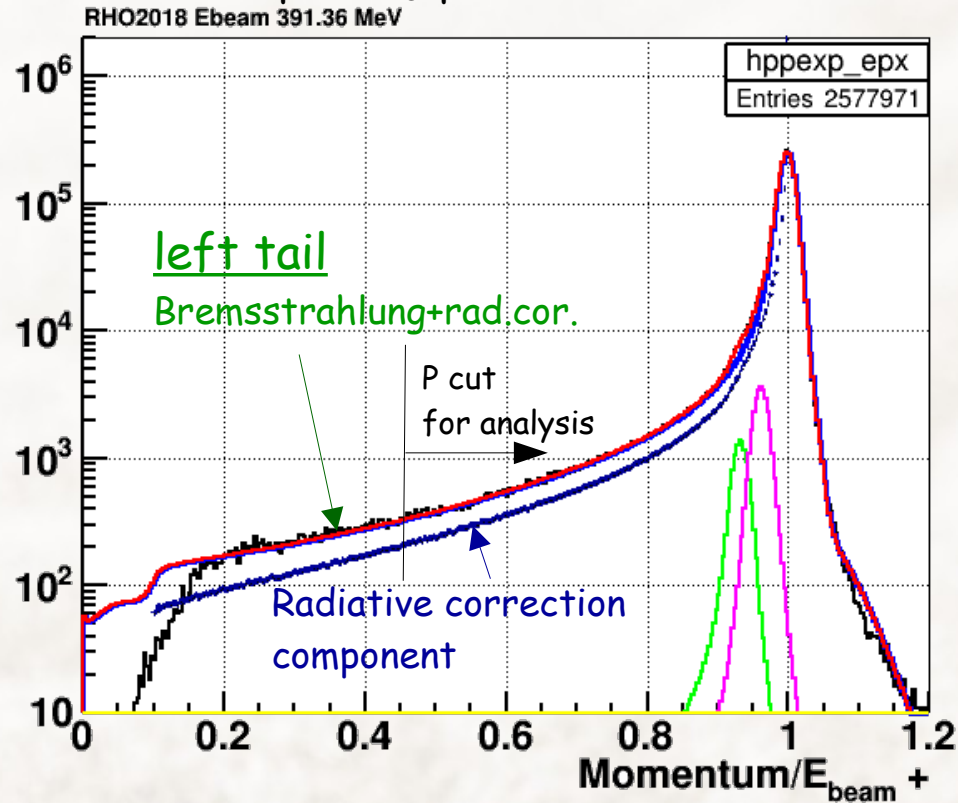
$N_{\text{hits}} \geq 10 \rightarrow 8$ ,  $\chi^2 < 10 \rightarrow 20$ ,  $|\Delta\rho| < 0.3 \rightarrow 0.6 \text{ cm}$

pion decay inefficiency changes by  $\times 1./ (2.-2.5)$

$\rightarrow \Delta|F|^2 / |F|^2 < 0.05\%$

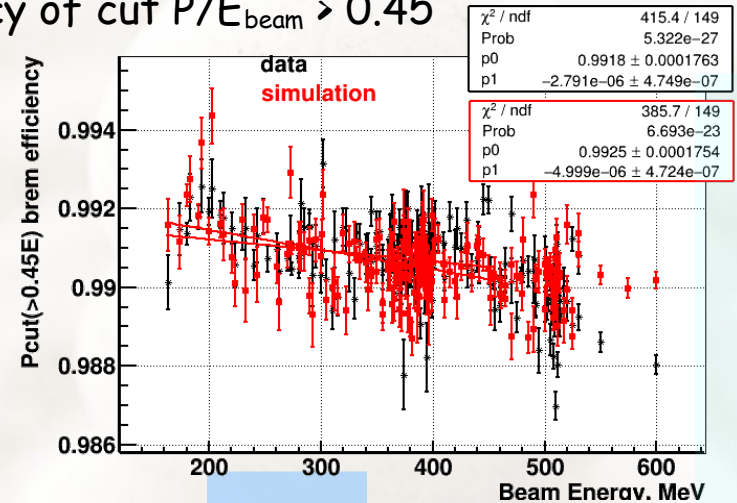
# Bremsstrahlung loss on vacuum tube

Experimental  $P^+$  spectrum  
with  $|P^- - P_e| < 10 \text{ MeV}$

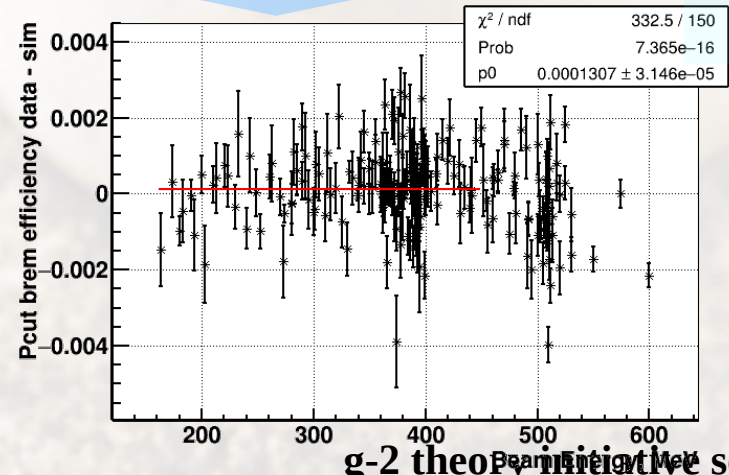


Brems. description is part of detector response function in momentum-based separation (with  $X/X_0$  as free param.)  
 $X/X_0$  of inner wall consistent with sim. within  $<5\%$   
→ Systematics on  $|F_\pi|^2 \sim 0.05\%$

Part of brems. correction (0.9% from 1.2%) can be extracted from fitted spectra:  
inefficiency of cut  $P/E_{\text{beam}} > 0.45$



The data vs sim agree  $\sim 0.02\%$



MCGPJ vs Babar/Yaga spectra gives difference  $<0.015\%$

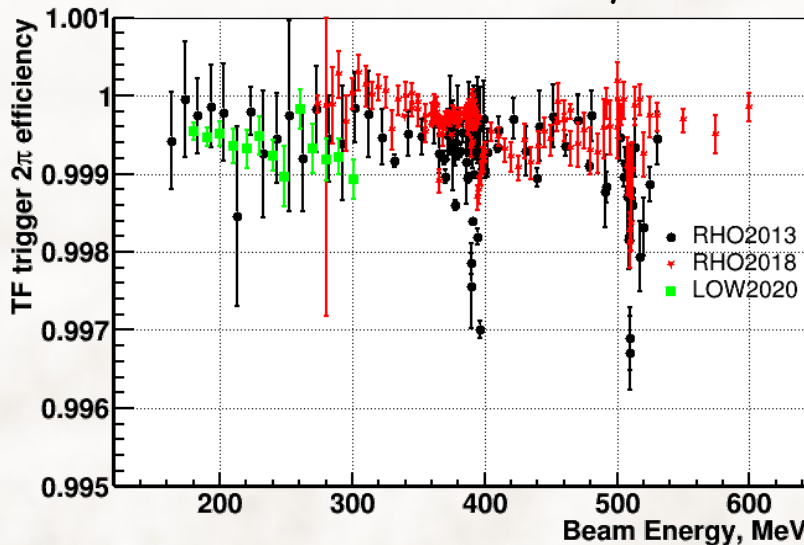
# Trigger inefficiency

Two independent triggers were used based on tracking or calorimeter information

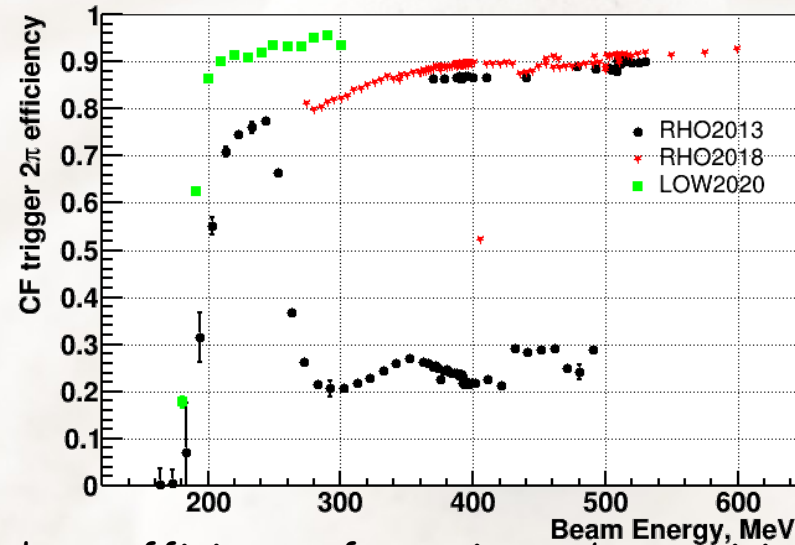
**TF:** 3 groups of fired wires in DCH from one track

**CF:** Energy deposition above threshold

TrackFinder 2 $\pi$  efficiency



ClusterFinder 2 $\pi$  efficiency



Having two “independent” triggers allows to study an efficiency of certain one by requiring that other presents in an event:

$$\epsilon_{TF}^{trig} = \left( N_{TF \& CF} / N_{CF} \right) / \left( \epsilon_{TF \& CF}^{rec} / \epsilon_{CF}^{rec} \right)$$

Efficiency correction accounts for correlation via time response

Trigger efficiencies are evaluated from dependence with polar angle (TF), with energy of two clusters (CF)

**Total TF|CF:  $\rightarrow \sim >0.9994$  for 2 $\pi$  events (and higher for e+e-)**

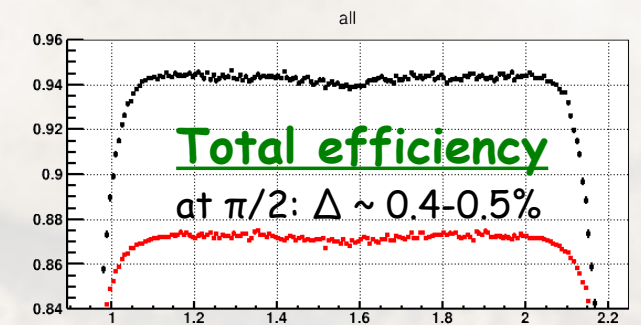
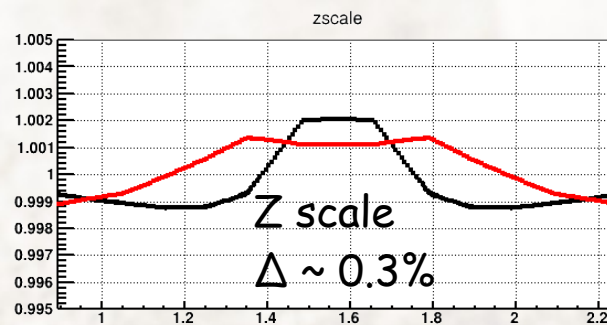
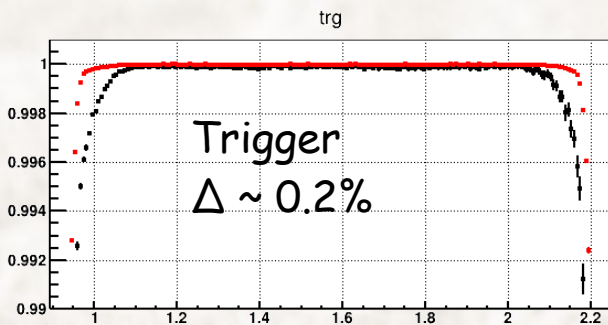
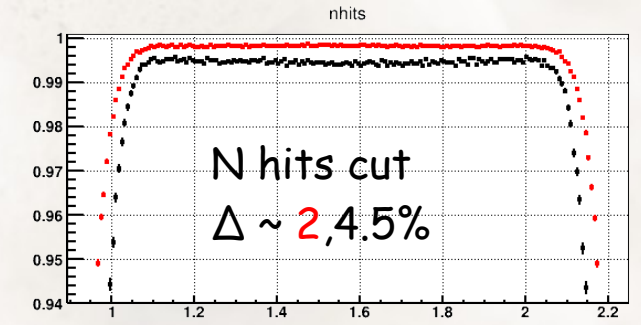
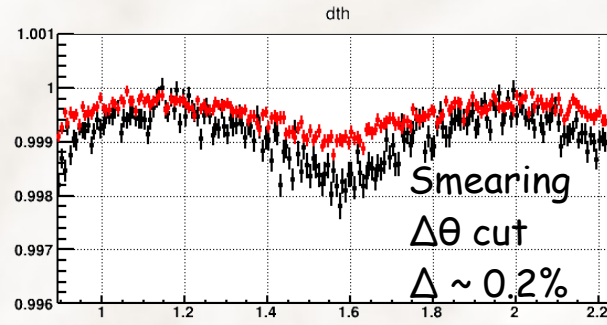
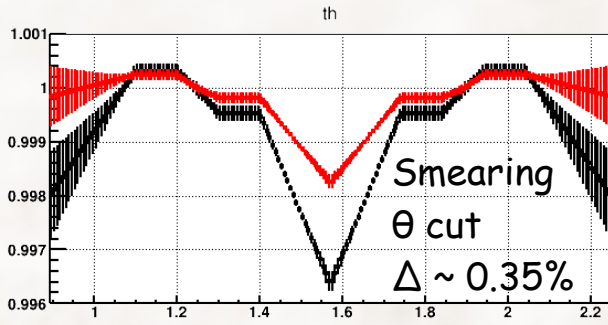
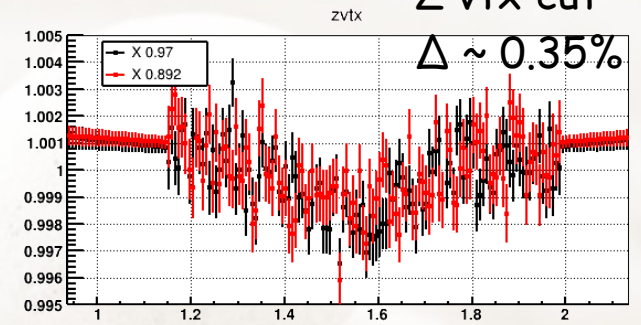
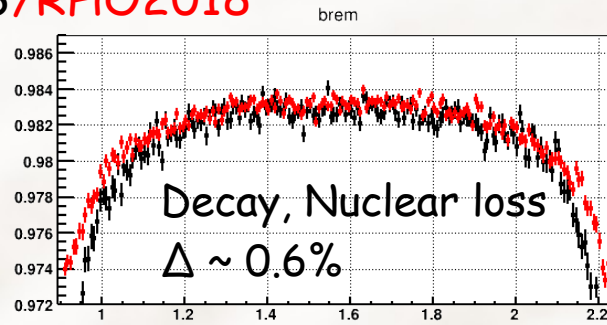
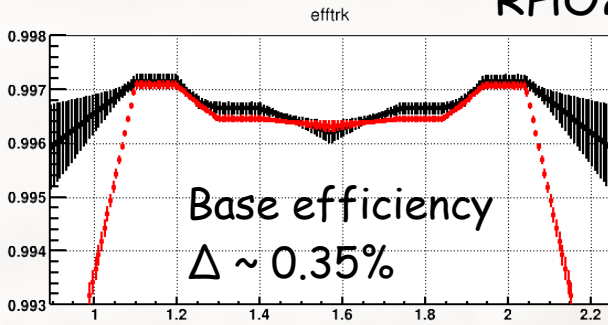
Out-of-sync trigger issue gives 0.1-0.5% effect to lose both tracks

$\rightarrow$  trigger systematics **0.05% (<1GeV) - 0.3% (>1GeV)** - as difference between 2 $\pi$ /e+e-

# $\pi^+\pi^-$ efficiency vs $\theta$ polar angle

RHO2013/RHO2018

Z vtx cut



Average at  $p$ -peak over  $\sqrt{s} = 0.7-0.82$  GeV

# Radiative corrections

Measurement of  $e^+e^- \rightarrow \pi^+\pi^-$  requires high precision calculation of radiative corrections.

Two high precision MC generators is used

MCGPJ(0.2%,  $e^+e^-$ ,  $\mu^+\mu^-$ ,  $\pi^+\pi^-$ ) vs BabaYaga@NLO (0.1%,  $e^+e^-$ ,  $\mu^+\mu^-$ )

They include exact NLO + Higher Order terms in some approximation.

$e^+e^- \rightarrow e^+e^-(\gamma)$  : great consistency  $<0.1\%$  in the total cross section

$e^+e^- \rightarrow \mu^+\mu^-(\gamma)$  : Mass term in FSR is missed in most of generators  
(effect 0.4% at  $\sqrt{s}=0.32$  GeV)

$e^+e^- \rightarrow \pi^+\pi^-(\gamma)$  : only MCGPJ available with 0.2% precision  
(for energy scan experiments)

Achieved precision in current analysis is also sensitive  
for precision of differential cross sections predictions

$e/\pi$  separation by momentum requires  $d\sigma/dP^+dP^-$  spectra as initial input

Asymmetry study requires  $d\sigma/d\theta$  spectra



# Radiative corrections

**BaBaYaga@NLO shows better agreement with the data:**

1) Momentum spectras better describe data:  
gives consistent results in  $N_{\mu\mu}/\text{QED}$   
(effect on  $|F_{\pi}|^2 \sim 0.2\%$  at  $\sqrt{s}=0.78 \text{ GeV}$ , and rising to 1.5%  
at 0.9 GeV when using momentum-based separation)

2) Experimental asymmetry in  $e+e-$  data  
relative to BabaYaga@NLO:

$$\delta A = -0.060 \pm 0.026 \%$$

relative to MCGPJ

$$\delta A = -0.140 \pm 0.026 \%$$

BabaYaga@NLO consistent with NNLO MCMule

$$\delta A = +0.006 \pm 0.003 \%$$

We adopted generators usage in this way:

$e+e-$  : BabaYaga@NLO

$\mu+\mu-$  : BabaYaga@NLO (differential cross section)

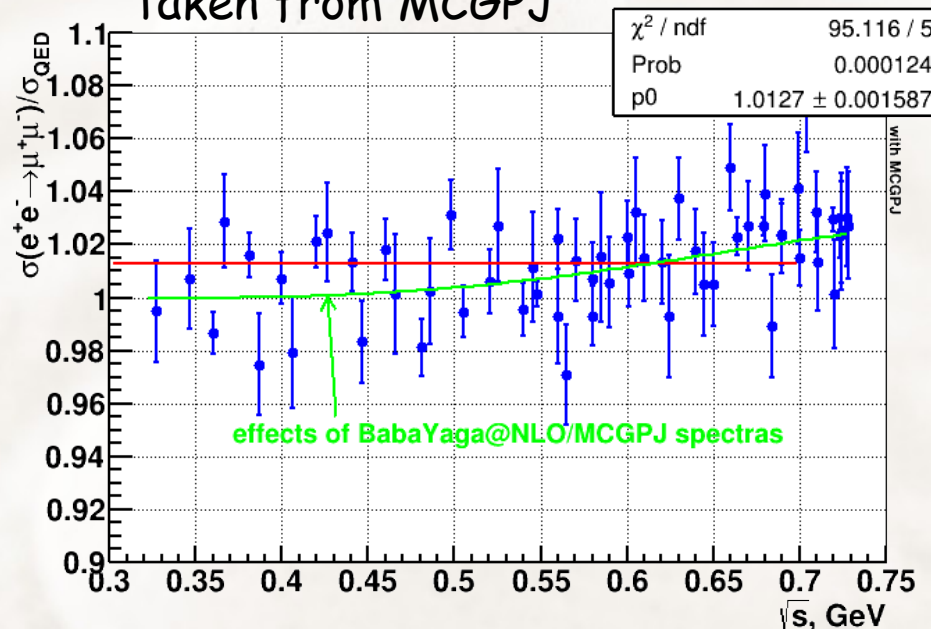
MCGPJ (integral)

$\pi+\pi-$  : MCGPJ

effect on  $N_{\mu\mu}/\text{QED}$

when input  $d\sigma/dP^+dP^-$  spectra

taken from MCGPJ



MCGPJ/BabaYaga@NLO difference gives systematics  
on  $|F_{\pi}|^2_{\pi}$  when using momentum-based separation

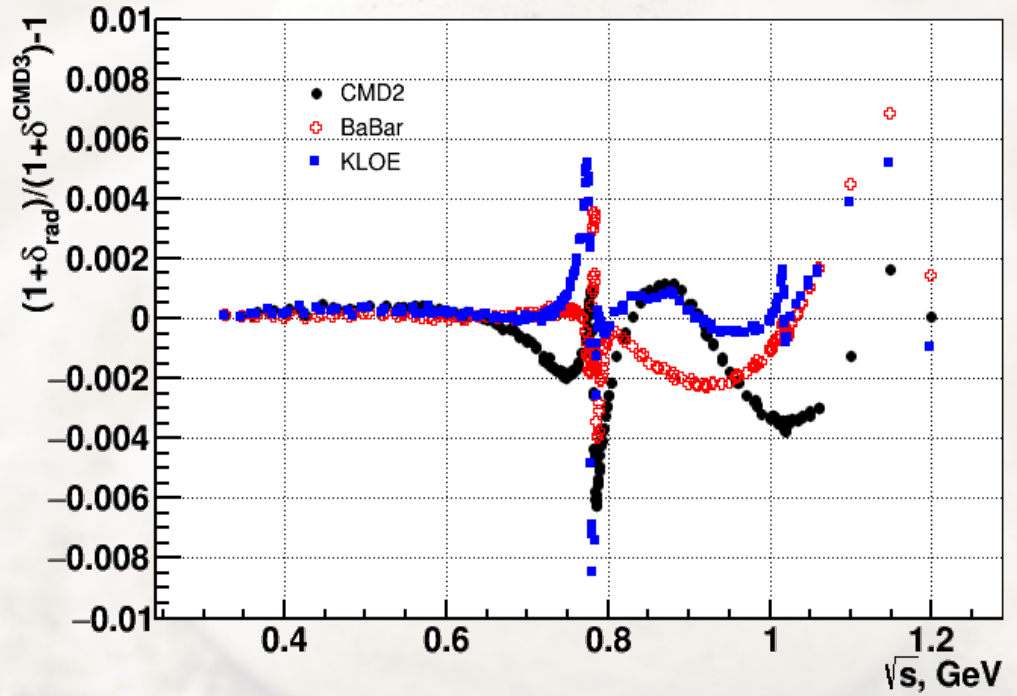
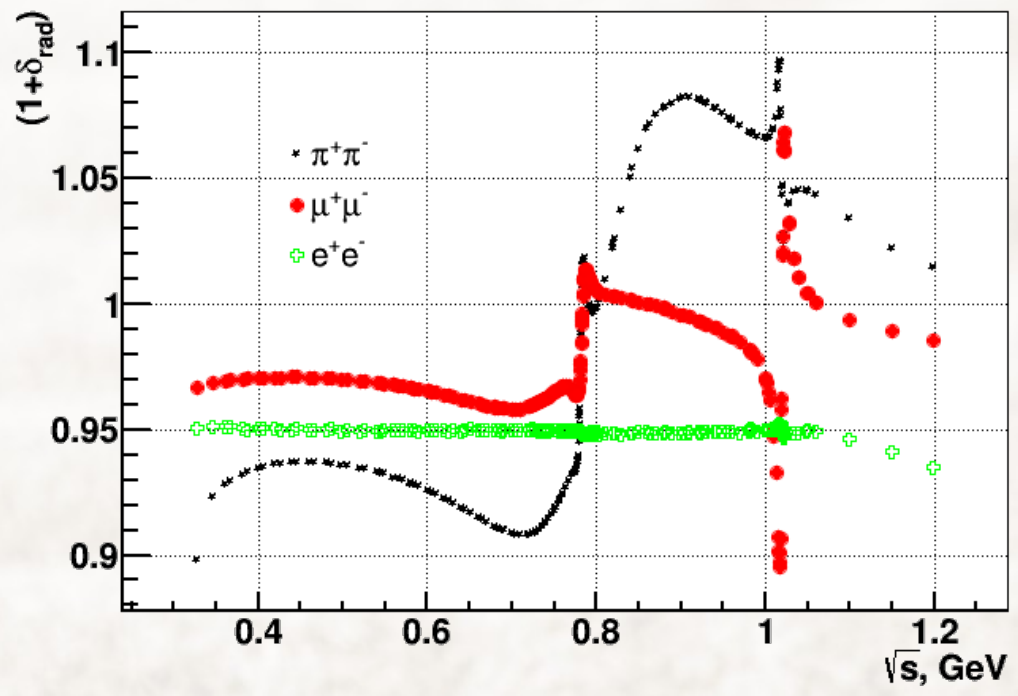
**Better NNLO generators are needed for higher  
precision**

# Radiative corrections

Radiative corrections within

$$1. <(\pi+\theta^+ - \theta^-)/2 < \pi - 1.\text{rad}, \quad |\Delta\phi| < 0.15, \quad |\Delta\theta| < 0.25$$

Effect on  $2\pi$  radiative correction from different  $|F|^2_\pi$  parametrizations (over different datasets)



Systematic uncertainty

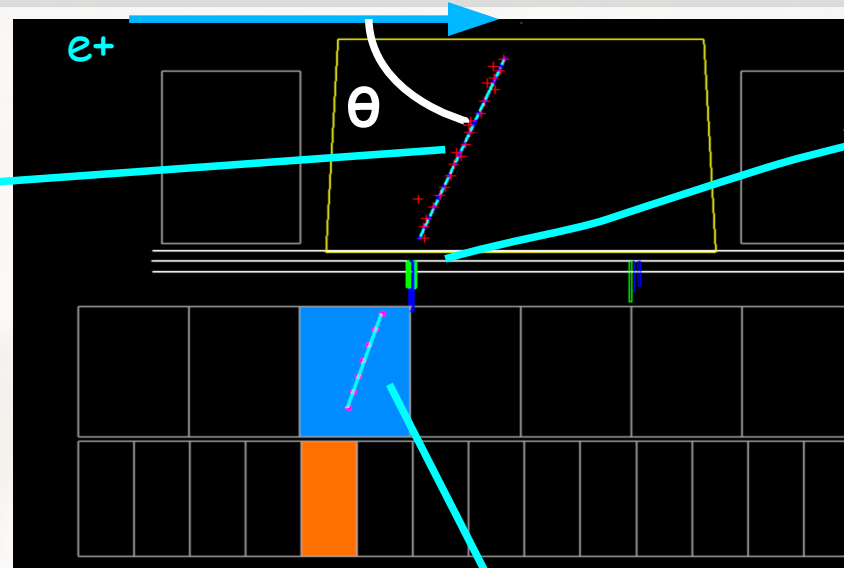
$$0.2\% (\pi + \pi -) \oplus 0.2\% (F\pi, s > 0.74 \text{ GeV}) \oplus 0.1\% (e+e-)$$

N.B. KLOE/BABAR systematic difference in derivative 4%/0.4GeV,  
in CMD-3 is also possible up 1%/0.1 GeV  $\rightarrow$  same 0.2% estimation (from  $F\pi$  model)

# Precision of fiducial volume

Polar angle measured by DCH chamber with help of charge division method

(Z resolution  $\sim 2\text{mm}$ ),  
Unstable, depends on calibration and thermal stability of electronic  
Calibration done relative to LXe (ZC)



## ZC chamber

(was in operation until mid 2017)  
multiwire chamber with 2 layers and with strip readout along Z coordinate

strip size: 6mm  
Z coordinate resolution  $\sim 0.7\text{ mm}$   
(for  $\theta_{\text{track}} \sim 1\text{ rad}$ )

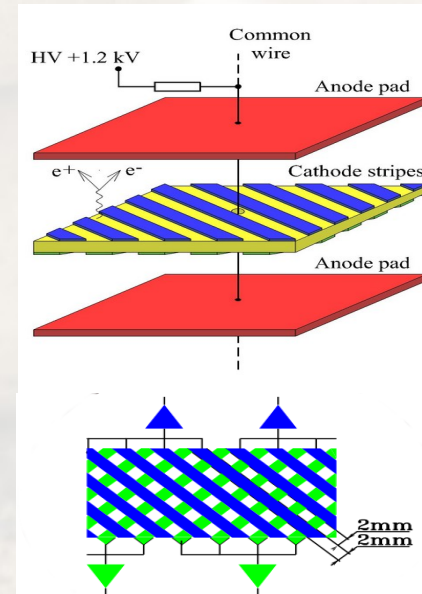
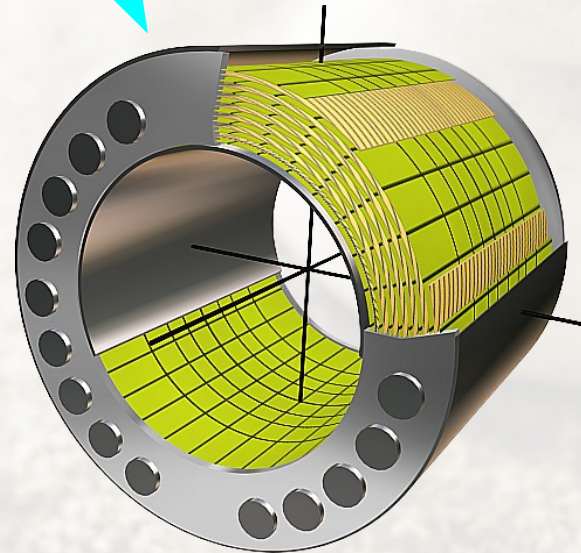
## LXe calorimeter

ionization collected in 7 layers with cathode strip readout,

combined strip size: 10-15 mm  
Coordinate resolution  $\sim 2\text{mm}$

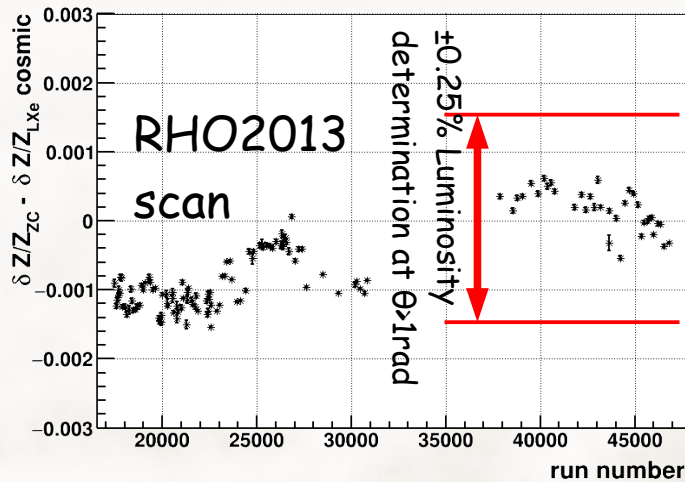
strip precision, coordinate biases  $\sim 100\text{ }\mu\text{m}$   
should give  $\sim 0.1\%$  in Luminosity determination

Can be spoiled by noise environment



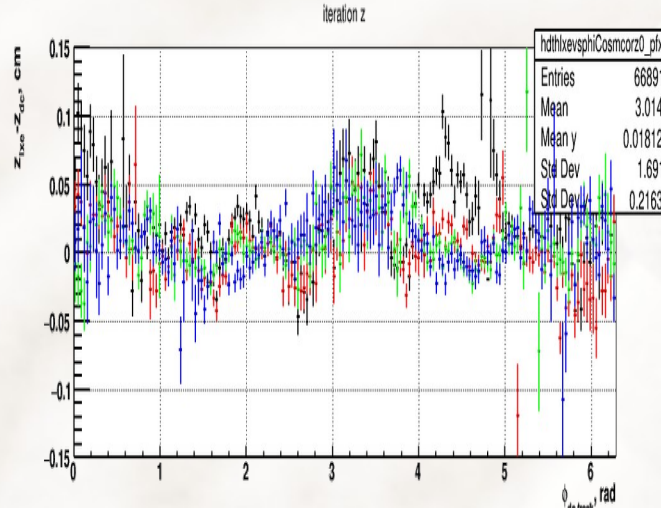
# Precision of fiducial volume

Monitoring of z-measurement between ZC vs LXe



Variation because of DCh instability, different B field, ZC, LXe noise level

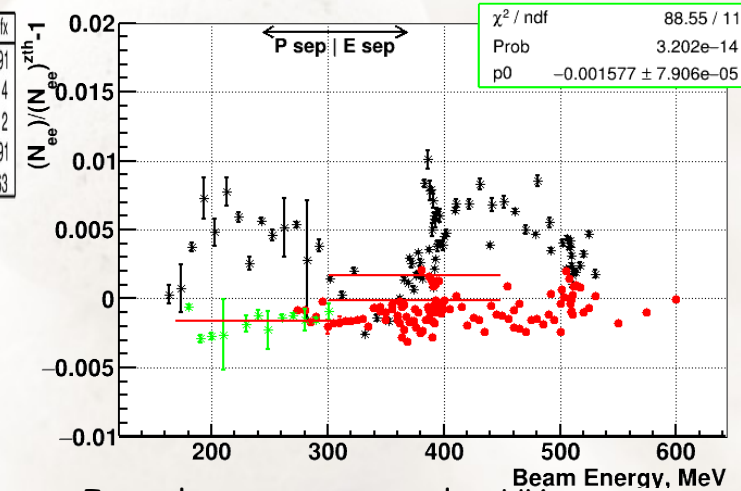
DC tracks vs LXe points



$\delta z \sim 0.5 \text{ mm}$  instability over regions at  $R=40 \text{ cm}$  (by  $\phi$ , track direction, etc)

N.B. in average  $\langle \delta z \rangle$  should be better

Inner DC radius effect:  $\theta$  - angle with Z vertex constrained vs unconstrained case for 2 tracks



Inner layers operate at low HV  $\rightarrow$  Low resolution, higher systematics  
 During RHO2013: 4 middle layers in DCH were switched off  $\rightarrow$  higher weights of inner layers

N.B.  $\theta$  - angle is defined with vertex constrain  $\rightarrow$  inner radius biases should be suppressed

Inner DC radius effect:

ZC/LXe comparison

0.25%

Systematic uncertainty to  $|F_\pi|^2$   
 LXe/ DC comparison

$\oplus$

0.3%

$\oplus$

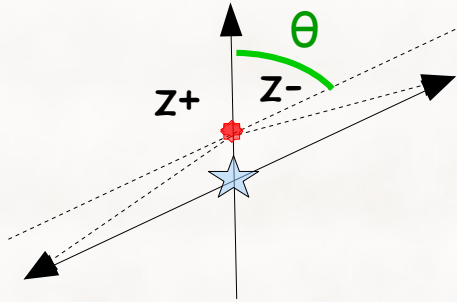
0.7%(RHO2013)/0.3%(RHO2018)

= 0.8% (RHO2013) / 0.5%(RHO2018)

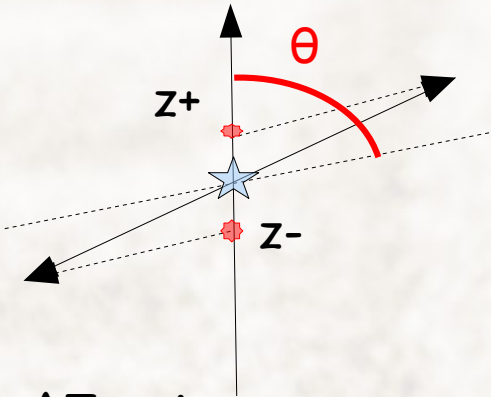
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# DCH's Inner radius effect on polar angle

$$\theta^{\text{event}} = (\theta^+ + \pi - \theta^-) / 2$$



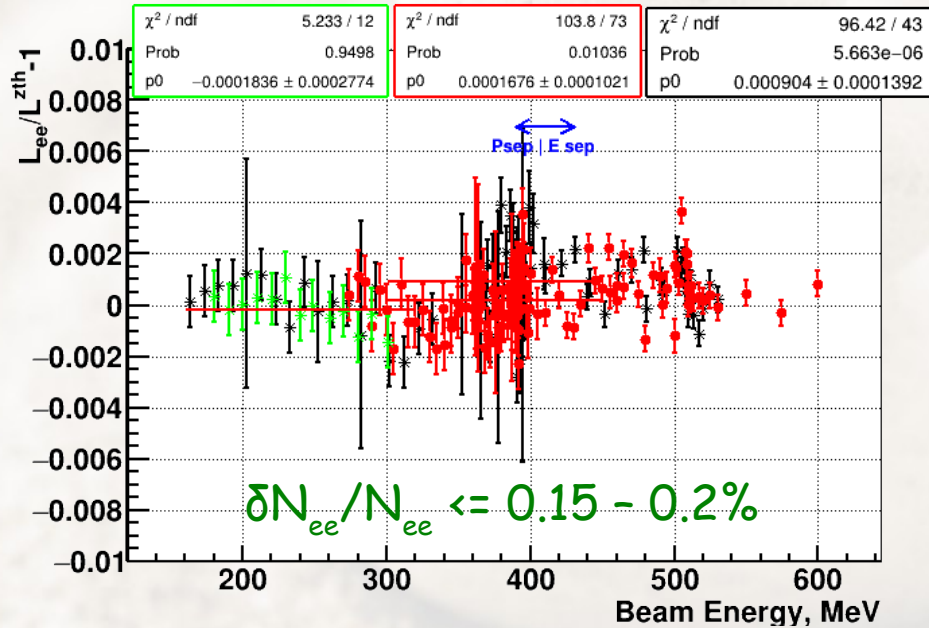
common Z vertex bias of +/- tracks doesn't give bias to  $\theta^{\text{event}}$



$\Delta Z$  at inner vertex gives bias to  $\theta^{\text{event}}$

The analysis uses  $\theta$  angle with Z vertex constrain  
 → inner radius biases should be suppressed

$\Delta Z$  correction can be applied for vertex unconstrained case,  
 + additional vs LXe monitoring on the same collinear events sample



Comparison of  
 Constrain/unconstrained  $\theta$ -angle  
 after  $\Delta Z$ , + vs LXe corrections

Conservative angle related systematics is kept 0.3/0.7% (RHO2013)  
 as Z-vertex constrained/unconstrained cases differences for  $\theta^{\text{event}}$   
 (without corrections)

# $F_\pi$ within different $\theta$ selection

Dependence on theta cut  $\theta_{\text{cut}} < \theta^{\text{event}} < \pi - \theta_{\text{cut}}$

or asymmetrical selection  $1 < \theta^{\text{event}} < \pi/2$  (or  $\pi/2 < \theta^{\text{event}} < \pi - 1$ )

Average at  $2E = 0.7-0.82 \text{ GeV}$

$|F_\pi|^2$  stable at  $<0.05-0.1\%$  level  
within different angle selections

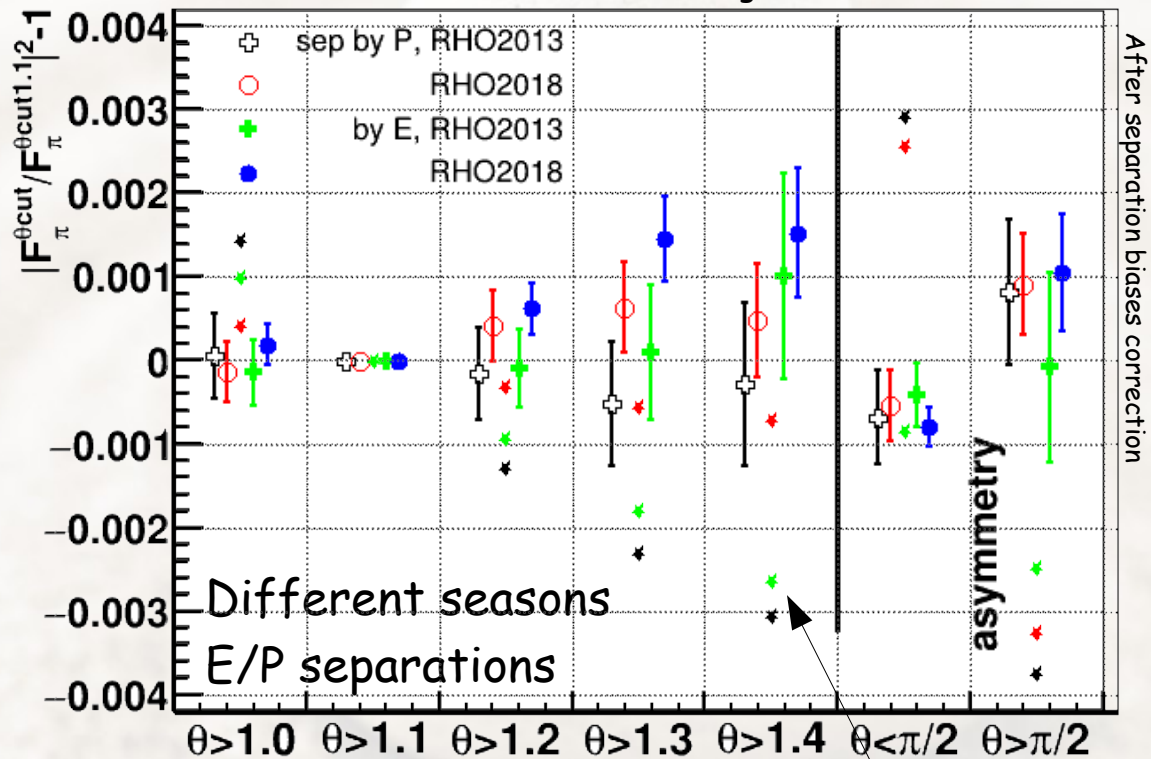
Angle related systematic uncertainty  
estimation is quite conservative:  
0.8% (RHO2013) / 0.5% (RHO2018)

Simplest possible systematics in  $\theta$  angle:

Z - length mis-calibration

$\Theta^{\text{event}}$  common bias

should be seen with  $\sim 0.3-0.4\%$  on this plot



With 0.5% systematic at 1 rad

$\star$  Z-length mis-calibration

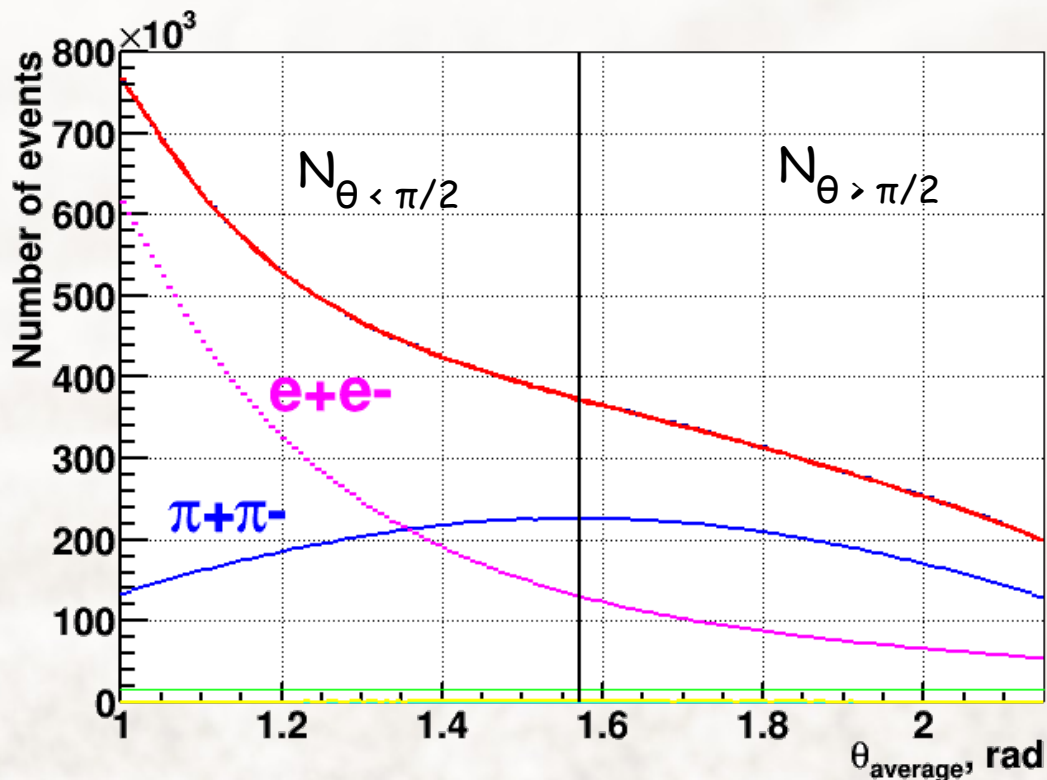
$\star$   $\theta$  bias

$\star$   $\theta$  bias opposite

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# Forward backward charge asymmetry

## $d\sigma/d\theta$ spectra



Asymmetry definition:

$$A = (N_{\theta < \pi/2} - N_{\theta > \pi/2})/N$$

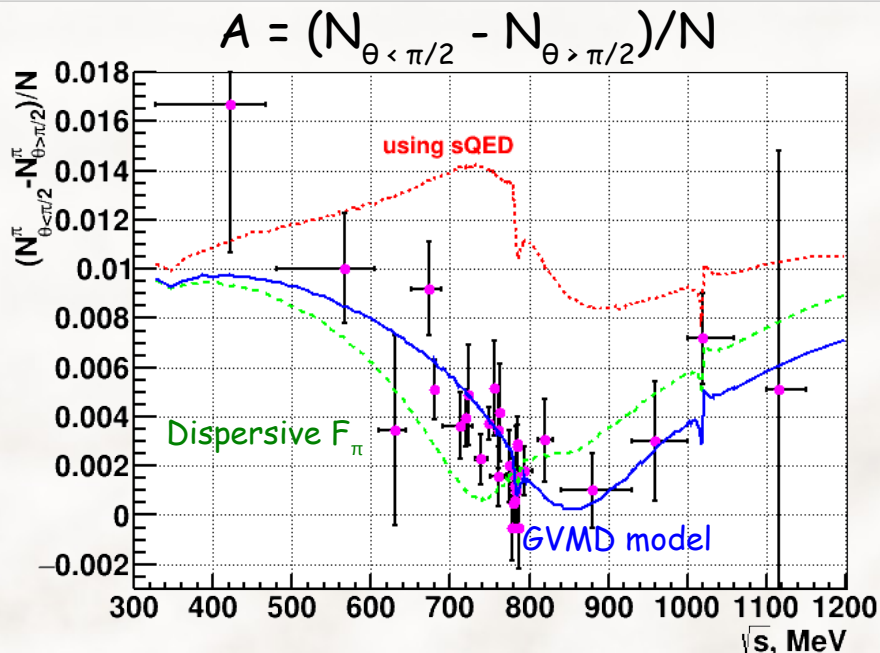
Sensitive to:

- $\times$  angle-related systematics
- $\times$  used model of  $\gamma$ - $\pi$  interaction

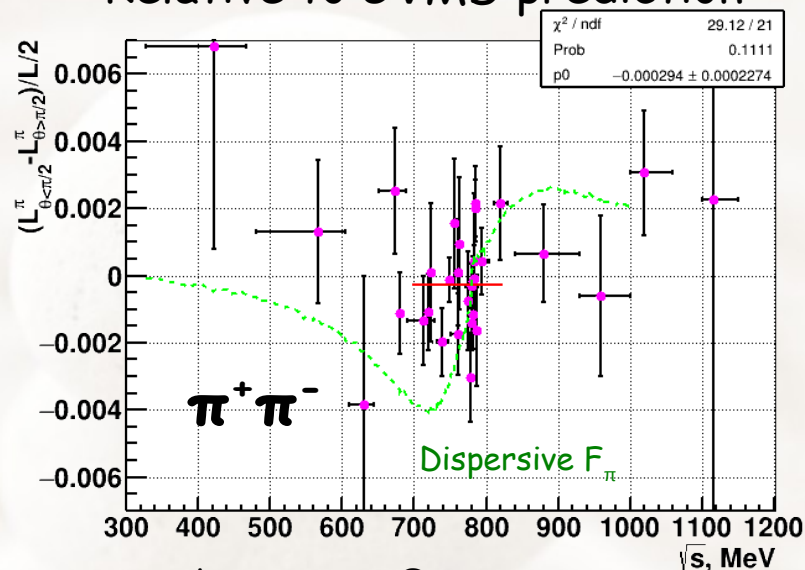
At first try:

1% inconsistency for  $\pi+\pi^-$  was observed between data and MC prediction

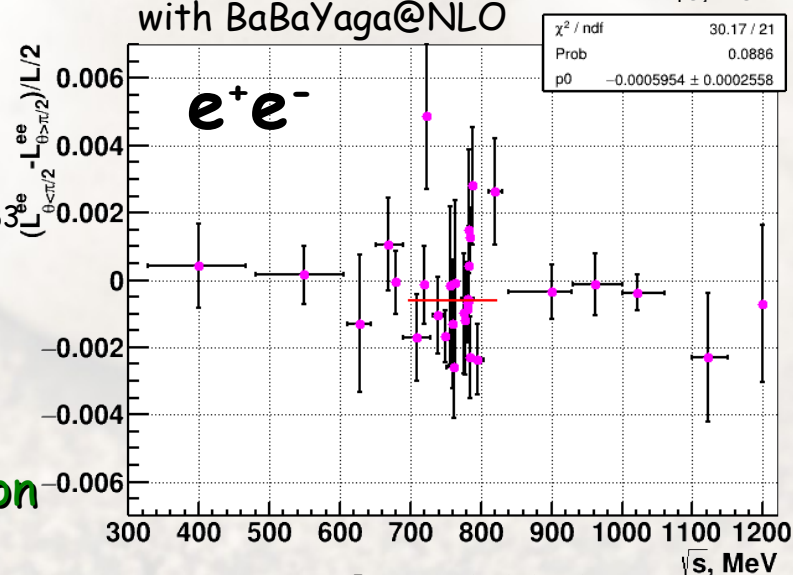
# Charge asymmetry in $e^+e^- \rightarrow \pi^+\pi^-$



Relative to GVMD prediction



with BaBaYaga@NLO



Conventional sQED approach gives  $\sim 1\%$  inconsistency

The theoretical model within **GVMD** was introduced, describes well the CMD-3 data R.Lee et al., Phys.Lett.B 833 (2022) 1372833, was confirmed by calculation in **dispersive formalism**

M.Hoferichter et al., JHEP 08 (2022) 295

Average at  $\sqrt{s} = 0.7-0.82$  GeV:

$\pi^+\pi^-$ :  $\langle \delta A \rangle = -0.029 \pm 0.023 \%$

$e^+e^-$ :  $\langle \delta A \rangle = -0.060 \pm 0.026 \%$



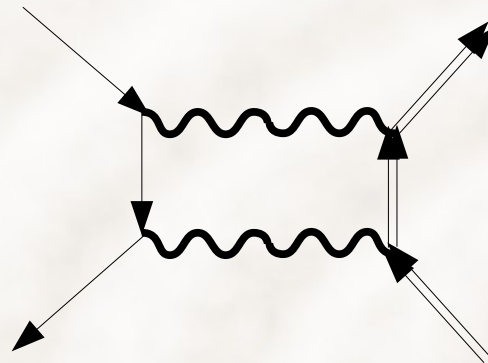
Ensure our  $\theta$  angle systematics estimation for  $|F_\pi|^2$



# sQED assumptions for radiative corrections

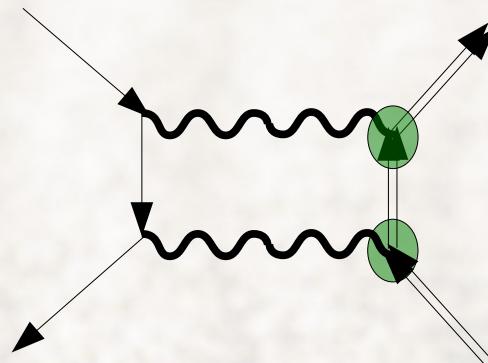
The radiative correction calculations is commonly done in the sQED approach, It's mean that the calculations are performed without form factor, then final Amplitude is scaled by  $F(q^2)$

Scalar QED approach



$$A = \text{sQED} * F(s)$$

Proper way

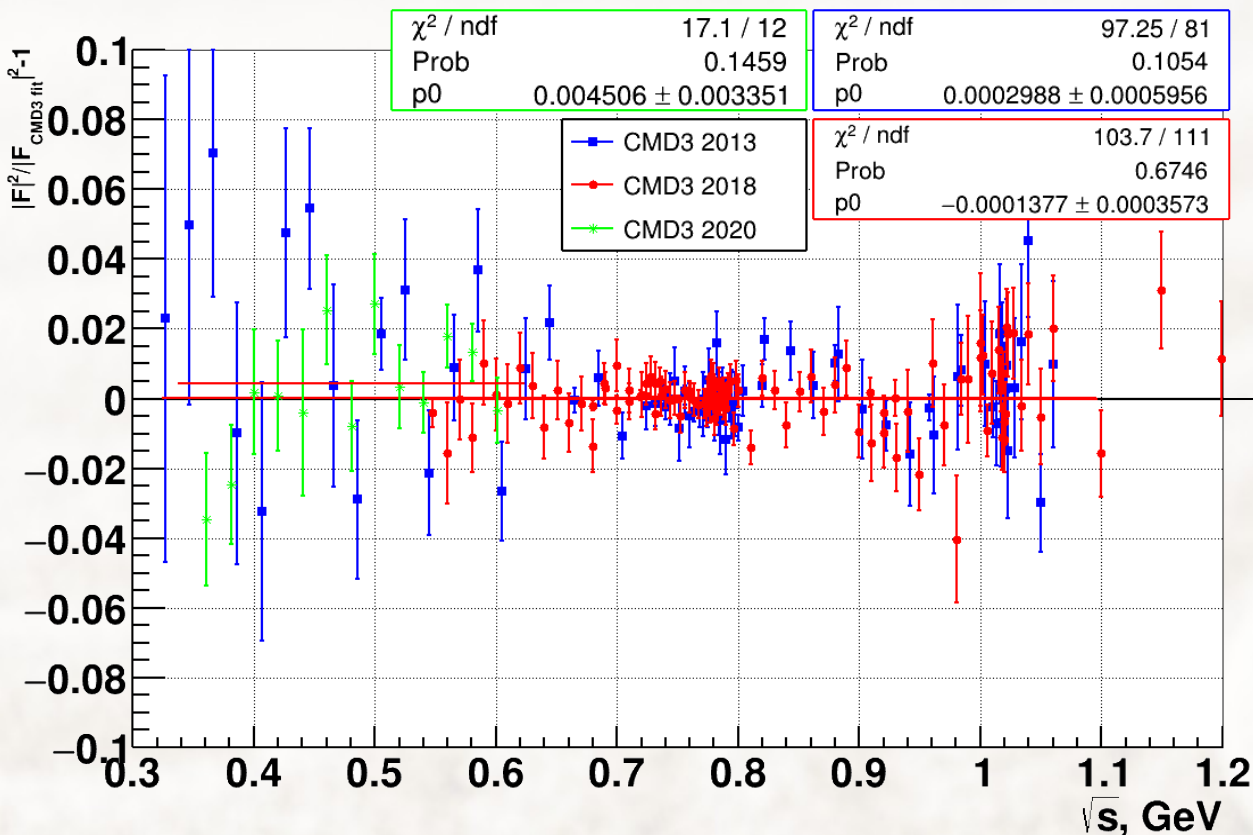


$$A \sim \int F(q_1)F(q_2)$$

Proper way will be to put  $F(q^2)$  to each vertex

**N.B. It will be important to re-calculate radiative corrections with above sQED for ISR measurement**

# Consistency checks



Result consistent between seasons  
within < 0.1%

DCH was in very different conditions:

x correlated noise

x 4 middle layers off (HV-related) in 2013

x etc....

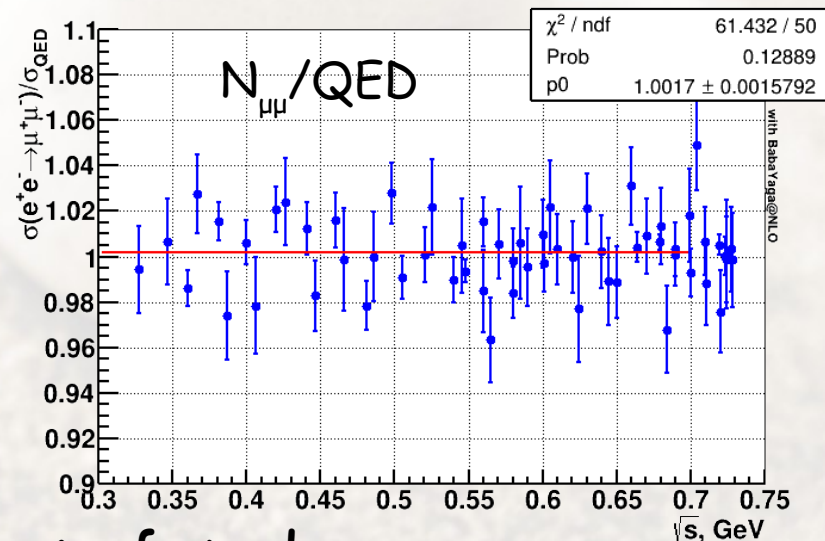
as result it gives ~x2 difference in some corrections

Good check of angle/tracking related systematics

$|F_\pi|^2$  RHO2018/RHO2013  $\Delta = -0.04 \pm 0.07 \%$

LOW2020/RHO2013  $\Delta = -0.5 \pm 0.6 \%$

$N_{\mu\mu}/\text{QED}$   $\Delta = +0.17 \pm 0.16 \%$

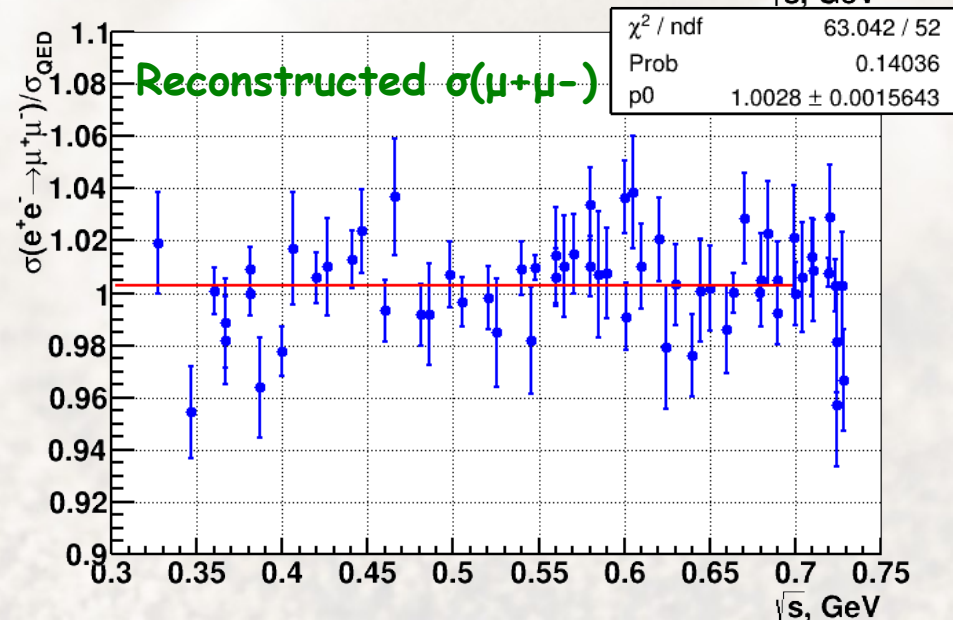
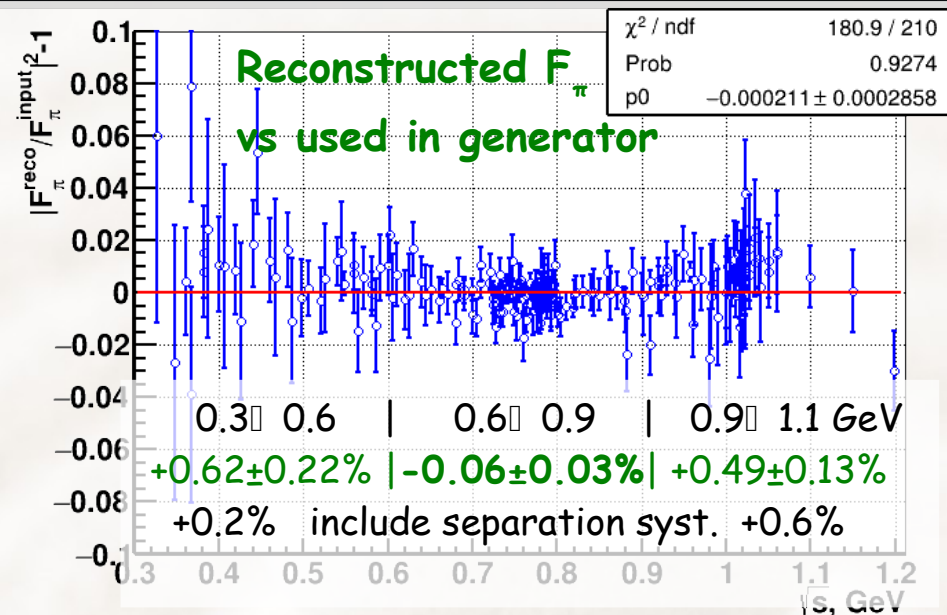


# Analysis workflow cross check on MC

Full analysis workflow was checked on mixed full MC data samples  
(with detector conditioned over time)

Same full analysis as for the data:  
efficiencies reconstructions,  
particle separation, etc  
same scripts,  
same intermediate files, etc

All underneath components (separation,  
efficiency reconstruction, etc)  
were also checked with better precision



# $|F_\pi|^2$ systematic uncertainty



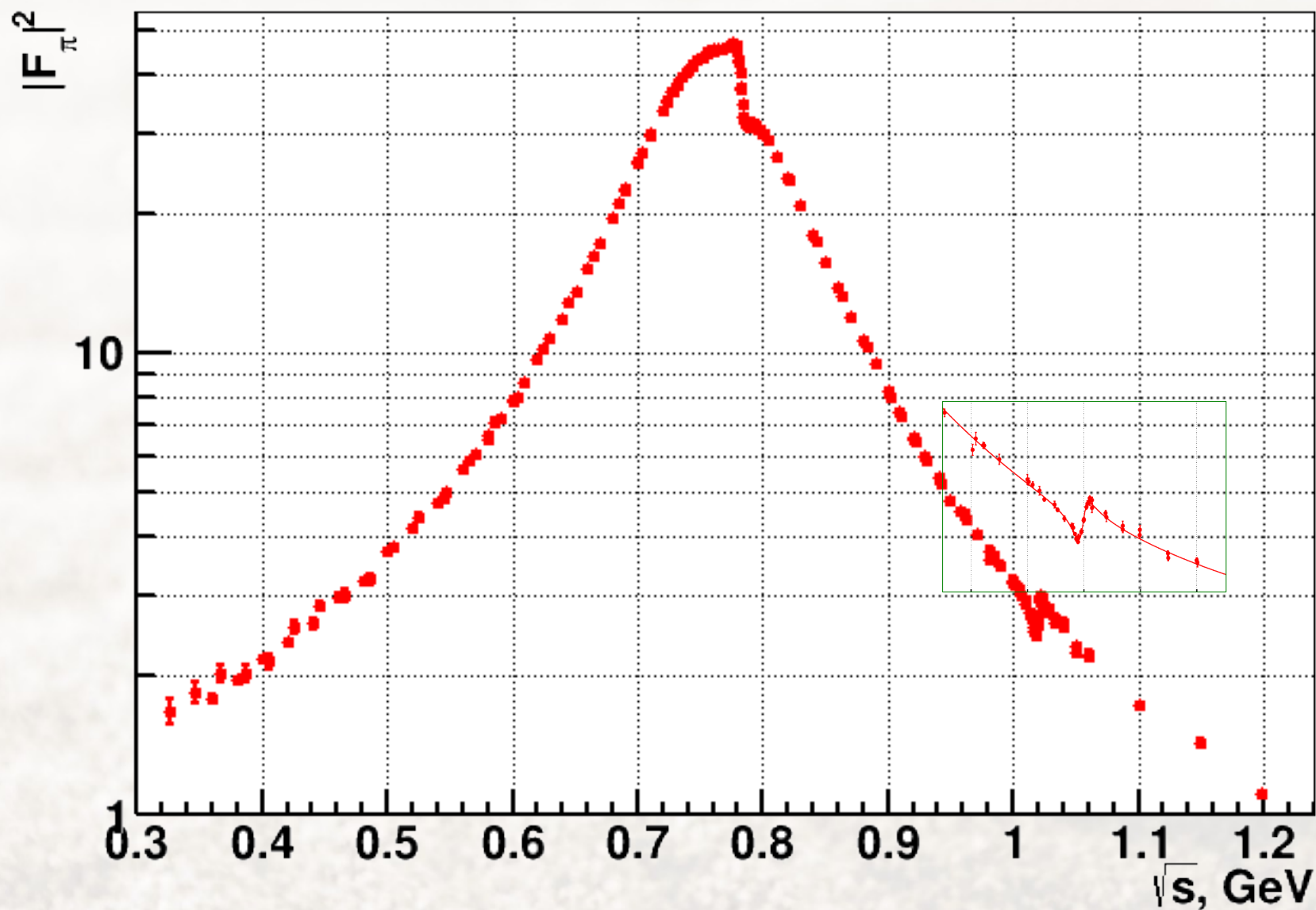
x Radiative corrections	<b>0.2% (<math>2\pi</math>) <math>\oplus</math> 0.2% (<math>F\pi</math>) <math>\oplus</math> 0.1% (<math>e+e-</math>)</b>
x $e/\mu/\pi$ separation	0.5 (low) - <b>0.2% (<math>\rho</math>) - 0.6 (<math>\varphi</math>) %</b>
x Fiducial volume	<b>0.5% / 0.8%</b> (RHO2013)
x Correlated inefficiency	<b>0.1% (<math>\rho</math>) - 0.15% (<math>&gt;1 \Gamma \ni B</math>)</b>
x Trigger	<b>0.05% (<math>\rho</math>) - 0.3% (<math>&gt;1 \Gamma \ni B</math>)</b>
x Beam Energy (by Compton $\sigma_{E < 50 \text{ keV}}$ )	<b>0.1%</b> (out of resonances), <b>0.5%</b> (at $\omega, \varphi$ -peaks)
x Bremsstrahlung loss	<b>0.05%</b>
x Pion specific loss	<b>0.2%</b> nuclear interaction
	<b>0.2%(low) - 0.1% (<math>\rho</math>) pion decay</b>
<hr/>	
	<b>0.8% (low) - 0.7% (<math>\rho</math>) - 1.6% (<math>\varphi</math>)</b>
	<b>1.1% (low) - 0.9% (<math>\rho</math>) - 2.0% (<math>\varphi</math>) (RHO2013)</b>

Fixing of  $N_{\mu\mu}$  adds scaling of correspondent sources with  $\sim (1 + a N_{\mu\mu}/N_{\pi\pi})$

at  $\varphi$  with  $N_{\mu\mu}/N_{\pi\pi} \sim 1$  : 1.05% / 1.2%(RHO2013)  $\rightarrow$  1.6% / 2.0% (RHO2013)

at 1.2 GeV with  $N_{\mu\mu}/N_{\pi\pi} \sim 2.4$  : 1.05%  $\rightarrow$  1.95% (RHO2018)

# Form factor



# Form Factor description

$$|F_\pi(s)|^2 = \left| \left( \text{BW}_\rho^{\text{GS}}(s) \cdot \left( 1 + \delta_\omega \frac{s}{m_\omega^2} \text{BW}_\omega(s) + \delta_\phi \frac{s}{m_\phi^2} \text{BW}_\phi(s) \right) + \right. \right. \\ \left. \left. + a_{\rho'} \text{BW}_{\rho'}^{\text{GS}}(s) + a_{\rho''} \text{BW}_{\rho''}^{\text{GS}}(s) + a_{\text{cont}} \right) / (1 + a_{\rho'} + a_{\rho''} + a_{\text{cont}}) \right|^2$$

$\rho, \rho', \rho''$  - by the Gounaris-Sakurai parameterization (GS)

$\omega, \phi$  - by the constant width relativistic Breit-Wigner

$a_{\text{cont}}$  - constant for continuum contribution (partially absorb  $\rho', \rho'', \rho''', \dots$ )

$\rho', \rho''$  - parameters fixed by combined fit together with CMD-2 and DM2,  $\sqrt{s} > 1.1 \text{ GeV}$

# Form Factor description

Both errors are statistical  
Second error correspond to  $\rho'$ ,  $\rho''$  fixing

Parameter	value	$M_{\phi,\omega}, \Gamma_{\phi,\omega}$ constrained by PDG's values	PDG(2022) <a href="#">[56]</a>
$m_\rho$ , MeV	$775.41 \pm 0.08 \pm 0.07$	$775.4 \pm 0.07 \pm 0.07$	$775.26 \pm 0.23$
$\Gamma_\rho$ , MeV	$148.8 \pm 0.16 \pm 0.05$	$148.76 \pm 0.16 \pm 0.06$	$147.4 \pm 0.8$
$m_\omega$ , MeV	$782.43 \pm 0.03 \pm 0.01$	$782.44 \pm 0.03 \pm 0.01$	$782.66 \pm 0.13$
$\Gamma_\omega$ , MeV	$8.57 \pm 0.06 \pm 0.01$	$8.59 \pm 0.06 \pm 0.01$	$8.68 \pm 0.13$
$\mathcal{B}_{\omega \rightarrow \pi^+\pi^-} - \mathcal{B}_{\omega \rightarrow e^+e^-}, 10^{-6}$	$1.204 \pm 0.009 \pm 0.003$	$1.204 \pm 0.009 \pm 0.004$	$1.28 \pm 0.05$
$\arg(\delta_\omega)$ , rad	$0.167 \pm 0.008 \pm 0.01$	$0.169 \pm 0.008 \pm 0.012$	
$m_\phi$ , MeV	$1019.761 \pm 0.128 \pm 0.022$	$1019.465 \pm 0.016 \pm 0$	$1019.461 \pm 0.016$
$\Gamma_\phi$ , MeV	$4.681 \pm 0.271 \pm 0.058$	$4.25 \pm 0.013 \pm 0$	$4.249 \pm 0.013$
$\mathcal{B}_{\phi \rightarrow \pi^+\pi^-} - \mathcal{B}_{\phi \rightarrow e^+e^-}, 10^{-8}$	$3.65 \pm 0.24 \pm 0.02$	$3.51 \pm 0.22 \pm 0.03$	$2.2 \pm 0.4$
$\arg(\delta_\phi)$ , rad	$2.883 \pm 0.052 \pm 0.011$	$2.77 \pm 0.023 \pm 0.006$	
$ a_{cont} $	$0.0975 \pm 0.0011 \pm 0.0096$	$0.0971 \pm 0.001 \pm 0.0106$	
$\arg(a_{cont})$ , rad	$2.337 \pm 0.021 \pm 0.286$	$2.344 \pm 0.02 \pm 0.309$	
$\chi^2/ndf$	212.53 / 195	223.42 / 199	
$m'_\rho$ , MeV		$1226.22 \pm 24.76$	$1465 \pm 25$
$\Gamma'_\rho$ , MeV		$272.97 \pm 45.53$	$400. \pm 60$
$m''_\rho$ , MeV		$1604.66 \pm 30.8$	$1720 \pm 20$
$\Gamma''_\rho$ , MeV		$249.39 \pm 52.24$	$250. \pm 100$
$ a'_\rho $		$0.3589 \pm 0.0693$	
$ a''_\rho $		$0.1042 \pm 0.031$	
$\arg(a'_\rho)$ , rad		$-1.831 \pm 0.07$	
$\arg(a''_\rho)$ , rad		$3.384 \pm 0.234$	
$\chi^2/ndf$		288.87/240	

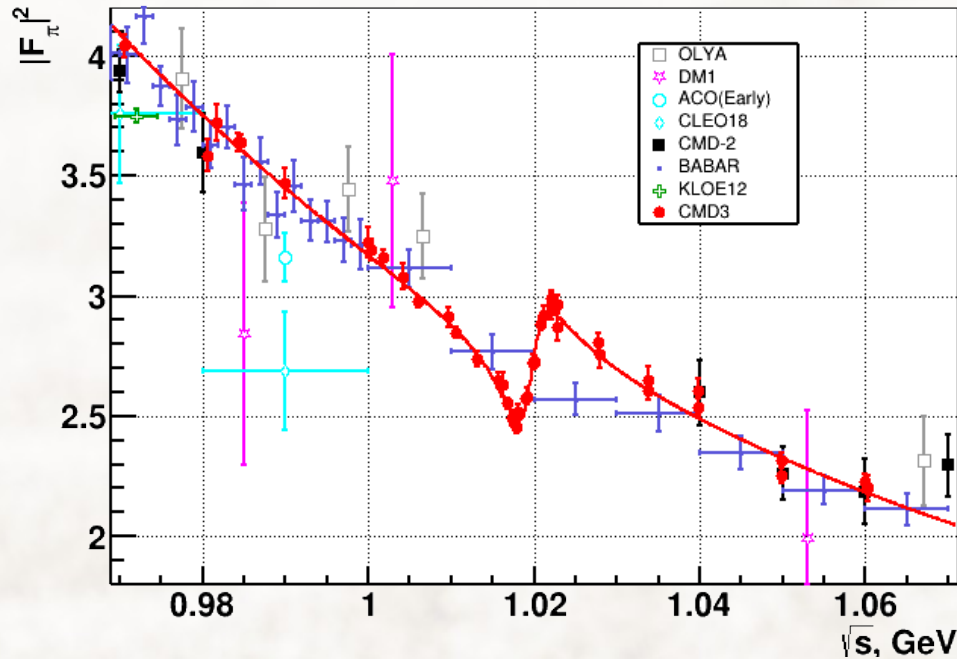
CMD3+CMD2+DM2

$$\chi^2 = 220.08(\text{CMD3}) + 25.30(\text{CMD2}) + 40.10(\text{DM2}) + 3.39(\text{PDG})$$

$$\text{ndf} = 207 + 29 + 20 + 4 - 12(\rho, \omega, \phi, cont) - 8(\rho', \rho'')$$

$$\varphi \rightarrow \pi^+\pi^-$$

## First direct $|F_\pi|^2$ measurement around $\varphi$ resonance



$$\psi_\pi = (-21.3 \pm 2.0 \pm 10.0)^\circ$$

$$B(\varphi \rightarrow e^+e^-)B(\varphi \rightarrow \pi^+\pi^-) = (3.51 \pm 0.33 \pm 0.24) \times 10^{-8}$$

CMD-3

Previous measurement using detected  $N_{\pi^+\pi^-}$   
or visible cross-section by OLYA, ND,  
SND (Phys.Lett.B474:188-193,2000)

$$\psi_\pi = (-34 \pm 5)^\circ$$

$$B(\varphi \rightarrow e^+e^-)B(\varphi \rightarrow \pi^+\pi^-) = (2.1 \pm 0.4) \times 10^{-8}$$

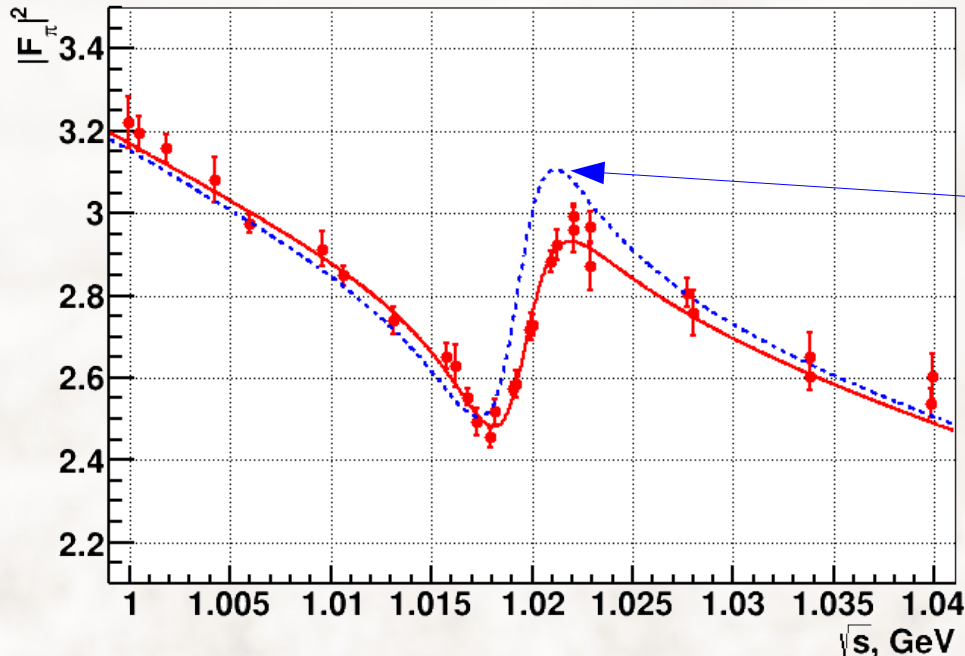
SND

**N.B.** radiative correction uncertainty (from  $F_\pi$  parametrisation)

gives **~1.5 scale factor of total statistical and systematic errors** (both for Br and  $\psi_\pi$ )



# $\phi \rightarrow \pi^+\pi^-$ via VP term



Assuming no direct  $\phi \rightarrow \pi^+\pi^-$   
if interference comes from VP

non resonant  $F_\pi$  with  
vacuum polarization term

$$\left| F_\pi^{\delta_\phi=0}(s) \frac{1 - P_{not-\phi-res}(m_\phi^2)}{1 - P(s)} \right|^2$$

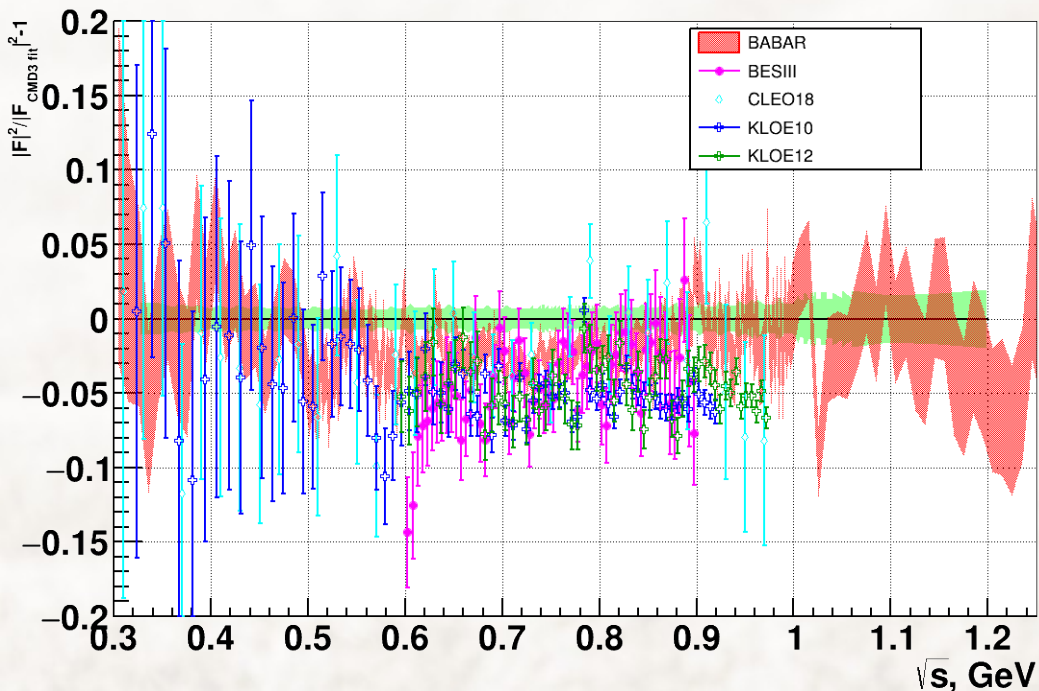
$$\frac{B_{\phi \rightarrow e^+e^-}}{B_{\phi \rightarrow \pi^+\pi^-}} = (3.51 \pm 0.43) \times 10^{-8}$$

$$(B_{\phi \rightarrow e^+e^-} / B_{\phi \rightarrow \pi^+\pi^-})^{VP} \sim 5.3 \times 10^{-8} \quad - \text{ as expected from VP only effect}$$

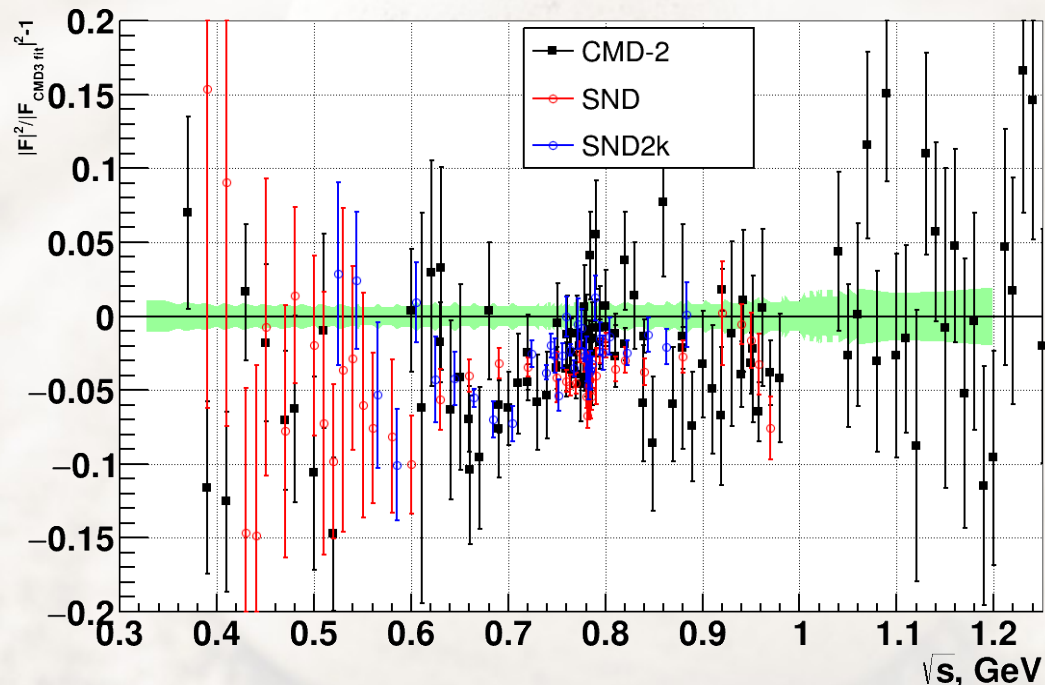
# Other experiments

Relative to CMD-3 fit, **yellow** band - systematic value

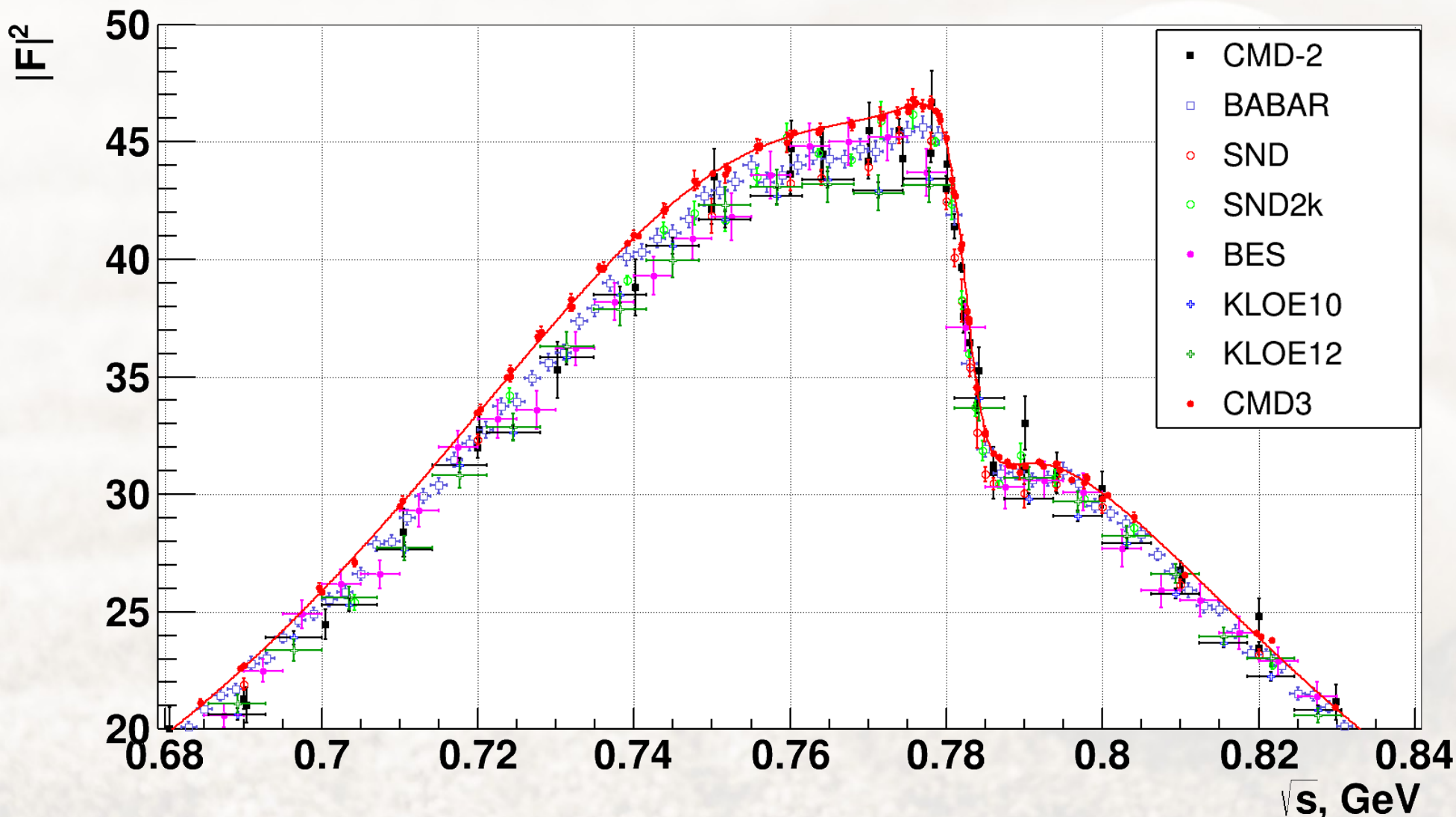
vs ISR



vs direct scan



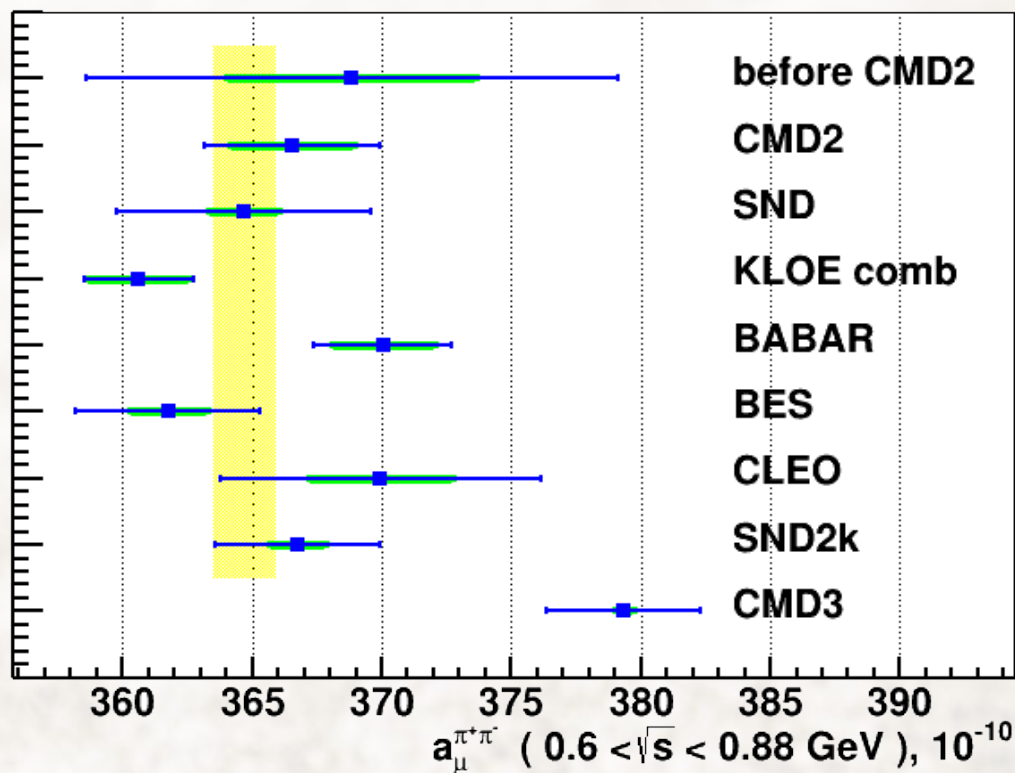
# Other experiments



# The $\pi^+ \pi^-$ contribution to $a_\mu^{\text{had}}$

$$a_\mu^{\text{had,LO}} = \frac{m_\mu^2}{12\pi^3} \int_{4m_\pi^2}^{\infty} \frac{\sigma_{e^+e^- \rightarrow \gamma^* \rightarrow \text{hadrons}}(s) K(s)}{s} ds$$

$0.6 < \sqrt{s} < 0.88 \text{ GeV}$



$a_\mu^{\pi\pi, LO}, 10^{-10}$

before CMD2	$368.8 \pm 10.3$
CMD2	$366.5 \pm 3.4$
SND	$364.7 \pm 4.9$
KLOE	$360.6 \pm 2.1$
BABAR	$370.1 \pm 2.7$
BES	$361.8 \pm 3.6$
CLEO	$370.0 \pm 6.2$
SND2k	$366.7 \pm 3.2$
CMD3	$379.3 \pm 3.0$

RHO2013	$380.06 \pm 0.61 \pm 3.64$
RHO2018	$379.30 \pm 0.33 \pm 2.62 \times 10^{-10}$
Sum	$379.35 \pm 0.30 \pm 2.95$

# Conclusion

- x VEPP-2000 collider is only one working this days on direct scanning below  $<2 \text{ GeV}$  for measurement of exclusive  $\sigma (e^+e^- \rightarrow \text{hadrons})$
- x CMD-3 pion formfactor measurement is based on full data set at  $\sqrt{s} < 1 \text{ GeV}$   
 $34 \times 10^6$  of  $\pi^+\pi^-$  events was used in analysis (at  $\sqrt{s} < 1 \text{ GeV}$ )
- x Total systematic uncertainty 0.7% (RHO2018) / 0.9%(RHO2013)
- x New KLOE, BaBar analyses, [SND@VEPP-2000](#), Belle-2 data are underway

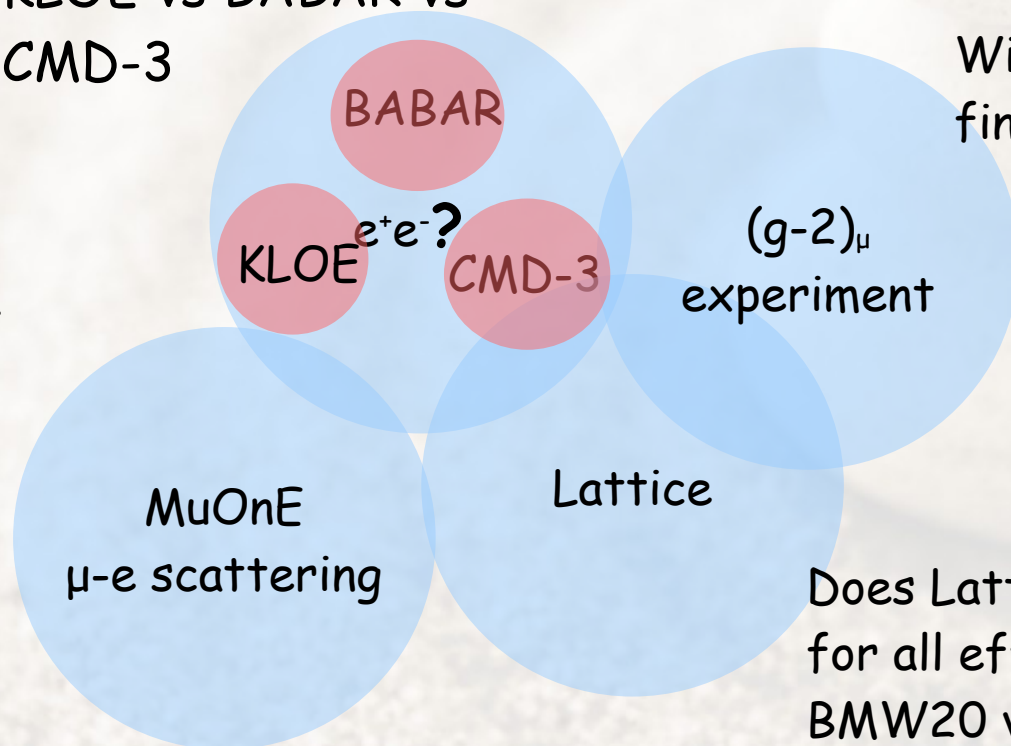
# Puzzles in puzzle

Question of comparison:  
 $e^+e^-$  vs  $(g-2)_\mu$  vs lattice

Where difference  
comes from:  
KLOE vs BABAR vs  
CMD-3

Will it be confirmed?  
final FNAL vs J-PARC

Hard effort  
against  
systematics



Does Lattice account  
for all effects?

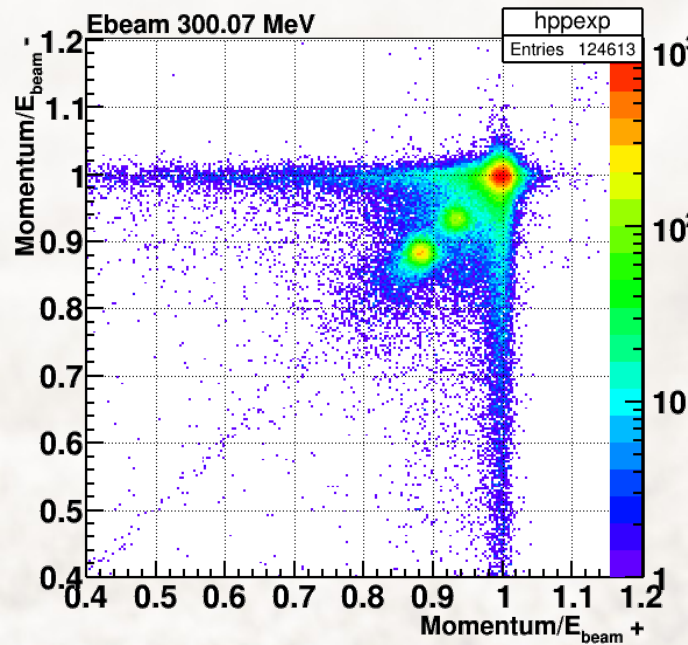
BMW20 vs others

$g-2$  theory initiative seminar

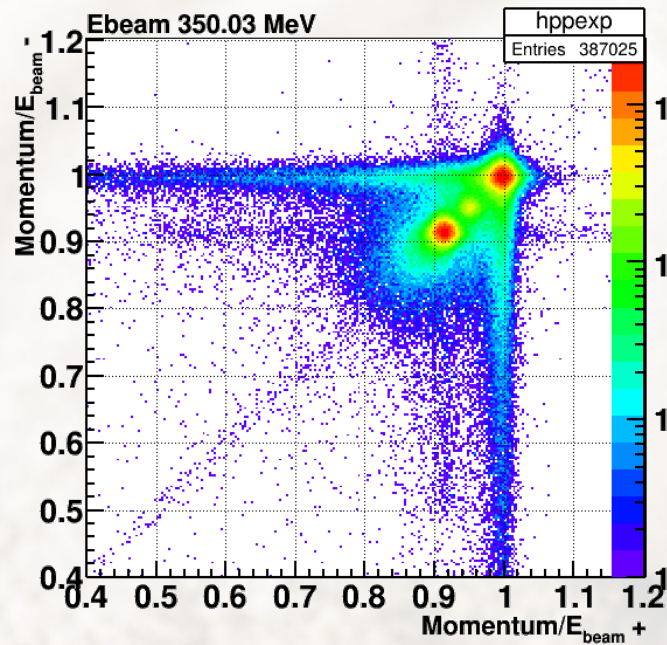
# Question 2

Fig.3-4 show 2D-plots for the momentum and energy deposition methods at 2 CM energies, one where each method work best (0.5 GeV for momentum and 0.956 GeV for energy) and the other at their limit where they do not perform well but are still used (0.9 GeV for momentum and 0.548 GeV for energy). In the comparison with other experiments the problematic region is 0.6 - 0.8 GeV. Need to see the corresponding plots at these energies, i.e. 0.6, 0.7, 0.8 GeV.

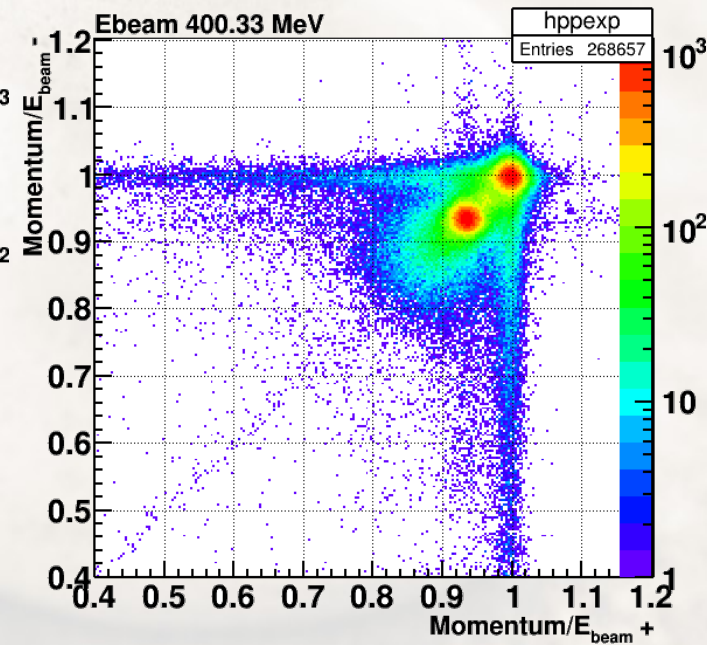
0.6 GeV



0.7 GeV



0.8 GeV

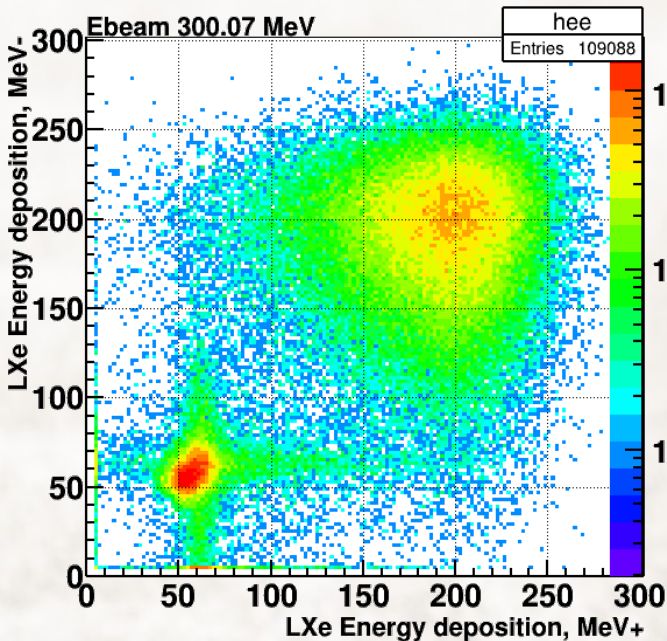


# Question 2

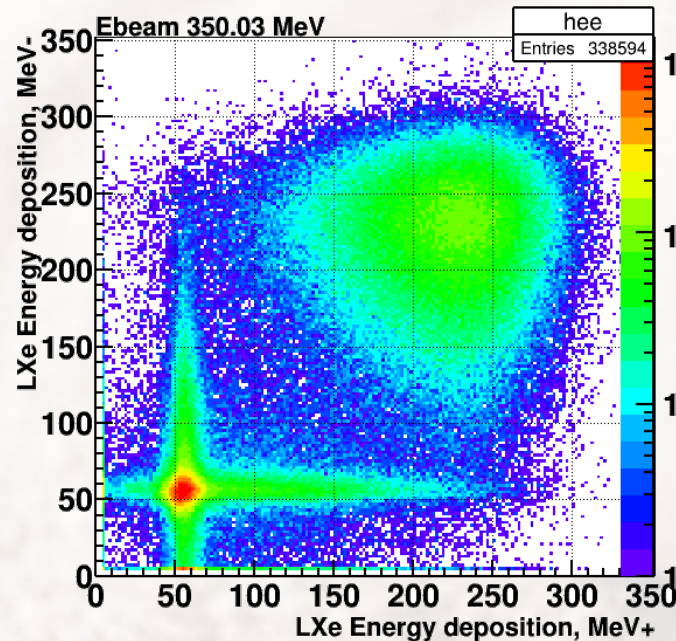
## Question 2

Fig.3-4 show 2D-plots for the momentum and energy deposition methods at 2 CM energies, one where each method work best (0.5 GeV for momentum and 0.956 GeV for energy) and the other at their limit where they do not perform well but are still used (0.9 GeV for momentum and 0.548 GeV for energy). In the comparison with other experiments the problematic region is 0.6 - 0.8 GeV. Need to see the corresponding plots at these energies, i.e. 0.6, 0.7, 0.8 GeV.

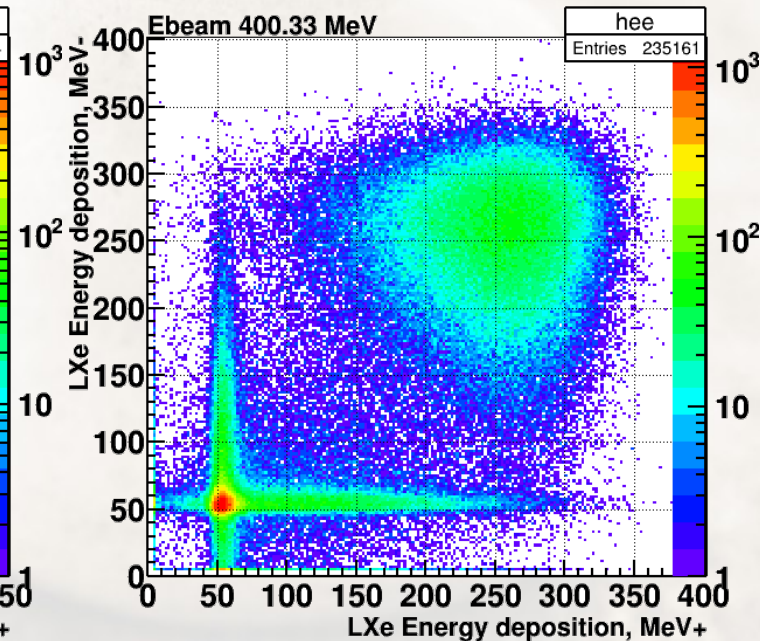
**0.6 GeV**



**0.7 GeV**



**0.8 GeV**





# Question 6

## Question 6

The 2D reference distributions contain 36 and 57 parameters treated as nuisance parameters in the likelihood fit. Provide more information on the nature of these parameters, their time dependence, the checks with data and how they impact the systematic uncertainty on the cross section. Is it possible to show a data-MC comparison for individual PDFs, e.g. by applying strong cuts for one of the tracks?

Separation of  $\pi^+\pi^-$ ,  $\mu^+\mu^-$ ,  $e^+e^-$ , .... final states is

based on likelihood minimization:

$$-\ln L = - \sum_{\text{events}} \ln \left[ \sum_i N_i f_i(X^+, X^-) \right] + \sum_i N_i$$

Momentum-based separation:

MC generator spectra are convolved with detector response function (resolution, brems., pion decays)

36 free parameters in fit per each point

PDF( $e+e^-$ ) detector response addition: brems. + 3 Gauss per axis + sigma (x-y correlation):

$$b^0(1-p/p_0)^{-1-b_1} f(b_0) \times (\Sigma \text{Gauss}(1/p'))$$

$$2 + 8 \times 2 + 1 = 19 \text{ parameters}$$

PDF( $\mu+\mu^-$ ): 3 Gauss from  $e+e^-$  + 1 Gauss(p) per axis + sigma (x-y correlation):

$$2 \times 2 + 1 = 5 \text{ parameters}$$

PDF( $\pi+\pi^-$ ): 3 Gauss from  $e+e^-$  + 1 Gauss(p) per axis + sigma (x-y correlation) + fixed from MC form of pion decays tails (ratio in tail free):

$$2 \times 2 + 1 + 2 = 7 \text{ parameters}$$

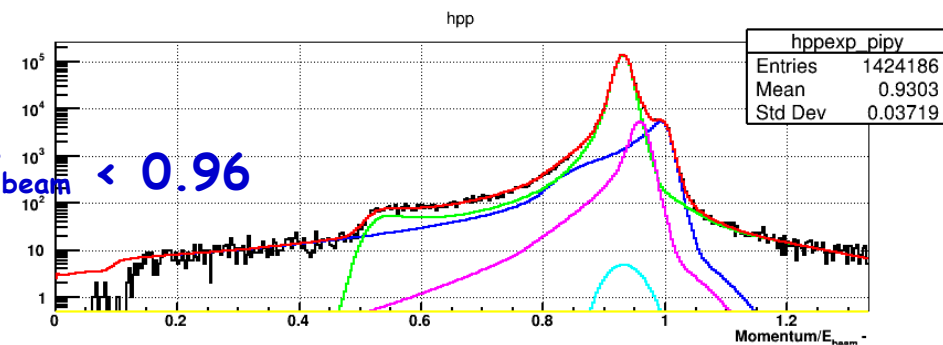
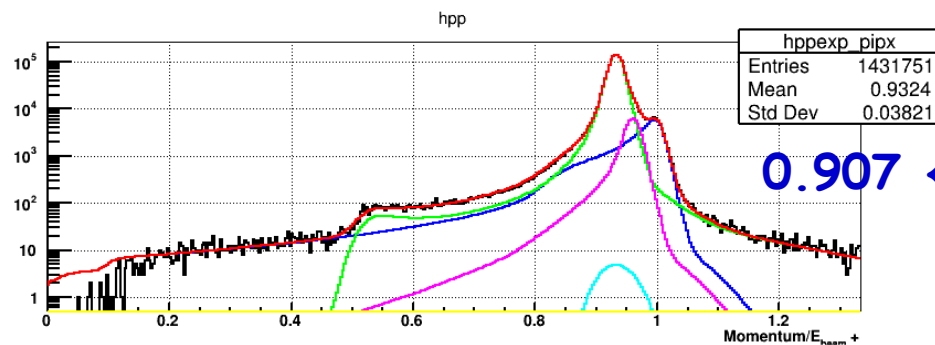
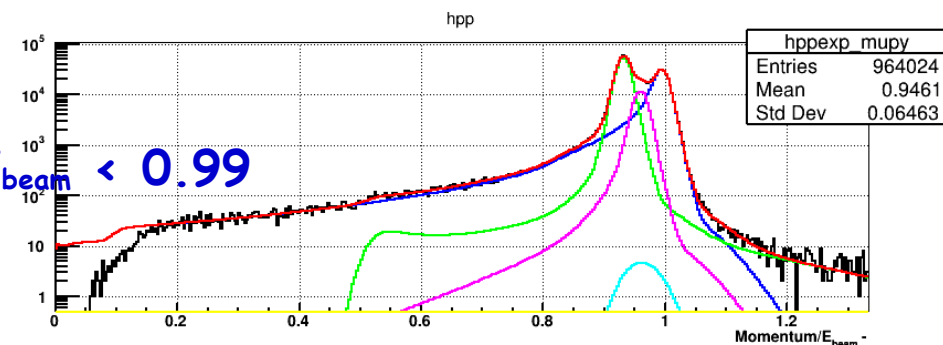
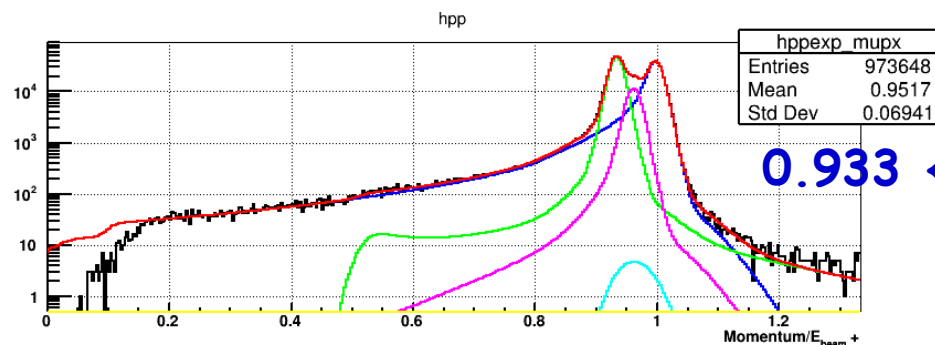
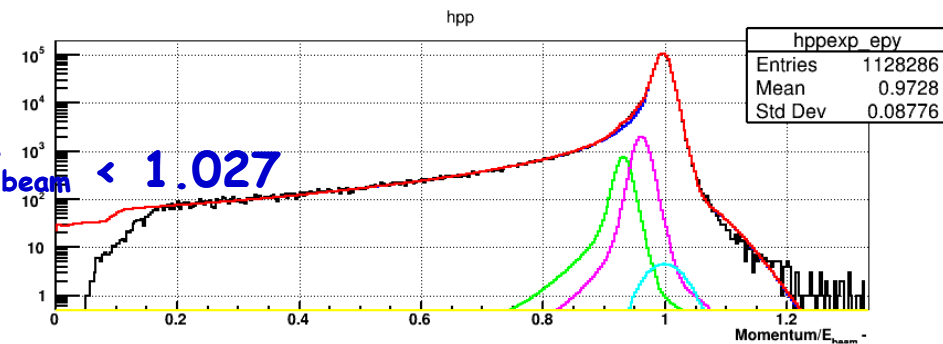
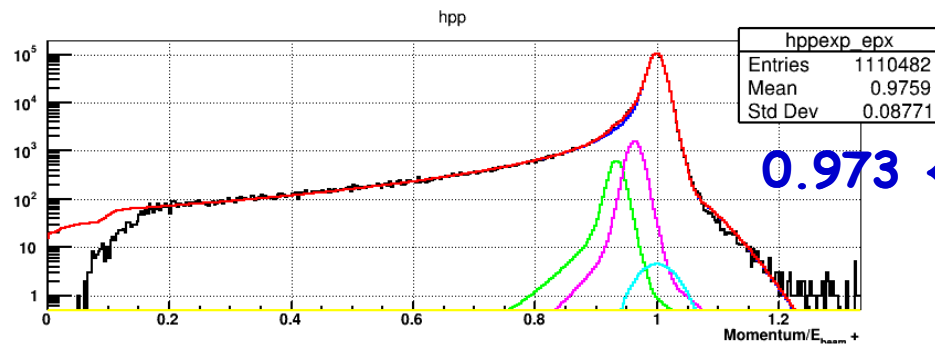
PDF(cosmic): form fixed from clean cosmic sample selected by time of event

PDF( $3\pi$ ,  $4l$ ): form fixed from full MC

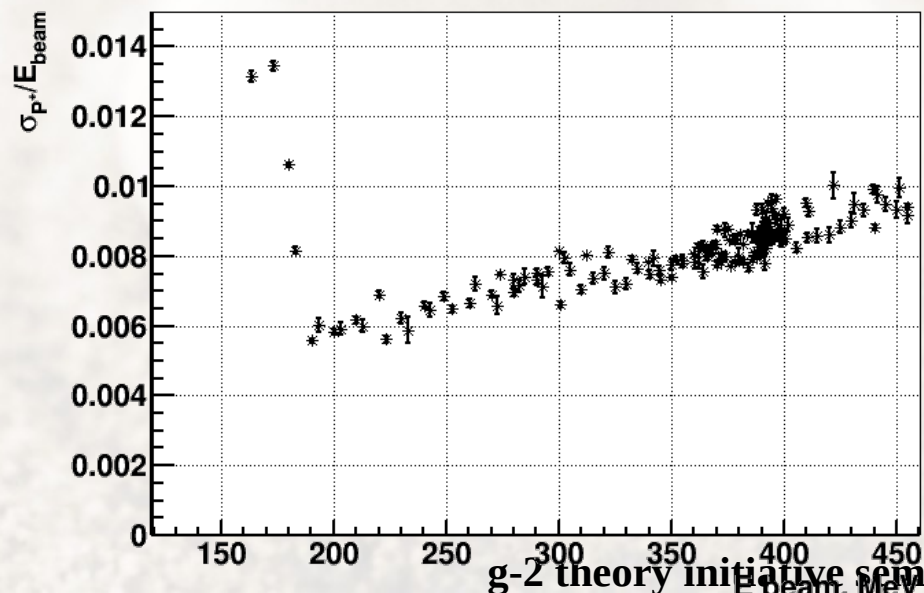
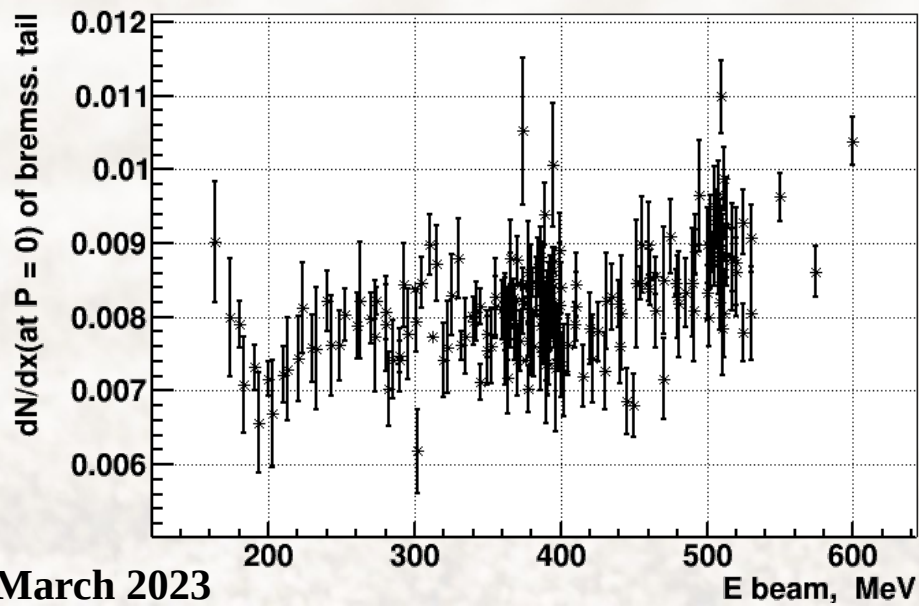
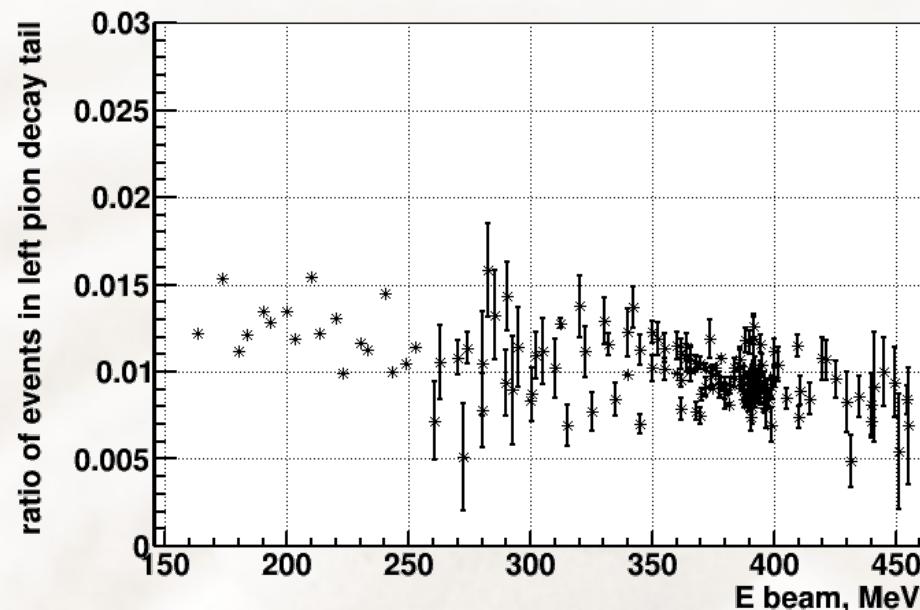
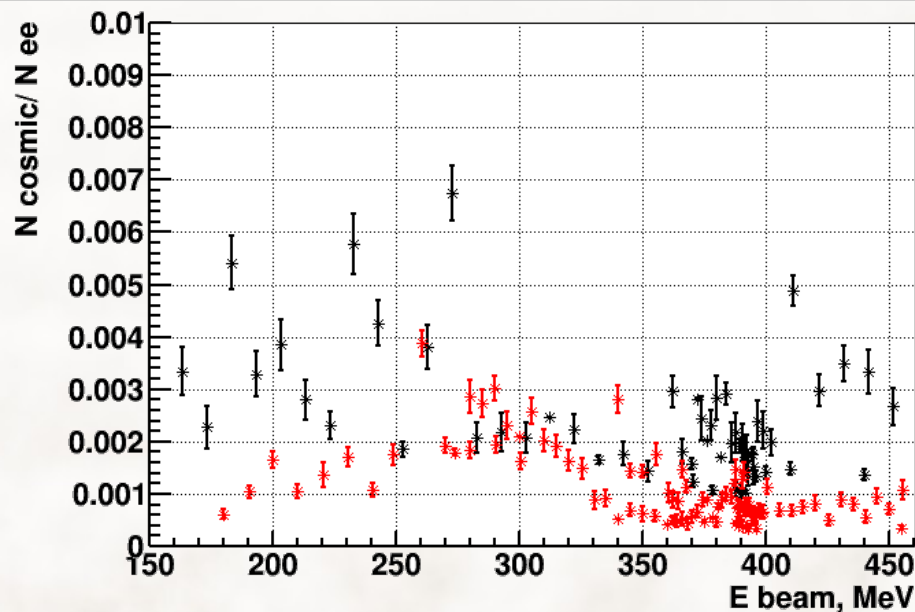
$N_{ee}$ ,  $N_{\pi\pi}/N_{ee}$ ,  $N_{\mu\mu}/N_{ee}$ ,  $N_{3\pi}/N_{ee}$ ,  $N_{\text{cosmic}}/N_{ee}$  - 5 parameters

# Fit result

Ebeam 391.48 MeV



# Some parameters dependences



# Question 6

## Question 6

The 2D reference distributions contain 36 and 57 parameters treated as nuisance parameters in the likelihood fit. Provide more information on the nature of these parameters, their time dependence, the checks with data and how they impact the systematic uncertainty on the cross section. Is it possible to show a data-MC comparison for individual PDFs, e.g. by applying strong cuts for one of the tracks?

### Energy deposition-based separation:

PDFs is described by a generic functional form (log-gaus, etc),  
trained on the data: by tagged electron, cosmic muons

56 free parameters in fit

PDF(e+e-): (2 Logarithmic Gaus + 1 Gaus) + 0-Energy probability - all per axis + fixed from MC X-Y correlation  $\sum a_i f(k_i X+, k_i X-)$

$10*2 + 1*2 = 22$  parameters

PDF( $\mu+\mu-$ ): form fixed from clean cosmic sample selected by time of event, and momentum,  
 $N_{\mu\mu}/N_{ee}$  fixed from QED

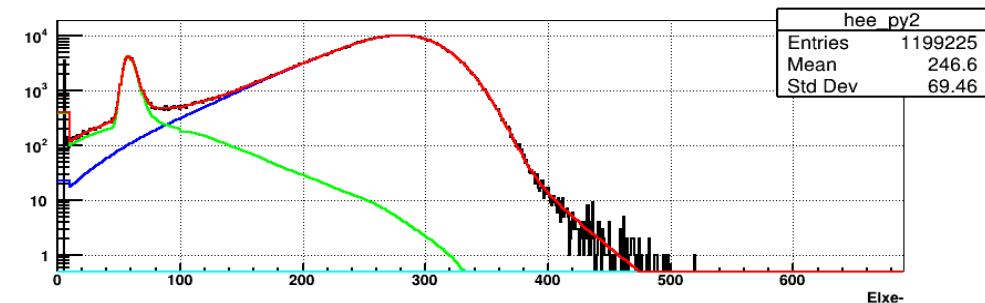
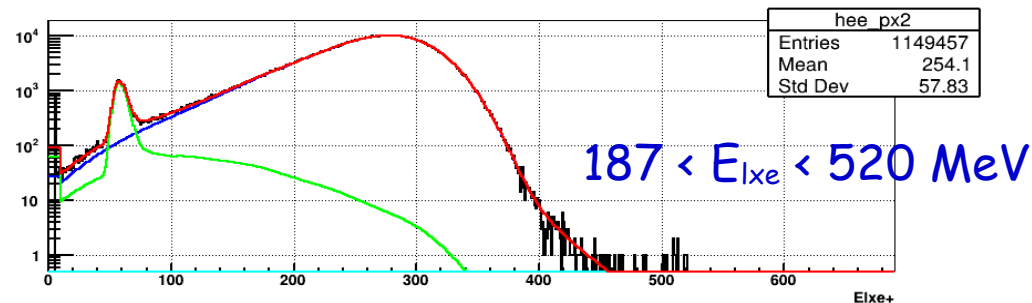
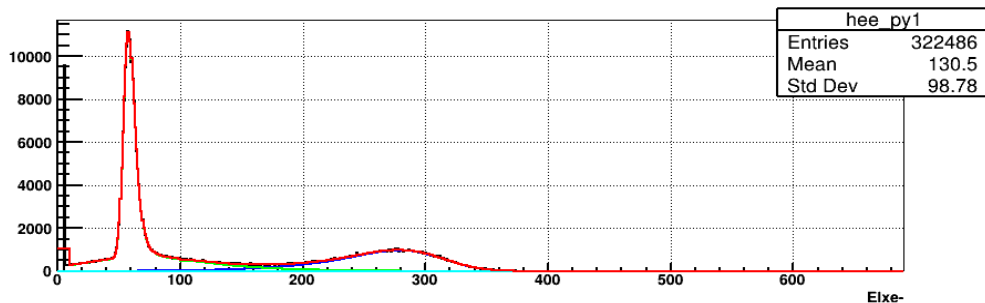
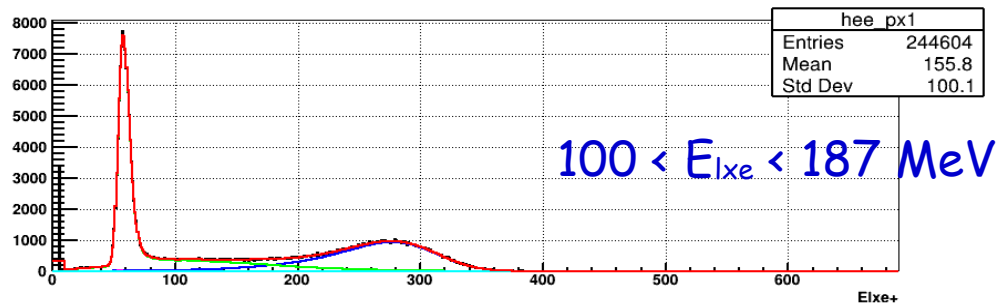
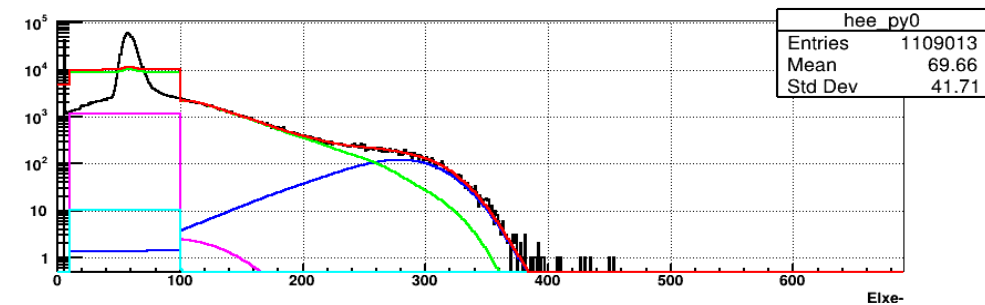
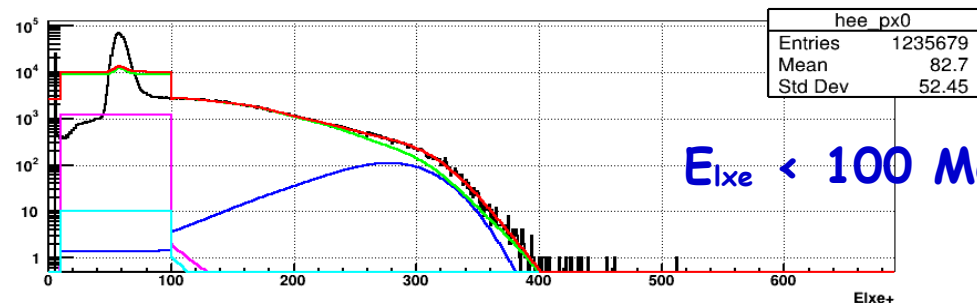
PDF( $\pi+\pi-$ ): MIP as "2 Logarithmic Gaus + 1 Gaus, 1 shift fixed" + MIP probability + 0-Energy probability  
+ Hadronic tail by sum of decreasing gaussians as  $\sum a_i \text{Gauss}(X - (E^{\max} - E^{\text{mip}}) * i / n + E^{\text{mip}}, \sigma_0)$  - all per axis  
 $9*2 + 1*2 + 1*2 + 5*2 = 32$  parameters

PDF(cosmic): form fixed from clean cosmic sample selected by time of event, N fixed from time distribution

$N_{ee}, N_{\pi\pi}/N_{ee}$  - 2 parameters

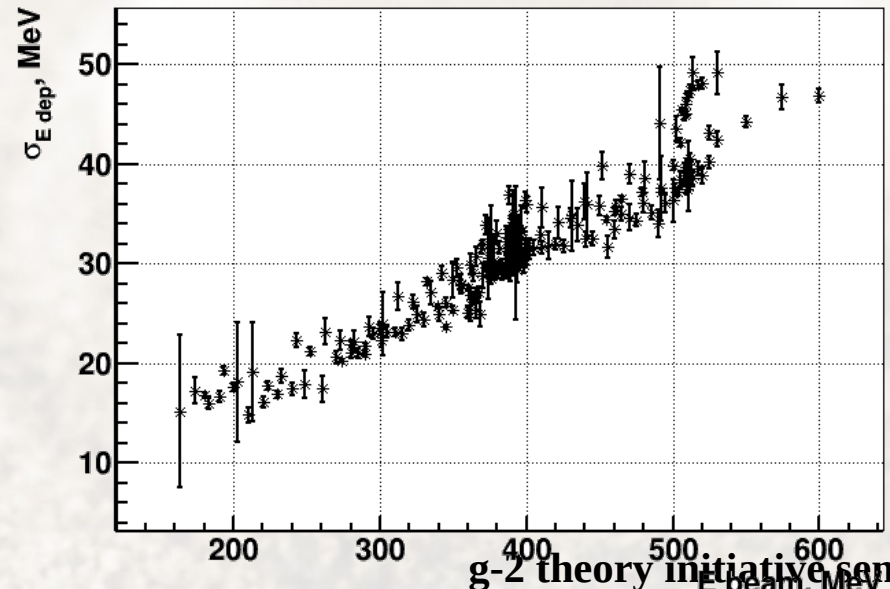
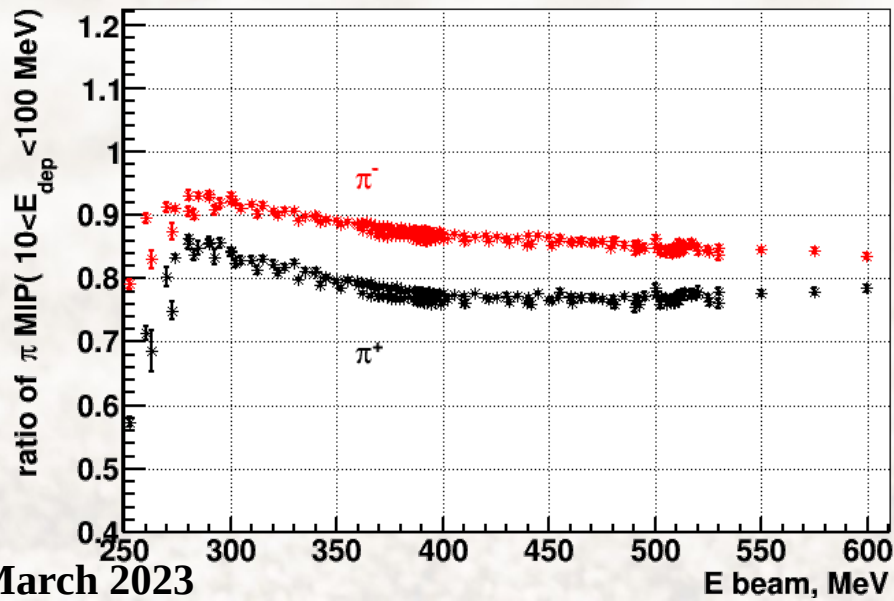
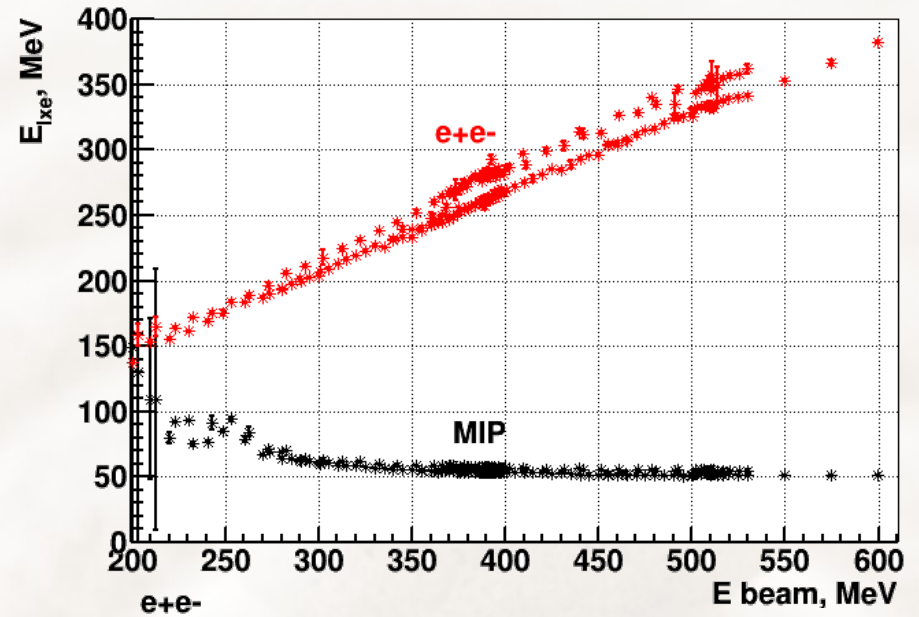
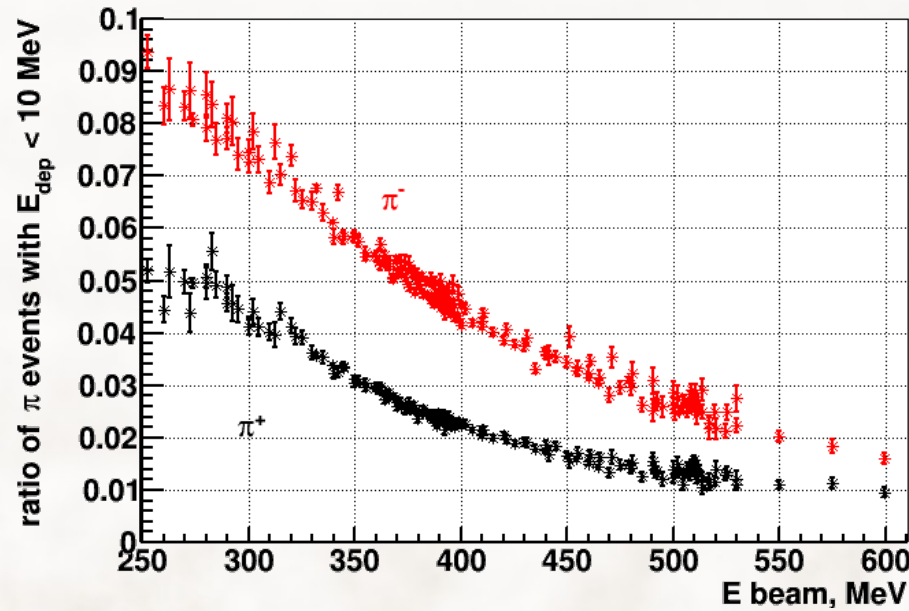
# Fit result

Ebeam 391.48 MeV



Muon & Pion MIP PDFs are strongly overlap,  
In  $10 < E_{lxe} < 100 \text{ MeV}$  constant PDF was used to suppress likelihood systematic  
biases from not exact PDF descriptions

# Some parameters dependences



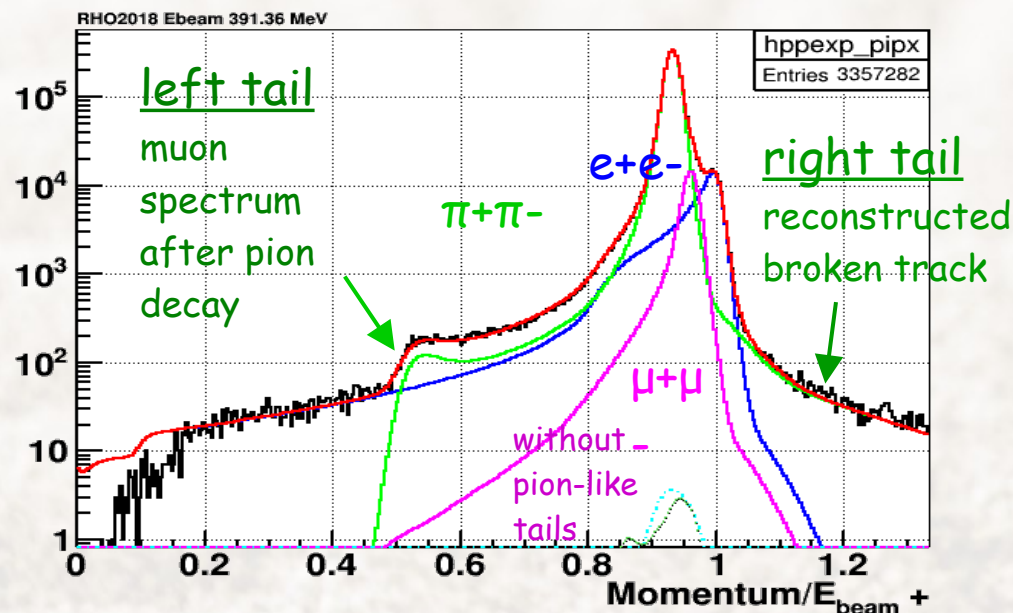
# Question 6 & 19

Question 6: The 2D reference distributions contain 36 and 57 parameters treated as nuisance parameters in the likelihood fit. Provide more information on the nature of these parameters, their time dependence, the checks with data and how they impact the systematic uncertainty on the cross section. Is it possible to show a data-MC comparison for individual PDFs, e.g. by applying strong cuts for one of the tracks?

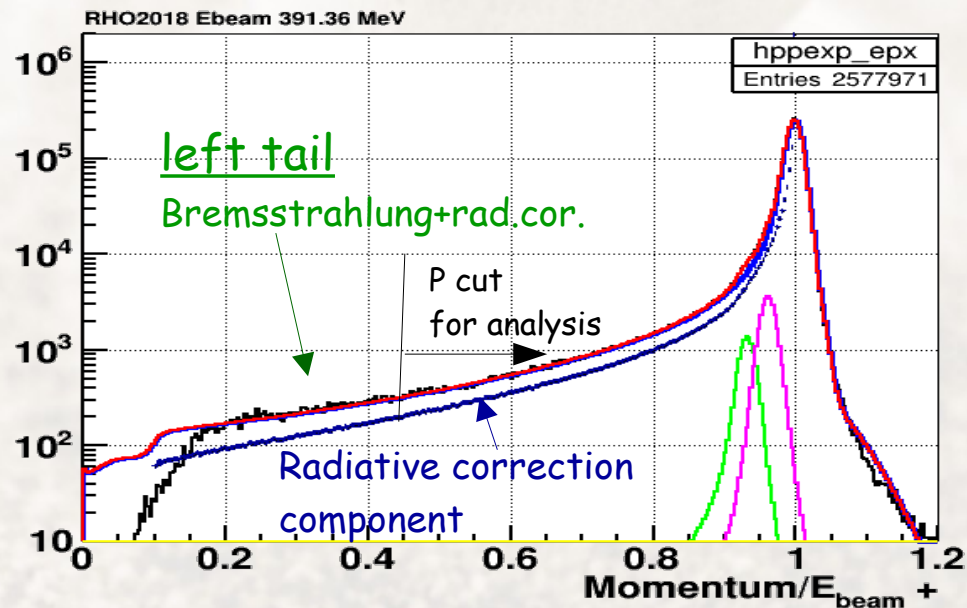
Question 19: Tracking plots (efficiency plot?) are given for MC simulation only. Need to see data/MC tests.

The PDFs are obtained from data itself, they are not necessary to be same as in simulation. Some features of PDF give possibility to control particle specific losses (pion decay, bremsstrahlung loss) - given in slides 27,28.

Experimental  $P^+$  spectrum with  $|P^- - P\pi| < 10$  MeV



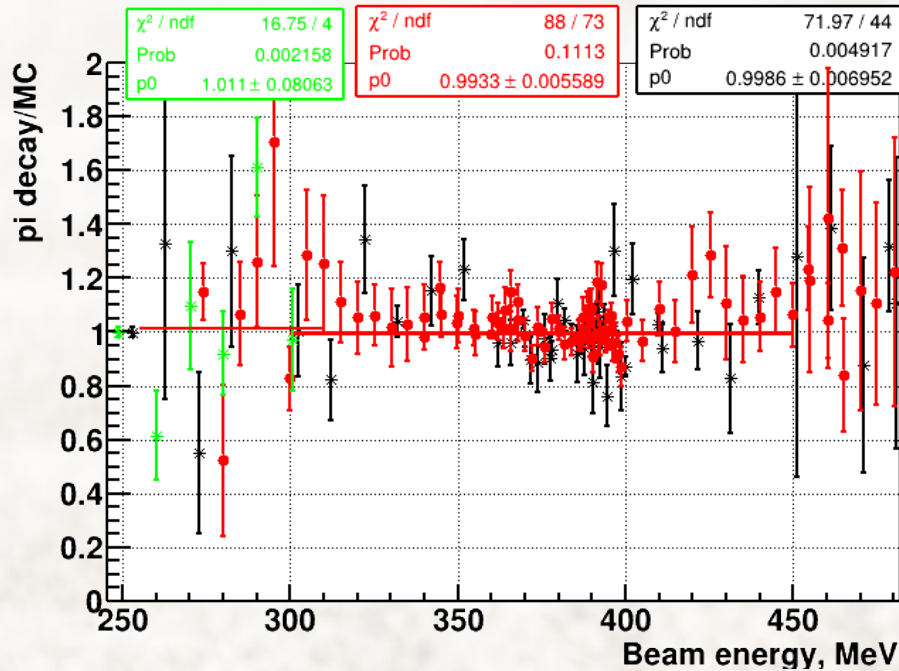
Experimental  $P^+$  spectrum with  $|P^- - P_e| < 10$  MeV



# Data/MC checks for particle specific losses

Some features of PDF give possibility to control particle specific losses (pion decay, bremsstrahlung loss) - slides 27,28.

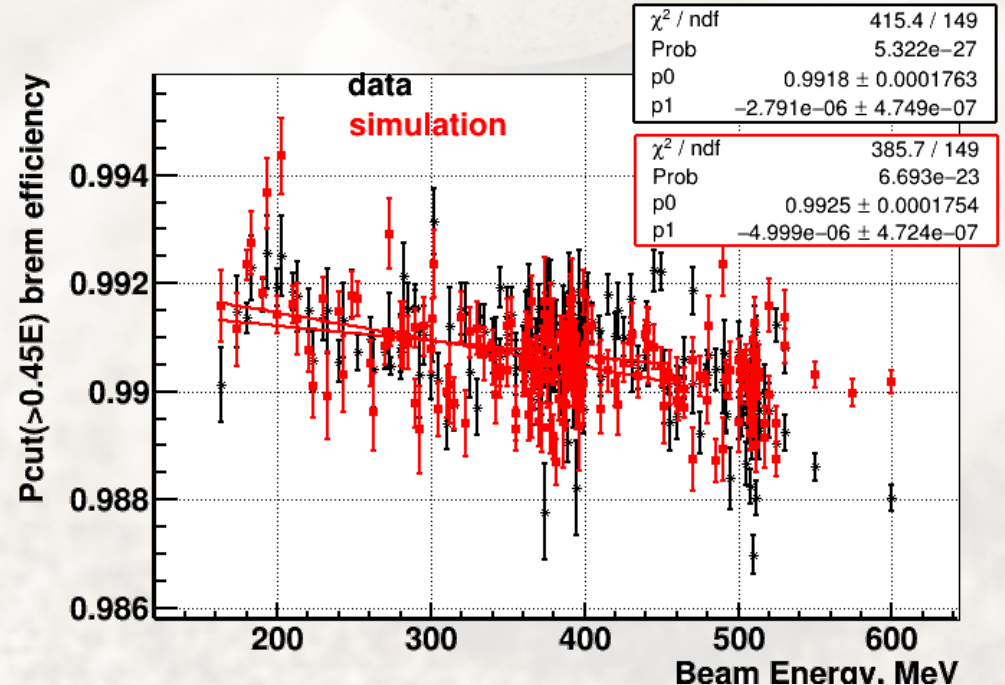
N events in Left+Right pion decay tails in PDF  
 The monitoring tool to control the reconstruction efficiency of decayed tracks in Data vs MC



Relative consistency ~ 2-3%

N events in Left + Right tails  $\Delta\text{Data}/\text{MC}$ :  
 RHO2013:  $0.0014 \pm 0.007$ , RHO2018:  $0.007 \pm 0.006$

Left tail in electron momentum spectra describe radiative + bremsstrahlung loss  
 N of events of brems. part at cut  $P/E_{\text{beam}} < 0.45$  gives part of brems. correction (0.9% of total 1.2%)

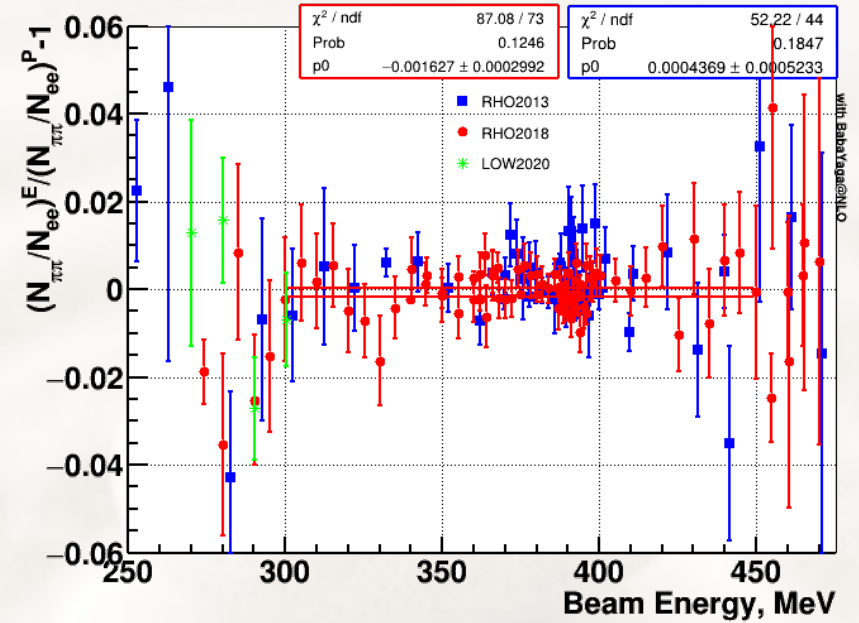


Relative consistency in inefficiency ~ 2%



# Question 8

Fig.8: the double ratio  $N_{\pi\pi}/N_{ee}$  for the 2 methods is fitted between 0.6 and 0.9 GeV and found to be consistent with 1 within 0.2%. The fit is dominated by the large statistics at the  $\rho$  peak while uncertainties are much larger in the tails. Is it reasonable to quote a constant systematic uncertainty on this ratio of 0.2% throughout the range 0.381-1 GeV?



The Logic is different:

Possible biases are checked on full MC  $\rightarrow$  systematics are estimated independently per each separation method.

Comparison of different methods gives the additional cross-check and ensure us, at least at central region, that 0.2% systematic uncertainty estimation is safe.

# Question 8

The separation biases of likelihood minimization was checked on mixed samples of full MC

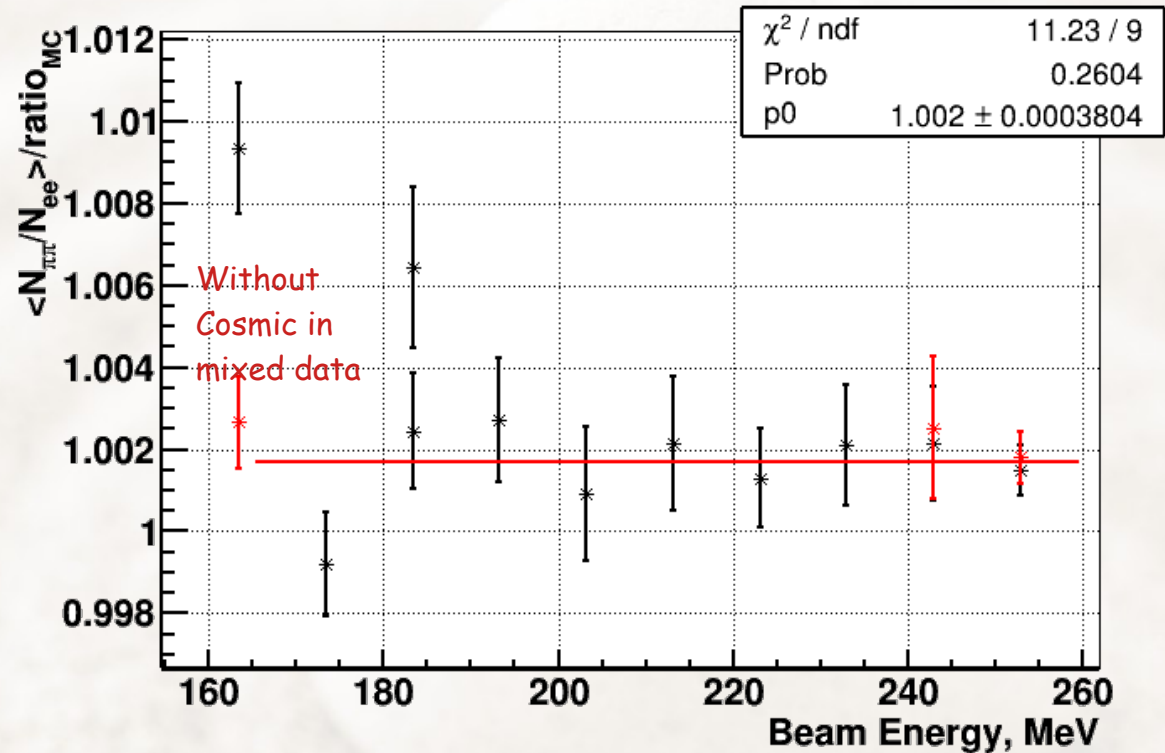
At lowest points statistical precision per point is low  $\sim 2-7\%$

100 independent mixed data samples were produced:

$$\langle N_{\pi\pi}/N_{ee} \rangle \sim +0.2\%$$

$$\langle N_{\mu\mu}/N_{ee} \rangle \sim +0.2\%$$

Momentum-based separation on full MC



At  $\sqrt{s} < 0.381 \text{ GeV}$ , the detector was operated with reduced magnetic field  $B=0.65\text{T}$  (1T) instead of 1.3 T  $\rightarrow$  there is not enough data for cosmic PDF determination  $\rightarrow$  **systematics 0.5%**

At lowest points stronger cut  $|t^{\text{event}} - t^{\text{beam}}| < 10 \text{ nsec}$  to suppress cosmic events was applied

# Question 18

Tracking: clarify the separation made between 'base efficiency' (track selection cuts) and inefficiency from sources specific to particle type (decay, multiple scattering, bremsstrahlung, nuclear interactions).

The efficiency analysis is based as much as possible on data itself.

The test sample for efficiency study was selected by 2 collinear clusters in calorimeter.

Unfortunately it doesn't cover the full data sample used in the particles separations.

Some events, when second cluster is not present, are not taken into account in test sample.

Test sample covers only ~30% of pion specific inefficiency (from ~2%-pion decay, nuclear interact)

~ 5% of electron specific (from ~1% - bremsstrahlung)

Also some of inefficiencies like cuts on  $N_{\text{hits}}$ ,  $Z_{\text{vtx}}$ , resolution in  $\theta$  are studied separately

Particle specific losses were taken from full MC (and controlled by data).

This corrections are applied as for full  $\pi^+\pi^-$ ,  $e^+e^-$ , ... data samples used in analysis(added),

as also for each specific test samples used in efficiency study (subtracted to exclude double-counting).

# Question 26

Two generators used (MCGPJ, BabaYaga) NLO+NNLO approximative with some differences found for  $e\bar{e}$ : give more information. Does it affect also the  $\mu\mu$  and  $\pi\pi$  samples?

Please see more details in: <https://agenda.infn.it/event/28089/contributions/147298/>

Yes,  $\mu+\mu-$  and  $\pi+\pi-$  differential cross sections have also some uncertainty

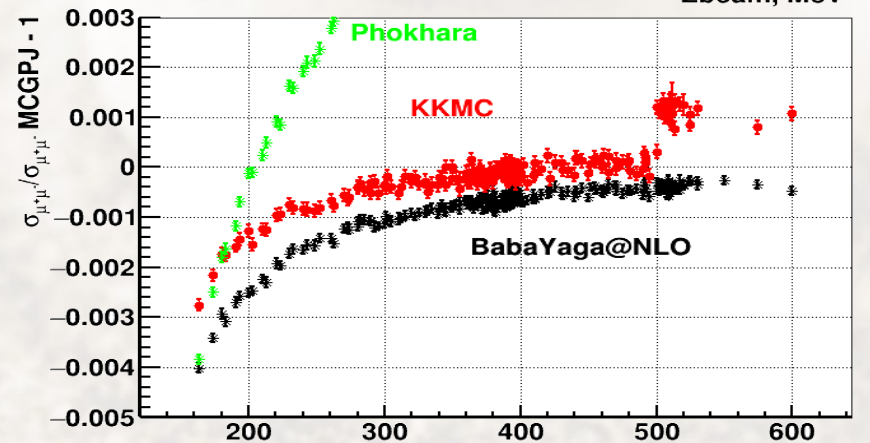
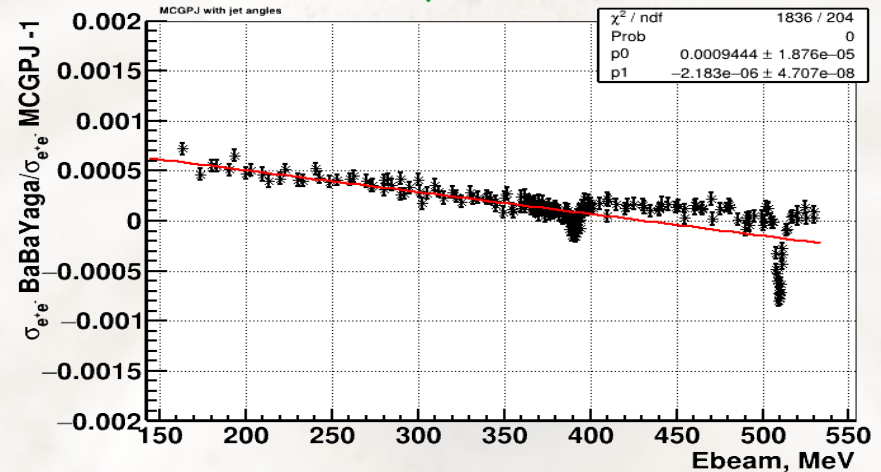
$e+e-$ :

Integrated cross-section is consistent at the level  $<0.1\%$  between generators

$\mu+\mu-$ :

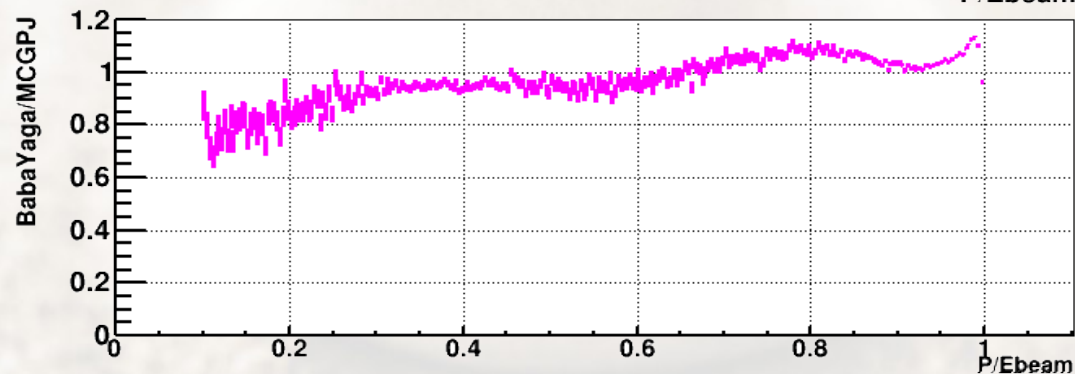
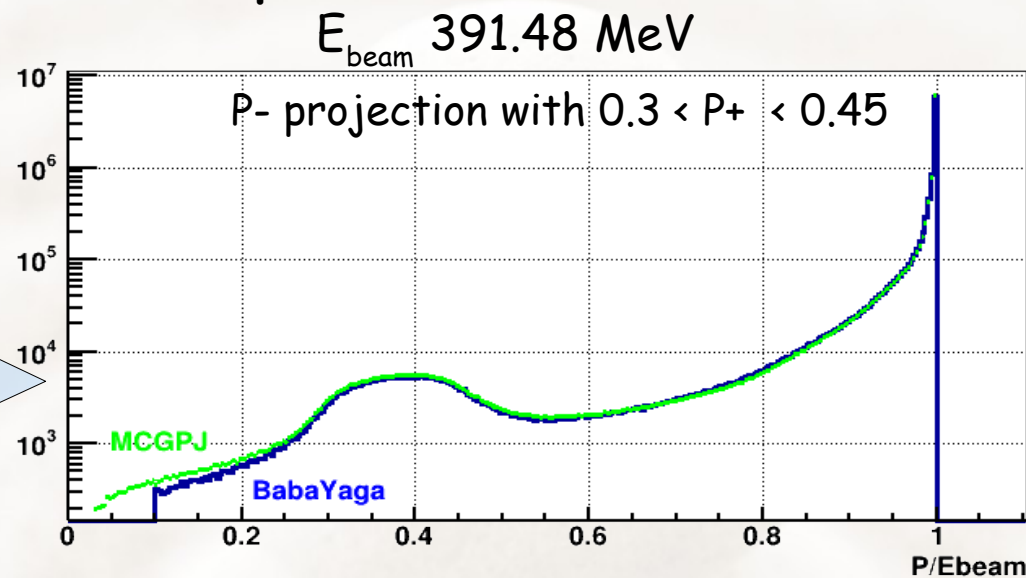
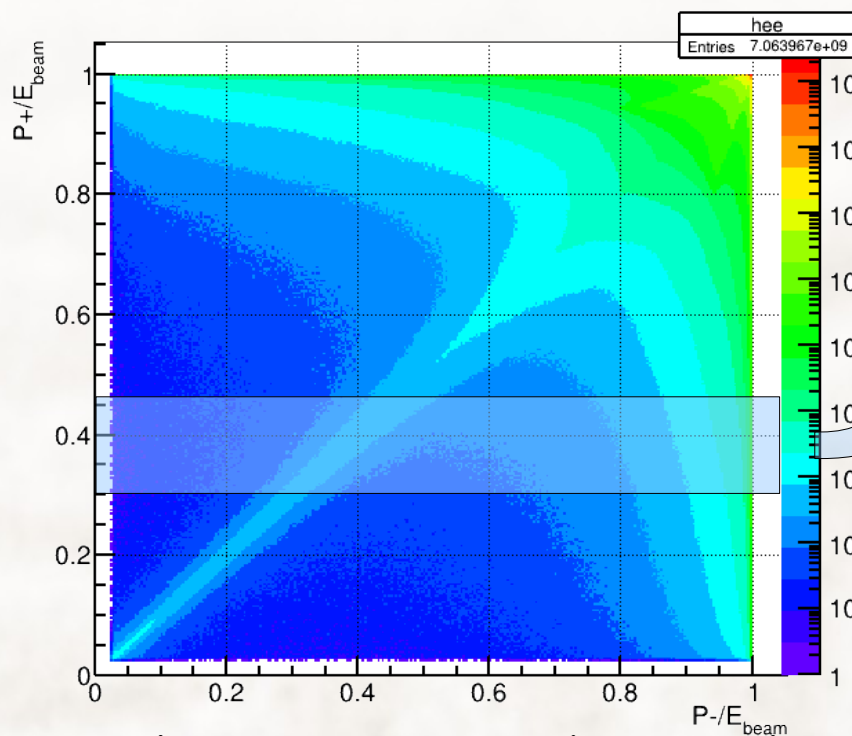
Integrated cross-section is inconsistent up  $0.4\%$

BabaYaga@NLO, KKMC, etc - missed mass term in FSR (arXiv:hep-ph/0505236)



# MCGPJ vs BabaYaga bhabha P+ vs P- spectrum

## Differential over momentum spectrum comparison



MCGPJ last improvement with jets angles  
reduce discrepancy from  $\times 1.6-3$  to  $\times 1.1$

Momentum spectrum still disagree at level  $\sim 10\%$

Tails comes from  $e^+e^- \rightarrow e^+e^- \gamma\gamma$ , NNLO order

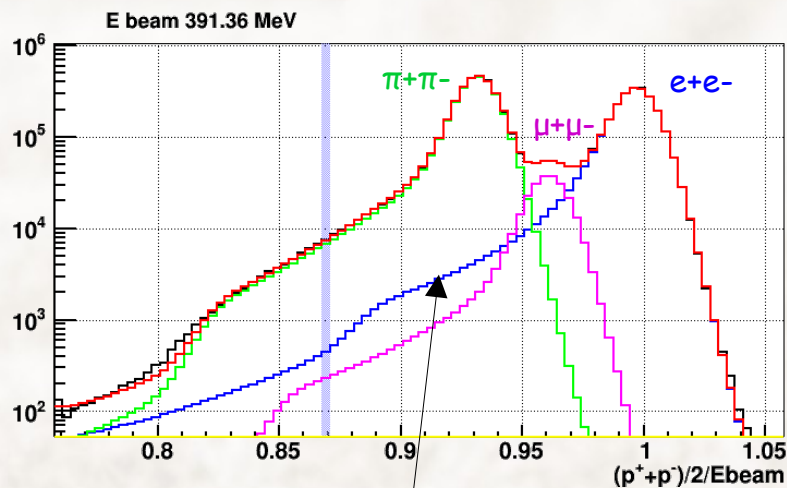
Very desirable to have more precise generators

Such discrepancy gives  $\sim 0.1-0.2\%$  systematic for  $\pi^+\pi^-$  at  $\rho$ -peak using momentum analysis at CMD3

# Differential cross section effect on form factor

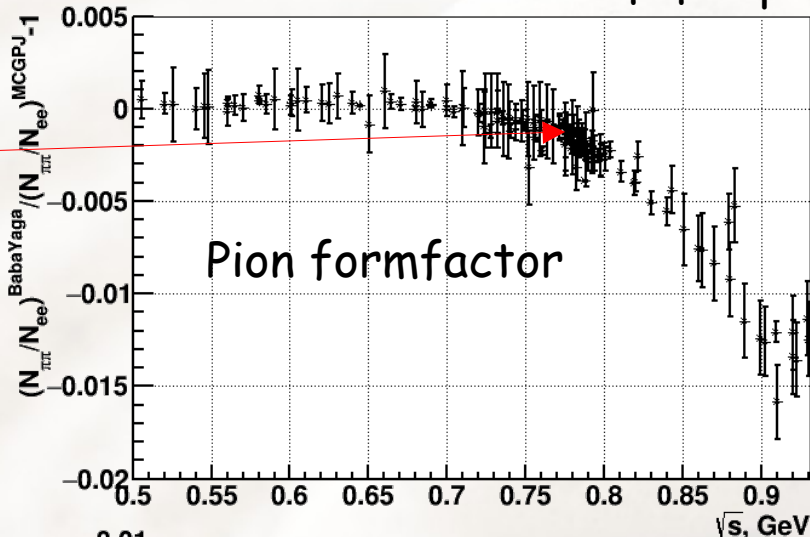
Differential cross section knowledge is necessary for momentum-based separation (not used in energy deposition separation)

Effect  $\sim 0.1-0.2\%$  at  $\rho$ -peak  
Effect comes when momentum peaks from  $\pi^+\pi^-$  and  $e^+e^-$  become close

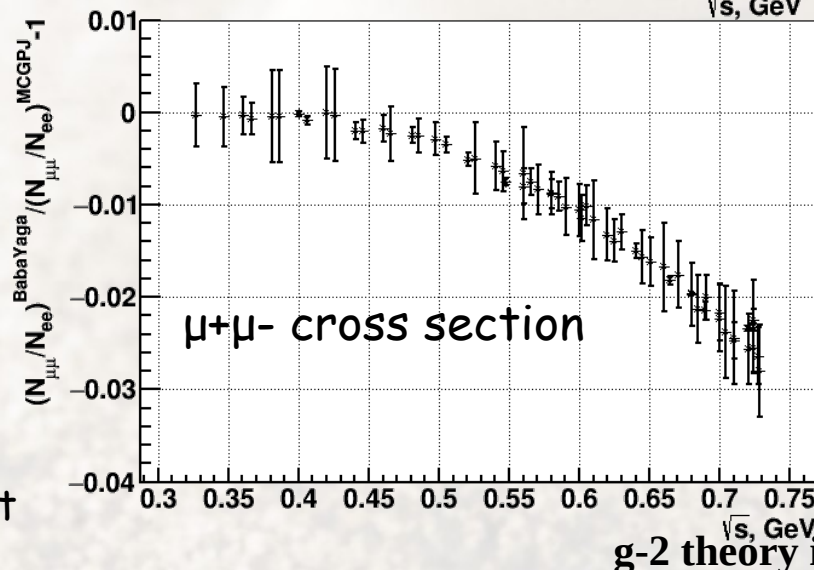


Important here soft photons radiation distribution:  
Looks like BaBaYaga@NLO approach with iterative photons generation gives better result

Difference of MCGPJ vs BabaYaga@NLO  
Cumulative from  $e^+e^-$  and  $\mu^+\mu^-$  spectra



$\mu^+\mu^-$  effect  $< 0.05-0.1\%$



$\mu^+\mu^-$  effect  $\sim 1/4 - 1/3$

# Questions 30, 32

Question 30: How can you justify a 0.2% error for the  $\pi\pi$  mode in MCGPJ given the large uncertainties seen for the Bhabha mode?

Question 32: The RC are large +8% at 0.9 GeV and -9% at 0.7 GeV. What is the uncertainty specific to this analysis, from the used generators. The number 0.2% quoted is for the integrated cross sections ('declared' by MCGPJ authors), but apparently not listed in Table 2. Also what about NLO+HO differential cross sections? Need to be clarified.

N.B. Integrated cross section in Bhabha mode was always consistent between generators at  $\sim < 0.1\%$

0.2% from MCGPJ is listed in Systematics Table 2:

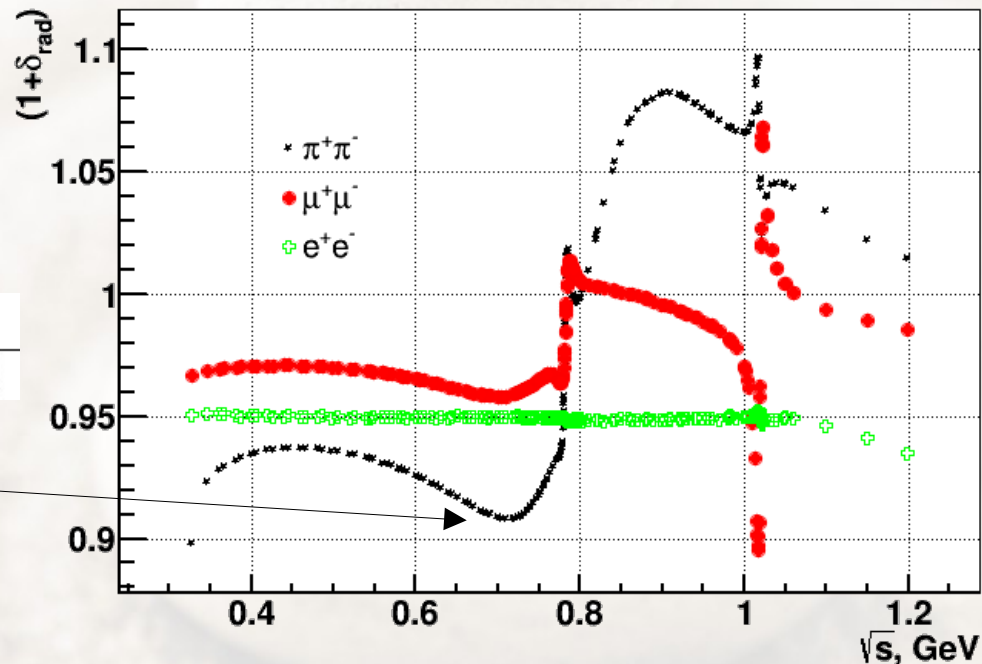
Contribution
0.2% ( $\pi^+\pi^-$ ) $\oplus$ 0.2% ( $F_\pi, \sqrt{s} > 0.74$ GeV) $\oplus$ 0.1% ( $e^+e^-$ )

+8%/-9% wave comes from  $F_\pi$  and ISR

Uncertainty from different  $F_\pi$  parametrizations is second part in radiative correction uncertainty

Differential cross section doesn't affect energy deposition-based separation.

Looking on  $N_{\mu\mu}/N_{ee}$  in momentum-based separation, the effect from  $\pi\pi$  spectra probably is smaller than from  $e+e-$  spectra (0.1-0.2% at  $\rho$ )



# $\pi\pi$ generator

For  $\pi\pi$  mode

Unfortunately only MCGPJ available with declared 0.2% precision (for energy scan experiments)

Phokara and BabaYaga 3.5 are incomplete at NLO level for energy scan mode:  
there is no FSR

Very desirable to have new precise generator with above sQED which will cover ISR up to  $E_\gamma=0$

The table with applied radiative corrections in this analysis is part of arXiv submission,  
It will be useful for cross-checks if new generators will be appeared.

Some cross checks to compare MCGPJ/Phokara were performed

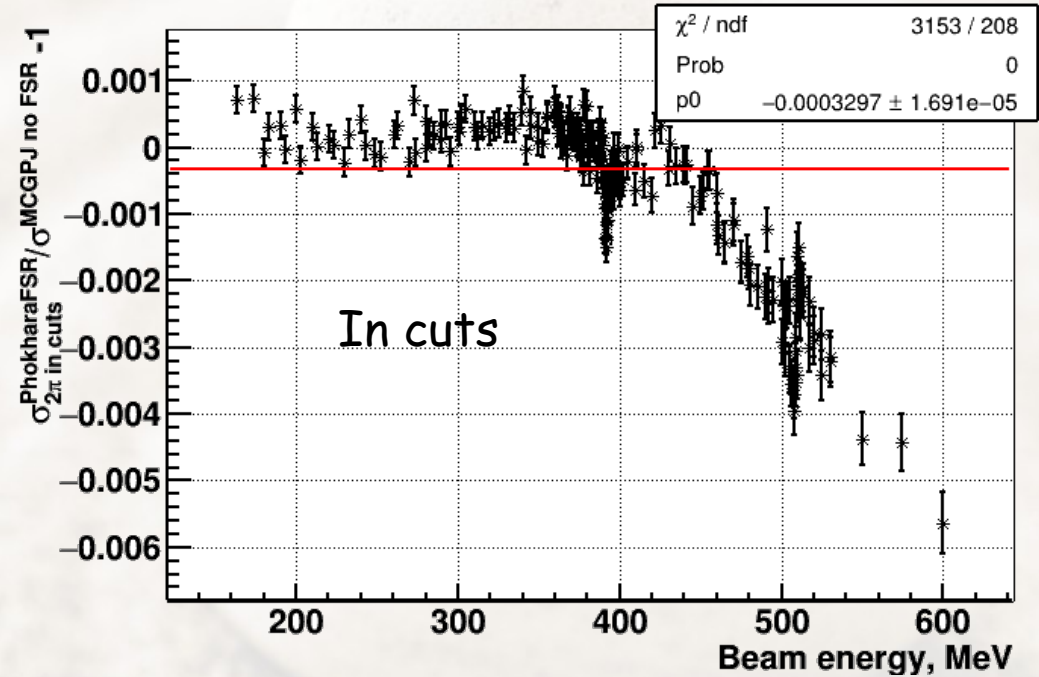
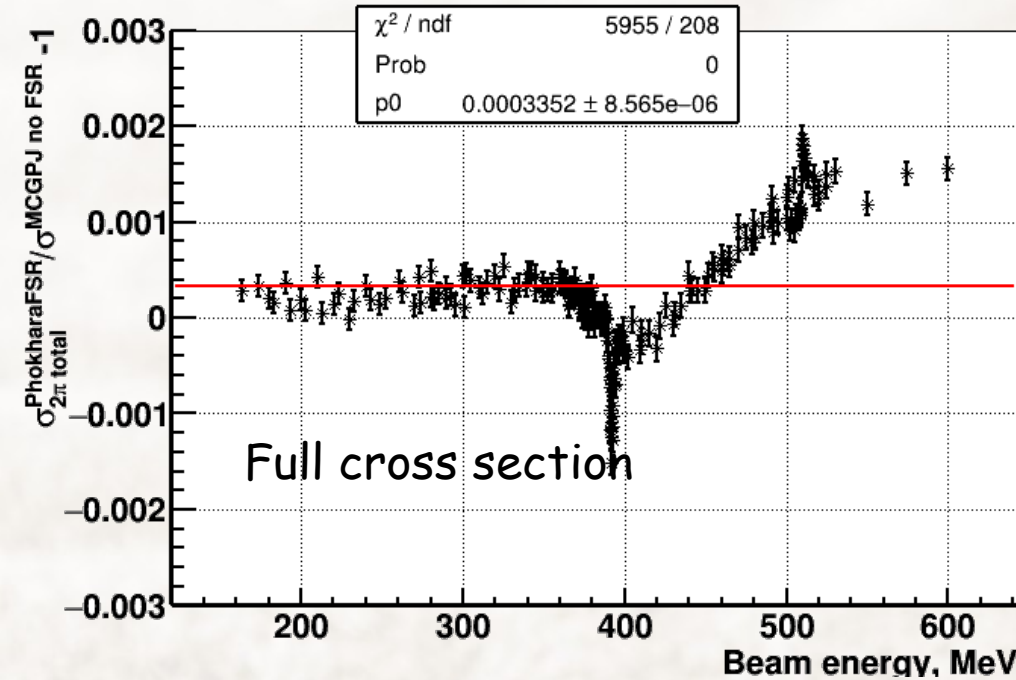
At  $E_{\text{beam}} 391.48 \text{ MeV}$  point: If to use Phokara momentum spectra for  $\pi\pi$  PDF instead of MCGPJ  $\rightarrow 0.03\%$  difference on  $F_\pi$



# MCGPJ/Phokara

ISR and  $F\pi$  cross check

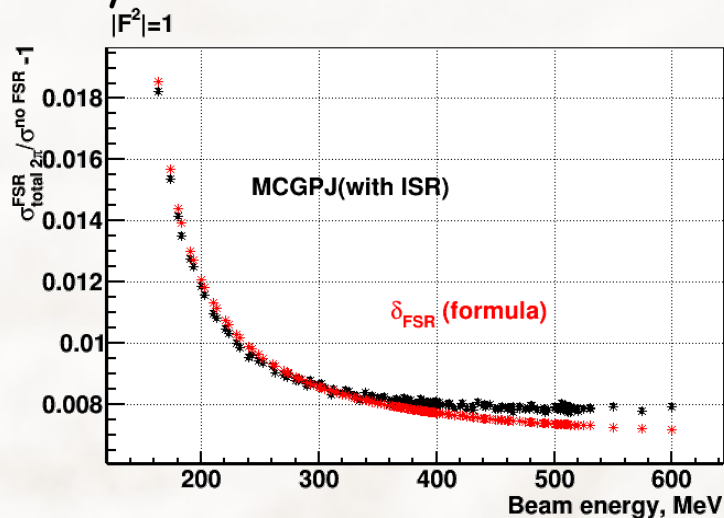
MCGPJ with FSR off,  
Phokara 10 with same  $|F\pi|$  as in MCGPJ, additional VP off



Cross section is consistent at  $\sim 0.05\%$  at  $\rho$ -peak  
(at  $\phi \sim 0.25\%$ )

# MCGPJ FSR contribution

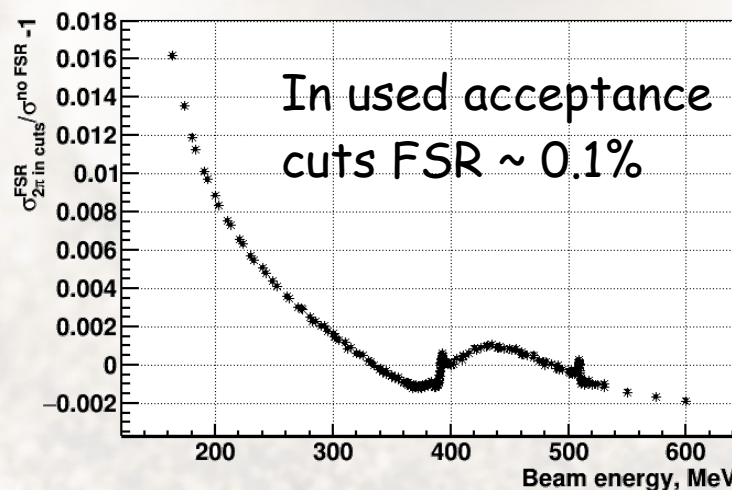
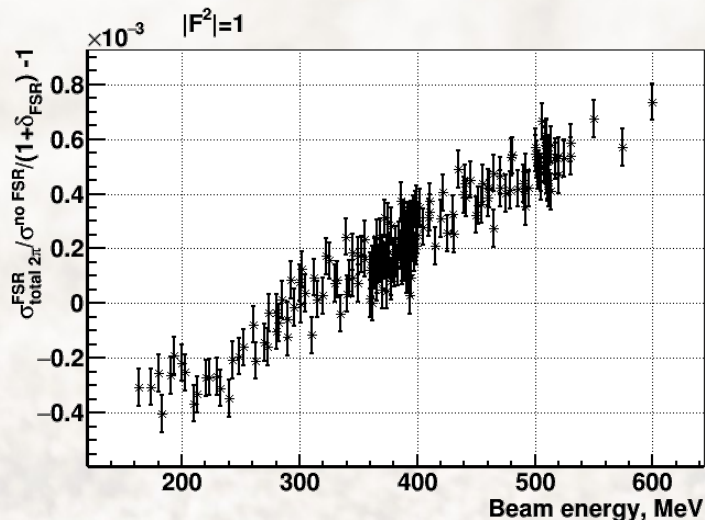
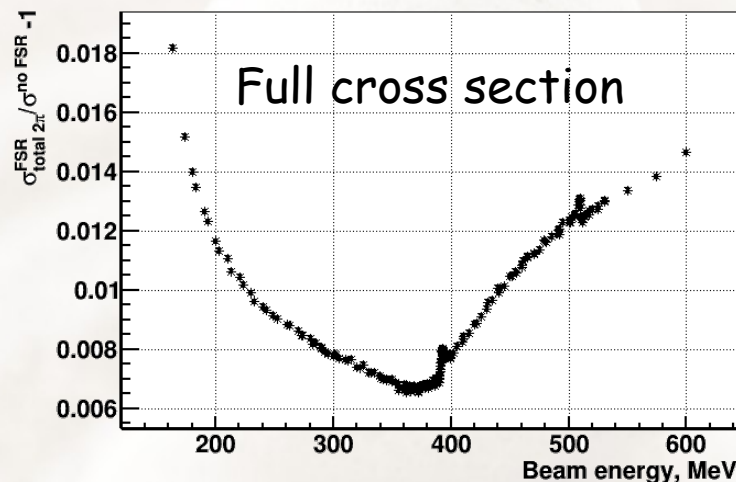
With  $F_{pi}=1$  FSR is consistent with analytical formula at  $< 0.05\%$



$$\frac{\sigma_{FSR}}{\sigma^{no FSR}} - 1$$

With full formfactor behaviour it is different because of ISR return.

Looks reasonable



# Question 43

Since it is only mentioned without any detail in the conclusion, can you clarify how the blinding of the results was achieved?

It was not "fully" blinding way.

The analysis was driven by self-consistency checks without comparing with others and by list of effects which should be checked giving effects  $\sim 0.1\%$ .

The main blocking difficulties were:

- Consistency between momentum/energy deposition-based separations

- (initial version of Energy based method (with LXe+CsI total energy) was having bias even on full MC data)

- Discrepancy in angle distribution

The detailed comparison with previous experiments appeared only at final stage, when it was performed accurate fitting of final measurement, iterative recalculation of radiative correction with CMD-3 form factor parametrization, with different parametrization over different experiments, etc

The collaboration was blinded to the last moment, the day before of the public institute seminar:

The discussions on all steps of the analysis over many years in local collaboration meetings, the paper preparation, the discussion on the systematic contribution (with all effects and problems involved) were without looking on final formfactor and comparison with others.

# Question 46

The paper cannot avoid a study and a discussion concerning the CMD-2/CMD-3 strong discrepancy which are absent at the moment, despite similar detectors, analysis and group: outline the major differences in the detector and the analysis procedure, compare distributions, dig out where the problem occurs. seen for the Bhabha mode?

**We don't know at the moment the source of difference between experiments.**

In principal CMD-2/CMD-3 detectors are totally different:

CMD-3 allows to study systematics at higher statistical level.

New Drift Chamber, new LXe calorimeter(with tracking capabilities),

new electronics, new implementation of trigger system, ....

Peoples involved in analysis at  $\rho$ -peak are different (except exchanged experiences)

# Question 48

The central values of the  $K+K^-$ ,  $\pi+\pi^-$ , ancillary  $3\pi$  measurements all tend to be higher than other experiments at a similar level of 4%, which of course for the  $2\pi$  channel looks most spectacular. Have possible common systematic effects across channels been investigated?

$3\pi$  process is well consistent with others experiment (except CMD-2)

The common excesses in  $K+K^-$  and  $\pi+\pi^-$  to others experiment are seen, it could be correlated or could be not....

Possible common sources:

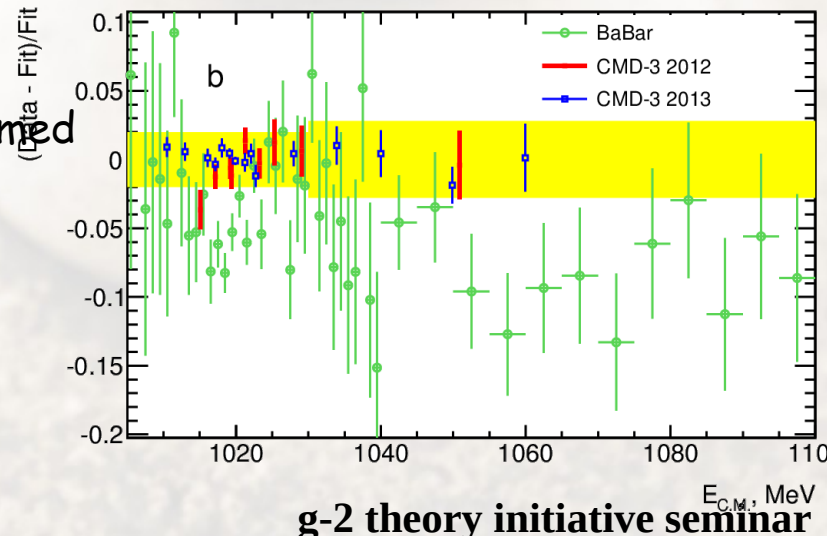
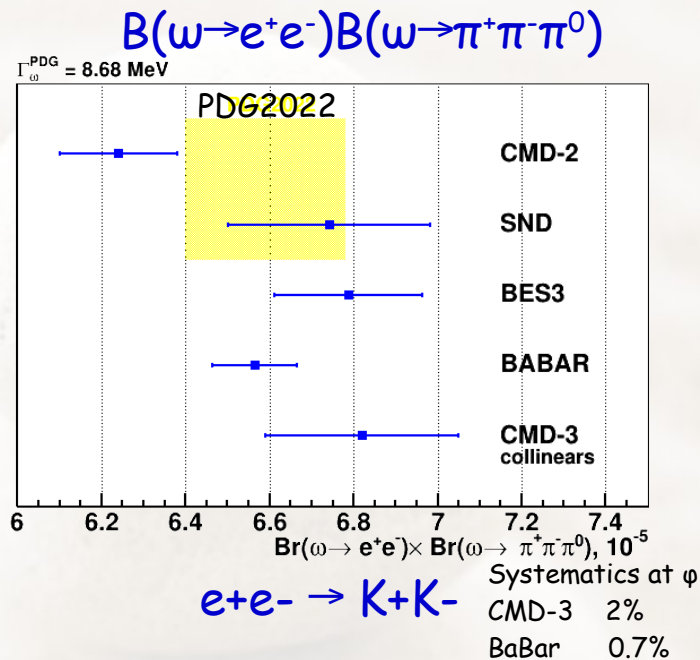
x Detector related:

$e+e^-$  trigger efficiencies, tracker efficiencies, .... :

- x not seen in  $N_{\mu\mu}/N_{ee}$  ratio
- x effort to catch triggers TF vs CF correlations was performed
- x not seen problems in angle distribution (if some resolution effect unaccounted...)

for future scans: new trigger system under commissioning,  
new DCH, ZC under consideration

x Radiative correction for  $K+K^-/\pi+\pi^-$  from MCGPJ generator: discussed in previous slides



# Question 49

What are the plans for publishing this analysis: short/long papers?

Do you intend to perform additional checks before submitting to a journal?

**Analysis is finished.**

(in fact, analysis was finished about a year ago, since then it was form factor fitting, polishing, paper preparation, internal paper reviewing, ....)

many self consistency checks were already performed, further may be with a better detector

**Current plans:**

short paper is under preparation, additional text polishing of the long paper and to submit both versions to journals in April (middle?)

**Future plans, other papers:**

New  $\rho$  scans with improved detector and possibly some specific systematics checks are expected

Analysis at  $\sqrt{s} > 1 \text{ GeV}$  is in progress by another person

(exploiting full shower profile information by neural network,  
as better separation is required at higher energies)

with same independent steps for efficiency determination, etc for formfactor evaluation

→ cross check between current and new analyses will be required at final stage

A stack of three smooth, light-colored stones is positioned on the right side of the image. The stones are stacked vertically, with the largest at the bottom and the smallest at the top. The background is a soft, out-of-focus sandy surface with gentle ripples.

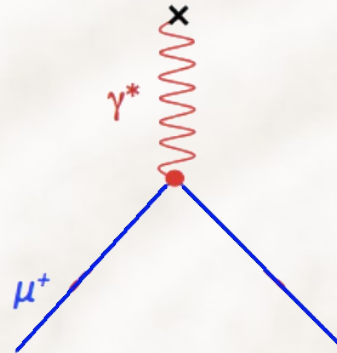
backups

# What is g-2 and how it is connected to R(s)

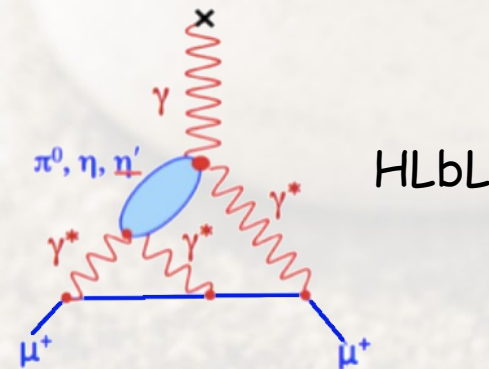
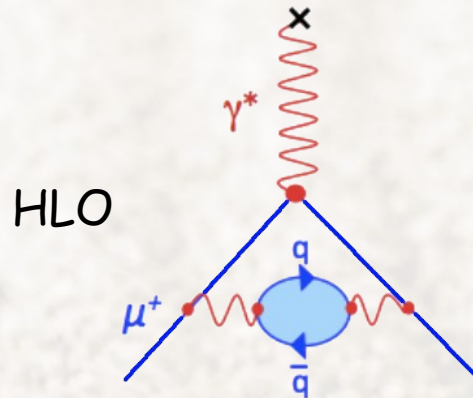
The magnetic moment of the particle relates spins to its angular momentum via the gyromagnetic ratio,  $g$ :

$$\vec{\mu} = g \frac{e}{2m} \vec{s}$$

In Dirac theory, point-like, spin  $\frac{1}{2}$  particle has exactly  $g=2$



Quantum loop effects via vacuum fluctuations lead a calculable deviation: the anomalous magnetic moment  $a = (g-2)/2 \sim \alpha/2\pi \sim 0.00116$





# The lowest-order hadronic contribution to $(g-2)_\mu$

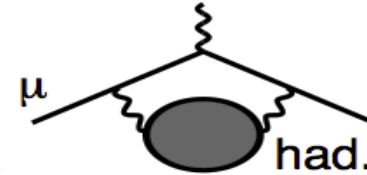
The hadronic contribution is calculated by integrating experimental cross-section  $\sigma(e^+e^- \rightarrow \text{hadrons})$ .

Starting at high energy the pQCD estimation of  $\sigma(e^+e^- \rightarrow \text{hadrons})$  is used. At lower energies only the experimental data can be used.

Weighting function  $\sim 1/s^2$ , therefore **lower energies contribute the most:**

**$< 2\text{GeV}$  gives 93% of the integral,  
 $\pi^+\pi^-$  gives the main contribution (73%) to  $a_\mu$**

The diagram to be evaluated:



pQCD not useful. Use the **dispersion relation** based on **analyticity** and the **optical theorem**:

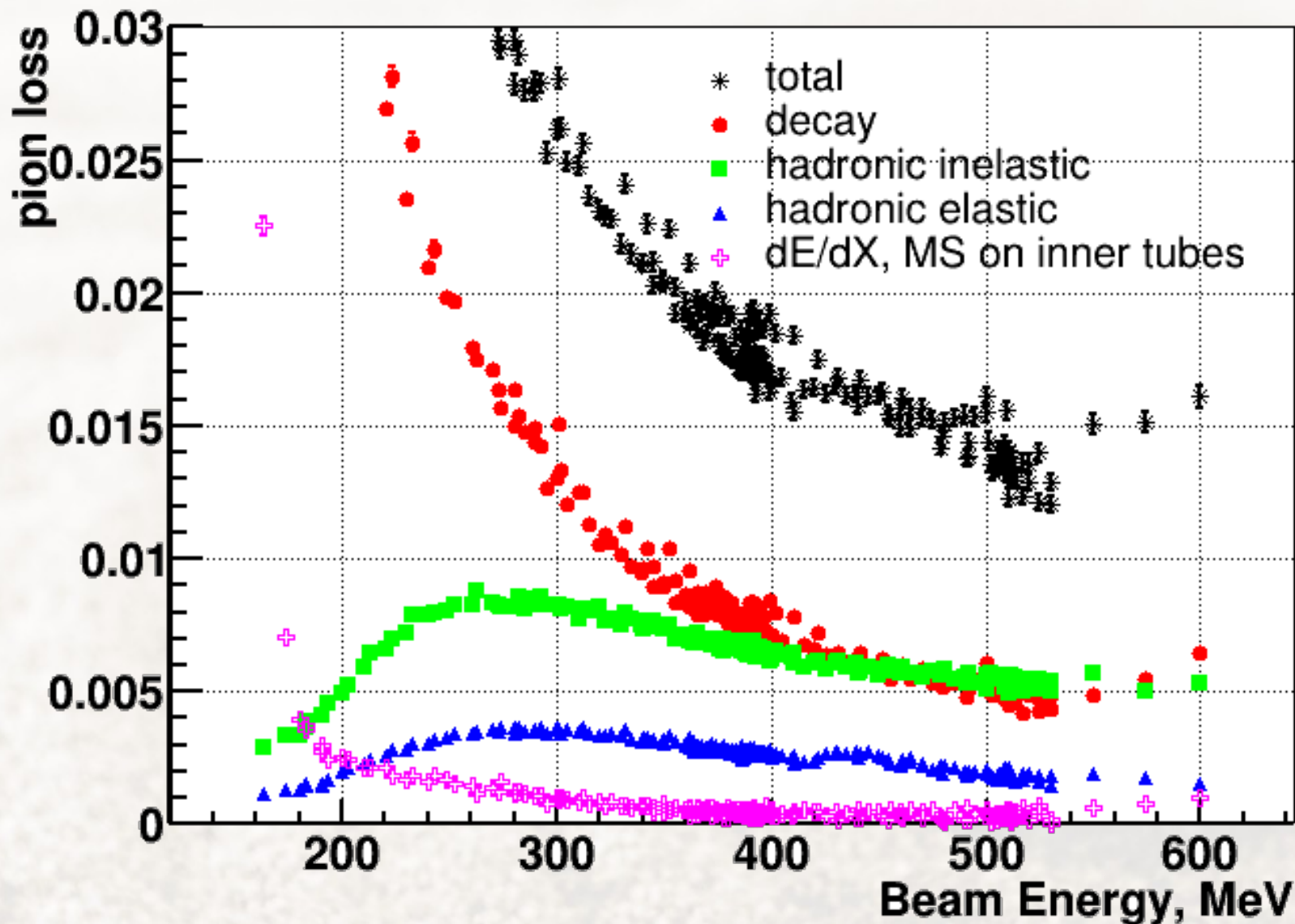
$$\text{had.} = \int \frac{ds}{\pi(s-q^2)} \text{Im had.}$$

$$2 \text{Im had.} = \sum_{\text{had.}} \int d\Phi \left| \text{had.} \right|^2$$

$$a_\mu^{\text{had, LO}} = \left( \frac{\alpha m_\mu}{3\pi} \right)^2 \int_{s_{\text{th}}}^{\infty} \frac{1}{s^2} \tilde{\mathbf{K}}(s) \mathbf{R}(s) ds$$

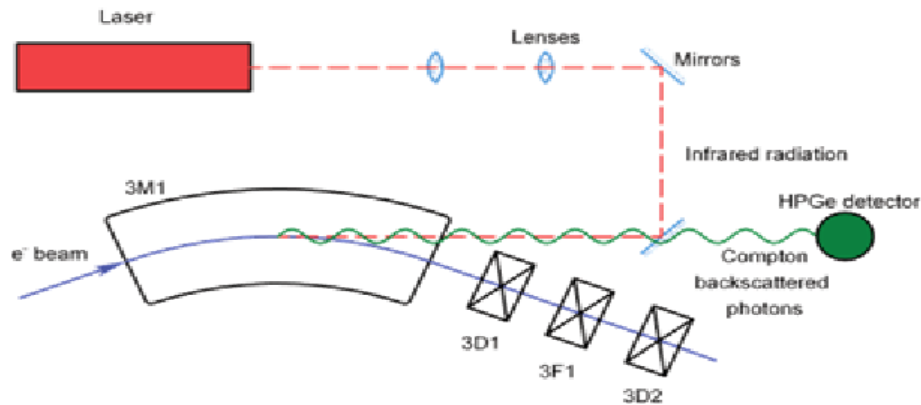
$$\tilde{\mathbf{K}}(s) = 0.6 \div 1.0$$

# Pion specific inefficiency

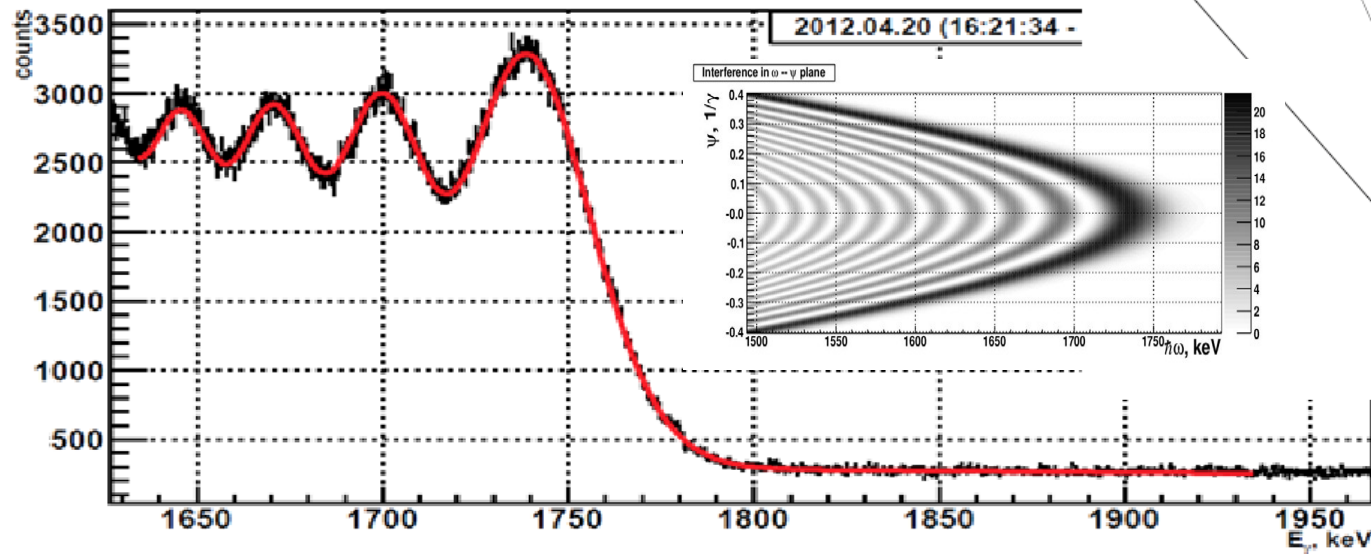
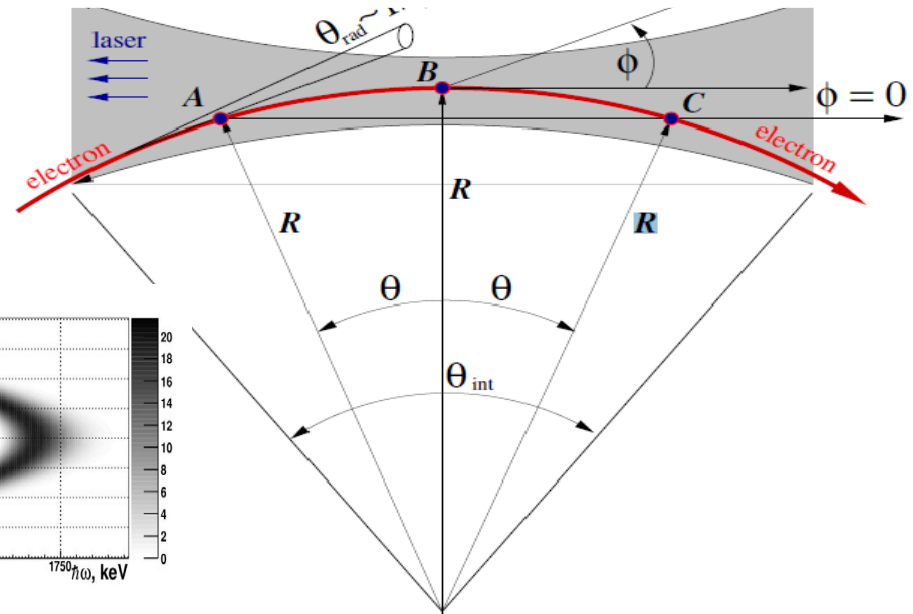


# Energy measurement by Compton back scattering

Starting from 2012, energy is monitored continuously using compton backscattering



Interference of photons from A and B



$$E = 993.662 \pm 0.016 \text{ MeV}$$

M.N. Achasov et al. arXiv:1211.0103v1 [physics.acc-ph] 1 Nov 2012

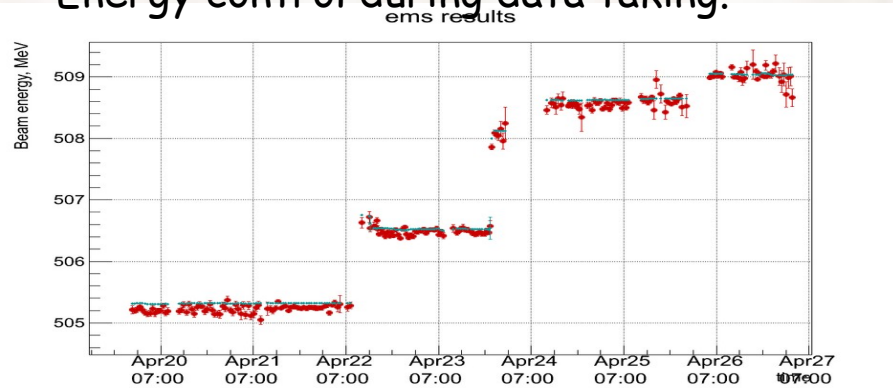
# Beam energy measurement at VEPP-2000

- **Magnetic field control in bending magnets  $\delta E/E < 10^{-3}$**

- 8x2 NMR probes, continuous control
- Absolute calibration using:
  - $\phi$ -meson ( $1019.455 \pm 0.020$  MeV),
  - $\omega$ -meson ( $782.65 \pm 0.12$  MeV).

- **Measurement of photon energy from back  $\delta E/E < 10^{-4}$  scattering laser light**

- Installed in 2012.
- Needs beam current (20  $\mu$ A),  $\sim 20$ -50 keV accuracy in 10 min
- Energy control during data taking.

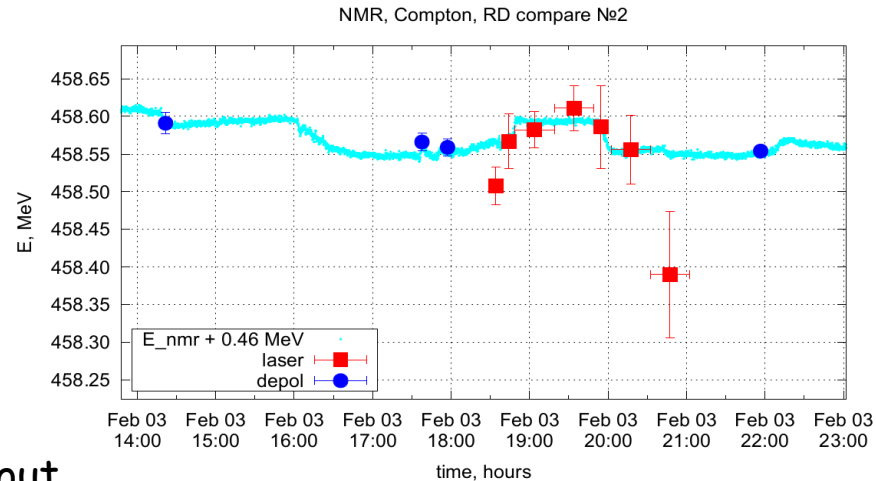
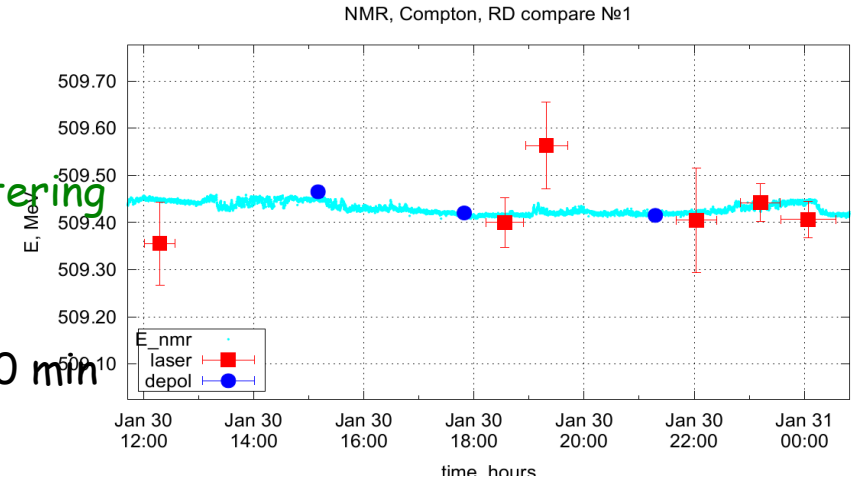


- **Resonance depolarization method**

$$\delta E/E < 10^{-5}$$

- Very high accuracy.
- Special configuration of VEPP-2000: "warm" optics without CMD-3 field.

## Methods comparison:



# Electron and muon g-2 Experiments

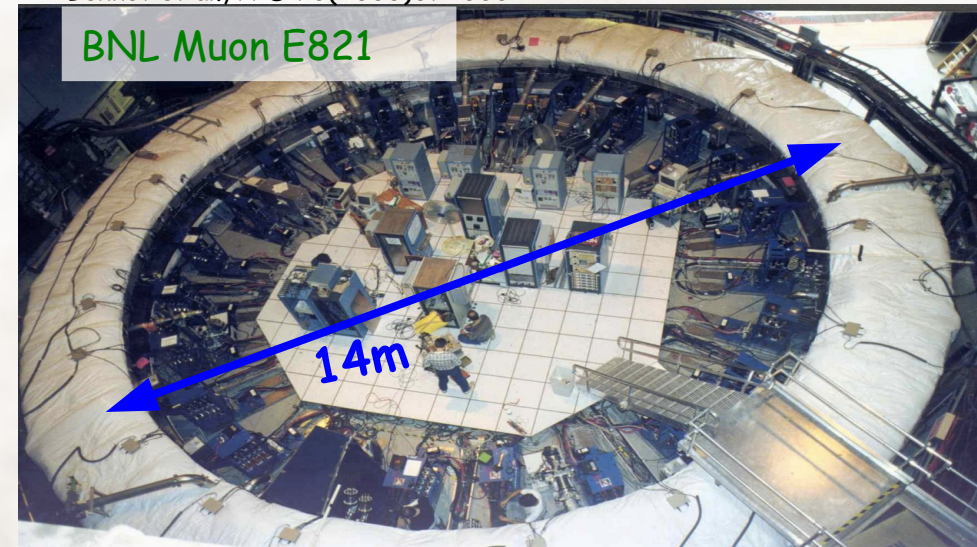
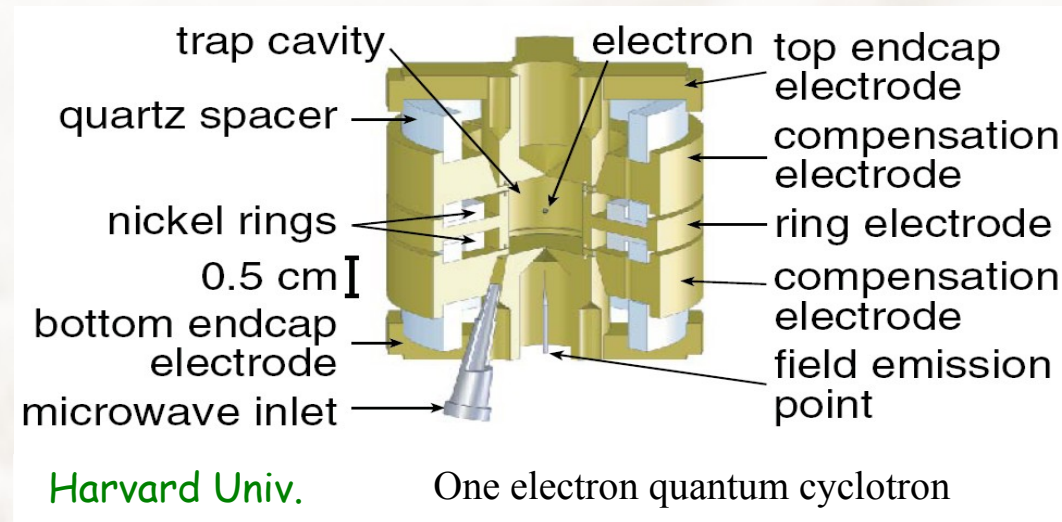
$$\vec{\mu} = g \frac{e}{2m} \vec{s}, g = 2(1+a)$$

$$a_e = 11\,596\,521.8073(0.0028) \cdot 10^{-10} [0.24\text{ppb}]$$

$$a_\mu = 11\,659\,208.9(6.3) \cdot 10^{-10} [0.54\text{ppm}]$$

Hanneke, Fogwell, Gabrielse, PRL 100(2008)120801

Bennet et al., PRD 73(2006)072003



The value of  $a_e$  was used to get the best determination of fine-structure constant  $\alpha$ .

R. Parker et al., Science 360 (2018) 191

Recent  $\alpha_{\text{QED}}$  measurement using the recoil frequency of Cs-133 atoms with 0.20ppb gives  $2.5\sigma$  tension with experimental  $a_e$

Muon (g-2) is 40,000 times more sensitive to non-QED fields than electron (g-2)  $\sim (m_\mu/m_e)^2$ , providing more sensitive probe for New Physics.

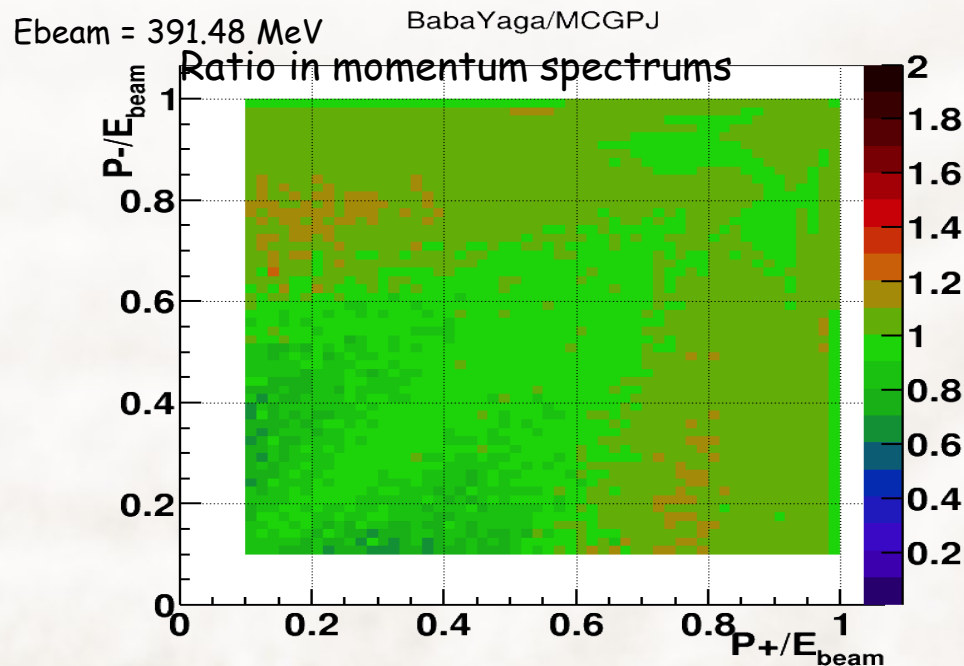
27 March 2023

g-2 theory initiative seminar



# MCGPJ vs BabaYaga spectra

After adding angular distribution for jets, etc

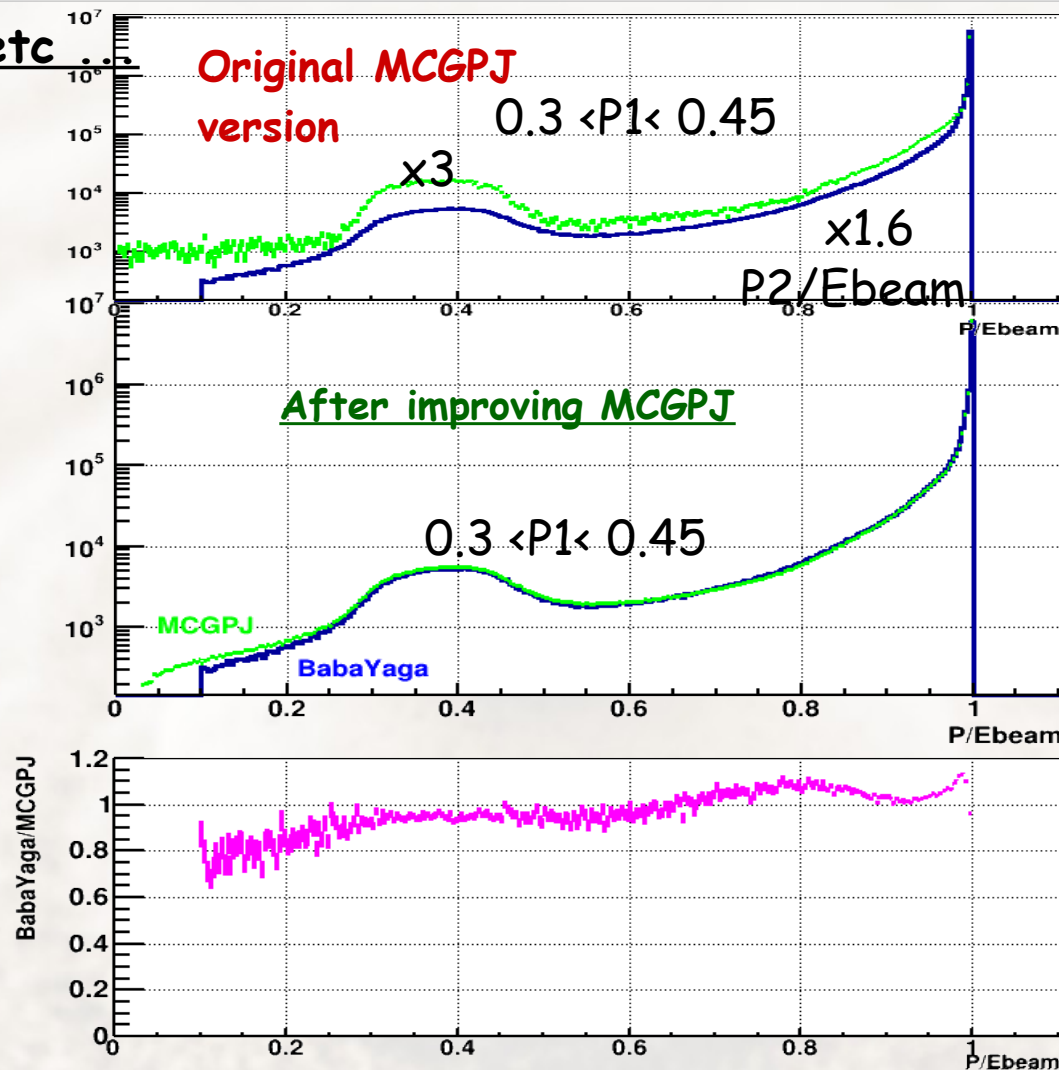


Momentum spectrum still disagrees at level  $\sim 10\%$   
 Need more experimental data for cross-check  
 We need more theoretical help

Result in  $|\mathcal{F}\pi|$  systematic by momentum  
 $\rightarrow 0.0 - 0.4\%$

**For precision  $\sim < 0.1\%$  necessary to have exact  $e^+e^- \rightarrow e^+e^- (\gamma\gamma)$  NNLO generator**

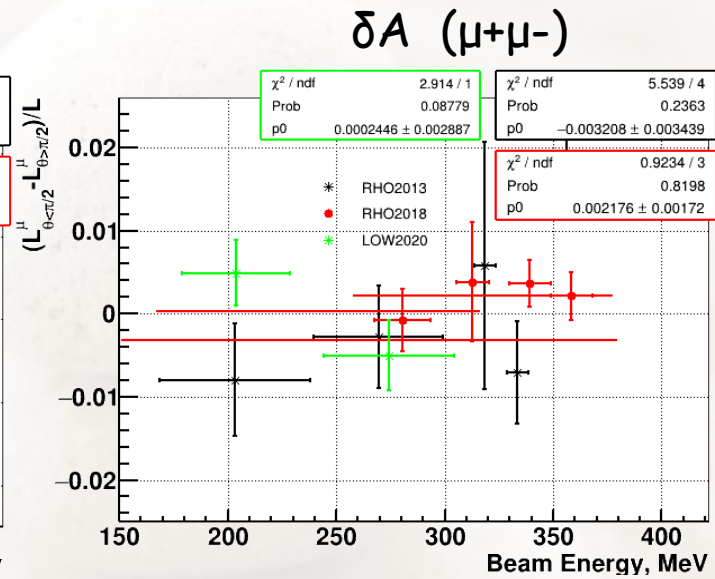
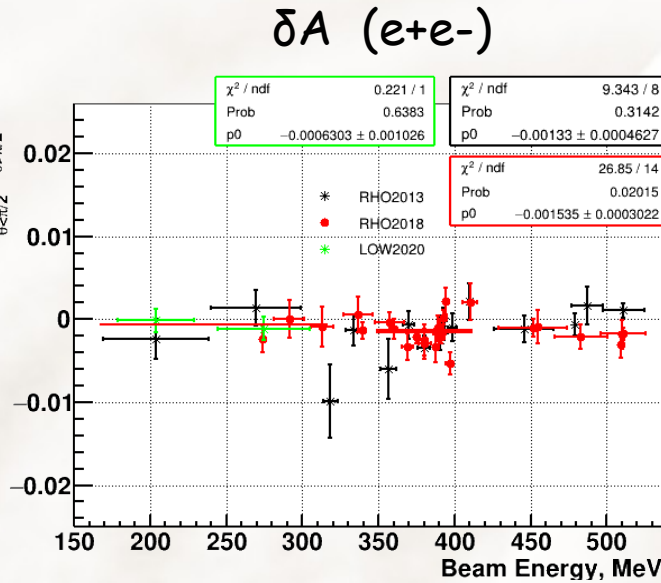
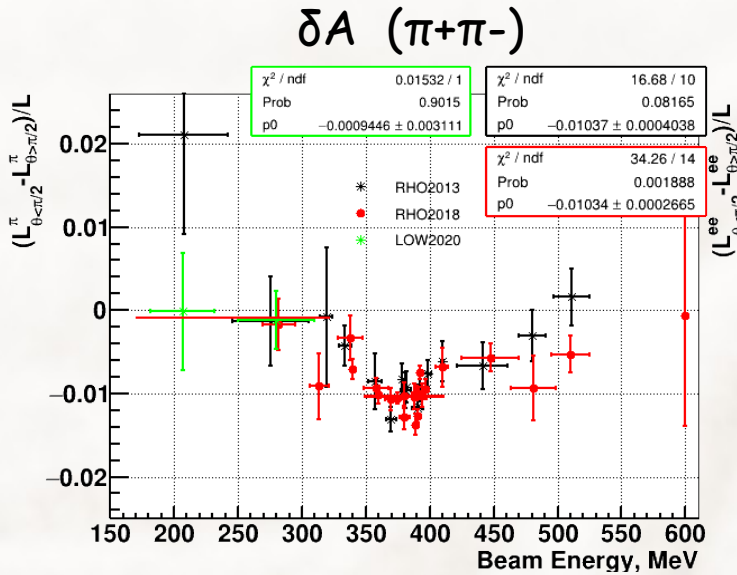
27 March 2023



g-2 theory initiative seminar

# Asymmetry $2\pi/e+e-/2\mu$

Asymmetry relative to generator prediction



Average at  $2E=350-410$  MeV

with MCGPJ:

$$\langle \delta A \rangle = -1.04 \pm 0.02 \%$$

$$\langle \delta A \rangle = -0.15 \pm 0.03 \%$$

$$\langle \delta A \rangle = 0.10 \pm 0.14 \%$$

with BaBaYaga@NLO:

$$-0.07 \pm 0.03 \%$$

$N_{\mu\mu}$  can be extracted  
only at lowest energies

$\rho$  - like behaviour

Fixed order NNLO  $\sim -0.06$

No trends for  $e+e-$

BabaYaga/MCGPJ difference gives  $\sim 0.08\%$

Detector systematic  $\sim 0.1\%$